

Behavior-Driven Synthesis of Human Dynamics

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Abstract

Generating and representing human behavior are of major importance for various computer vision applications. Commonly, human video synthesis represents behavior as sequences of postures while directly predicting their likely progressions or merely changing the appearance of the depicted persons, thus not being able to exercise control over their actual behavior during the synthesis process. In contrast, controlled behavior synthesis and transfer across individuals requires a deep understanding of body dynamics and calls for a representation of behavior that is independent of appearance and also of specific postures. In this work, we present a model for human behavior synthesis which learns a dedicated representation of human dynamics independent of postures. Using this representation, we are able to change the behavior of a person depicted in an arbitrary posture, or to even directly transfer behavior observed in a given video sequence. To this end, we propose a conditional variational framework which explicitly disentangles posture from behavior. We demonstrate the effectiveness of our approach on this novel task, evaluating capturing, transferring, and sampling fine-grained, diverse behavior, both quantitatively and qualitatively. Project page is available at <https://cutt.ly/517rXEp>

1. Introduction

Understanding human appearance, posture and behavior are key problems of computer vision with numerous applications in autonomous driving [39, 41, 23], surveillance [12, 50, 60], medical treatment [6, 54] and beyond. While there has been major progress on representation [59, 48] and - with the advent of deep generative models [34, 24] - synthesis [7, 30] and manipulation [20, 13, 17] of *posture and appearance*, the understanding of representation and synthesis of *behavior* is an open problem. Human motor behavior is defined by the distinct dynamics of our limbs and the entire body. Take for example a person raising their arm. This is fully determined by the upward movement of the arm. Since the remaining body

posture is mostly unaffected, the behavior can be directly performed independently of a particular initial body configuration such as a sitting or standing posture (cf. Fig. 1). Moreover, rather complex behavior like running involves an interplay between certain body limbs, e.g. arms swinging synchronously with the movement of legs, and, thus, is naturally limited to certain postures to start with. To nevertheless enact such behavior from arbitrary starting poses, first a transition to fitting initial body configurations may be required - for instance, a sitting person needs to stand up before being able to walk. Finally, specific body features like size or build do not affect the ability to perform a walking behavior.

While behavior is eventually instantiated as a sequence of individual postures that can be observed in a video, this would be a suboptimal representation: We want the overall behavior to be the same, e.g. raising arm or walking, regardless of the initial posture it starts with. Although we are looking at different realizations it should still be represented as being the same behavior. Consequently, understanding, controlling, and synthesizing behavior calls for separate disentangled representations of the characteristic behavior and of individual (in particular the initial) posture. In contrast, present work on human motion synthesis typically represents behavior directly by means of the observed sequence of postures [3, 40, 63, 57]. Thus, as no explicit understanding and representation of behavior is developed, synthesizing human behavior has been limited to only changing person appearance [57, 9, 56] or forecasting the most likely continuation of the depicted posture sequence [3, 40, 63, 11]. However, controlling such sequences, e.g. to re-enact a novel behavior by an observed person, asks for a posture independent representation which captures only the behavior dynamics to be transferred. Moreover, instantiating the re-enacted behavior requires combining these dynamics with the, potentially significantly different, posture of the target person. In this paper we propose a conditional variational generative model for controlled human behavior synthesis which only requires a collection of sequences without any class labels provided. Our model learns to understand the characteristic motor dynamics of behavior, which enables us to transfer behavior between videos. We learn a dedicated representa-

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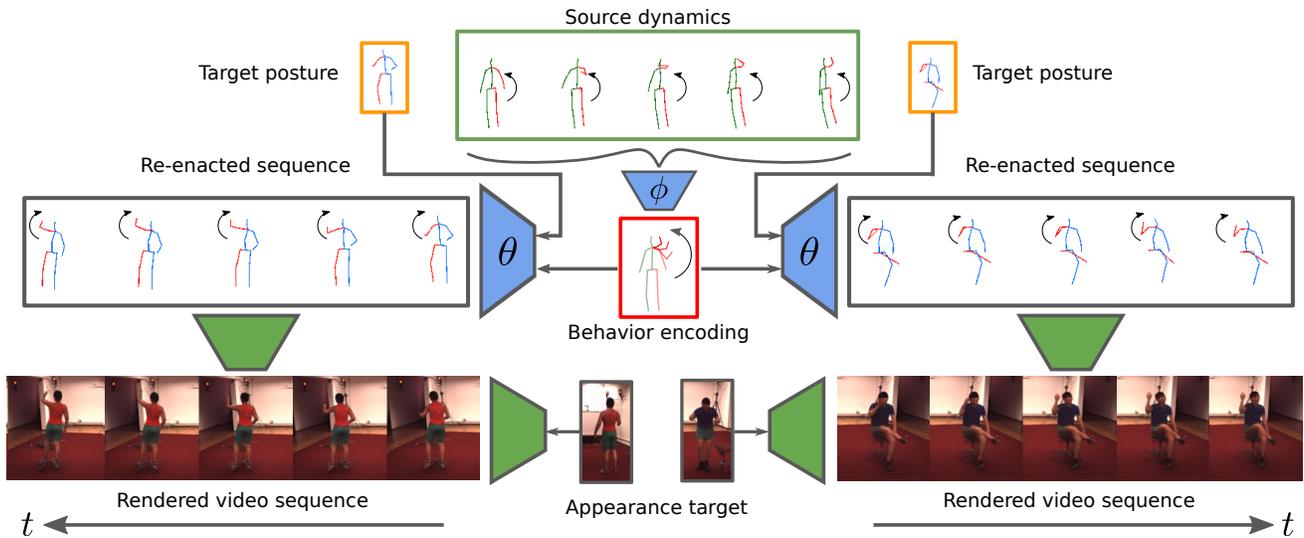


