

Human Pose Regression with Residual Log-likelihood Estimation

Jiefeng Li¹ Siyuan Bian¹ Ailing Zeng² Can Wang³
Bo Pang¹ Wentao Liu³ Cewu Lu^{1†}

¹Shanghai Jiao Tong University ²The Chinese University of Hong Kong ³SenseTime Research

Abstract

Heatmap-based methods dominate in the field of human pose estimation by modelling the output distribution through likelihood heatmaps. In contrast, regression-based methods are more efficient but suffer from inferior performance. In this work, we explore maximum likelihood estimation (MLE) to develop an efficient and effective regression-based method. From the perspective of MLE, adopting different regression losses is making different assumptions about the output density function. A density function closer to the true distribution leads to a better regression performance. In light of this, we propose a novel regression paradigm with Residual Log-likelihood Estimation (RLE) to capture the underlying output distribution. Concretely, RLE learns the change of the distribution instead of the unreferenced underlying distribution to facilitate the training process. With the proposed reparameterization design, our method is compatible with off-the-shelf flow models. The proposed method is effective, efficient and flexible. We show its potential in various human pose estimation tasks with comprehensive experiments. Compared to the conventional regression paradigm, regression with RLE bring **12.4 mAP** improvement on MSCOCO without any test-time overhead. Moreover, for the first time, especially on multi-person pose estimation, our regression method is superior to the heatmap-based methods. Our code is available at <https://github.com/Jeff-sjtu/res-loglikelihood-regression>.

1. Introduction

Human pose estimation has been extensively studied in the area of computer vision [21, 22, 1, 29, 19]. Recently, with deep convolutional neural networks, significant progress has been achieved. Existing methods can be divided into two categories: heatmap-based [57, 56, 62, 4, 64, 54, 46, 52] and regression-based [58, 5, 53, 70, 42, 61].

[†]Cewu Lu is the corresponding author. He is the member of Qing Yuan Research Institute, Qi Zhi Institute and MoE Key Lab of Artificial Intelligence, AI Institute, Shanghai Jiao Tong University, China.

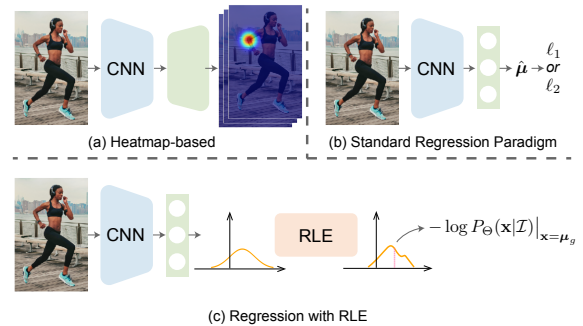


Figure 1: **Illustration** of (a) heatmap-based method, (b) standard regression paradigm, and (c) regression with the proposed RLE.

Heatmap-based methods are dominant in the field of human pose estimation. These methods generate a likelihood heatmap for each joint and locate the joint as the point with the argmax [56, 64, 46] or soft-argmax [40, 31, 54] operations. Despite the excellent performance, heatmap-based methods suffer from high computation and storage demands. Expanding the heatmap to 3D or 4D (spatial + temporal) will be costly. Additionally, it is hard to deploy heatmap in modern one-stage methods.

Regression-based methods directly map the input to the output joints coordinates, which is flexible and efficient for various human pose estimation tasks and real-time applications, especially on edge devices. A standard heatmap head (3 deconv layers) costs $1.4\times$ FLOPs of the ResNet-50 backbone, while the regression head costs only **1/20000** FLOPs of the same backbone. Nevertheless, regression suffers from inferior performance. In challenging cases like occlusions, motion blur, and truncations, the ground-truth labels are inherently ambiguous. Heatmap-based methods are robust to these ambiguities by leveraging the likelihood heatmap. But current regression methods are vulnerable to these noisy labels.

In this work, we facilitate human pose regression by exploring maximum likelihood estimation (MLE) to model the output distribution. From the perspective of MLE, standard Euclidean distance loss (ℓ_1 or ℓ_2) can be viewed as a particular assumption that the output conforms to a distribu-

tion family (Laplace or Gaussian distribution) with constant variance. Intuitively, the performance can be improved if we construct the likelihood function with the true underlying distribution instead of the inappropriate hypothesis.

To this end, we propose a novel and effective regression paradigm, named Residual Log-likelihood Estimation (RLE), that leverages normalizing flows to estimate the underlying distribution and boosts human pose regression. Given a tractable preset assumption of the likelihood function, RLE estimates the residual log-likelihood, *i.e.* the change of the distribution. It is easier to be optimized compared to the original unreferenced underlying distribution. Besides, we design a reparameterization strategy for the flow model to learn the intrinsic characteristics of the underlying distribution. This strategy makes our regression framework feasible and allows us to utilize the off-the-shelf flow model to approximate the distribution without a sophisticated network architecture.

During training, the regression model and the RLE module can be optimized simultaneously. Since the form of the underlying distribution is unknown, the RLE module is also trained via the maximum likelihood estimation process. Besides, the RLE module does not participate in the inference phase. In other words, the proposed method can bring significant improvement to the regression model without any test-time overhead.

The proposed regression framework is general. It can be applied to various human pose estimation algorithms (*e.g.* two-stage approaches [45, 14, 12, 64, 52], one-stage approaches [70, 42, 61]) and various tasks (*e.g.* single and multi-person 2D/3D pose estimation [1, 29, 19, 34, 21, 22]). We benchmark the proposed method on three pose estimation datasets, including MPII [1], MSCOCO [29] and Human3.6M [19]. With a simple yet effective architecture, RLE boosts the conventional regression method by **12.4** mAP and achieves superior performance to the heatmap-based methods. Moreover, it is more computation and storage efficient than heatmap-based methods. Specifically, on MSCOCO [29], our regression-based model with ResNet-50 [15] backbone achieves **71.3** mAP with **4.0** GFLOPs, compared to 71.0 mAP with 9.7 GFLOPs of heatmap-based SimplePose [64]. We hope our method will inspire the field to rethink the potential of regression-based methods.

