

## Efficient Visual Pretraining with Contrastive Detection

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### Abstract

Self-supervised pretraining has been shown to yield powerful representations for transfer learning. These performance gains come at a large computational cost however, with state-of-the-art methods requiring an order of magnitude more computation than supervised pretraining. We tackle this computational bottleneck by introducing a new self-supervised objective, contrastive detection, which tasks representations with identifying object-level features across augmentations. This objective extracts a rich learning signal per image, leading to state-of-the-art transfer accuracy on a variety of downstream tasks, while requiring up to  $10\times$  less pretraining. In particular, our strongest ImageNet-pretrained model performs on par with SEER, one of the largest self-supervised systems to date, which uses  $1000\times$  more pretraining data. Finally, our objective seamlessly handles pretraining on more complex images such as those in COCO, closing the gap with supervised transfer learning from COCO to PASCAL.

### 1. Introduction

Since the AlexNet breakthrough on ImageNet, transfer learning from large labeled datasets has become the dominant paradigm in computer vision [34, 50]. While recent advances in self-supervised learning have alleviated the dependency on labels for pretraining, they have done so at a tremendous computational cost, with state-of-the-art methods requiring an order of magnitude more computation than supervised pretraining [7, 10, 21]. Yet the promise of self-supervised learning is to harness massive unlabeled datasets, making its computational cost a critical bottleneck.

In this work, we aim to alleviate the computational burden of self-supervised pretraining. To that end we introduce *contrastive detection*, a new objective which maximizes the similarity of object-level features across augmentations. The benefits of this objective are threefold. First, it extracts separate learning signals from all objects in an image, enriching the information provided by each training example for free—object-level features are simply ob-

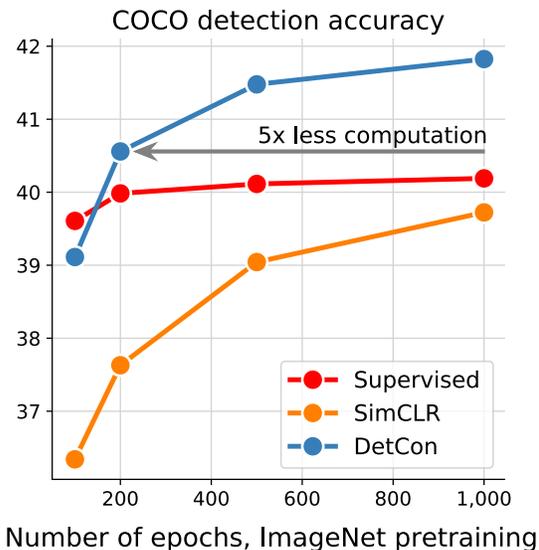


Figure 1. **Efficient self-supervised pretraining with DetCon.** Self-supervised pretraining with SimCLR [9] matches the transfer performance of supervised pretraining only when given  $10\times$  more training iterations. Our proposed DetCon objective surpasses both, while requiring  $5\times$  less computation than SimCLR. Transfer performance is measured by fine-tuning the representation on the COCO dataset for 12 epochs, using a Mask-RCNN.

tained from intermediate feature arrays. Second, it provides a larger and more diverse set of *negative samples* to contrast against, which also accelerate learning. Finally, this objective is well suited to learning from complex scenes with many objects, a pretraining domain that has proven challenging for self-supervised methods.

We identify approximate object-based regions in the image through the use of unsupervised segmentation algorithms. Perceptual grouping [32, 41]—the idea that low and mid-level regularities in the data such as color, orientation and texture allow for approximately parsing a scene into connected surfaces or object parts—has long been theorized to be a powerful prior for vision [22, 40, 56]. We leverage these priors by grouping local feature vectors accordingly, and applying our contrastive objective to each object-level feature separately. We investigate the use of

several unsupervised, image-computable masks [17, 2], and find our objective to work well despite their inaccuracies.

We test the ability of our objective to quickly learn transferable representations by applying it to the ImageNet dataset and measuring its transfer performance on challenging tasks such as COCO detection and instance segmentation, semantic segmentation on PASCAL and Cityscapes, and NYU depth estimation. Compared to representations obtained from recent self-supervised objectives such as SimCLR and BYOL [9, 21], our representations are more accurate and can be obtained with much less training time. We also find this learning objective to better handle images of more complex scenes, bridging the gap with supervised transfer from the COCO dataset. In summary, we make the following contributions:

1. We formulate a new contrastive objective which maximizes the similarity across augmentations of all objects in a scene, where object regions are provided by a simple, unsupervised heuristic.
2. We find this objective to alleviate the computational burden of self-supervised transfer learning, reducing by up to  $10\times$  the computation required to match supervised transfer learning from ImageNet. Longer training schedules lead to state-of-the-art transfer to COCO detection and instance segmentation, and our best model matches the very recent state-of-the-art self-supervised system SEER [20] which is trained on  $1000\times$  more—if less curated—images.
3. When transferring from complex scene datasets such as COCO, our method closes the gap with a supervised model which learns from human-annotated segmentations.
4. Finally, we assess to what extent the existing contrastive learning paradigm could be simplified in the presence of high quality image segmentations, raising questions and opening avenues for future work.