Figure 1. *Our Approach for Behavior Transfer.* Given a source sequence of human dynamics our model infers a behavior encoding which is independent of posture. We can re-enact the behavior by combining it with an unrelated target posture and thus control the synthesis process. The resulting sequence is combined with an appearance to synthesize a video sequence.

tion extracting these dynamics from pose sequences while factorizing out posture information. To this end, we propose an explicit disentanglement framework for behavior and posture based on an alternating optimization procedure while simultaneously controlling the information flow through our model. In particular, the explicit disentanglement allows our model to re-enact extracted behavior from arbitrary target postures and, if needed, to infer required corresponding transitions itself. Our experiments demonstrate qualitatively and quantitatively that our model meaningfully transfers behavior between sequences and is also able to sample novel and diverse behavior. Quantitative comparison against current approaches for human motion synthesis confirms the competitive performance of our approach.

2. Related Work

Static person rendering. Much work has been proposed to alter certain characteristics of humans depicted in static images like age, gender or body features [31, 33, 35, 52] or synthesizing individual persons in different, unseen poses [20, 19, 38, 13]. The latter task typically requires for explicit disentanglement between certain factors of interest, often depending on paired image data [19, 38, 26]. While these approaches work well factors in static images, our work aims at transferring human behavior and, thus, requires disentanglement of a temporal factor, which is significantly more complex.

Human video synthesis. Human video synthesis has been addressed in multiple ways. Some approaches synthesize videos directly in the pixel space [53, 2]. Due to the vast complexity of this problem, most approaches are based on

mid-level representation of human shape, such as segmentation masks [57, 22] or pose estimates [56, 9, 62, 18, 37]. Chan et al. [9] generate video sequences of dancing persons by first learning correspondences between frames and postures before adding appearance information. A similar sequence-to-sequence translation task is performed in [57, 56, 36]. These works represent behavior directly on instantiated pose sequences, thus lacking the ability to exercise control. Our model understands and explicitly learns a behavior representation which can be used to transfer characteristic behavior dynamics between persons. Another line of research is future human motion prediction based on an initially observed posture sequence [14, 29, 21, 55]. Yuan et al. [64, 63] extend the future motion prediction task using multiple transformations on the latent space to increase the diversity of predicted motions. Chiu et al. [11] propose a hierarchical multi-scale RNN to learn dependencies between individual postures. Martinez et al. [40] use residual RNN architectures to directly model motion velocities. Milbich et al. [43] synthesize behavior by arranging frames from different video sequences based on nearest neighbour retrieval in a dedicated activity space. In contrast to our approach, these methods can not control the predicted behavior but only extrapolate the observed posture sequence.

Controlled behavior synthesis. Controlling the behavior to be generated requires a considerable higher degree of understanding than unconditioned prediction or sequence translation. Recent works control mostly only in form of a small, fixed set of predefined actions [22, 25]. Yang et al. [62] condition the synthesis process on action labels. In contrast, we require only a collection of unpaired video sequences and

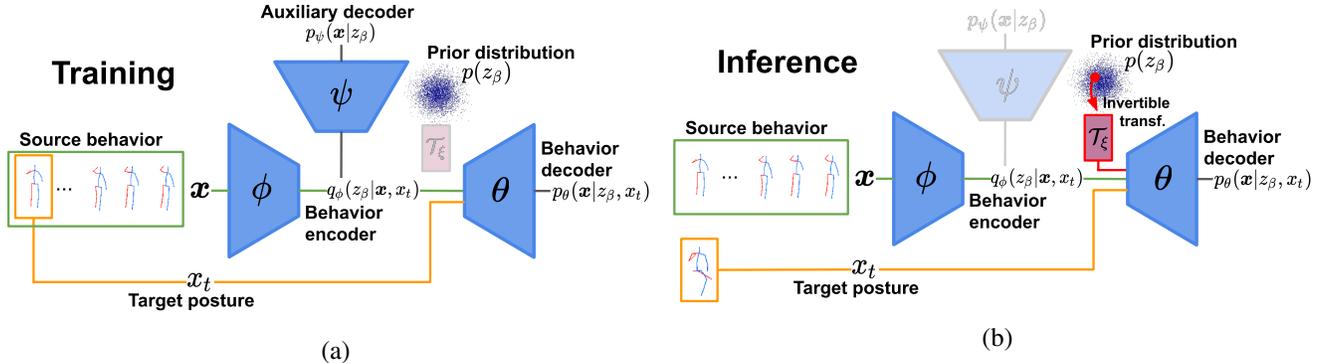


Figure 2. Overview over model training (a) and inference (b). Each distribution is realized by a deep neural network. During training, the first posture of \mathbf{x} serves as conditioning x_t (yellow). Note, that consequently x_t is also part of the encoder input since we do not have multiple training sequences \mathbf{x} starting from the same posture x_t available. In inference, i.e. after disentangling posture and behavior, we transfer source behavior (green) to an arbitrary target posture (yellow) or synthesize novel behavior from the prior distribution which is matched to $q_\phi(z_\beta|\mathbf{x}, x_t)$ by a learned invertible transformation \mathcal{T}_ξ (red).

condition the synthesis process on a dedicated representation of behavior independent of posture. DLow [63] splits posture into different sets of keypoints to vary the diversity of predicted future movements for predefined body parts while keeping the others close to the groundtruth future sequence and, thus, cannot exercise detailed control. MT-VAE [61] uses latent space arithmetics to enable transformations between different motions. However, transfer of more complex behavior is limited since only linear arithmetics are considered which makes a strong assumption on the latent space that typically cannot be met. In contrast, we learn a dedicated representation of behavior disentangled from posture. Hence our model naturally allows for recombination of behavior and posture.

Action recognition Action recognition [8, 58] aims at classifying a predefined set of actions from a given video, potentially based on intermediate representations such as 3D keypoints. Although our learned behavior representation is also based on keypoints, we aim at capturing behavior dynamics for detailed synthesis of full behavior. In contrast, action recognition learns discriminative representations which only focus on separating between action classes [51].

3. Approach

Our goal is to control and synthesize videos of human behavior. Since powerful pose estimators [59, 48] are readily available, pose sequences $\mathbf{x} = [x_0, \dots, x_n]$, $x_i \in \mathbb{R}^{K \times 3}$ are directly used as a basis to represent the behavior observed in video [57, 56, 9], e.g. for changing the depicted person's appearance or predicting likely sequence continuations. While this representation is sufficient to perform the aforementioned tasks, changing the posture sequence to re-enact a different behavior asks for a deeper understanding. Thus, behavior transfer requires separate representations modelling the characteristic motor dynamics of behavior and individual

postures. We now present a generative model which extracts and represents human behavior β from a source sequence \mathbf{x} independent of the instantiated postures. Given an observed target posture x_t , e.g. in another video, we can then synthesize a re-enacted posture sequence and subsequently translate it to the video domain.

Extracting behavior β from \mathbf{x} into a representation $z_\beta \in \mathbb{R}^D$ and subsequently re-combining it with a target pose x_t to instantiate the behavior can be naturally formulated by means of latent variable models such as encoder-decoder frameworks. Such frameworks have been successfully applied for predicting future postures based on \mathbf{x} , i.e. directly extrapolating the observed posture sequence [63, 55]. However, as we seek to control the behavior to be generated, we require the latent representation z_β to be disentangled from posture information.

3.1. Synthesis using conditional generative models

Generative models are powerful frameworks which are particularly suited for synthesis tasks. As we not only aim to learn a representation for behavior, but also need to extract it from our input sequences \mathbf{x} , variational autoencoders (VAE) [34] are a natural choice. Such models approximate the true data distribution $p(\mathbf{x}, z_\beta)$ which is assumed to follow the generative process $p(\mathbf{x}, z_\beta) = p(\mathbf{x}|z_\beta)p(z_\beta)$. To optimize the intractable marginal log-likelihood $\mathbb{E}_{p(\mathbf{x})}[\log p_\theta(\mathbf{x})]$ of the model distribution $p_\theta(\mathbf{x}, z_\beta)$, a variational posterior $q_\phi(z_\beta|\mathbf{x})$ is introduced allowing to maximize a lower bound $L(p_\theta, q_\phi) \leq \mathbb{E}_{p(\mathbf{x})}[\log p(\mathbf{x})]$ [34]. Now, since we want to transfer behavior and condition it on arbitrary target postures, we condition the generative process [49] additionally on x_t , which modifies the lower variational bound and its optimization to

$$\max_{\theta, \phi} L(p_\theta, q_\phi) := \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log p_\theta(\mathbf{x}|z_\beta, x_t)] - D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t) || p(z_\beta)) \quad (1)$$

where $p(z_\beta)$ is the prior on the latent representation z_β which is typically modelled as a standard Gaussian distribution $\mathcal{N}(0, I)$. The first term of (1) can be considered to optimize the synthesis quality of the generator $p_\theta(\mathbf{x}|z_\beta, x_t)$ while the second part regularizes the encoder $q_\phi(z_\beta|\mathbf{x}, x_t)$ to match the Gaussian prior.

Although our generator p_θ has access to both z_β and the conditioning posture x_t , optimizing (1) will in general not encourage our model to learn a factorization of posture information and the behavior representation z_β . Moreover, we have no ground-truth provided for different behaviors starting from the same target posture x_t . Thus, we are only able to train our model by choosing x_t to be the first posture of \mathbf{x} , which aggravates the need for an explicit disentanglement during the optimization process.

3.2. Disentangling posture from behavior

While explicit disentanglement between factors of variation has been studied in the domain of static images [42, 26, 38], disentangling complex temporal information, however, is significantly still lacking. Existing works for static images typically resort to supervision by exploiting pairs of data samples sharing one factor while differing in the remaining factors [42, 26], which allows for a natural disentanglement signal. Without having similar supervision available, we need to explicitly disentangle the posture information in \mathbf{x} from our latent behavior representation z_β . To this end, we would ideally want to minimize the predictability of the individual postures in \mathbf{x} given z_β . However, performing this operation directly on basis of our generator p_θ does not prevent the erasure of body dynamics as well. Instead, we can frame this task using an auxiliary generative model.

Let $\hat{p}_\psi(\mathbf{x}|z_\beta)$ be a second generative model aiming at generating \mathbf{x} from our behavior representation z_β only, i.e. optimizing the log-likelihood,

$$\max_{\psi} \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log \hat{p}_\psi(\mathbf{x}|z_\beta)] . \quad (2)$$

Solving this task requires $\hat{p}_\psi(\mathbf{x}|z_\beta)$ to represent posture information which it has to be able to extract from z_β . Exploiting this, we can formulate our disentanglement task as an alternating optimization between our behavior model, i.e. p_θ, q_ϕ , optimizing $L(p_\theta, q_\phi)$ and $\hat{p}_\psi(\mathbf{x}|z_\beta)$ optimizing (2), both depending on the posterior $q_\phi(z_\beta|\mathbf{x}, x_t)$.¹ To limit the predictability of $\hat{p}_\psi(\mathbf{x}|z_\beta)$, we extend (1) resulting in

$$\max_{\theta, \phi} L(p_\theta, q_\phi) - \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log \hat{p}_\psi(\mathbf{x}|z_\beta)] . \quad (3)$$

This objective does not explicitly optimize parameters ψ , thus the predictability of $\hat{p}(\psi)$ can only be diminished by removing information about \mathbf{x} from z_β . Further, note that p_θ

¹However, note that (2) is not optimized over parameters ϕ and consequently does not affect $q_\phi(z_\beta|\mathbf{x}, x_t)$.

has access to the conditional x_t providing posture information and consequently only requires q_ϕ to provide missing dynamics to generate \mathbf{x} . The overall procedure can be considered as an adversarial task, alternating between optimizing (2) and (3) in each training iteration. As a result, factoring out posture information from z_β is indeed the most viable solution. Moreover, since posture information is excluded from our representation z_β , $p_\theta(\mathbf{x}|z_\beta, x_t)$ is required to infer a meaningful continuation of x_t depicting behavior β .

Due to the additional constraint in (3), the already existing pressure to reduce the overall encoded information in z_β imposed by $D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta))$ is further amplified. This also increases the risk of posterior collapses when using recurrent decoders [5], thus strongly affecting the generative process. Next, we discuss how to alleviate this problem by relaxing the information bottleneck.

3.3. Relaxing the information bottleneck for improved synthesis

The quality of synthesis depends on the expressiveness of $p_\theta(\mathbf{x}|z_\beta, x_t)$ which stands in contrast to the regularization of the variational posterior $q_\phi(z_\beta|\mathbf{x}, x_t)$ in vanilla variational autoencoding settings [10, 65]. This becomes evident as the regularization $D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta))$ minimizes an upper bound on the mutual information $I_{q_\phi}(\mathbf{x}; z_\beta)$ [47], thus reducing the information captured in z_β . Consequently, a typical solution is to explicitly maximize the mutual information [65, 46]. However, computing reliable estimates of $I_{q_\phi}(\mathbf{x}; z_\beta)$ is difficult for complex data [19, 4]. Instead, we resort to a relaxation of the regularization in the original variational problem by only optimizing $D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta))$ to maintain a certain information budget I_{KL} , i.e. optimizing

$$\begin{aligned} \max_{\theta, \phi} \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log p_\theta(\mathbf{x}|z_\beta, x_t)] \\ \text{s.t. } D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta)) \leq I_{\text{KL}} . \end{aligned} \quad (4)$$

Similar to Peng et al. [45] who constrain discriminator networks, we can optimize (4) using dual gradient decent. Overall, we arrive at our final objective $L(p_\theta, q_\phi)$ by inserting the relaxation constraint into (3) and introducing a scalar coefficient γ_C and the Lagrange multiplier γ_{KL} (which is still optimized via dual gradient decent), i.e.

$$\begin{aligned} L(p_\theta, q_\phi) = & \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log p_\theta(\mathbf{x}|z_\beta, x_t)] \\ & - \gamma_{\text{KL}} (D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta)) - I_{\text{KL}}) \\ & - \gamma_C \mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log \hat{p}_\psi(\mathbf{x}|z_\beta)] . \end{aligned} \quad (5)$$

Note, that without our explicit disentanglement, relaxing $D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta))$ would further encourage the entanglement of posture and behavior dynamics in z_β .

Relaxing the regularization $D_{\text{KL}}(q_\phi(z_\beta|\mathbf{x}, x_t)||p(z_\beta))$ comes at the cost of a reduced overlap between the

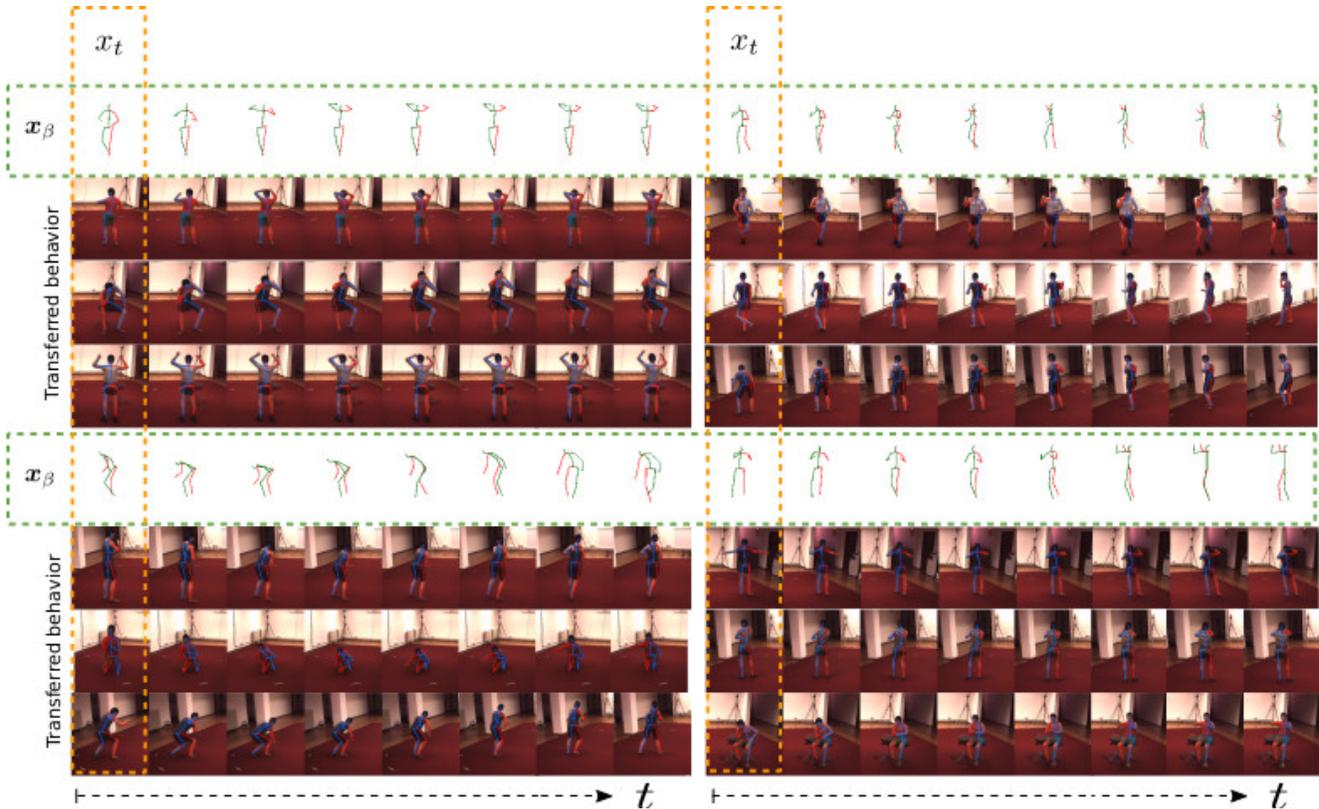


Figure 3. *Behavior Transfer on Human3.6m*. We transfer fine-grained, characteristic body dynamics of an observed behavior x_β to unrelated, significantly different target postures x_t . If required, the target posture is first adjusted by a transition phase before re-enacting the inferred behavior (e.g. top-right example, third row: walking starting from a bent down posture). Note that both transferred postures and images are generated by our models.

variational posterior q_ϕ and prior $p(z_\beta)$ impairing the sampling ability of our model. Next, we correct this mismatch by means of a subsequently learned normalizing flow transformation [33, 15].

3.4. Bridging the gap between prior and posterior

We want to use our model not only to transfer behavior between videos, but also to synthesize novel behavior based on sampling z_β from the prior distribution. Thus, strong deviations of the posterior $q_\phi(z_\beta|\mathbf{x}, x_t)$ from $p(z_\beta)$ may reduce the syntheses results due to out-of-distribution samples. To alleviate this issue, we train a normalizing flow model [44, 33] after our variational behavior model is optimized. Normalizing flows yield an explicit, invertible transformation from q_ϕ to $p(z_\beta)$, thus bridging any potential gap between them. To this end, these models learn flexible probability distributions $p_u(u)$ over continuous random variables, such as our behavior representation z_β . In particular, normalizing flows establish a bijective mapping $z_\beta \xleftrightarrow{\mathcal{T}_\xi} u$ using the transformation $\mathcal{T}_\xi = h_{\xi_1} \circ h_{\xi_2} \circ \dots \circ h_{\xi_m}$, a sequence of m invertible functions h_{ξ_j} parametrized by ξ_j by

maximizing the likelihood

$$\mathbb{E}_{q_\phi(z_\beta|\mathbf{x}, x_t)} [\log p_u(\mathcal{T}_\xi(z_\beta)) - \log |\det J_{\mathcal{T}_\xi}(z_\beta)|] . \quad (6)$$

Here, $\det J_{\mathcal{T}_\xi}$ is the Jacobian determinant of the invertible transformation. Choosing $p_u(u)$ to follow the same distribution as $p(z_\beta)$ establishes our desired bijective mapping between $q_\phi(z_\beta|\mathbf{x}, x_t)$ and $p(z_\beta)$. Sampling novel behavior representations z_β is then performed by $z_\beta = \mathcal{T}_\xi^{-1}(u)$, $u \sim p_u(u)$.

4. Experiments

We now investigate the capabilities of the proposed method to disentangle pose of a sequence from the underlying behavior. The resulting model is evaluated for the tasks of behavior transfer to different start poses and diverse sampling from the behavior representation. Evaluation is performed on the *Human3.6m* dataset [28], a large-scale motion capture dataset which contains 3.6 million video frames of 11 subjects, each of which performs 17 actions. Following previous work [64, 63] we use a 17-joint skeleton of 3D joint locations for training on 5 (S1,S5,S6,S7,S8) and

Method	T=1		T=10		T=20		T=30		T=40		T=50		acc. gt: 0.45	d_β $\mu \pm \sigma$
	RE	TDE												
cAE	0.72	8.30	0.28	1.94	0.26	0.34	0.28	0.23	0.30	0.23	0.33	0.23	0.45	0.92±0.34
cVAE	5.29	9.07	5.28	8.95	5.05	8.81	4.82	8.87	4.55	8.86	4.46	8.80	0.13	0.00 ± 0.00
MT-VAE [61]	1.36	8.90	1.40	8.95	1.39	8.66	1.38	8.45	1.34	8.27	1.37	8.12	0.20	4.44 ± 2.05
Ours ($\gamma_C = 0, I_{KL} = 50$)	1.71	9.01	1.46	7.92	1.22	6.95	1.17	6.15	1.18	5.58	1.30	5.33	0.35	2.82 ± 0.79
Ours ($\gamma_C = 0, I_{KL} = 100$)	1.24	8.99	0.89	7.09	0.81	5.55	0.78	4.33	0.73	3.48	0.80	3.13	0.39	3.47 ± 0.93
Ours ($\gamma_C = 0, I_{KL} = 200$)	1.01	8.92	0.67	5.93	0.61	3.74	0.59	2.29	0.58	1.48	0.60	1.30	0.40	4.06 ± 1.18
Ours ($I_{KL} = 50$)	1.96	9.06	1.83	8.74	1.74	8.54	1.67	8.33	1.53	8.12	1.59	7.94	0.38	1.55 ± 0.61
Ours ($I_{KL} = 100$)	2.01	9.08	1.96	8.78	1.88	8.57	1.76	8.37	1.77	8.15	1.76	8.0	0.38	1.60 ± 0.78
Ours ($I_{KL} = 200$)	1.62	9.06	1.47	8.97	1.56	8.90	1.47	8.77	1.47	8.58	1.38	8.36	0.39	1.58 ± 0.71

Table 1. *Evaluation of Behavior Transfer.* We compare different models on the task of behavior transfer using different metrics. The regression error 'RE' denotes the mean squared error (MSE) when predicting the source behavior sequence x_β from the learned behavior representation z_β using a regression network trained on this task. 'TDE' refers to the total displacement error measured as the MSE between x_β and the re-enactment x_R . 'acc' denotes action classifier accuracy when using the respective behavior representations z_β as input. 'gt:0.45' denotes the accuracy of an action classifier directly trained in ground-truth keypoint sequences, thus representing an upper bound on performance. For the latent space distance d_β between the encodings of the source behavior x_β and the re-enactment x_R we report mean and standard deviation. Each metric is evaluated at timesteps $T \in \{1, 10, 20, 30, 40, 50\}$. Since we have no ground-truth data available for behavior transfer we cannot directly measure transfer performance. Instead, in Sec. 4.2 we show how the interplay of these metrics allow to evaluate transfer performance.

testing on two subjects (S9,S11). We refer the reader to the supplementary or project page² for video material.

4.1. Architecture and implementation details

For the task of human behavior transfer, we use sequences of 50 frames as input for our network. The encoder-decoder networks representing $q_\phi(z_\beta|\mathbf{x}, x_t)$ and $p_\theta(\mathbf{x}|z_\beta, x_t)$ are both implemented as a single-layer LSTM [27] with a hidden dimensionality of 1024. Mean and variance of $q_\phi(z_\beta|\mathbf{x}, x_t)$ are realized as linear layers based on the final hidden state of the encoder. For our decoder $p_\theta(\mathbf{x}|z_\beta, x_t)$ we initialize the hidden state with the behavior representation z_β . The target posture x_t is the input state of the decoder at the first time step. Subsequently the decoder uses its own predictions from the previous time step as input. For generating the individual postures, we follow [40] and use a single linear layer on top of the LSTM output combined with residual skip connection to the input. The generative model \hat{p}_ψ is implemented as a three-layer MLP to predict postures \mathbf{x} given z_β . We model $p_\theta(\mathbf{x}|z_\beta, x_t)$ and $p_\psi(\mathbf{x}|z_\beta)$ as Gaussian, thus the expectations in Eq. 5 translate to mean squared errors. We train the network for 50 epochs and set $\gamma_C = 0.1$ and $I_{KL} = 100$ as discussed in the quantitative evaluation.

Normalizing flow model \mathcal{T}_ξ . Our normalizing flow model \mathcal{T}_ξ is implemented as a stacked sequence of 15 invertible neural networks based on an input dimensionality of $D = 1024$. Each consists of 3 blocks of subsequently applied actnorm [33], affine coupling layers [16] and shuffling layers. The affine coupling layers consist of 2 fully connected layers with dimensionality $D = 1024$. We trained the normalizing flow model on a single Titan Xp for 5 epochs with batchsize

²<https://cutt.ly/517rXEp>

64 and ADAM [32] optimizer with learning rate 6.5×10^{-6} . Further information regarding our normalizing flow model is provided in the supplemental.

Model for posture-appearance transfer. In order to be able to synthesize realistic RGB videos of human behavior, we translate our generated postures to RGB images. To this end, we utilize our proposed framework for the task of shape and appearance disentanglement [13]. We train a model to obtain an appearance representation from static images, which is independent of the corresponding posture information. Thus, we can use our method to transfer behavior from a source sequence to a given target posture and generate an animated video sequence by frame-wise synthesizing RGB images. More details on our posture and appearance model and further results can be found in the supplemental.

4.2. Behavior re-enactment

We now evaluate our proposed model qualitatively and quantitatively for the task of behavior transfer and its abilities to sample and synthesize novel behavior.

Qualitative evaluation. Figure 3 shows examples of transferred behavior. We show the posture sequence x_β exhibiting a source behavior β (top row) and its transfer to different, unrelated postures x_t . The re-enactments depict both the re-enacted posture sequence and the rendered RGB video frames based on the model for posture and appearance transfer. Since our model captures behavior independent of posture, it successfully transfers only the characteristic body dynamics of β and infers potentially needed transitions itself. As a result, the target posture x_t is naturally animated to perform behavior β independent of diverse target postures,

Method	N=10		N=50	
	ASD	FSD	ASD	FSD
cVAE [64]	0.25	0.36	0.16	0.22
DSF [64]	0.38	0.62	0.31	0.42
Ours	0.63	0.88	0.45	0.58

Table 2. *Evaluation of Sampling Capabilities.* (a) Quantitative evaluation of diversity with ASD and FSD [64], numbers are taken from [64].

such as standing or sitting. For instance, in the example at the left top, each person accurately raises both hands to its head. Note that, in the last example on the top left, the person does not change its posture since the hands are already up. Moreover, the kneeling person on the bottom left only lowers its torso as its knees are already placed on the ground and cannot be bent further. More visual examples can be found in the supplemental. Video examples are provided on our project page².

Quantitative evaluation. We now evaluate how well our model transfers behavior β extracted from a source sequence x_β to an initial, unrelated target posture x_t taken from random, different sequences. Meaningful re-enactment of β should only transfer characteristic body dynamics to a target posture x_t . We compare our model to different baseline models, i.e. conditional autoencoder (cAE), vanilla conditional variational autoencoder (cVAE) and our model with and without our proposed posture disentanglement. Each model uses the same architectures except for deviations due to individual training objectives: The cAE is trained without disentanglement and without variational bottleneck. The cVAE is trained on the training objective Eq. (1). Moreover, we compare the MT-VAE [61] which uses latent space arithmetics to transform between different actions.

A model failing this task would typically generate (i) sequences which rather exactly copy full postures of the source sequence x_β in contrast to transferring only its characteristic dynamics to x_t ; or (ii) generating behavior different to β such as some likely future behavior of x_t . To identify (i), we measure the transfer displacement error (TDE), i.e. the displacement error between postures of the re-enactment x_R and source x_β at time-steps T . For (ii), since we have no ground-truth available for behavior transfer, we measure the average euclidean distance d_β in the representation space z_β between encodings of x_β and x_R . Combined, a well transferring model should yield re-enacted sequences x_R which is dissimilar to x_β , thus not merely copying postures (i.e. large TDE). Given this, both sequences should be similar in representation space (i.e. small d_β) to indicate their similarity in behavior. Moreover, the representations need to be informative to exclude degenerated solutions. For the latter we examine their benefit for action classification on H3.6M

Method	Type of synthesis			
	self	transfer	prior	flow
MT-VAE [61]	0.49	0.17	-	-
Ours ($\gamma_C = 0$)	0.49	0.14	0.09	0.12
Ours	0.49	0.23	0.13	0.23

Table 3. *Realism of behavior generations.* Evaluation of sampling quality using a discriminator classifying between ground-truth sequences and behavior generations of different origins: 'self' denotes video reconstructions, 'transfer' denotes generations depicting actual behavior transfer, i.e. using a randomly sampled starting posture and an extracted behavior $q_\phi(z_\beta|x, x_t)$, 'prior' denotes synthesizing behavior sampled from the prior representation $p(z_\beta)$ and 'flow' refers to synthesizing behavior sampled using the invertible mapping \mathcal{T}_ξ .

(acc.). For each experiment we provide detailed protocols and implementation details in the supplemental.

Tab. 1 evaluates these experiments. We observe that cAE exhibits a strong decline in TDE values as T increases, resulting in TDE values close to 0. Thus, this model accurately copies the posture sequence x_β , instead of inferring behavior β and potentially needed transitions itself (cf. suppl. video material). Consequently, its behavior representation only captures posture information, rather than body dynamics. In contrast, the cVAE model consistently reaches high TDE scores, thus generating posture sequences which are very different from x_β . However, the distance d_β shows that the model suffers from posterior collapse, hence z_β is neglected and only likely continuations following x_t are predicted (see also supplemental). Relaxing the information bottleneck of cVAE (i.e. our model without disentanglement, Eq.(4)) alleviates the posterior collapse and z_β becomes informative. Looking at different settings for I_{KL} , we see that TDE values slowly decrease with T and ranges between cAE and cVAE, while exhibiting large values of d_β . We attribute this to a distorted latent representation being learned. In contrast, our full model with explicit disentanglement of behavior and posture exhibits large TDE values matching those of the cVAE while at the same time mapping x_β and x_R close in z_β . Thus, since postures are very different, closeness in z_β arises from similarity in body dynamics, highlighting actual behavior transfer. The accuracy of the action classifier (*acc.*) confirms that the captured dynamics are informative, almost matching the classifier result when training on ground truth sequences. Moreover, the classifier performance for MT-VAE reveals that their latent space is significantly less informative than our behavior representation, which indicates limited motion transfer capabilities. Indeed, a large mean distance d_β of 4.44 shows a strong difference in representation between source and re-enacted behavior, most likely due to the linear arithmetics assumption not being hold.

To provide an additional, explicit measure for disentan-

	Pose-Knows	HP-GAN	GMVAE	DSF	DLOW	Ours
APD	6.72	7.24	6.77	9.33	11.74	12.24

Table 4. *Evaluation of Sampling Diversity*. Our model outperforms other approaches on human motion synthesis in terms of APD [63]. Numbers are taken from [63].

gement of behavior and posture, we adapt an evaluation procedure inspired by works on identifying latent factors of variation [42]. To this end, we train a regression network to predict posture coordinates of x_β from its encoding z_β at different time-steps and report the average regression errors (RE) in Tab. 1. Naturally, the cAE model results in very low errors due to copying, while the cVAE exhibits large REs due to the posterior collapse. Comparing our model with and without disentanglement demonstrates consistently higher prediction errors, indicating that only few posture information is encoded in z_β . Moreover, our analysis shows that our model is robust to the choice of I_{KL} . In the remainder of the experiments we choose $I_{KL} = 100$.

4.3. Sampling and synthesis of novel behavior

We now evaluate our model on the task of synthesizing novel behavior by sampling behavior representations z_β from the prior distribution $p(z_\beta)$. Following other approaches for human motion synthesis [63, 64, 1] we evaluate the aspect of sampling quality [1] and diversity [63, 64]. To address the first we train a binary classifier to distinguish between 25k ground-truth and 25k generated sequences. The accuracy of the classifier determines the realism of the evaluated samples and is reported in Tab. 3. The implementation details for the classifier can be found in the supplemental. Posture sequences synthesized using the explicit invertible mapping \mathcal{T}_ξ between prior and posterior $q_\phi(z_\beta|x, x_t)$ are more realistic than directly using prior samples. This is explained by the corrected mismatch between posterior and prior distribution and clearly demonstrated by the visual comparisons in the

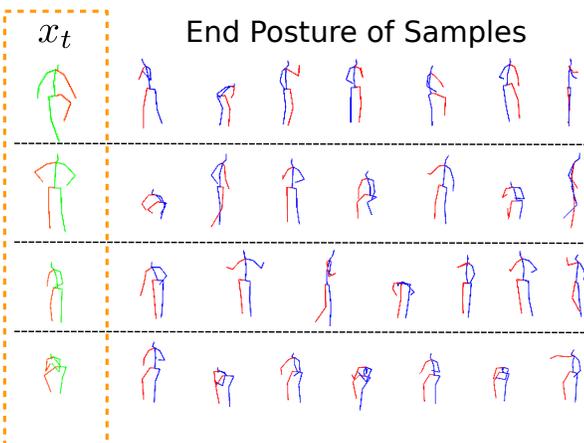


Figure 4. Qualitative visualization of diversity by showing the end poses from our sampled behaviors.

videos contained in the accompanying video material. Moreover, we observe that our explicit disentanglement of posture and behavior significantly improves the quality of samples. In particular, we also outperform MT-VAE [61] by relative 35% in behavior re-enactment (‘transfer’).

For evaluating diversity we follow the evaluation protocol of [63, 64] by using the following metrics: (i) Average Pairwise Distance (APD): Average euclidean distance between all pairwise combinations of generated sequences; (ii) Average Self Distance (ASD): Average euclidean distance between a generated sequence and its closest neighbor sequence among generations; and (iii) Final Self Distance (FSD): Euclidean distance between the last posture of a generated sequence and its closest neighbor’s final posture. Note, while APD is measuring the overall variance of the generated sequences, ASD and FSD assess the uniqueness of samples. Tab. 2 compares ASD and FSD scores of our model with the cVAE and the diversity sampler function (DSF) from [64] for sample-set sizes of $K \in \{10, 50\}$ while Tab. 4 we provide APD comparisons with various motion synthesis approaches. For each metric we outperform existing approaches by a significant margin, in particular such approaches [64, 63] which explicitly aim at sampling diversity. Finally, we visually demonstrate the diversity of our samples in Fig 4 by showing the final postures of sampled behaviors.

5. Discussion

We presented a conditional generative model for controlled synthesis and transfer of human behavior. To this end, we learn a dedicated representation for human behavior disentangled from posture. By extracting the characteristic body dynamics from a video depicting a certain behavior, our model is able to animate persons observed in significantly different postures. A particular challenge arises from animating postures which allow for no direct transfer of behavior dynamics, but require an intermediate transition. Correct inference of such transition is essentially a generalization problem asking for synthesis outside the training distribution. While our model successfully infers such transitions to a certain degree, it fails in cases of complex transitions needed, such as enacting a walking behavior by a person which is lying on the ground. This shows that our introduced problem requires a deep understanding of behavior, thus posing a new challenge for research on human motion synthesis in general.

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