The contributions of our approach can be summarized as follows:

- We propose a novel and effective regression paradigm with the reparameterization design and Residual Log-likelihood Estimation (RLE). The proposed method boosts human pose regression without any test-time overhead.
- For the first time, regression-based methods achieve superior performance to the heatmap-based methods,

and it is more computation and storage efficient.

- We show the potential of the proposed paradigm by applying it to various human pose estimation methods. Considerable improvements are observed in all these methods.

2. Related Work

Heatmap-based Pose Estimation. The idea of utilizing likelihood heatmaps to represent human joint locations is proposed by Tompson *et al.* [57]. Since then, heatmap-based approaches dominate in the field of 2D human pose estimation. Pioneer works [57, 56, 62, 39] design powerful CNN models to estimate heatmaps for single-person pose estimation. Many works [45, 14, 12, 64, 36, 27, 52] extend this idea to multi-person pose estimation following the top-down framework, *i.e.* detection and single-person pose estimation. In the bottom-up framework [48, 18, 20, 4, 38, 44, 8], multiple body joints are retrieved from the heatmaps and grouped into different human poses. Pavlakos *et al.* [46] first extend the heatmap to 3D space. The 3D heatmap representation is followed by several works [54, 35, 7, 69, 59, 28]. Sun *et al.* [54] leverage the soft-argmax operation to retrieve joint locations from heatmaps in a differentiable manner, which allows end-to-end training. It prevents quantization error, but the model is still required to generate high-resolution features and heatmaps.

Regression-based Pose Estimation. In the context of human pose estimation, only a few works are regression-based. Toshev *et al.* [58] first leverage the convolutional network for human pose estimation. Carreira *et al.* [5] propose an Iterative Error Feedback (IEF) network to improve the performance of the regression model. Zhou *et al.* [70] and Tian *et al.* [55] propose direct pose regression in the one-stage object detection framework. Nie *et al.* [42] factorize the long-range displacement into accumulative shorter ones. However, it is vulnerable to occlusions. Wei *et al.* [61] regress the displacement w.r.t. the pre-defined pose anchors. In 3D pose estimation, Sun *et al.* [53] propose compositional pose regression to learn the internal structures of 3D human pose. Rogez *et al.* [50, 51] classify the human pose into a set of K anchor-poses and a regression module is proposed to refine the anchor to the final prediction. Two-stage methods [32, 13, 47, 68, 60, 9, 30, 67] lift the 2D poses to 3D space by regression. But the 2D poses are still predicted by the heatmap-based 2D pose estimator. Despite lots of progress that have been made by previous works, there is still a huge performance gap between the pure regression-based approaches and the heatmap-based approaches.

In this work, for the first time, we improve the performance of the regression-based approach to a comparable

level of the heatmap-based approaches. Our method is flexible and can be applied to various human pose estimation algorithms.

Normalizing Flow in Human Pose Estimation. Some recent works leverage normalizing flows to build priors in 3D human pose estimation. Xu *et al.* [65] propose new 3D human shape and articulated pose models with the kinematic prior based on normalizing flows. Zanfir *et al.* [66] use normalizing flows to build a prior on SMPL joint angles for their weakly-supervised method. Biggs *et al.* [3] learn a pose prior by normalizing flows to sample the best output from the ambiguous image. Different from previous methods, we leverage normalizing flows to estimate the underlying output distribution.

Adaptive Loss Function. In our method, the output distribution is learnable, which resulting in a learnable loss function. There have been several works towards adaptive loss functions. Imani *et al.* [17] propose histogram loss, which use histogram (*i.e.* heatmap) to represent the output distribution. Some works define a superset of loss functions and change the loss by tuning the parameters of the function. Wu *et al.* [63] using a teacher model to dynamically change the loss function of the student model. Barron [2] presents a generalization of common loss functions, which automatically adapts itself during training. Different from previous methods, we do not set the form of the distribution family in advance. The loss function can learn to be arbitrary forms within the maximum likelihood estimation framework.

3. Method

In this work, we aim at improving the performance of the regression-based method to a competitive level of the heatmap-based method. Compared with the heatmap-based method, regression-based method has lots of merits: i) It gets rid of the high-resolution heatmaps and has low computation and storage complexity. ii) It has a continuous output and does not suffer from the quantization problem. iii) It can be extended to a wide variety of scenarios (*e.g.* one-stage methods, video-based methods, 3D scenes) at a minimal cost. However, existing regression-based methods suffer from poor performance, which is fatal and restricts its wide usage.

In this section, before introducing our solution, we first review the general formulation of regression from the perspective of maximum likelihood estimation in §3.1. Then, in §3.2, we present the Residual Log-likelihood Estimation (RLE), an approach that leverages normalizing flows to capture the underlying residual log-likelihood function and facilitate human pose regression. Finally, the necessary im-

plementation details are provided in §3.3.

3.1. General Formulation of Regression

The standard regression paradigm is to apply ℓ_1 or ℓ_2 loss to the regressed output $\hat{\mu}$. Loss functions are empirically chosen for different tasks. Here, we review the regression problem from the perspective of maximum likelihood estimation (MLE). Given an input image \mathcal{I} , the regression model predicts a distribution $P_{\Theta}(\mathbf{x}|\mathcal{I})$ that indicates the probability of the ground truth appearing in the location \mathbf{x} , where Θ denotes the learnable model parameters. Due to the inherent ambiguities in the labels, the labelled location μ_g can be viewed as an observation sampled near the ground truth by the human annotator. The learning process is to optimize the model parameters Θ that makes the observed label μ_g most probable. Therefore, the loss function of this maximum likelihood estimation (MLE) process is defined as:

$$\mathcal{L}_{mle} = -\log P_{\Theta}(\mathbf{x}|\mathcal{I}) \Big|_{\mathbf{x}=\mu_g}. \quad (1)$$

In this formulation, different regression losses are essentially different hypotheses of the output probability distribution. For example, in some works of object detection [16, 26, 25] and dense correspondences [37], the density is assumed to be a Gaussian distribution. The model needs to predict two values, $\hat{\mu}$ and $\hat{\sigma}$, to construct the density function $P_{\Theta}(\mathbf{x}|\mathcal{I}) = \frac{1}{\sqrt{2\pi}\hat{\sigma}} e^{-\frac{(\mathbf{x}-\hat{\mu})^2}{2\hat{\sigma}^2}}$. To maximize the likelihood of the observed label μ_g , the loss function becomes:

$$\mathcal{L} = -\log P_{\Theta}(\mathbf{x}|\mathcal{I}) \Big|_{\mathbf{x}=\mu_g} \propto \log \hat{\sigma} + \frac{(\mu_g - \hat{\mu})^2}{2\hat{\sigma}^2}. \quad (2)$$

If we assume the density function has a constant variance, *i.e.* $\hat{\sigma}$ is a constant, the loss degenerates to standard ℓ_2 loss: $\mathcal{L} = (\mu_g - \hat{\mu})^2$. Further, if we assume the density follows the Laplace distribution with a constant variance, the loss function becomes the standard ℓ_1 loss. In the inference phase, the value $\hat{\mu}$ used to control the location of distribution serves as the regressed output.

From this perspective, the loss function depends on the shape of the distribution $P_{\Theta}(\mathbf{x}|\mathcal{I})$. Therefore, a more accurate density function could lead to better results. However, since the analytical expression of the underlying distribution is unknown, the model can not simply regress several values to construct the density function like Eq. 2. To estimate the underlying distribution and facilitate human pose regression, in the following section, we propose a novel regression paradigm by leveraging *normalizing flow*.

3.2. Regression with Normalizing Flows

In this subsection, we introduce three variants of the proposed paradigm that utilize normalizing flows for regression (see Fig. 2).

Basic Design. The basic design of the proposed regression paradigm with normalizing flows is illustrated in Fig. 2(a). Here, normalizing flows [49, 10, 24, 43, 23] learn to construct a complex distribution by transforming a simple distribution through an invertible mapping. We consider the distribution $P_{\Theta}(\mathbf{z}|\mathcal{I})$ on a random variable \mathbf{z} as the initial density function. It is defined by the output $\hat{\boldsymbol{\mu}}$ and $\hat{\boldsymbol{\sigma}}$ from the regression model Θ . For simplicity, we assume $P_{\Theta}(\mathbf{z}|\mathcal{I}) = \frac{1}{\sqrt{2\pi}\hat{\boldsymbol{\sigma}}} e^{-\frac{(\mathbf{z}-\hat{\boldsymbol{\mu}})^2}{2\hat{\boldsymbol{\sigma}}^2}}$, *i.e.* the Gaussian distribution. A smooth and invertible mapping $f_{\phi} : \mathbb{R}^2 \rightarrow \mathbb{R}^2$ is chosen to transform \mathbf{z} to \mathbf{x} , *i.e.* $\mathbf{x} = f_{\phi}(\mathbf{z})$, where ϕ is the learnable parameters of the flow model.

The transformed variable \mathbf{x} follows another distribution $P_{\Theta,\phi}(\mathbf{x}|\mathcal{I})$. The probability density function $P_{\Theta,\phi}(\mathbf{x}|\mathcal{I})$ depends on both the regression model Θ and the flow model f_{ϕ} , which can be calculated as:

$$\log P_{\Theta,\phi}(\mathbf{x}|\mathcal{I}) = \log P_{\Theta}(\mathbf{z}|\mathcal{I}) + \log \left| \det \frac{\partial f_{\phi}^{-1}}{\partial \mathbf{x}} \right|, \quad (3)$$

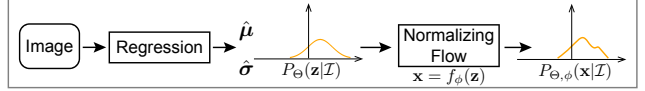
where f_{ϕ}^{-1} is the inverse of f_{ϕ} and $\mathbf{z} = f_{\phi}^{-1}(\mathbf{x})$. In this way, given arbitrary \mathbf{x} , the corresponding log-probability can be estimated through Eq. 3 by reversely computing \mathbf{z} . Besides, $P_{\Theta,\phi}(\mathbf{x}|\mathcal{I})$ is learnable and can fit arbitrary distribution as long as f_{ϕ} is complex enough. In practice, we can compose several simple mappings successively to construct arbitrarily complex functions, *i.e.* $\mathbf{x} = f_{\phi}(\mathbf{z}) = f_K \circ \dots \circ f_2 \circ f_1(\mathbf{z})$.

The maximum likelihood process is performed on the learned distribution $P_{\Theta,\phi}(\mathbf{x}|\mathcal{I})$. Hence, the loss function is formulated as:

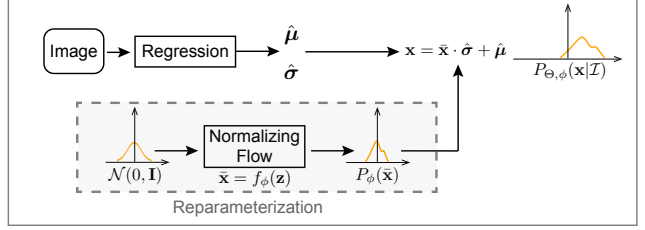
$$\begin{aligned} \mathcal{L}_{mle} &= -\log P_{\Theta,\phi}(\mathbf{x}|\mathcal{I}) \Big|_{\mathbf{x}=\boldsymbol{\mu}_g} \\ &= -\log P_{\Theta}(f_{\phi}^{-1}(\boldsymbol{\mu}_g) | \mathcal{I}) - \log \left| \det \frac{\partial f_{\phi}^{-1}}{\partial \boldsymbol{\mu}_g} \right|. \end{aligned} \quad (4)$$

Note that the underlying optimal distribution $P_{opt}(\mathbf{x}|\mathcal{I})$ is unknown. The flow model is learned in an unsupervised manner by maximizing the likelihood of the labelled locations. For example, for the challenging cases (*e.g.* occlusions) with larger deviations in the labels from human annotators, the predicted distribution should have a large variance to maximize the log-probability.

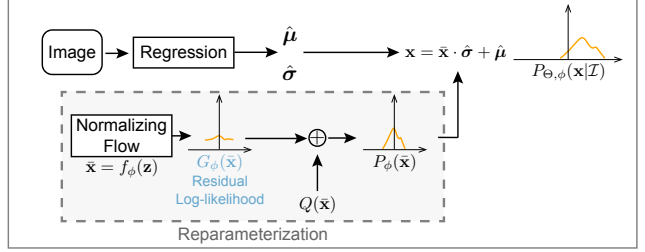
Reparameterization. Although the basic design seems reasonable, it is not feasible in practice. The learning of f_{ϕ} relies on the terms $\log \left| \det \frac{\partial f_{\phi}^{-1}}{\partial \boldsymbol{\mu}_g} \right|$ and $f_{\phi}^{-1}(\boldsymbol{\mu}_g)$ in the loss function (Eq. 4). Therefore, ϕ will learn to fit the distribution of $\boldsymbol{\mu}_g$ across all images. Nevertheless, the distribution that we want to learn is about how the output deviates from the ground truth conditioning on the input image, not the distribution of the ground truth itself across all images.



(a) Basic Design



(b) Direct likelihood estimation with reparameterization



(c) Residual log-likelihood estimation with reparameterization

Figure 2: Illustration of the proposed regression frameworks. (a) The basic design. (b) Direct likelihood estimation with reparameterization. (c) Residual log-likelihood estimation with reparameterization.

Here, to make our regression framework feasible and compatible with the off-the-shelf flow models, we further design the regression paradigm with the reparameterization strategy. The new paradigm is illustrated in Fig. 2(b). We assume all the underlying distribution share the same density function family but with different mean and variance conditioning on the input \mathcal{I} . Firstly, the flow model f_{ϕ} is leveraged to map a zero-mean initial distribution $\bar{\mathbf{x}} \sim \mathcal{N}(0, \mathbf{I})$ to a zero-mean deformed distribution $\bar{\mathbf{x}} \sim P_{\phi}(\bar{\mathbf{x}})$. Then the regression model Θ predicts two values, $\hat{\boldsymbol{\mu}}$ and $\hat{\boldsymbol{\sigma}}$, to control the position and scale of the distribution. The final distribution $P_{\Theta,\phi}(\mathbf{x}|\mathcal{I})$ is obtained by shifting and rescaling $\bar{\mathbf{x}}$ to \mathbf{x} , where $\mathbf{x} = \bar{\mathbf{x}} \cdot \hat{\boldsymbol{\sigma}} + \hat{\boldsymbol{\mu}}$.

Therefore, the loss function with reparameterization can be written as:

$$\begin{aligned} \mathcal{L}_{mle} &= -\log P_{\Theta,\phi}(\mathbf{x}|\mathcal{I}) \Big|_{\mathbf{x}=\boldsymbol{\mu}_g} \\ &= -\log P_{\phi}(\bar{\boldsymbol{\mu}}_g) - \log \left| \det \frac{\partial \bar{\boldsymbol{\mu}}_g}{\partial \boldsymbol{\mu}_g} \right| \\ &= -\log P_{\phi}(\bar{\boldsymbol{\mu}}_g) + \log \hat{\boldsymbol{\sigma}}, \end{aligned} \quad (5)$$

where $\bar{\boldsymbol{\mu}}_g = (\boldsymbol{\mu}_g - \hat{\boldsymbol{\mu}})/\hat{\boldsymbol{\sigma}}$, and $\partial \bar{\boldsymbol{\mu}}_g / \partial \boldsymbol{\mu}_g = 1/\hat{\boldsymbol{\sigma}}$. With the reparameterization design, now the flow model can focus on learning the distribution of $\bar{\boldsymbol{\mu}}_g$, which reflects the deviation of the output from the ground truth.

Residual Log-likelihood Estimation. After reparameterization, the regression framework can be trained in an end-to-end manner. The training of the regressed value $\hat{\mu}$ and the flow model f_ϕ are coupled together, depending on the term $\log P_\phi(\bar{\mu}_g)$ in the loss function (Eq. 5). However, there are intricate dependencies between these two models. The training of the regression model entirely relies on the distribution estimated by the flow model f_ϕ . At the beginning stage of training, the shape of the distribution is far from correct, which increases the difficulty to train the regression model and might degrade the model performance.

To facilitate the training process, we develop a gradient shortcut to reduce the dependence between these two models. Formally, the distribution estimated by the flow model $P_\phi(\bar{\mathbf{x}})$ is trying to fit the optimal underlying distribution $P_{opt}(\bar{\mathbf{x}})$, which can be split into three terms:

$$\begin{aligned} \log P_{opt}(\bar{\mathbf{x}}) &= \log \left(Q(\bar{\mathbf{x}}) \cdot \frac{P_{opt}(\bar{\mathbf{x}})}{s \cdot Q(\bar{\mathbf{x}})} \cdot s \right) \\ &= \log Q(\bar{\mathbf{x}}) + \log \frac{P_{opt}(\bar{\mathbf{x}})}{s \cdot Q(\bar{\mathbf{x}})} + \log s, \end{aligned} \quad (6)$$

where the term $Q(\bar{\mathbf{x}})$ can be a simple distribution, *e.g.* Gaussian distribution $Q(\bar{\mathbf{x}}) = \mathcal{N}(0, \mathbf{I})$, the term $\log \frac{P_{opt}(\bar{\mathbf{x}})}{s \cdot Q(\bar{\mathbf{x}})}$ is what we call *residual log-likelihood*, and the constant s is to make sure the residual term is a distribution. We assume that $Q(\bar{\mathbf{x}})$ can roughly match the underlying distribution but not perfectly. The residual log-likelihood is to compensate for the difference. Thus, we split the log-probability of $P_\phi(\bar{\mathbf{x}})$ the same way as Eq. 6:

$$\log P_\phi(\bar{\mathbf{x}}) = \log Q(\bar{\mathbf{x}}) + \log G_\phi(\bar{\mathbf{x}}) + \log s, \quad (7)$$

where $G_\phi(\bar{\mathbf{x}})$ is the distribution learned by the flow model. The value of $s = \frac{1}{\int G_\phi(\bar{\mathbf{x}})Q(\bar{\mathbf{x}})d\bar{\mathbf{x}}}$ can be approximated by the Riemann sum. The derivation of s is provided in the supplemental document.

In this way, $G_\phi(\bar{\mathbf{x}})$ will try to fit the underlying residual likelihood $\frac{P_{opt}(\bar{\mathbf{x}})}{s \cdot Q(\bar{\mathbf{x}})}$ instead of learning the entire distribution. Finally, combining the reparameterization design (Eq. 5) and residual log-likelihood estimation (Eq. 7), the total loss function can be defined as:

$$\begin{aligned} \mathcal{L}_{rle} &= -\log P_{\Theta, \phi}(\mathbf{x}|\mathcal{I}) \Big|_{\mathbf{x}=\bar{\mu}_g} \\ &= -\log P_\phi(\bar{\mu}_g) + \log \hat{\sigma} \\ &= -\log Q(\bar{\mu}_g) - \log G_\phi(\bar{\mu}_g) - \log s + \log \hat{\sigma}. \end{aligned} \quad (8)$$

This process is illustrated in Fig. 2(c).

During training, the backward propagated gradients from $Q(\bar{\mu}_g)$ do not depend on the flow model, which accelerates the training of the regression model. Besides, as the hypothesis of ResNet [15], it is easier to optimize the residual mapping than to optimize the original unreferenced mapping.

To the extreme, if the preset approximation $Q(\bar{\mathbf{x}})$ is optimal, it would be easier to push the residual log-probability to zero than to fit an identity mapping by a stack of invertible mappings in f_ϕ . The effectiveness of the residual log-likelihood estimation is validated in §4.1.

3.3. Implementation Details

In the training phase, the regression model and the flow model are simultaneously optimized in an end-to-end manner. We replace the standard regression loss (ℓ_1 and ℓ_2) with the proposed residual log-likelihood estimation loss \mathcal{L}_{rle} . The initial density is set to Laplace distribution by default. In the testing phase, the predicted mean $\hat{\mu}$ serves as the regressed output. Therefore, the flow model does not need to be run during inference. This characteristic makes the proposed method flexible and easy to apply to various regression algorithms without any test-time overhead. Besides, the prediction confidence can be obtained from $\hat{\sigma}$:

$$\hat{c} = 1 - \frac{1}{K} \sum_i^K \hat{\sigma}_i, \quad (9)$$

where $\hat{\sigma}_i$ is the learned deviation of the i th joint, and K denotes the total number of joints. The deviation $\hat{\sigma}_i$ is predicted with a sigmoid function. Hence we have $\hat{\sigma}_i \in (0, 1)$ and $\hat{c} \in (0, 1)$.

Flow Model. The proposed regression paradigm is agnostic to the flow models. Hence, various off-the-shelf flow models [49, 10, 24, 43, 23] can be applied. In the experiments, we adopt RealNVP [10] for fast training. We denote the invertible function with L_{fc} fully-connected layers with N_n neurons as $L_{fc} \times N_n$. We set $L_{fc} = 3$ and $N_n = 64$ by default. The flow model is light-weighted and barely affects the training speed. More detailed descriptions of the flow model architecture are provided in the supplemental document.

Tasks. The proposed regression paradigm is general and is ready for various human pose estimation tasks. In the experiments, we validate the proposed regression paradigm on **seven** different algorithms in **five** tasks: *single-person 2D pose estimation, top-down 2D pose estimation, one-stage 2D pose estimation, single-stage 3D pose estimation* and *two-stage 3D pose estimation*. Detailed training settings are provided in §4 and §5. The experiments on *single-person 2D pose estimation* are provided in the supplemental document.

4. Experiments on COCO

We first evaluate the proposed regression paradigm on a large-scale in-the-wild 2D human pose benchmark COCO Keypoint [29].

Method	# Params	GFLOPs	AP	AP ₅₀	AP ₇₅
Direct Regression (with ℓ_1)	23.6M	4.0	58.1	82.7	65.0
Regression with DLE	23.6M	4.0	62.7	86.1	70.4
Regression with RLE	23.6M	4.0	70.5	88.5	77.4
*Regression with RLE	23.6M	4.0	71.3	88.9	78.3

Table 1: **Comparison with the conventional regression paradigm.** RLE provides significant improvements with the same test-time computational complexity.

	Method	AP	AP ₅₀	AP ₇₅
(a)	SimplePose [64]	71.0	89.3	79.0
	Integral Pose [54]	63.0	85.6	70.0
	*Regression with RLE	71.3	88.9	78.3
(b)	HRNet-W32 [52]	74.1	90.0	81.5
	HRNet-W32 + RLE (Regression)	74.3	89.7	80.8
(c)	Mask R-CNN [14]	66.0	86.9	71.5
	Mask R-CNN + RLE	66.7	86.7	72.6
(d)	PointSet Anchor [61]	67.0	87.3	73.5
	PointSet Anchor + RLE	67.4	87.5	73.9

Table 2: **Comparison with heatmap-based methods** on COCO validation set. The proposed paradigm achieves competitive performance to the heatmap-based methods.

Implementation Details. We embed RLE into the *top-down* approaches and a *one-stage* approach. For the *top-down* approach, we adopt a simple architecture consisting of a ResNet-50 [15] backbone, followed by an average pooling layer and an FC layer. The FC layer consists of $K \times 4$ neurons, where 4 is for $\hat{\mu}$ and $\hat{\sigma}$, and $K = 17$ denotes the number of body keypoints. For human detection, we use the person detectors provided by SimplePose [64] for both the validation set and the test-dev set. Data augmentations and training settings follow previous work [52]. The end-to-end approach, Mask R-CNN [14], is also adopted for ablation study. Implementation is based on Detectron2 [11]. The keypoint head is a stack of 8 convolutional layers, followed by an average pooling layer and an FC layer. We train for 270,000 iterations, with 4 images per GPU and 4 GPUs in total. Other parameters are the same as the original Detectron2.

For the *one-stage* approach, we adopt the state-of-the-art method [61]. We replace its 2K-channel regression head with a 4K-channel head for the prediction of both $\hat{\mu}$ and $\hat{\sigma}$. Implementation is based on the official code of [61]. The other training details are the same as them.

4.1. Main Results

Comparison with Conventional Regression. To study the effectiveness of the proposed regression paradigm, we compare it with the conventional direct regression method. The direct regression model has the same “ResNet-50 + FC” architecture, and ℓ_1 loss is adopted. The experimental results on COCO validation set are shown in Tab. 1.

Method	Backbone	AP	AP ₅₀	AP ₇₅	AP _M	AP _L
<i>Heatmap-based</i>						
CMU-Pose [4]	3CM-3PAF	61.8	84.9	67.5	57.1	68.2
Mask R-CNN [14]	ResNet-50	63.1	87.3	68.7	57.8	71.4
G-RMI [45]	ResNet-101	64.9	85.5	71.3	62.3	70.0
RMPE [12]	PyraNet	72.3	89.2	79.1	68.0	78.6
AE [38]	Hourglass-4	65.5	86.8	72.3	60.6	72.6
PersonLab [44]	ResNet-152	68.7	89.0	75.4	64.1	75.5
CPN [6]	ResNet-Inception	72.1	91.4	80.0	68.7	77.2
SimplePose [64]	ResNet-152	73.7	91.9	81.1	70.3	80.0
Integral [54]	ResNet-101	67.8	88.2	74.8	63.9	74.0
HRNet [52]	HRNet-W48	75.5	92.5	83.3	71.9	81.5
EvoPose [33]	EvoPose2D-L	75.7	91.9	83.1	72.2	81.5
<i>Regression-based</i>						
CenterNet [70]	Hourglass-2	63.0	86.8	69.6	58.9	70.4
SPM [42]	Hourglass-8	66.9	88.5	72.9	62.6	73.1
PointSet Anchor [61]	HRNet-W48	68.7	89.9	76.3	64.8	75.3
ResNet + RLE (Ours)	ResNet-152	74.2	91.5	81.9	71.2	79.3
*ResNet + RLE (Ours)	ResNet-152	75.1	91.8	82.8	72.0	80.2
HRNet + RLE (Ours)	HRNet-W48	75.7	92.3	82.9	72.3	81.3

Table 3: **Comparison with the SOTA** on COCO test-dev.

As shown, the proposed method brings significant improvement (**12.4** mAP) to the regression-based method. Then we compare the result with direct likelihood estimation (DLE) to study the effectiveness of residual log-likelihood estimation. The DLE model only adopts the reparameterization strategy and no residual log-likelihood estimation. It is seen that the residual manner provides **7.8** mAP improvements. Like previous work [54], we further adopt the network backbone that pre-trained by the heatmap loss. This model achieves the best performance with **71.3** mAP, which is denoted with *.

Note that the flow model does not participate in the inference phase. Therefore, no extra computation is introduced in testing. Besides, the training overhead of the flow model is negligible. Detailed results are reported in the supplemental document. These experiments demonstrate the superiority of the proposed regression paradigm.

Comparison with Heatmap-based Methods. We further compare our regression method with heatmap-based methods. As shown in Tab. 2(a), our regression method outperforms Integral Pose [54] by **7.5** mAP, and the heatmap supervised SimplePose [64] by **0.3** mAP. For the first time, the direct regression method achieves superior performance to the heatmap-based method.

In Tab. 2(b), we also implement RLE with HRNet [52] to show our approach is flexible and can be easily embedded into various backbone networks. Since HRNet maintains high resolution throughout the whole process, we adopt soft-argmax to produce coordinates $\hat{\mu}$ and an FC layer to produce $\hat{\sigma}$. It shows that integral with RLE surpasses conventional heatmap by **0.2** mAP.

Tab. 2(c) shows the superiority of RLE on Mask R-CNN, the end-to-end *top-down* approach. Our regression version outperforms the heatmap-based Mask R-CNN by **0.7** mAP. In Tab. 2(d), RLE brings **0.4** mAP improvement to the state-of-the-art *one-stage* approach. Note that the out-



Figure 3: **Qualitative** results on COCO dataset: containing crowded scenes, occlusions and appearance change.

Method	Correlation
SimplePose (Heatmap)	0.479
Regression with Gaussian	0.476
Regression with Laplace	0.522
RLE ($Q(\bar{x}) \sim \text{Gaussian}$)	0.540
RLE ($Q(\bar{x}) \sim \text{Laplace}$)	0.553

Table 4: **Correlation testing** on different methods.

Method	#Params	GFLOPs	GFLOPs of Net. Head	AP
<i>Heatmap-based</i>				
Integral Pose [54]	34.0M	9.7	5.7	63.4
SimplePose [64]	34.0M	9.7	5.7	71.0
<i>Regression-based</i>				
*Regression with RLE	23.6M	4.0	0.0002	71.3

Table 5: **Computation complexity and model parameters.**

$L_{fc} \times N_n$	AP	AP ₅₀	AP ₇₅
3×64	70.5	88.5	77.4
3×128	70.2	88.5	77.3
3×256	69.6	87.9	76.5
5×32	70.0	88.2	76.8
5×64	70.3	88.7	77.4

Table 6: **Different RealNVP Architecture.**

Distribution	AP	AP ₅₀	AP ₇₅
Const. Variance Gaussian (ℓ_2)	36.6	70.9	33.6
Const. Variance Laplace (ℓ_1)	58.1	82.7	65.0
Gaussian	60.2	82.9	66.6
Laplace	67.4	86.8	74.2
RLE ($Q(\bar{x}) \sim \text{Gaussian}$)	70.0	88.1	76.7
RLE ($Q(\bar{x}) \sim \text{Laplace}$)	70.5	88.5	77.4

Table 7: **Initial Density:** Performance with different hypotheses of the output distribution.

put of PointSet Anchor [61] relies on the heatmap predictions. The regressed values are used for joint association. The superiority of RLE is demonstrated by embedding it in various approaches.

Comparison with the SOTA on COCO test-dev In this experiment, we compare the proposed RLE with the state-of-the-art methods on COCO test-dev. Quantitative results are reported in Tab. 3. The proposed regression paradigm significantly outperforms other regression-based methods by **7.0** mAP and achieves state-of-the-art performance. Compared to the same backbone heatmap-based methods, our regression method is **1.4** mAP higher with ResNet-152 and **0.2** mAP higher with HRNet-W48. We demonstrate that heatmap is not the only solution to human pose estimation. Regression-based methods have great potential and can achieve superior performance than heatmap-based methods. Qualitative results are shown in Fig. 3.

Correlation with Prediction Correctness. The estimated standard deviation $\hat{\sigma}$ establishes the correlation with the prediction correctness. The model will output a larger $\hat{\sigma}$ for a more uncertain result. Therefore, $\hat{\sigma}$ plays the same role as the confidence score in the heatmap. We transform

the deviation to confidence with Eq. 9. To analysis the correlation of $\hat{\sigma}$ and the prediction correctness, we calculate the *Pearson correlation coefficient* between the confidence and the OKS to the ground truth on the COCO validation set. The confidence of the heatmap-based prediction [64] is the maximum value of the heatmap. Tab. 4 reveals that RLE has much a stronger correlation to OKS than the heatmap-based method (relative **15.2%** improvement). In real-world applications and other downstream tasks, a reliable confidence score is useful and necessary. RLE address the lack of confidence scores in regression-based methods and provide a more reliable score than the heatmap-based methods.

Computation Complexity. The experimental results of computation complexity and model parameters are listed in Tab. 5. The proposed method achieves comparable results to the heatmap-based methods with significantly lower computation complexity and fewer model parameters. Specifically, the total FLOPs are reduced by **58.8%**, and the parameters are reduced by **30.6%**. We further calculate the FLOPs of the network head to remove the influence of the network backbone. It shows that the FLOPs of the regression head is only **1/28500** of the heatmap head, which is almost negligible. The computational superiority of our proposed regression paradigm is of great value in the industry.

4.2. Ablation Study

RealNVP Architecture. In Tab. 6, we compare different network architectures of the RealNVP [10] model. It shows that the final AP keeps stable with different RealNVP architectures. We argue that learning the residual log-likelihood is easy for the flow model. Thus the results are robust to the change of the architecture.

Initial Density. To examine how the assumption of the output distribution affects the regression performance in the context of MLE, we compare the results of different density functions with our method. The Laplace distribution and Gaussian distribution will degenerate to standard ℓ_1 and ℓ_2 loss if they are assumed to have constant variances. As shown in Tab. 7, the learned distributions of our method provide more than **21.3%** improvements. Besides, we study the baselines that assuming the output follows the Gaussian and Laplace distributions with the learnable deviation σ . The distributions with learnable σ outperform those with constant variance, but are still inferior to RLE.

Moreover, different initial densities $Q(\bar{x})$ for RLE are also tested. There is a large gap between the original Gaussian and Laplace distribution. However, with RLE to learn the change of the density, the difference between these two distributions is significantly reduced. It demonstrates that RLE is robust to different assumptions of the initial density.

5. Experiments on Human3.6M

Human3.6M [19] is an indoor benchmark for 3D pose estimation. For evaluation, MPJPE and PA-MPJPE are used. Following typical protocols [54, 35], we use (S1, S5, S6, S7, S8) for training and (S9, S11) for evaluation.

Implementation Details. For the *single-stage* approach, we adopt the same ResNet-50 + FC architecture. The input image is resized to 256×256 . Data augmentation includes random scale ($\pm 30\%$), rotation ($\pm 30^\circ$), color ($\pm 20\%$) and flip. The learning rate is set to 1×10^{-3} at first and reduced by a factor of 10 at the 90th and 120 epoch. We use the Adam solver and train for 140 epochs, with a mini-batch size of 32 per GPU and 8 GPUs in total. The 2D and 3D mixed data training strategy (MPII + Human3.6M) is applied. The testing procedure is the same as the previous works [54].

For the *two-stage* approach, we embed the proposed regression paradigm into the classic baseline [32] and the state-of-the-art model [67]. 2D ground-truth poses are taken as inputs. For data normalization, we follow previous works [67, 47, 68]. The initial learning rate is 1×10^{-3} and decays 5% after each epoch. We use the Adam solver and train for 80 epochs, with a mini-batch size of 1024.

Ablation Study. In Tab. 8, we report the performance comparison between RLE and the baselines on both *single-stage* and *two-stage* approaches. It is seen that RLE reduces the error of *single-stage* regression baseline by **1.5 mm** and the heatmap-based Integral Pose [54] by **0.6 mm**. Besides, without 3D heatmaps, our regression method significantly reduces the FLOPs by **61.7%** and the model parameters by **30.6%**. For the *two-stage* approach, RLE brings **2.7 mm** im-

Method	#Params	GFLOPs	MPJPE ↓	PA-MPJPE ↓
<i>Single-stage</i>				
Direct Regression	23.8M	5.4	50.1	39.3
Integral Pose [54]	34.3M	14.1	49.2	39.1
Regression with RLE	23.8M	5.4	48.6	38.5
<i>Two-stage</i>				
FC Baseline	4.3M	0.275	43.6	33.2
FC Baseline + RLE	4.3M	0.275	40.9	31.1

Table 8: Ablation study on Human3.6M.

Method	Sun [53]	Nibali [41]	Sun [54]	Moon [35]	Zhou [69]	Ours
#Params	-	57.9M	34.3M	34.3M	49.6M	23.8M
GFLOPs	-	29.3	14.1	14.1	41.4	5.4
MPJPE	59.1	49.5	49.6	53.3	47.7	48.6

Table 9: Single-stage Results on Human3.6M.

Method	Choi [9]	Martinez [32]	Zhao [68]	Fang [13]	Liu [30]	Zeng [67]	Ours
MPJPE	55.5	45.5	43.8	42.5	37.8	36.5	36.3

Table 10: Two-stage Results on Human3.6M. Our result is based on SRNet [67] with RLE.

provement to the regression baseline without any test-time overhead.

Comparison with the State-of-the-art. In this experiment, we compare the proposed regression paradigm with both *single-stage* and *two-stage* state-of-the-art methods in Tab. 9 and Tab. 10. For *single-stage*, our method achieves comparable performance to the state-of-the-art methods while reducing the FLOPs by **86.7%**. The model parameters and FLOPs are calculated using the official code of these methods. Note that [69] only releases the testing code. For fair comparison, we re-train the model with the same training settings as ours. For *two-stage*, our method is based on SRNet [67] with RLE. It achieves state-of-the-art performance by 0.2 mm improvement to the original SRNet.

6. Conclusion

In this paper, we propose a novel and effective regression paradigm from the perspective of maximum likelihood estimation. The learning process is to maximize the probability of the observation. We leverage the normalizing flow model to learn the residual log-likelihood w.r.t. to the tractable initial density function. Comprehensive experiments are conducted to validate the efficacy of the proposed paradigm. For the first time, the regression-based methods achieve superior performance to the heatmap-based methods. Regression-based methods are efficient and flexible. We hope our method would inspire the field to rethink the potential of regression.

References

- [1] Mykhaylo Andriluka, Leonid Pishchulin, Peter Gehler, and Bernt Schiele. 2d human pose estimation: New benchmark and state of the art analysis. In *CVPR*, 2014.
- [2] Jonathan T Barron. A general and adaptive robust loss function. In *CVPR*, 2019.
- [3] Benjamin Biggs, Sébastien Ehrhardt, Hanbyul Joo, Benjamin Graham, Andrea Vedaldi, and David Novotny. 3d multi-bodies: Fitting sets of plausible 3d human models to ambiguous image data. In *NeurIPS*, 2020.
- [4] Zhe Cao, Tomas Simon, Shih-En Wei, and Yaser Sheikh. Realtime multi-person 2d pose estimation using part affinity fields. In *CVPR*, 2017.
- [5] Joao Carreira, Pulkit Agrawal, Katerina Fragkiadaki, and Jitendra Malik. Human pose estimation with iterative error feedback. In *CVPR*, 2016.
- [6] Yilun Chen, Zhicheng Wang, Yuxiang Peng, Zhiqiang Zhang, Gang Yu, and Jian Sun. Cascaded pyramid network for multi-person pose estimation. In *CVPR*, 2018.
- [7] Zerui Chen, Yiru Guo, Yan Huang, and Liang Wang. Learning depth-aware heatmaps for 3d human pose estimation in the wild. In *BMVC*, 2019.
- [8] Bowen Cheng, Bin Xiao, Jingdong Wang, Honghui Shi, Thomas S Huang, and Lei Zhang. Higherhrnet: Scale-aware representation learning for bottom-up human pose estimation. In *CVPR*, 2020.
- [9] Hongsuk Choi, Gyeongsik Moon, and Kyoung Mu Lee. Pose2mesh: Graph convolutional network for 3d human pose and mesh recovery from a 2d human pose, 2020.
- [10] Laurent Dinh, Jascha Sohl-Dickstein, and Samy Bengio. Density estimation using real nvp. In *ICRL*, 2016.
- [11] facebookresearch. Detectron2. <https://github.com/facebookresearch/detectron2>, 2021.
- [12] Hao-Shu Fang, Shuqin Xie, Yu-Wing Tai, and Cewu Lu. Rmpe: Regional multi-person pose estimation. In *ICCV*, 2017.
- [13] Hao-Shu Fang, Yuanlu Xu, Wenguan Wang, Xiaobai Liu, and Song-Chun Zhu. Learning pose grammar to encode human body configuration for 3d pose estimation. In *AAAI*, 2018.
- [14] Kaiming He, Georgia Gkioxari, Piotr Dollár, and Ross Girshick. Mask r-cnn. In *ICCV*, 2017.
- [15] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *CVPR*, 2016.
- [16] Yihui He, Chenchen Zhu, Jianren Wang, Marios Savvides, and Xiangyu Zhang. Bounding box regression with uncertainty for accurate object detection. In *CVPR*, 2019.
- [17] Ehsan Imani and Martha White. Improving regression performance with distributional losses. In *ICML*, 2018.
- [18] Eldar Insafutdinov, Leonid Pishchulin, Bjoern Andres, Mykhaylo Andriluka, and Bernt Schiele. Deeppercut: A deeper, stronger, and faster multi-person pose estimation model. In *ECCV*, 2016.
- [19] Catalin Ionescu, Dragos Papava, Vlad Olaru, and Cristian Sminchisescu. Human3.6m: Large scale datasets and predictive methods for 3D human sensing in natural environments. *TPAMI*, 2014.
- [20] Umar Iqbal and Juergen Gall. Multi-person pose estimation with local joint-to-person associations. In *ECCV*, 2016.
- [21] Sam Johnson and Mark Everingham. Clustered pose and nonlinear appearance models for human pose estimation. In *BMVC*, 2010.
- [22] Sam Johnson and Mark Everingham. Learning effective human pose estimation from inaccurate annotation. In *CVPR*, 2011.
- [23] Diederik P Kingma and Prafulla Dhariwal. Glow: Generative flow with invertible 1x1 convolutions. In *NeurIPS*, 2018.
- [24] Diederik P Kingma, Tim Salimans, Rafal Jozefowicz, Xi Chen, Ilya Sutskever, and Max Welling. Improving variational inference with inverse autoregressive flow, 2016.
- [25] Youngwan Lee, Joong-won Hwang, Hyung-Il Kim, Kimin Yun, and Joungyoul Park. Localization uncertainty estimation for anchor-free object detection. *arXiv preprint arXiv:2006.15607*, 2020.
- [26] Chen Li and Gim Hee Lee. Generating multiple hypotheses for 3d human pose estimation with mixture density network. In *CVPR*, 2019.
- [27] Jiefeng Li, Can Wang, Hao Zhu, Yihuan Mao, Hao-Shu Fang, and Cewu Lu. Crowdpose: Efficient crowded scenes pose estimation and a new benchmark. In *CVPR*, 2019.
- [28] Jiefeng Li, Chao Xu, Zhicun Chen, