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# MixPHM: Redundancy-Aware Parameter-Efficient Tuning for Low-Resource Visual Question Answering

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# Abstract

Recently, finetuning pretrained vision-language models (VLMs) has been a prevailing paradigm for achieving stateof-the-art performance in VQA. However, as VLMs scale, it becomes computationally expensive, storage inefficient, and prone to overfitting when tuning full model parameters for a specific task in low-resource settings. Although current parameter-efficient tuning methods dramatically reduce the number of tunable parameters, there still exists a significant performance gap with full finetuning. In this paper, we propose MixPHM, a redundancy-aware parameterefficient tuning method that outperforms full finetuning in low-resource VQA. Specifically, MixPHM is a lightweight module implemented by multiple PHM-experts in a mixtureof-experts manner. To reduce parameter redundancy, we reparameterize expert weights in a low-rank subspace and share part of the weights inside and across MixPHM. Moreover, based on our quantitative analysis of representation redundancy, we propose Redundancy Regularization, which facilitates MixPHM to reduce task-irrelevant redundancy while promoting task-relevant correlation. Experiments conducted on VQA v2, GQA, and OK-VQA with different low-resource settings show that our MixPHM outperforms state-of-the-art parameter-efficient methods and is the only one consistently surpassing full finetuning.

# 1. Introduction

Adapting pretrained vision-language models (VLMs) [4, 5, 24, 29, 30, 50, 57] to the downstream VQA task [1] in a finetuning manner has emerged as a dominant paradigm to achieve state-of-the-art performance. As the scale of VLMs continues to grow, finetuning the full model with millions or billions of parameters causes a substantial rise in computation and storage costs, as well as exposing the overfitting (poor performance) issue in low-resource learning. Parameter-efficient tuning methods [15, 16, 23, 38, 51, 56],

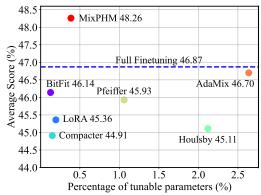


Figure 1. **Comparison between parameter-efficient methods.** In a low-resource setting (*i.e.*, with 64 training samples), we show the average score across five seeds on VQA v2 (y-axis) and the percentage of tunable parameters w.r.t. pretrained VL-T5 (x-axis).

updating only a tiny number of original parameters of pretrained models or the newly-added lightweight modules, are thus proposed to handle such challenges.

However, as illustrated in Figure 1, the aforementioned parameter-efficient tuning methods substantially reduce the number of tunable parameters, but their performance still lags behind full finetuning. Among them, the adapter-based methods (Houlsby [15], Pfeiffer [38], Compacter [23], and AdaMix [51]) are more storage-efficient, as they only store newly-added modules instead of a copy of entire VLMs, and they allow more flexible parameter sharing [43]. In particular, AdaMix enhances the capacity of adapters with a mixture-of-experts (MoE) [42] architecture and achieves comparable performance to full finetuning while slightly increasing the number of tunable parameters.

In this paper, we build upon adapter-based methods to investigate more parameter-efficient tuning methods that can outperform full finetuning on low-resource VQA. Specifically, when adapting pretrained VLMs to the given task, we consider two improvements: (*i*) *Reducing parameter redundancy while maintaining adapter capacity*. However, an excessive reduction of tunable parameters can lead to underfitting, preventing adapters from learning enough task-relevant information [23]. Therefore, it is crucial to strike

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a compromise between parameter efficiency and capacity. (*ii*) *Reducing task-irrelevant redundancy while promoting task-relevant correlation in representations*. Practically, through residual connection, adapters integrate task-specific information learned from a target dataset and prior knowledge already implied in pretrained VLMs. However, recent works [21, 33, 48] have suggested that pretrained models inevitably contain redundant and irrelevant information for target tasks, resulting in a statistically spurious correlation between representations and labels, thereby hindering performance and generalization [46, 49]. To improve their effectiveness, we thus expect adapters to learn as much task-relevant information as possible while discarding the task-irrelevant information from versatile pretrained VLMs.

To this end, we propose MixPHM, a redundancy-aware parameter-efficient tuning method, which can efficiently reduce the tunable parameters and task-irrelevant redundancy, and promote task-relevant correlation in representations. MixPHM is implemented with multiple PHM-experts in a MoE fashion. To reduce (i) parameter redundancy in Mix-PHM, we first decompose and reparameterize the expert weights into a low-rank subspace. Afterwards, we further reduce the number of parameters and transfer information with global and local weight sharing. To achieve the improvement (ii), we first quantify representation redundancy in adapter. The result shows that representations of adapters are redundant with representations of pretrained VLMs but exhibit limited correlation with the final task-used representations. Inspired by this insight, we then propose Redundancy Regularization. In MixPHM, the regularizer reduces task-irrelevant redundancy via decorrelating the similarly matrix between representations learned by MixPHM and representations obtained by pretrained VLMs. Simultaneously, it promotes task-relevant correlation by maximizing the mutual information between the learned representations and the final task-used representations.

We conduct extensive experiments on three datasets, *i.e.*, VQA v2 [11], GQA [19], and OK-VQA [36]. The proposed MixPHM consistently outperforms full finetuning and state-of-the-art parameter-efficient tuning methods. To gain more insights, we discuss the generalizability of our method and the effectiveness of its key components. Our contributions are summarized as follows: (1) We propose MixPHM, a redundancy-aware parameter-efficient tuning method that outperforms full finetuning in adapting pretrained VLMs to low-resource VQA. (2) We quantitatively analyze representation redundancy and propose redundancy regularization, which can efficiently reduce task-irrelevant redundancy while prompting task-relevant correlation. (3) Extensive experiments show that MixPHM achieves a better trade-off between performance and parameter efficiency, and a significant performance improvement over current parameter-efficient tuning methods.

# 2. Related Work

**Vision-Langauge Pretraining.** Vision-language pretraining [5,8,18,20,24,30,45,60,62] aims to learn task-agnostic multimodal representations for improving the performance of downstream tasks in a finetuning fashion. Recently, a line of research [4, 17, 29, 30, 50] has been devoted to leveraging encoder-decoder frameworks and generative modeling objectives to unify architectures and objectives between pretraining and finetuning. VLMs with an encoder-decoder architecture generalize better. In this paper, we explore how to better adapt them to low-resource VQA [1].

**Parameter-Efficient Tuning.** Finetuning large-scale pretrained VLMs on downstream datasets has become one mainstream paradigm for vision-language tasks. However, finetuning the full model consisting of millions of parameters is time-consuming and resource-intensive. Parameterefficient tuning [12, 34, 35, 41, 55, 56, 59] vicariously tunes lightweight trainable parameters while keeping (most) pretrained parameters frozen, which has shown great success in NLP tasks. According to whether new trainable parameters are introduced, these methods can be roughly categorized into two groups: (1) tuning partial parameters of pretrained models, such as BitFit [56] and FISH Mask [44], (2) tuning additional parameters, such as prompt (prefix)-tuning [27, 31], adapter [15, 38], and low-rank methods [16, 23].