## 2. Related work

Transferring the knowledge contained in one task and dataset to solve other downstream tasks (i.e. *transfer learning*) has proven very successful in a range of computer vision problems [19, 39]. While early work focused on improving the pretraining architecture [27, 52] and data [53], recent work in self-supervised learning has focused on the choice of pretraining objective and task. Early self-supervised pretraining typically involved image restoration, including denoising [60], inpainting [46], colorization [66, 36], egomotion prediction [1], and more [15, 43, 67]. Higher-level pretext tasks have also been studied, such as predicting context [13], orientation [18], spatial layouts [44], temporal ordering [42], and cluster assignments [5].

Contrastive objectives, which maximize the similarity of a representation across views, while minimizing its similarity with distracting negative samples, have recently gained

considerable traction [23]. These views have been defined as local and global crops [29, 4, 57, 28] or different input channels [54]. Instance-discrimination approaches generate global, stochastic views of an image through data-augmentation, and maximize their similarity relative to marginally sampled negatives [9, 14, 16, 24, 63], although the need for negative samples has recently been questioned [12, 21]. While the benefits of instance-discrimination approaches have mostly been limited to pretraining from simple datasets such as ImageNet, clustering-based pretraining has proven very successful in leveraging large amounts of uncurated images for transfer learning [3, 6, 7, 20, 31].

While most work has focused on learning whole-image representations, there has been increasing interest in learning local descriptors that are more relevant for downstream tasks such as detection and segmentation. Examples of such work include the addition of auxiliary losses [51, 55], architectural components [48], or both [64]. While perceptual grouping has long been used for representation learning, often relying on coherent motion in videos [37, 45, 61], it has only recently been combined with contrastive learning [30, 59, 68]. Most related to our work are [59, 68] that also leverage image segmentations for self-supervised learning, although both differ from ours in that they learn backbones that are specialized for semantic segmentation and employ different loss functions. Although these works arrive at impressive unsupervised segmentation accuracy, neither report gains in pretraining efficiency for transfer learning tasks such as COCO detection and instance segmentation, which we study next.

## 3. Method

We introduce a new contrastive objective which maximizes the similarity across views of local features which represent the same object (Figure 2). In order to isolate the benefit of these changes, we make the deliberate choice of re-using elements of existing contrastive learning frameworks where possible. To test the generality of our approach, we derive two variants, DetCon<sub>S</sub> and DetCon<sub>B</sub>, based on two recent self-supervised baselines, SimCLR [9] and BYOL [21] respectively. We adopt the data augmentation procedure and network architecture from these methods while applying our proposed *contrastive detection* loss to each.

### 3.1. The contrastive detection framework

**Data augmentation.** Each image is randomly augmented twice, resulting in two images:  $x, x'$ . DetCon<sub>S</sub> and DetCon<sub>B</sub> adopt the augmentation pipelines of SimCLR and BYOL respectively, which roughly consist of random cropping, flipping, blurring, and point-wise color transformations. We refer the reader to appendix A.1 for more details. In all cases, images are resized to  $224\times 224$  pixel resolution.

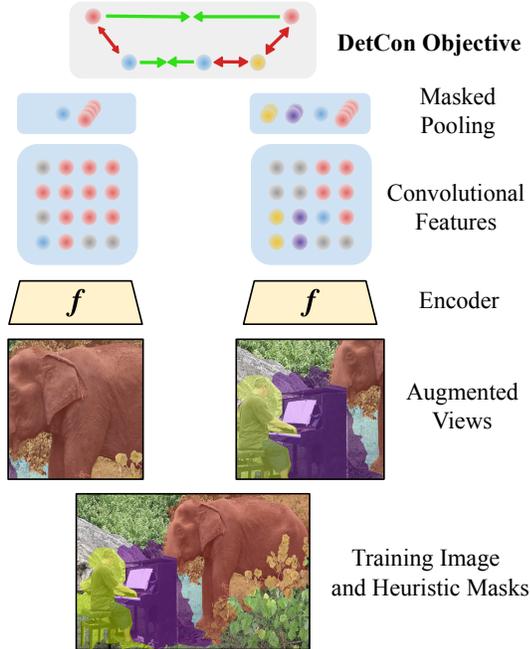


Figure 2. **The contrastive detection method.** We identify object-based regions with approximate, image-computable segmentation algorithms (bottom). These masks are carried through two stochastic data augmentations and a convolutional feature extractor, creating groups of feature vectors in each view (middle). The contrastive detection objective then pulls together pooled feature vectors from the same mask (across views) and pushes apart features from different masks and different images (top).

In addition, we compute for each image a set of masks which segment the image into different components. As described in Section 3.2, these masks can be computed using efficient, off-the-shelf, unsupervised segmentation algorithms. If available, human-annotated segmentations can also be used. In any case, we transform each mask (represented as a binary image) using the same cropping and resizing as used for the underlying RGB image, resulting in two sets of masks  $\{\mathbf{m}\}, \{\mathbf{m}'\}$  which are aligned with the augmented images  $\mathbf{x}, \mathbf{x}'$  (see Figure 2, *augmented views*).

**Architecture.** We use a convolutional feature extractor  $f$  to encode each image with a spatial map of hidden vectors:  $\mathbf{h} = f(\mathbf{x})$  where  $\mathbf{h} \in \mathbb{R}^{H \times W \times D}$ . We use the output of a standard ResNet-50 encoder [27], before the final mean-pooling layer, such that hiddens form a  $7 \times 7$  grid of 2048-dimensional vectors  $\mathbf{h}[i, j]$ . For every mask  $\mathbf{m}$  associated with the image, we compute a mask-pooled hidden vector

$$\mathbf{h}_m = \frac{1}{\sum_{i,j} m_{i,j}} \sum_{i,j} m_{i,j} \mathbf{h}[i, j],$$

having spatially downsampled the binary mask to a  $7 \times 7$  grid with average pooling. We then transform each of these vectors with a two-layer MLP, yielding non-linear projec-

tions  $\mathbf{z}_m = g(\mathbf{h}_m) \in \mathbb{R}^d$ .

For  $\text{DetCon}_S$  we process both views with the same encoder  $f_\theta$  and projection network  $g_\theta$ , where  $\theta$  are the learned parameters. For  $\text{DetCon}_B$  one view is processed with  $f_\theta$  and  $g_\theta$  and the other with  $f_\xi$  and  $g_\xi$ , where  $\xi$  is an exponential moving average of  $\theta$ . The first view is further transformed with a prediction network  $q_\theta$ . Here again we reuse the details of SimCLR and BYOL for  $\text{DetCon}_S$  and  $\text{DetCon}_B$  respectively in the definition of the projection and prediction networks (see appendix A.2). In summary, we represent each view and mask as latents  $\mathbf{v}_m$  and  $\mathbf{v}'_{m'}$  where

$$\mathbf{v}_m = g_\theta(\mathbf{h}_m), \quad \mathbf{v}'_{m'} = g_\theta(\mathbf{h}'_{m'})$$

for  $\text{DetCon}_S$  and

$$\mathbf{v}_m = q_\theta \circ g_\theta(\mathbf{h}_m), \quad \mathbf{v}'_{m'} = g_\xi(\mathbf{h}'_{m'})$$

for  $\text{DetCon}_B$ . We rescale all latents with a temperature hyperparameter  $\tau$ , such that their norm is equal to  $1/\sqrt{\tau}$ , with  $\tau = 0.1$ . Note that for downstream tasks, we retain only the feature extractor  $f_\theta$  and discard all other parts of the network (the prediction and projection heads, as well as any exponential moving averages).

**Objective: contrastive detection.** Let  $\mathbf{v}_m, \mathbf{v}'_{m'}$  be the latents representing masks  $\mathbf{m}, \mathbf{m}'$  in the views  $\mathbf{x}, \mathbf{x}'$ . The contrastive loss function

$$\ell_{m,m'} = -\log \frac{\exp(\mathbf{v}_m \cdot \mathbf{v}'_{m'})}{\exp(\mathbf{v}_m \cdot \mathbf{v}'_{m'}) + \sum_n \exp(\mathbf{v}_m \cdot \mathbf{v}_n)} \quad (1)$$

defines a prediction task: having observed the projection  $\mathbf{v}_m$ , learn to recognize the latent  $\mathbf{v}'_{m'}$  in the presence of negative samples  $\{\mathbf{v}_n\}$ . We include negative samples from different masks in the image and different images in the batch. Note that we make no assumptions regarding these masks, allowing negative masks to overlap with the positive one.

A natural extension of this loss would be to jointly sample paired masks  $\mathbf{m}, \mathbf{m}'$  which correspond to the same region in the original image, and maximize the similarity of features representing them

$$\mathcal{L} = \mathbb{E}_{(\mathbf{m}, \mathbf{m}') \sim \mathcal{M}} \ell_{\mathbf{m}, \mathbf{m}'}. \quad (2)$$

We make a few practical changes to this objective. First, in order to facilitate batched computation we randomly sample at each iteration a set of 16 (possibly redundant) masks from the variable-sized sets of masks  $\{\mathbf{m}\}$  and  $\{\mathbf{m}'\}$ . Second, we densely evaluate the similarity between all pairs of masks and all images, such that each image contributes 16 negative samples to the set  $\{\mathbf{v}_n\}$  in equation (1), rather than a single one. We aim to make these negatives as diverse as possible by choosing masks that roughly match different objects in the scene (Section 3.2). Finally, we mask out the loss to only maximize the similarity of paired locations, allowing us to handle cases where a mask is present in one



Figure 3. **Example masks used by the DetCon model.** 1<sup>st</sup> column: random images from the COCO training set. 2<sup>nd</sup> column: masks based on spatial proximity only. Global masks (top) are implicitly used by methods such as SimCLR, MoCo, and BYOL. 3<sup>rd</sup> column: image-computable masks obtained from the Felzenszwalb-Huttenlocher (FH, [17]) algorithm, with  $s = 500$ . 4<sup>th</sup> column: image-computable masks inferred using Multiscale Combinatorial Grouping (MCG) [2]. 5<sup>th</sup> column: “oracle” masks used to assess potential improvements from higher-quality segmentations.

view but not another (see Figure 2). Together, these simple modifications bring us to the DetCon objective:

$$\mathcal{L} = \sum_m \sum_{m'} \mathbb{1}_{m,m'} \ell_{m,m'} \quad (3)$$

where the binary variable  $\mathbb{1}_{m,m'}$  indicates whether the masks  $m, m'$  correspond to the same underlying region.

**Optimization.** When pretraining on ImageNet we adopt the optimization details of SimCLR and BYOL for training DetCon<sub>S</sub> and DetCon<sub>B</sub> respectively. When pretraining on COCO we make minor changes to the learning schedule to alleviate overfitting (see appendix A.3).

**Computational cost.** The computational requirements of self-supervised learning are largely due to forward and backward passes through the convolutional backbone. For the typical ResNet-50 architecture applied to 224×224-resolution images, a single forward pass requires approximately 4B FLOPS. The additional projection head in SimCLR and DetCon<sub>S</sub> requires an additional 4M FLOPS. Since we forward 16 hidden vectors through the projection head instead of 1, we increase the computational cost of the forward pass by 67M FLOPS, less than 2% of total. Together with the added complexity of the contrastive loss, this increase is 5.3% for DetCon<sub>S</sub> and 11.6% for DetCon<sub>B</sub> (see appendix A.2). Finally, the cost of computing image segmentations is negligible because they can be computed once and reused throughout training. Therefore the increase in complexity of our method relative to the baseline is sufficiently small for us to interchangeably refer to “training iterations” and “computational cost”.

### 3.2. Unsupervised mask generation

To produce masks required by the DetCon objective, we investigate several segmentation procedures, from simple spatial heuristics to graph-based algorithms from the literature.

**Spatial heuristic.** The simplest segmentation we consider groups locations based on their spatial proximity only. Specifically, we divide the image into an  $n \times n$  grid of non-overlapping, square sub-regions (Figure 3, 2<sup>nd</sup> column). Note that when using a single, global mask ( $n = 1$ ), the DetCon<sub>S</sub> objective reverts to SimCLR.

**Image-computable masks: FH.** We also consider the Felzenszwalb-Huttenlocher algorithm [17], a classic segmentation procedure which iteratively merges regions using pixel-based affinity (Figure 3, 3<sup>rd</sup> column). We generate a diverse set of masks by varying two hyperparameters, the scale  $s$  and minimum cluster size  $c$ , using  $s \in \{500, 1000, 1500\}$  and  $c = s$  when training on COCO and  $s = 1000$  when training on ImageNet.

**Image-computable masks: MCG.** Multiscale Combinatorial Grouping [2] is a more sophisticated algorithm which groups superpixels into many overlapping object proposal regions [8], guided by mid-level classifiers (Figure 3, 4<sup>th</sup> column). For each image we use 16 MCG masks with the highest scores. Note that the fact that these masks can overlap is supported by our formulation.

**Human annotated masks.** Throughout this work we consider the benefits afforded by the use of the *unsupervised* masks detailed above. In the final section, we ask whether higher quality masks (provided by human annotators; Figure 3, 5<sup>th</sup> column) can improve our results.

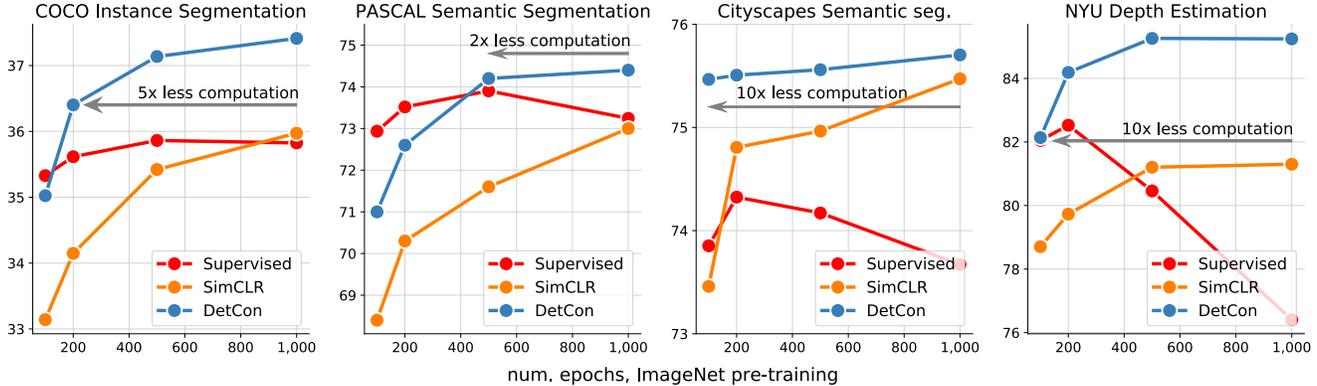


Figure 4. **Efficient ImageNet pretraining with DetCon<sub>S</sub>**. We pretrain networks with SimCLR, DetCon<sub>S</sub>, or supervised learning on ImageNet for different numbers of epochs, and fine-tune them for COCO detection and instance segmentation (for 12 epochs), semantic segmentation on PASCAL or Cityscapes, or depth estimation on NYU v2. DetCon<sub>S</sub> outperforms SimCLR, with up to 10× less pretraining.

Pretrain epochs	Detection COCO		Instance Segmentation COCO		Semantic Segmentation PASCAL		Semantic Segmentation Cityscapes		Depth Estimation NYU v2	
	300	1000	300	1000	300	1000	300	1000	100	1000
BYOL	41.2	41.6	37.1	37.2	74.7	75.7	73.4	74.6	83.7	84.2
<b>DetCon<sub>B</sub></b>	<b>42.0</b>	42.7	<b>37.8</b>	38.2	<b>75.6</b>	77.3	<b>75.1</b>	77.0	<b>85.1</b>	86.3
Efficiency Gain	> 3×		> 3×		≈ 3×		> 3×		> 10×	

Table 1. **Efficient ImageNet pretraining with DetCon<sub>B</sub>**. We pretrain networks on ImageNet with BYOL or DetCon<sub>B</sub>, and fine-tune them for COCO detection and instance segmentation (for 12 epochs), semantic segmentation on PASCAL or Cityscapes, or depth estimation on NYU v2. DetCon<sub>B</sub> outperforms BYOL, with up to 10× less pretraining (colors highlight gains in pretraining efficiency).

### 3.3. Evaluation protocol

Having trained a feature extractor in an unsupervised manner, we evaluate the quality of the representation by fine-tuning it for object detection and instance segmentation on COCO, segmentatic segmentation on PASCAL and Cityscapes, and depth estimation on NYU v2.

**Object detection and instance segmentation.** We use the pretrained network to initialize the feature extractor of a Mask-RCNN [26] equipped with feature pyramid networks [38] and cross-replica batch-norm [47]. We adopt the Cloud TPU implementation<sup>1</sup> and use it without modification. We fine-tune the entire model on the COCO train2017 set, and report bounding-box AP (AP<sup>bb</sup>) and mask AP (AP<sup>m</sup>) on the val2017 set. We use two standard training schedules: 12 epochs and 24 epochs [24].

**Semantic segmentation.** Following [24] we use our network to initialize the backbone of a fully-convolutional network [39]. For PASCAL, we fine-tune on the train\_aug2012 set for 45 epochs and report the mean intersection over union (mIoU) on the val2012 set. For Cityscapes, we finetune on the train\_fine set for 160 epochs and evaluate on the val\_fine set.

**Depth estimation.** Following [21] we stack the deconvolu-

<sup>1</sup><https://github.com/tensorflow/tpu/tree/master/models/official/detection>

tional network from [35] on top of our feature extractor, and fine-tune on the NYU v2 dataset. We report accuracy as the percentage of errors below 1.25 (pct<1.25).

## 4. Experiments

Our main self-supervised learning experiments employ FH masks, because as we will show, with DetCon they outperform simple spatial heuristics and approach the performance of MCG masks while being fast and easy to apply to large datasets such as ImageNet, given their availability in scikit-image [58].

### 4.1. Transfer learning from ImageNet

We first study whether the DetCon objective improves the pretraining efficiency of transfer learning from ImageNet.

**Pretraining efficiency.** We train SimCLR and DetCon<sub>S</sub> models on ImageNet for 100, 200, 500 and 1000 epochs, and transfer them to several datasets and tasks. Across all downstream tasks and pretraining regimes, DetCon<sub>S</sub> substantially outperforms SimCLR (Figures 1 and 4, blue and orange curves). When fine-tuning on COCO, the performance afforded by 1,000 epochs of SimCLR pretraining is surpassed by only 200 epochs of DetCon<sub>S</sub> pretraining (i.e. a 5× gain in pretraining efficiency). We found similar results when transferring to other downstream tasks: DetCon<sub>S</sub> yields a 2× gain in pretraining efficiency for PAS-

method	Fine-tune 1×		Fine-tune 2×	
	AP <sup>bb</sup>	AP <sup>mk</sup>	AP <sup>bb</sup>	AP <sup>mk</sup>
Supervised	39.6	35.6	41.6	37.6
VADeR [48]	39.2	35.6	-	-
MoCo [24]	39.4	35.6	41.7	37.5
SimCLR [9]	39.7	35.8	41.6	37.4
MoCo v2 [11]	40.1	36.3	41.7	37.6
InfoMin [55]	40.6	36.7	42.5	38.4
PixPro [64]	41.4	-	-	-
BYOL [21]	41.6	37.2	42.4	38.0
SwAV [7]	41.6	37.8	-	-
<b>DetCon<sub>S</sub></b>	<b>41.8</b>	<b>37.4</b>	<b>42.9</b>	<b>38.1</b>
<b>DetCon<sub>B</sub></b>	<b>42.7</b>	<b>38.2</b>	<b>43.4</b>	<b>38.7</b>

Table 2. **Comparison to prior art:** all methods are pretrained on ImageNet then fine-tuned on COCO for 12 epochs (1× schedule) or 24 epochs (2× schedule).

CAL semantic segmentation (Figure 4, 2<sup>nd</sup> column), and 10× gains for Cityscapes semantic segmentation and NYU depth prediction. (Figure 4, 3<sup>rd</sup>, and 4<sup>th</sup> columns).

We also evaluated the transfer performance of a supervised ResNet-50 trained on ImageNet (Figures 1 and 4, red curve). While supervised pretraining performs well with small computational budgets (e.g. 100 pretraining epochs), it quickly saturates, indicating that ImageNet labels only partially inform downstream tasks. This is emphasized for Cityscapes semantic segmentation and NYU depth prediction, which represent a larger shift in the domain and task.

**From BYOL to DetCon<sub>B</sub>.** How general is DetCon? We tested this by comparing DetCon<sub>B</sub> to the BYOL framework, upon which it is based. We adopt the underlying framework details (e.g. data-augmentation, architecture, and optimization) *without modification*, possibly putting the DetCon objective at a disadvantage. Despite this, DetCon<sub>B</sub> outperforms BYOL across pretraining budgets and downstream tasks. In particular, DetCon<sub>B</sub> yields a 3× gain in pretraining efficiency when transferring to COCO, PASCAL, and Cityscapes detection and segmentation, and a 10× gain when transferring to NYU depth prediction (Table 1).

**Comparison with prior art.** We now compare to other works in self-supervised transfer learning, and use fully-trained DetCon<sub>S</sub> and DetCon<sub>B</sub> models for the comparison. Here we focus on transfer to COCO as it is more widely studied. Note that other methods use a slightly different implementation of the Mask-RCNN [62] however their results for supervised ImageNet pretraining and SimCLR match our own [55, 64], enabling a fair comparison. Table 2 shows that DetCon outperforms all other methods for supervised and self-supervised transfer learning.

**Scaling model capacity.** Prior works in self-supervised learning have been shown to scale very well with model capacity [14, 33, 9]. Could the gains afforded by DetCon

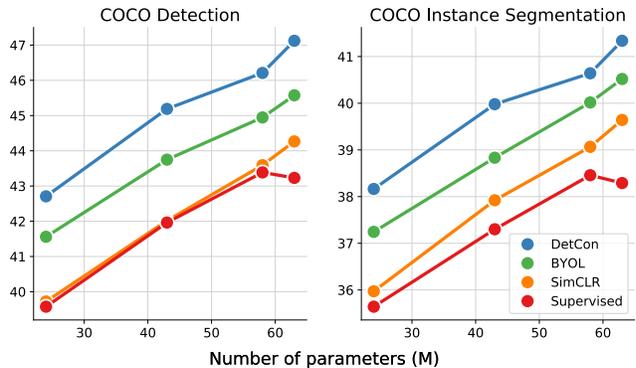


Figure 5. **Scaling DetCon to larger models.** We pretrain ResNet-50, ResNet-101, ResNet-152, and ResNet-200 feature extractors on ImageNet using supervised learning, SimCLR, BYOL, or DetCon<sub>B</sub> and fine-tune them on COCO for 12 epochs.

disappear with larger models? We trained SimCLR, BYOL, and DetCon<sub>B</sub> models on ImageNet, using ResNet-101, -152, and -200 feature extractors instead of ResNet-50. Figure 5 and Table A.1 show that DetCon continues to outperform other methods in this higher-capacity regime.

We went a step further and trained a ResNet-200 with a 2× width multiplier [33], containing 250M parameters. Surprisingly, despite only being trained on ImageNet, this model’s transfer performance matches that of a very recently proposed large-scale self-supervised model, SEER [20], having 693M parameters and trained on 1000× more data (Table 3). While the comparison is imperfect (large-scale data is necessarily more noisy), it highlights the potential of improvements from the self-supervised learning objective alone.

	pretrain	Data	Params	AP <sup>bb</sup>	AP <sup>mk</sup>
Supervised [20]	IN-1M	250 M	45.9	41.0	
SEER [20]	<b>IG-1B</b>	<b>693 M</b>	<b>48.5</b>	<b>43.2</b>	
<b>DetCon<sub>B</sub></b>	IN-1M	250 M	<b>48.9</b>	43.0	

Table 3. **Comparison to large-scale transfer learning:** all methods pretrain a backbone and transfer to COCO detection and instance segmentation using a Mask-RCNN. SEER trains on a billion Instagram images whereas DetCon<sub>S</sub> trains on ImageNet (1.3 million images). SEER and the supervised baseline use the recent RegNet architecture [49], whereas DetCon<sub>S</sub> uses a generic ResNet-200 (2× width). Despite this, DetCon pretraining matches the performance of large-scale SEER pretraining.

## 4.2. Transfer learning from COCO

We next investigate the ability of the DetCon objective to handle complex scenes with multiple objects. For this we pretrain on the COCO dataset and compare to SimCLR.

**Training efficiency.** We train SimCLR and DetCon<sub>S</sub> for a range of schedules (324–5184 epochs), and transfer all models to semantic segmentation on PASCAL. We find

DetCon<sub>S</sub> to outperform SimCLR across training budgets (Figure 6). As before, the maximum accuracy attained by SimCLR is reached with 4× less pretraining time.

**Surpassing supervised transfer from COCO.** We also evaluated the transfer performance of representations trained on COCO in a supervised manner. Specifically, we trained a Mask-RCNN with a long schedule (108 epochs, a “9×” schedule), and use the learned feature extractor (a ResNet-50, as for SimCLR and DetCon pretraining) as a representation for PASCAL segmentation. Unlike SimCLR, DetCon pretraining surpasses the performance of this fully supervised baseline (Figure 6).

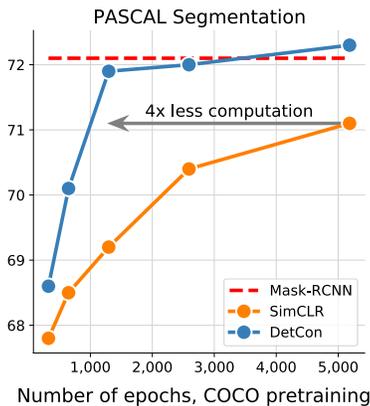


Figure 6. **Efficient transfer from COCO.** We pre-train representations using SimCLR or DetCon<sub>S</sub> on COCO for different numbers of epochs, and transfer to PASCAL semantic segmentation by fine-tuning them for 45 epochs.

### 4.3. Ablations and analysis

We now dissect the components of the DetCon objective and assess the benefits of each. For this we pretrain on COCO as it contains complex scenes with many objects and associated ground-truth masks, allowing us to measure the impact of segmenting them accurately. We evaluate learned representations with a *frozen-feature analysis*, in which the feature extractor is kept fixed while we train the other layers of a Mask-RCNN also on COCO. This controlled setting is analogous<sup>2</sup> to the linear classification protocol used to evaluate the quality of self-supervised representations for image recognition [13, 15, 45, 66]

**What makes good masks?** The DetCon objective can be used with a variety of different image segmentations, which ones lead to the best representation? We first consider spatial heuristics which partition the image into 2×2, 5×5, or 10×10 grids, a 1×1 grid being equivalent to using the SimCLR objective. We find downstream performance increases with finer grids, a 5×5 grid being optimal (Figure 7).

Next we consider image-computable FH and MCG masks, both of which outperform the spatial heuristic masks, MCG masks leading to slightly better representations. Interestingly, the quality of the representation *corre-*

<sup>2</sup>But note that the Mask-RCNN contains several non-linear layers due to the additional complexity of the output space relative to classification.

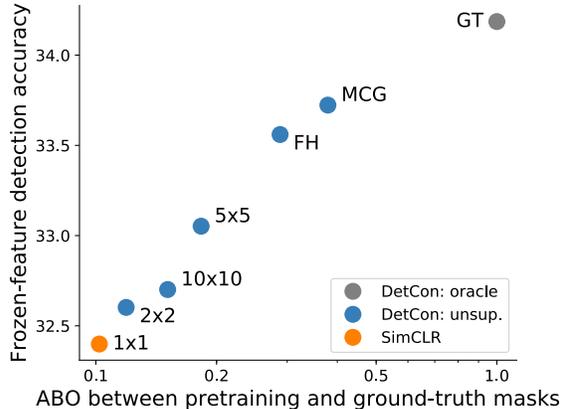


Figure 7. **Effect of type of masks used in DetCon objective.** We train DetCon models on COCO using unsupervised masks (blue), or the ground-truth COCO masks (grey). Using a single, global mask (i.e. a “1×1” grid) is equivalent to SimCLR (orange). We compute the Average Best Overlap (ABO) by measuring the IoU between each ground-truth mask and the closest pretraining mask, and averaging over all ground truth instances and images (x-axis). We evaluate the accuracy of each model on COCO detection using the *frozen-feature* paradigm (y-axis).

*lates very well with the overlap between pretraining masks and ground-truth*—the better each ground truth object is covered by some mask, the better DetCon performs.

**Contrastive detection vs contrastive recognition.** How does the DetCon objective benefit from these image segmentations? We assess the impact of each of its components by incrementally adding them to the SimCLR framework. As mentioned previously, we recover SimCLR when using a single, global mask in the DetCon objective. As a sanity check, we verify that duplicating this mask several times and including the resulting (identical) features in the DetCon objective makes no difference in the quality of the representation (Table 4, row a). Interestingly, using FH masks but only sampling a single mask per image slightly deteriorates performance, presumably because the model only learns from part of the image at every iteration (Table 4, row b). By densely sampling object regions DetCon<sub>S</sub> learns from the entire image, while also benefiting from a diverse set of positive and negative samples, resulting in increased detection and segmentation accuracy (Table 4, final row).

model	masks	#latents	AP <sup>bb</sup>	AP <sup>mk</sup>
SimCLR	global	1	31.6	29.2
(a)	global	16	31.5	29.3
(b)	FH	1	31.2	28.8
<b>DetCon<sub>S</sub></b>	FH	16	<b>33.4</b>	<b>30.6</b>

Table 4. **Ablation: from SimCLR to DetCon<sub>S</sub>.** We pretrain on COCO and evaluate *frozen feature* accuracy also on COCO. **masks:** specifies whether hidden vectors are pooled globally, or within individual FH masks. **#latents:** number of masks.

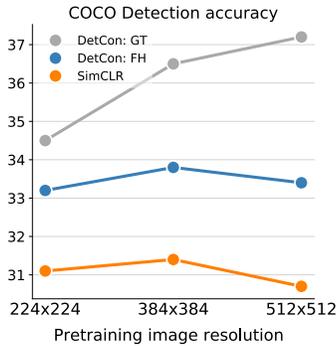


Figure 8. **Better segmentations benefit from higher resolutions.** We pretrain backbone networks on COCO using SimCLR and DetCon<sub>S</sub> (with FH or GT masks) at various resolutions. We report *frozen-feature* performance with a fixed resolution of  $1024 \times 1024$ .

#### 4.4. What if segmentation were solved?

The DetCon objective function leads to fast transfer learning and strong performance despite using fairly approximate segmentation masks. In Section 4.3 we found higher quality segmentations (such as those computed using MCG, or obtained from human annotators) to improve representational quality. How might we improve the learning objective given more accurate segmentations? We assessed this question by revisiting our design choices for the contrastive objective, when given ground-truth masks from the COCO dataset as opposed to the approximate FH masks.

**Scaling image resolution.** We hypothesized that higher image resolutions might enable the network to benefit more from these more informative segmentations. To preserve fine-grained information we sample local features from within each mask and optimize them using the DetCon objective. We pretrain SimCLR and DetCon<sub>S</sub> models equipped with FH or ground-truth (GT) masks, given  $384 \times 384$  or  $512 \times 512$  resolution images. While DetCon with FH masks only modestly benefited and SimCLR’s performance deteriorated with high-resolution images, DetCon with GT masks improves substantially (Figure 8). Note that this is solely due to an improved representation quality; the image resolution used for downstream evaluation is maintained at  $1024 \times 1024$  for all models.

**Revisiting the contrastive framework.** Finally, we asked whether the current contrastive learning paradigm—which utilizes large numbers of negatives and predictions across stochastic augmentations—remains optimal in the context of the DetCon objective with high-quality segmentations.

*Are large numbers of negative samples necessary?* Not with high-quality masks. When dividing the total number of negative samples by 128 (by only gathering negatives from within a worker) the performance of DetCon with FH masks drops (Table 5, row a), consistently with other contrastive learning frameworks [9, 24]. In contrast, DetCon<sub>S</sub> using GT masks improves despite this limitation.

*Are positive pairs sampled across augmented views necessary?* Not with high-quality masks. We run DetCon

model	all neg	two views	Masks	
			FH	GT
DetCon	✓	✓	<b>33.6</b>	37.0
(a)		✓	32.2	38.5
(b)			27.7	<b>38.8</b>

Table 5. **Simplifying the contrastive framework.** We train DetCon<sub>S</sub> models on COCO using approximate FH masks or higher-quality ground-truth (GT) masks, and evaluate them in the *frozen-feature* setting. “**all neg**”: Negative samples are collected from the entire batch as opposed to only within a worker (out of 128 workers). “**two views**”: Contrastive predictions are made across augmentations, as opposed to within a view.

models while sampling a single augmentation for each image and maximizing the similarity of mask-based features *within* this view. Here again, the DetCon objective suffers from this handicap when using approximate FH masks, but not with high-quality segmentations (Table 5, row b).

*How can this be?* One interpretation is that other images give us clean negative examples because images in COCO depict different scenes. However it appears that negatives from the same image provide a stronger learning signal (in that they share features such as lighting, background, etc) as long as they are clean—i.e., we are not pushing features from the same object apart. Positives from the same image are also at least as good as those across augmentations if again they are clean—i.e., we are not pulling together features from different objects.

## 5. Discussion

We have proposed DetCon, a simple but powerful self-supervised learning algorithm. By exploiting low-level cues for organizing images into entities such as objects and background regions, DetCon accelerates pretraining on large datasets while improving accuracy on a variety of downstream tasks. Our best models achieve state-of-the-art performance among self-supervised methods pretrained on ImageNet and match recent state-of-the-art methods training larger models on a much larger dataset [20].

We showed that the power of DetCon strongly correlates with how well the masks used align with object boundaries. This seems intuitive—the DetCon objective can only leverage independent learning signals from each image region if they contain distinct content. Similarly, the resulting negative samples are genuinely diverse only if they represent different objects. This opens exciting prospects of research in jointly discovering objects and learning to represent them. Given the improved performance of DetCon representations for instance segmentation, a natural question is whether they could be used to perform better unsupervised segmentations than the ones used during pretraining. If so, these might be used to learn better representations still, leading to a virtuous crescendo of unsupervised scene understanding.

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