Motivated by the success in NLP, some works [32,43,61] have begun to introduce parameter-efficient methods to tune pretrained VLMs for vision-language tasks. Specifically, Lin *et al.* [32] investigate action-level prompts for vision-language navigation. VL-Adapter [43] extends adapters to transfer VLMs for various vision-language tasks. HyperPELT [61] is a unified parameter-efficient framework for vision-language tasks, incorporating adapter and prefix-tuning. In addition, Frozen [47] and PICa [54] use prompt-tuning techniques [27] to transfer the few-shot learning ability of large-scale pretrained language models to handle few-shot vision-language tasks. FewVLM [22] designs hand-crafted prompts to finetune pretrained VLMs for low-resource adaptation. In contrast, low-rank methods are more parameter-efficient but are rarely explored.

**Mixture-of-Experts.** MoE [42] aims to scale up model capacities and keep computational efficiency with conditional computation. Most recent works [6, 7, 26, 28, 39, 40] investigate how to construct large-scale vision or language transformer models using MoE and well-designed routing mechanisms in the pretraining stage. Despite its success in pretraining, MoE has not been widely explored in parameter-efficient tuning. MPOE [10] and AdaMix [51] are two recent works that tune pretrained language models by MoE. Specifically, MPOE considers additional FFN layers as experts and decomposes weight matrices of experts with MPO. AdaMix treats the added adapters as experts and increases adapter capacity by a stochastic routing strategy.

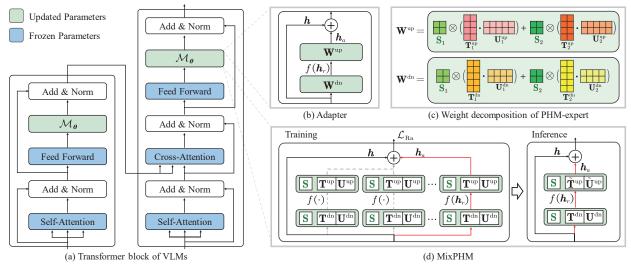


Figure 2. Illustration of MixPHM inserted into (a) one transformer block of VLMs. (b) The structure of standard adapter. (c) An example of the weight matrix decomposition in Eq. (13) for a PHM-expert (here n = 2, d = 10,  $d_r = 8$ ,  $d_k = 2$ ). (d) MixPHM architecture with  $N_e = 3$  PHM-experts. During training, MixPHM randomly activates one PHM-expert to learn robust representations and exploits the proposed redundancy regularization  $\mathcal{L}_{Ra}$  to reduce task-irrelevant redundancy while promoting task-relevant correlation.

### 3. Preliminary

forms an input  $\boldsymbol{x} \in \mathbb{R}^d$  to an output  $\boldsymbol{y} \in \mathbb{R}^{d_e}$ , *i.e.*,

$$\boldsymbol{y} = \mathbf{W}^{\mathrm{T}} \boldsymbol{x} + \boldsymbol{b}, \qquad (2)$$

**Problem Definition.** We follow recent work [4, 52] to formulate VQA as a generative modeling task, *i.e.*, generating free-form textual answers for a given question instead of selecting a specific one from the predefined set of answers. Formally, we denote a VQA dataset with  $\mathcal{D} = \{(I, Q, y) \in \mathcal{I} \times \mathcal{Q} \times \mathcal{Y}\}$ , where *I* is an image, *Q* is a question, and *y* is an answer. Assuming that a given pretrained VLMs  $\mathcal{M}_{\Theta}$ is parameterized by a tiny number of tunable parameters  $\theta$ , the general problem of adapting pretrained VLMs for VQA is to tune  $\mathcal{M}_{\theta}$  in a parameter-efficient manner on  $\mathcal{D}$ .

**Mixture-of-Experts.** A standard MoE [42] is implemented with a set of  $N_e$  experts  $\{E_i\}_{i=1}^{N_e}$  and a gating network G. Each expert is a sub-neural network with unique weights and can learn from a task-specific subset of inputs. The gate conditionally activates  $N_a$   $(1 \le N_a \le N_e)$  experts. Formally, given an input representation  $x \in \mathbb{R}^d$ , the *i*-th expert maps x into  $d_e$ -dimensional space, *i.e.*,  $E_i(\cdot) : x \to \mathbb{R}^{d_e}$ , the gate generates a sparse  $N_e$ -dimensional vector, *i.e.*,  $G(\cdot) : x \to \mathbb{R}^{N_e}$ . Then, the output  $y \in \mathbb{R}^{d_e}$  of the MoE can be formulated as

$$\boldsymbol{y} = \sum_{i=1}^{N_e} G(\boldsymbol{x})_i E_i(\boldsymbol{x}), \tag{1}$$

where,  $G(\boldsymbol{x})_i$  denotes the probability of assigning  $\boldsymbol{x}$  to the *i*-th expert, satisfying  $\sum_{i=1}^{N_e} G(\boldsymbol{x})_i = 1$ .

**Parameterized Hypercomplex Multiplication.** The PHM layer [58] aims to generalize hypercomplex multiplications to fully-connected layer by learning multiplication rules from data. Formally, for a fully-connected layer that trans-

where, 
$$\mathbf{W} \in \mathbb{R}^{d \times d_e}$$
. In PHM, the weight matrix  $\mathbf{W}$  is learned via the summation of *n* Kronecker products between  $\mathbf{S}_i \in \mathbb{R}^{n \times n}$  and  $\mathbf{A}_i \in \mathbb{R}^{\frac{d}{n} \times \frac{d_e}{n}}$ :

$$\mathbf{W} = \sum_{j=1}^{n} \mathbf{S}_{j} \otimes \mathbf{A}_{j}, \tag{3}$$

where, the hyperparameter  $n \in \mathbb{Z}_{>0}$  controls the number of the above summations, d and  $d_e$  are divisible by n, and  $\otimes$  indicates the Kronecker product that generalizes the vector outer products to higher dimensions in real space. For example, the Kronecker product between  $\mathbf{S} \in \mathbb{R}^{m \times k}$  and  $\mathbf{A} \in \mathbb{R}^{p \times q}$  is a block matrix  $\mathbf{S} \otimes \mathbf{A} \in \mathbb{R}^{mp \times kq}$ , *i.e.*,

$$\mathbf{S} \otimes \mathbf{A} = \begin{bmatrix} s_{11}\mathbf{A} & \cdots & s_{1k}\mathbf{A} \\ \vdots & \ddots & \vdots \\ s_{m1}\mathbf{A} & \cdots & s_{mk}\mathbf{A} \end{bmatrix}, \quad (4)$$

where,  $s_{ij}$  denotes the element of matrix **S** at the *i*-th row and *j*-th column. As a result, replacing a fully-connected layer with PHM can reduce the trainable parameters by at most 1/n of the fully-connected layer.

# 4. Methodology

We propose MixPHM, a redundancy-aware parameterefficient tuning method to adapt pretrained VLMs. This section first quantifies and analyzes the redundancy in adapters toward low-resource VQA (Sec. 4.1). Then, we sequentially elaborate on architecture (Sec. 4.2), redundancy regularization (Sec. 4.3), and inference (Sec. 4.4) of MixPHM.

#### 4.1. Rethinking Redundancy in Adapter

As shown in Figure 2 (b), adapter [15] is essentially a lightweight module, usually implemented by a two-layer feed-forward network with a bottleneck, a nonlinear function, and a residual connection. When learning downstream tasks, adapters are inserted between the transformer layers of VLMs, and only the parameters of the newly added adapters are updated, while the original parameters of pre-trained VLMs remain frozen. Formally, given an input representation  $h \in \mathbb{R}^d$ , the down-projection layer  $\mathbf{W}^{dn} \in \mathbb{R}^{d \times d_r}$  maps h to a lower-dimensional space specified by the bottleneck dimension  $d_r$ , *i.e.*,  $h_r \in \mathbb{R}^{d_r}$ . The upprojection layer  $\mathbf{W}^{up} \in \mathbb{R}^{d_r \times d}$  maps  $h_r$  back to the input size, *i.e.*,  $h_a \in \mathbb{R}^d$ . Considering the residual and nonlinear function f, an adapter is defined as

$$\boldsymbol{h}_a = f(\boldsymbol{h} \mathbf{W}^{\mathrm{dn}}) \mathbf{W}^{\mathrm{up}},\tag{5}$$

$$\boldsymbol{h} \leftarrow \boldsymbol{h}_a + \boldsymbol{h}.$$
 (6)

Ideally, by incorporating task-specific information learned from a downstream dataset ( $h_a$ ) and prior knowledge already encoded in pretrained VLMs (h), adapters can quickly transfer pretrained VLMs to new tasks without over-parameterization or under-parameterization.

**Redundancy Analysis of Adapter.** However, recent investigation has shown that some of the information captured by adapters is task-agnostic [13]. To get the facts, we leverage Representational Similarity Analysis (RSA) [25] to assess the redundancy in representation spaces. Specifically, we first tune the pretrained VL-T5 [4] with Pfeiffer [38] on 1k samples from VQA v2 training set [11]. Then, we randomly sample 1k samples from VQA v2 val set and extract token-level representations (*i.e.*, h and  $h_a$ ) at each transformer layer as well as the final output representation  $\tilde{h}$  of transformer encoder/decoder. Finally, for each sample, we can obtain  $N_t$  token-level representations at each layer, *i.e.*,  $\mathbf{H} = \{h\}_{i=1}^{N_t} \in \mathbb{R}^{N_t \times d}, \mathbf{H}_a = \{h_a\}_{i=1}^{N_t} \in \mathbb{R}^{N_t \times d}$  and  $\tilde{\mathbf{H}} = \{\tilde{h}\}_{i=1}^{N_t} \in \mathbb{R}^{N_t \times d}$ . In each layer, we compute RSA similarity between  $h_a$  and h as well as  $h_a$  and  $\tilde{h}$  by

$$\operatorname{RSA}(\boldsymbol{h}_a, \boldsymbol{h}) = f_{\rho}(f_{\mathrm{U}}[\mathbf{H}_a \mathbf{H}_a^{\mathrm{T}}], f_{\mathrm{U}}[\mathbf{H} \mathbf{H}^{\mathrm{T}}]), \qquad (7)$$

$$\operatorname{RSA}(\boldsymbol{h}_a, \boldsymbol{\dot{h}}) = f_{\rho}(f_{\mathrm{U}}[\mathbf{H}_a \mathbf{H}_a^{\mathrm{T}}], f_{\mathrm{U}}[\mathbf{\ddot{H}}\mathbf{\ddot{H}}^{\mathrm{T}}]), \qquad (8)$$

where,  $f_{\rm U}[\cdot]$  denotes an operation of taking the upper triangular elements from a matrix,  $f_{\rho}$  is a function to compute the Pearson correlation coefficient. Figure 3 illustrates the average RSA similarity across 1k samples, which demonstrates that in transformer layers, the adapter representation  $h_a$  is redundant with the representation h of pretrained VLMs, but has limited correlation to the final output  $\tilde{h}$ .

Intuitively, to transfer pretrained VLMs to downstream tasks efficiently, the representation  $h_a$  learned by adapter needs to contain as much information as possible from

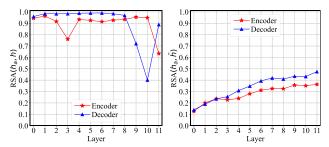


Figure 3. The average RSA similarity across 1k samples between  $h_a$  and h (left) as well as  $h_a$  and  $\tilde{h}$  (right) at each transformer layer. The higher the RSA, the more similar (redundant) the representation spaces are.

the task-relevant representation  $\tilde{h}$ , while reducing taskirrelevant redundancy with the representation h of pretrained VLMs. However, Figure 3 exhibits a counterintuitive result. Therefore, in order to improve the effectiveness of adapters, it is crucial to *encourage task-relevant correlation between*  $h_a$  *and*  $\tilde{h}$  *while reducing task-irrelevant redundancy between*  $h_a$  *and* h.

#### 4.2. MixPHM Architecture

As illustrated in Figure 2, MixPHM is also a lightweight module inserted into each transformer block of VLMs. We utilize transformer-based encoder-decoder models as underlying pretrained VLMs, which consists of repeated Lencoder and L decoder blocks. Specifically, for the *l*-th  $(1 \le l \le L)$  block, we insert a MixPHM composed of a set of  $N_e$  PHM-experts  $\{E_i^l\}_{i=1}^{N_e}$  after the feed-forward layer to capture the knowledge and learn task-specific information. As with the adapter, each PHM-expert is implemented by a bottleneck network with down- and up-projection layers.

To reduce *parameter redundancy* in MixPHM, we first decompose and reparameterize the projection matrices of experts in MixPHM into low-dimensional subspace. Then, we further reduce the number of parameters and transfer information using a strategy of global and local expert weight sharing. Moreover, a stochastic routing [51,63] is employed for expert selection to avoid gating networks from introducing additional trainable parameters.

**Parameter-Efficient Tuning.** At each training (tuning) iteration, we randomly select one expert from the inserted  $N_e$  PHM-experts in the *l*-th transformer block. Once the expert  $E_i^l$  is selected, all inputs in a given batch are processed by the same expert. Formally, in the *l*-th block<sup>1</sup>, for a token input representation  $h \in \mathbb{R}^d$ , the randomly selected *i*-th expert encodes and updates h by

$$\boldsymbol{h} \leftarrow f(\boldsymbol{h} \mathbf{W}_i^{\mathrm{dn}}) \mathbf{W}_i^{\mathrm{up}} + \boldsymbol{h}. \tag{9}$$

In Eq. (9), the down-projection matrix  $\mathbf{W}_{i}^{dn} \in \mathbb{R}^{d \times d_{r}}$  and up-projection matrix  $\mathbf{W}_{i}^{up} \in \mathbb{R}^{d_{r} \times d}$  are firstly decomposed

<sup>&</sup>lt;sup>1</sup>For brevity, the superscript l is omitted hereafter.

into low-dimensional matrices using PHM, i.e.,

$$\mathbf{W}_{i}^{\mathrm{dn}} = \sum_{j=1}^{n} \mathbf{S}_{i,j} \otimes \mathbf{A}_{i,j}^{\mathrm{dn}}, \quad \mathbf{W}_{i}^{\mathrm{up}} = \sum_{j=1}^{n} \mathbf{S}_{i,j} \otimes \mathbf{A}_{i,j}^{\mathrm{up}}, \quad (10)$$

where,  $\mathbf{S}_{i,j} \in \mathbb{R}^{n \times n}$ ,  $\mathbf{A}_{i,j}^{dn} \in \mathbb{R}^{\frac{d}{n} \times \frac{d_{r}}{n}}$ ,  $\mathbf{A}_{i,j}^{up} \in \mathbb{R}^{\frac{d}{n} \times \frac{d}{n}}$ . To be more parameter-efficient, the matrix  $\mathbf{A}_{i,j}^{dn}$  ( $\mathbf{A}_{i,j}^{up}$ ) is further factorized into two low-rank matrices by

$$\mathbf{A}_{i,j}^{\text{dn}} = \mathbf{T}_{i,j}^{\text{dn}} (\mathbf{U}_{i,j}^{\text{dn}})^{\text{T}}, \quad \mathbf{A}_{i,j}^{\text{up}} = \mathbf{T}_{i,j}^{\text{up}} (\mathbf{U}_{i,j}^{\text{up}})^{\text{T}},$$
(11)

where,  $\mathbf{T}_{i,j}^{\text{dn}} \in \mathbb{R}^{\frac{d}{n} \times d_k}$ ,  $\mathbf{U}_{i,j}^{\text{dn}} \in \mathbb{R}^{\frac{d_r}{n} \times d_k}$ ,  $\mathbf{T}_{i,j}^{\text{up}} \in \mathbb{R}^{\frac{d_r}{n} \times d_k}$ ,  $\mathbf{U}_{i,j}^{\text{up}} \in \mathbb{R}^{\frac{d}{n} \times d_k}$ , and  $d_r$  is the rank of these matrices. Finally, we learn the weight matrices of the *i*-th PHM-expert by

$$\mathbf{W}_{i}^{\mathrm{dn}} = \sum_{j=1}^{n} \mathbf{S}_{i,j} \otimes (\mathbf{T}_{i,j}^{\mathrm{dn}} (\mathbf{U}_{i,j}^{\mathrm{dn}})^{\mathrm{T}}), \qquad (12)$$

$$\mathbf{W}_{i}^{\mathrm{up}} = \sum_{j=1}^{n} \mathbf{S}_{i,j} \otimes (\mathbf{T}_{i,j}^{\mathrm{up}} (\mathbf{U}_{i,j}^{\mathrm{up}})^{\mathrm{T}}).$$
(13)

**Information Sharing across PHM-Experts.** When tuning pretrained VLMs with MixPHM on a downstream dataset, the set of *n* matrices  $\{S_{i,j}\}_{j=1}^{n}$  of the *i*-th PHM-expert are globally shared among all PHM-experts across transformer blocks to capture general information for the target task. On the contrary,  $\{A_{i,j}^{dn}\}_{j=1}^{n}$  and  $\{A_{i,j}^{up}\}_{j=1}^{n}$  are expert-specific weight matrices that are unique to each PHM-expert. To better transfer information between PHM-experts of Mix-PHM and further reduce parameter redundancy, we locally share  $\{A_{i,j}^{dn}\}_{j=1}^{n}$  among PHM-experts in each MixPHM.

At this point, the total number of trainable parameters inserted into pretrained VLMs using MixPHM is reduced from the original  $4LN_e(dd_r)$  to  $2Ld_k(d+d_r)(N_e+1)+n^3$ .

# 4.3. Redundancy Regularization

Motivated by the insight discussed in Sec. 4.1, we propose redundancy regularization. Specifically, for the Mix-PHM in the *l*-th transformer block, we ensemble its token-level output representation  $\{h_a\}_{i=1}^N$  and its residual  $\{h\}_{i=1}^N$  of a batch to  $\mathbf{Z}_a \in \mathbb{R}^{N \times d}$  and  $\mathbf{Z} \in \mathbb{R}^{N \times d}$ ,  $N = N_b N_t$  ( $N_b$  indicates batch size). For the transformer encoder/decoder, we average the final output representation  $\{\tilde{h}\}_{i=1}^N$  of a batch along the token dimension and obtain a global task-relevant representation  $\{\bar{h}\}_{i=1}^{N_b}$ . Then, the redundancy regularization can be expressed by

$$\mathcal{L}_{\text{Ra}} \triangleq \sum_{i}^{N} \sum_{j \neq i}^{N} \frac{\mathbf{Z}_{a} \mathbf{Z}^{\text{T}}}{\|\mathbf{Z}_{a}\|_{2} \|\mathbf{Z}\|_{2}} - \sum_{i}^{N_{b}} \sum_{j}^{N_{t}} \hat{\mathcal{I}}(\boldsymbol{h}_{ai,j}; \bar{\boldsymbol{h}}_{i}), \quad (14)$$

where,  $\|\cdot\|_2$  denotes the  $L_2$  norm,  $\hat{\mathcal{I}}(\cdot; \cdot)$  means the estimation of mutual information, and  $h_{a_{i,j}}$  is the output representation of the *j*-th token of the *i*-th sample in a batch. In

this paper, we adopt the JSD MI estimator [14] to maximize the mutual information between two representations. In redundancy regularization  $\mathcal{L}_{Ra}$ , the first term is a redundancy reduction term, which encourages  $h_a$  to discard taskirrelevant information from pretrained VLMs via approximating the off-diagonal elements of the cosine similarity matrix between  $h_a$  and h to zero. The second term aims to advocate  $h_a$  contain more task-relevant information from downstream datasets by maximizing the mutual information between  $h_a$  and  $\bar{h}$ .

Formulating VQA as a generative modeling task, the objective is to minimize the negative log-likelihood of answer y tokens given input image I and question Q. Therefore, the total training loss in parameter-efficient tuning is

$$\mathcal{L} = -\sum_{j=1}^{|y|} \log P_{\theta}(y_j | y_{< j}; I, Q) + \alpha \mathcal{L}_{\text{Ra}}, \qquad (15)$$

where,  $\alpha$  is a factor to balance redundancy regularization.

#### 4.4. Inference

In contrast to the stochastic routing utilized during training, we adopt a weight aggregation strategy [53] to obtain a final PHM-expert for each MixPHM during inference. Specifically, one MixPHM has  $N_e$  PHM-experts. When learning weights in a low-rank subspace, each expert has 2nexpert-specific matrices  $\{\mathbf{T}_j^{up}, \mathbf{U}_j^{up}\}_{j=0}^n$ , and the  $N_e$  experts have the same 2n locally-shared matrices  $\{\mathbf{T}_j^{dn}, \mathbf{U}_j^{dn}\}_{j=0}^n$ as well as n globally-shared matrices  $\{\mathbf{S}_j\}_{j=1}^n$ . To obtain weights of the final PHM-expert, we first merge the weights of up-projection matrices by averaging the corresponding  $N_e$  weight matrices. Mathematically, the *j*-th up-projection matrices can be computed with

$$\widetilde{\mathbf{T}}_{j}^{\mathrm{up}} = \frac{1}{N_{e}} \sum_{i=1}^{N_{e}} \mathbf{T}_{ji}^{\mathrm{up}}, \quad \widetilde{\mathbf{U}}_{j}^{\mathrm{up}} = \frac{1}{N_{e}} \sum_{i=1}^{N_{e}} \mathbf{U}_{ji}^{\mathrm{up}}.$$
 (16)

Due to the global and local weight sharing, we need not perform weight aggregation on  $\{S_j\}_{j=1}^n$  and  $\{T_j^{dn}, U_j^{dn}\}_{j=0}^n$ . Finally, we employ the merged expert to compute the output representations of MixPHM at each transformer block.

#### 5. Experiment

#### 5.1. Experimental Setting

**Datasets and Metrics.** We conduct experiments on three datasets, VQA v2 [11], GQA [19], and OK-VQA [36]. To simulate the low-resource setting for VQA, we follow the work [3] and consider the training data size  $N_D$  for low-resource VQA to be smaller than 1,000. For more practical low-resource learning, we follow *true fewshot learning* [9, 37] and utilize the development set  $D_{dev}$ , which has the same size with the training set  $D_{train}$  (*i.e.*,

D. ( )	M-411	#Param		#Sample					
Dataset	Method	(M)	(%)	$N_{\mathcal{D}}$ =16	$N_{\mathcal{D}}=32$	$N_{\mathcal{D}}$ =64	$N_{\mathcal{D}}=100$	$N_{\mathcal{D}}$ =500	$N_{\mathcal{D}}$ =1,000
	Finetuning	224.54	100%	$41.82 \pm 1.58$	$43.09 \pm 3.10$	$46.87 \pm 0.57$	$48.12 \pm 0.87$	$53.46 \pm 0.41$	$55.56 \pm 0.13$
	BitFit [56]	0.29	0.13%	$40.61 \pm 4.15$	$43.86 \pm 2.19$	$46.14 \pm 1.00$	$47.53 \pm 0.67$	$51.91 \pm 0.40$	$53.18 \pm 0.58$
	LoRA [16]	0.44	0.20%	$41.60 \pm 2.27$	$42.62 \pm 2.41$	$45.36 \pm 1.66$	$47.57 \pm 0.91$	$51.93 \pm 0.38$	$54.15 \pm 0.45$
VQA v2	Compacter [23]	0.34	0.15%	$39.28 \pm 1.87$	$42.47 \pm 2.76$	$44.91 \pm 1.27$	$46.28 \pm 1.37$	$51.21 \pm 0.90$	$53.39 \pm 0.54$
[11]	Houlsby [15]	4.76	2.12%	$41.71 \pm 2.16$	$44.01 \pm 2.09$	$45.11 \pm 1.40$	$47.71 \pm 0.78$	$52.27 \pm 1.05$	$54.31 \pm 0.34$
	Pfeiffer [38]	2.38	1.06%	$41.48 \pm 1.86$	$44.18 \pm 2.13$	$45.93 \pm 1.11$	$47.42 \pm 1.15$	52.35 ±0.52	$53.98 \pm 0.38$
	AdaMix [51]	5.92	2.64%	$40.59 \pm 2.05$	$43.42 \pm 2.08$	$46.70 \pm 1.32$	$47.34 \pm 0.91$	$51.72 \pm 1.05$	$54.12 \pm 0.63$
	MixPHM	0.87	0.39%	$43.13 \ _{\pm 1.78}$	$45.97 \pm 2.01$	$48.26 \pm 0.56$	$49.91 \pm 0.76$	$54.30 \ _{\pm 0.33}$	$56.11 \pm 0.40$
	Finetuning	224.54	100%	$28.24 \pm 2.08$	$30.80 \pm 2.49$	$34.22 \pm 0.59$	36.15 ±0.99	$41.49 \pm 0.54$	$43.04 \pm 0.57$
GQA [19]	BitFit [56]	0.29	0.13%	$26.13 \pm 2.83$	$29.00 \pm 4.81$	$34.25 \pm 1.16$	$35.91 \pm 1.22$	$40.08 \pm 0.42$	$41.84 \pm 0.15$
	LoRA [16]	0.44	0.20%	$26.89 \pm 2.74$	$30.40 \pm 2.27$	$34.40 \pm 0.99$	$36.14 \pm 1.10$	$40.20 \pm 1.02$	$42.06 \pm 1.12$
	Compacter [23]	0.34	0.15%	$23.70 \pm 2.10$	$27.18 \pm 2.61$	$32.70 \pm 1.30$	$35.28 \pm 1.45$	$38.68 \pm 0.50$	$41.17 \pm 0.95$
	Houlsby [15]	4.76	2.12%	$25.13 \pm 2.32$	$28.34 \pm 1.17$	$33.23 \pm 0.94$	$35.88 \pm 1.79$	$40.85 \pm 0.48$	$41.90 \pm 0.72$
	Pfeiffer [38]	2.38	1.06%	$25.08 \pm 1.81$	$29.18 \pm 1.32$	$32.97 \pm 0.84$	$35.08 \pm 1.01$	$40.30 \pm 0.40$	$41.39 \ {\pm 0.27}$
	AdaMix [51]	5.92	2.64%	$24.62 \pm 2.34$	$28.01 \pm 1.33$	$32.74 \pm 0.96$	$35.64 \pm 0.94$	$40.14 \pm 0.42$	$41.97 \pm 0.86$
	MixPHM	0.87	0.39%	$28.33 \pm 2.63$	$32.40 \pm 2.52$	$36.75 \pm 0.55$	$37.40 \pm 0.87$	$41.92 \pm 0.55$	$43.81 \pm 0.50$
OK-VQA [36]	Finetuning	224.54	100%	$11.66 \pm 2.08$	$14.20 \pm 0.78$	$16.65 \pm 1.02$	$18.28 \pm 0.67$	$24.07 \pm 0.40$	$26.66 \pm 0.72$
	BitFit [56]	0.29	0.13%	$11.29 \pm 1.79$	$13.66 \pm 1.49$	$15.29 \pm 0.57$	$16.51 \pm 0.53$	$22.54 \pm 0.57$	$24.80 \pm 0.63$
	LoRA [16]	0.44	0.20%	$10.26 \pm 1.53$	$12.46 \pm 1.82$	$15.95 \pm 0.38$	$17.03 \pm 0.82$	$23.02 \pm 0.41$	$25.26 \pm 0.53$
	Compacter [23]	0.34	0.15%	$9.64 \pm 2.73$	$11.04 \pm 1.39$	13.57 ±1.07	$15.92 \pm 1.18$	$22.20 \pm 0.89$	$24.52 \pm 0.59$
	Houlsby [15]	4.76	2.12%	$9.79 \pm 1.71$	$12.25 \pm 2.13$	$15.04 \pm 1.25$	$16.58 \pm 0.65$	$22.67 \pm 0.77$	$25.04 \pm 0.44$
	Pfeiffer [38]	2.38	1.06%	$9.06 \pm 0.53$	$11.39 \pm 0.79$	$14.23 \pm 1.54$	$16.34 \pm 0.79$	$22.90 \pm 1.03$	$26.70 \pm 0.71$
	AdaMix [51]	5.92	2.64%	$8.39 \pm 1.20$	$11.55 \pm 1.37$	13.66 ±2.29	$16.27 \pm 0.92$	$23.20 \pm 0.78$	$26.34 \pm 0.88$
	MixPHM	0.87	0.39%	13.87 ±2.39	$16.03 \pm 1.23$	$18.58 \pm 1.42$	$20.16 \pm 0.97$	$26.08 \pm 0.88$	$28.53 \pm 0.85$

Table 1. **Experimental results with pretrained VL-T5.** The average VQA-Score with standard deviation across 5 seeds are evaluated on VQA v2 validation set, GQA test-dev, and OK-VQA test set. The best and second best parameter-efficient tuning methods are highlighted. The number of tuned parameters and the percentage of tuned parameters relative to VL-T5 (*i.e.*, 224.54M) are reported.

 $|\mathcal{D}_{\text{dev}}| = |\mathcal{D}_{\text{train}}| = N_{\mathcal{D}}$ ), instead of using large-scale validation set, for best model selection and hyperparameter tuning. Specifically, we conduct experiments on  $N_{\mathcal{D}} \in \{16, 32, 64, 100, 500, 1000\}$ . To construct the  $\mathcal{D}_{\text{train}}$  and  $\mathcal{D}_{\text{dev}}$  of VQA v2, we randomly sample  $2N_{\mathcal{D}}$  samples from its training set and divide them equally into the  $\mathcal{D}_{\text{train}}$  and  $\mathcal{D}_{\text{dev}}$ . Analogously, we construct  $\mathcal{D}_{\text{train}}$  and  $\mathcal{D}_{\text{dev}}$  for GQA and OK-VQA. VQA-Score [1] is the accuracy metric of the low-resource VQA task.

**Baselines.** We compare our method with several state-ofthe-art parameter-efficient tuning methods and finetuning. For a fair comparison, we perform hyperparameter search on their key hyperparameters (KHP) and report their best performance. Specifically,

- **BitFit** [56] only tunes the bias weights of pretrained models while keeping the rest parameters frozen.
- LoRA [16] tunes additional low-rank matrices, which are used to approximate the query and value weights in each transformer self-attention and cross-attention layer. KHP is the matrix rank (r).
- **Compacter** [23] adds adapters after each feed-forward layer of transformer blocks and reparameterizes adapter weights with low-rank PHM layers [58]. KHP are the number of summations of Kronecker product (n), the bot-tleneck dimension  $(d_r)$ , and r.
- Houlsby [15] adds adapters after self-attention and feedforward layers in each transformer block. KHP is  $d_r$ .

Method	Model Size	#Param (%)	VQAv2	GQA	OK-VQA
Frozen [47]	7B	-	38.2	12.6	-
PICa-Base [54]	175B	-	54.3	43.3	-
PICa-Full [54]	175B	-	56.1	48.0	-
FewVLM [22]	225M	100%	48.2	32.2	15.0
$MixPHM^{\dagger}$	226M	0.39%	49.3	33.4	19.2

Table 2. Comparison with few-shot learner ( $N_D$ =64). FewVLM is a prompt-based full finetuning method. MixPHM<sup>†</sup> means using MixPHM to tune FewVLM in a parameter-efficient manner.

- **Pfeiffer** [38] is to determine the location of adapter based on pilot experiments. In this work, we place it after each transformer feed-forward layer. KHP is  $d_r$ .
- AdaMix [51] adds multiple adapters after each transformer feed-forward layer in a MoE manner. KHP are the number of adapters  $(N_e)$ , and  $d_r$ .

**Implementation Details.** We use four pretrained VLMs, *i.e.*, VL-T5 [4], X-VLM [57], BLIP [29], and OFA<sub>Base</sub> [50], as underlying encoder-decoder transformers, which formulate VQA as a generation task in finetuning and do not introduce additional parameters from VQA heads. Since the original pretraining datasets used by VL-T5 contain samples of the above VQA datasets, we instead load the weights<sup>2</sup> released by Jin *et al.* [22], which is re-trained without the overlapped samples. All results are reported across five seeds  $\{13, 21, 42, 87, 100\}$ . More details and hyperparameter setups are provided in the supplementary material.

<sup>&</sup>lt;sup>2</sup>https://github.com/woojeongjin/FewVLM

Method	VQA v2	GQA	OK-VQA
Finetuning	$46.87 \pm 0.57$	$34.22 \pm 0.59$	$16.65 \pm 1.02$
MixPHM*	$47.30 \pm 0.67$	$34.66 \pm 0.78$	$18.05 \pm 1.16$
+ $\mathcal{L}_{cs}$	$46.70 \pm 0.66$	$34.83 \pm 1.35$	17.37 ±1.38
$+ \mathcal{L}_{Ra}^{I}$	$47.42 \pm 0.71$	$34.69 \pm 0.96$	$18.25 \pm 1.54$
$\mathcal{L}_{Ra}^{I}$ + $\mathcal{L}_{Ra}^{II}$	$47.71 \pm 0.85$	$36.10 \pm 0.83$	$18.21 \pm 1.08$
$+ \mathcal{L}_{Ra}$	<b>48.26</b> $\pm 0.56$	$36.75 \pm 0.55$	$\textbf{18.58} \pm 1.42$

Table 3. Ablation on different regularizers with  $N_D = 64$ . MixPHM<sup>\*</sup> means the baseline without any regularizer.  $\mathcal{L}_{cs}$  is a consistency regularizer [63].  $\mathcal{L}_{Ra}^{I}$  and  $\mathcal{L}_{Ra}^{II}$  indicate that only using the first and the second term of  $\mathcal{L}_{Ra}$ , respectively.

#### 5.2. Low-Resource Visual Question Answering

Table 1 shows the results with pretrained VL-T5 [4] on three datasets. Overall, our MixPHM outperforms state-ofthe-art parameter-efficient tuning methods and is the only one that consistently outperforms full finetuning. Next, we detail the different comparisons.

**Comparison with AdaMix.** AdaMix and MixPHM adopt MoE to boost the capacity of adapters, but MixPHM considers further reducing parameter redundancy and learning more task-relevant representations. Table 1 shows that on all datasets with different  $N_D$ , our MixPHM markedly outperforms AdaMix and full finetuning, while AdaMix fails to outperform full finetuning (except VQA v2 with  $N_D = 32$ ). This result demonstrates the effectiveness of MixPHM in terms of performance and parameter efficiency, which also suggests the importance of prompting task-relevant correction while reducing parameter redundancy.

**Comparison with Houlsby and Pfeiffer.** PHM-expert in MixPHM has the same bottleneck structure with adapter. However, PHM-expert is more parameter-efficient due to the reduction of parameter redundancy and can better capture task-relevant information owing to the proposed redundancy regularization. The result in Table 1 shows that compared to Finetuning, the performance of Houlsby and Pfeiffer falls far short of the ceiling performance in most low-resource settings. Conversely, the proposed MixPHM exhibits advantages in terms of performance and parameter efficiency under all dataset settings.

**Comparison with Compacter.** To reduce parameter redundancy, Compacter and MixPHM reparameterize adapter weights with low-rank PHM. However, in reducing parameter redundancy, MixPHM encourages task-relevant correction with redundancy regularization and improves the model capacity with MoE, avoiding overfitting and underparameterization concerns. Table 1 shows that Compacter does not perform as expected. One possible explanation is that Compacter is under-parameterized on the low-resource VQA task. Because too few trainable parameters do not guarantee that model capture enough task-relevant information in the tuning stage. This suggests that when tuning pretrained VLMs for low-resource VQA, it is necessary to

	/D	$\begin{bmatrix} WS \\ S A^{dn} A^{up} \end{bmatrix}$		#Param	VQA v2	GQA	OK-VQA	
D1	D2			(M)	VQA V2	UQA	UK-VQA	
Finetuning				224.54	$46.87 \pm 0.57$	$34.22 \pm 0.59$	$16.65 \pm 1.02$	
$\checkmark$					2.45	$48.15 \pm 0.89$	$36.42 \pm 0.64$	$17.34 \pm 1.59$
$\checkmark$		$\checkmark$	$\checkmark$		1.55	47.79 ±1.11	$36.59 \pm 0.64$	$18.77 \pm 0.99$
$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$		0.87	$48.26 \pm 0.56$	$\textbf{36.75} \pm 0.55$	$18.58 \pm 1.42$
$\checkmark$	$\checkmark$				1.37	47.67 ±1.13	$36.22 \pm 0.89$	17.65 ±2.38
$\checkmark$	$\checkmark$	$\checkmark$			1.36	$48.05 \pm 0.99$	$\textbf{36.76} \pm 0.78$	$17.02 \pm 1.70$
$\checkmark$	$\checkmark$			$\checkmark$	0.83	$47.30 \pm 0.92$	$36.05 \pm 1.05$	$17.27 \pm 0.63$
$\checkmark$	$\checkmark$	$\checkmark$		$\checkmark$	0.82	$47.83 \pm 0.65$	$36.39 \ _{\pm 0.84}$	17.75 ±1.36
$\checkmark$	$\checkmark$		$\checkmark$		0.88	47.78 ±1.20	$36.57 \pm 0.81$	$18.07 \pm 1.73$
$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$		0.87	$\textbf{48.26} \pm 0.56$	$36.75 \pm 0.55$	$\textbf{18.58} \pm 1.42$

Table 4. Ablation on weight decomposition (WD) and weight sharing (WS). D1: the decomposition of expert weights in Mix-PHM with PHM. D2: the further low-rank reparameterization of the decomposed weights.

balance the effectiveness and parameter efficiency.

**Comparison with LoRA and BitFit.** LoRA and BitFit are two typical parameter-efficient methods that tune a part of parameters of original pretrained VLMs and are more parameter-efficient. The results are shown in Table 1. We observe that compared with MixPHM, the tunable parameters of LoRA and BitFit are relatively lightweight. However, their performance trails much below MixPHM. In particular, the performance gap becomes larger as  $N_D$  increases. Similar to the discussion on Compacter, too few trainable parameters in the tuning process may lead to overfitting on the given dataset.

**Comparison with SoTA Few-Shot Learner.** Few-shot VQA is a special case of low-resource VQA. The comparisons with SoTA multimodal few-shot learner are shown in Table 2. Frozen [47] and PICa [54] are two in-context learning methods that use prompt-tuning to transfer large-scale language models (*i.e.*, GPT-2 and GPT-3 [2]) without parameter tuning. While FewVLM [22] is a prompt-based full finetuning method to adapt VL-T5, which inserts hand-crafted prompts into model inputs and finetunes full model parameters. We utilize MixPHM to tune FewVLM in a parameter-efficient manner. With only a tiny number of parameters tuned, MixPHM outperforms FewVLM in few-shot performance, especially on OK-VQA (**19.2** vs. 15.0). This demonstrates the superiority of MixPHM in terms of performance and parameter efficiency.

#### 5.3. Ablation Study

We conduct all ablated experiments with pretrained VL-T5 on VQA v2, GQA, and OK-VQA with  $N_{\mathcal{D}} = 64$ . **Effectiveness of Redundancy Regularization.** To demonstrate the effectiveness of the proposed redundancy regularization, we first introduce a consistency regularizer  $\mathcal{L}_{cs}$  [63] for comparison. Moreover, to further analyze the contribution of different terms in  $\mathcal{L}_{Ra}$ , we consider two variations of  $\mathcal{L}_{Ra}$ : (*i*)  $\mathcal{L}_{Ra}^{I}$ : only using the first term in Eq. (14) as the regularizer during training. (*ii*)  $\mathcal{L}_{Ra}^{II}$ : only using the second term in Eq. (14) during training. Table 3 shows that

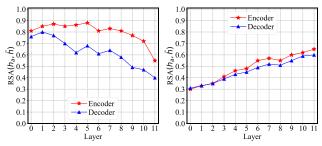


Figure 4. The average RSA similarity of MixPHM between  $h_a$  and h (left) as well as  $h_a$  and  $\tilde{h}$  (right) at each transformer layer.

 $\mathcal{L}_{cs}$  improves MixPHM performance only on GQA and the improvement is minor. In contrast,  $\mathcal{L}_{Ra}$  shows a significant improvement in MixPHM performance on all datasets. This observation demonstrates the effectiveness and superiority of the proposed regularizer  $\mathcal{L}_{Ra}$ . Furthermore, analyzing the impact of  $\mathcal{L}_{Ra}^{II}$  and  $\mathcal{L}_{Ra}^{II}$  on MixPHM performance, we find that only reducing the redundancy between the representation of MixPHM and the representation of pretrained VLMs (*i.e.*,  $\mathcal{L}_{Ra}^{I}$ ) makes limited contribution to performance gains. However, the joint effect of  $\mathcal{L}_{Ra}^{I}$  and  $\mathcal{L}_{Ra}^{II}$  is better than  $\mathcal{L}_{Ra}^{II}$  alone. This suggests that the trade-off between reducing task-irrelevant redundancy and prompting task-relevant correlation is critical for MixPHM.

Impact of Reducing Parameter Redundancy. MixPHM reduces parameter redundancy by first decomposing expert weights with PHM (D1) and then reparameterizing the decomposed weights (D2). We ablate D1 and D2 to analyze their effects on MixPHM performance (*i.e.*, the third column in Table 4). In addition, weight sharing can further reduce parameter redundancy in MixPHM. We thus conduct ablation on different meaningful combinations of shared weights in the fourth column of Table 4. Aside from the globally shared matrices (S), we also locally share downprojection  $(A^{dn})$  or up-projection  $(A^{up})$  matrices between experts in one MixPHM. Table 4 shows that there is a tradeoff between parameter efficiency and performance, *i.e.*, excessive parameter reduction may harm performance. Therefore, we advocate reducing parameter redundancy while maintaining model capacity.

**Impact of Hyperparameters.** Results on 1) routing mechanisms and hyperparameters ( $N_e$ ,  $d_r$ ,  $d_k$ , n,  $\alpha$ ), and 2) visualization are available in the supplementary material.

#### 5.4. Discussion

**Redundancy Analysis of MixPHM.** In this paper, we propose an insight that aims to improve the effectiveness of adapters by reducing task-irrelevant redundancy and promoting task-relevant correlation in representations. To assess whether our method actually leads to performance improvements based on this insight, we conduct the redundancy analysis of MixPHM under the same experimental settings as described in Sec. 4.1. Figure 4 illustrates the

VI M-	Made a d	#Param	#Sample				
VLMs	Method	(M)	$N_{\mathcal{D}}$ =16	$N_{\mathcal{D}}$ =64	$N_{\mathcal{D}}=500$	$N_D$ =1000	
X-VLM	Finetuning	294	26.63	30.45	38.96	43.92	
[57]	MixPHM	0.66	<b>27.54</b>	<b>31.80</b>	<b>41.05</b>	<b>48.06</b>	
BLIP	Finetuning	385	27.01	30.05	37.00	42.22	
[29]	MixPHM	0.87	<b>29.17</b>	<b>32.09</b>	<b>41.80</b>	<b>46.78</b>	
OFA <sub>Base</sub>	Finetuning	180	27.48	31.75	42.99	46.81	
[50]	MixPHM	0.70	<b>28.46</b>	<b>33.00</b>	<b>45.88</b>	<b>50.01</b>	

Table 5. **Experimental results of MixPHM on other pretrained VLMs.** We report the average VQA-Score across five seeds on VQA v2 validation set under different low-resource settings.

RSA similarity across 1k samples on VQA v2. Compared with the redundancy analysis of Adapter shown in Figure 1, we observe that MixPHM markedly reduces the representation redundancy between  $h_a$  and h, while increasing the representation correlation between  $h_a$  and  $\tilde{h}$ . This finding provides a perceptive demonstration for the soundness of our motivation and the effectiveness of our method.

Generalizability to Other Pretrained VLMs. To demonstrate the generalization capability of our method on other pretrained VLMs, we apply MixPHM to adapt pretrained X-VLM [57], BLIP [29], and OFA<sub>Base</sub> [50] for the low-resource VQA task. Table 5 presents a lite comparison between our method and full finetuning on VQA v2. We observe that MixPHM consistently outperforms full finetuning in all settings, with significant performance gains observed when  $N_D \in \{500, 1000\}$ . Notably, the largest performance gaps from finetuning are achieved by X-VLM (+4.14), BLIP (+4.80), and OFA<sub>Base</sub> (+3.20) at  $N_D$ =1000,  $N_D$ =500, and  $N_D$ =1000, respectively. These findings demonstrate the generalizability of MixPHM to various pretrained VLMs. More results are available in the supplementary material.

### 6. Conclusion and Limitation

In this paper, we propose a redundancy-aware parameterefficient tuning method to adapt pretrained VLMs to the low-resource VQA task. Our proposed MixPHM reduces task-irrelevant redundancy while prompting task-relevant correlation via a proposed redundancy regularization. Experiments demonstrate its effectiveness and superiority in terms of performance and parameter efficiency.

Redundancy is a double-edged sword. In addition to reducing task-irrelevant redundancy, we can also exploit taskrelevant redundancy already learned by pretrained VLMs to enhance performance. Although MixPHM emphasizes reducing task-irrelevant redundancy, there is no explicit guarantee that the reduced redundancy is ineffective for given tasks. As such, a potential prospect is to investigate how to explicitly delimit and minimize task-irrelevant redundancy. **Acknowledgements.** This work was supported by the National Science Foundation of China (Grant No. 62088102).

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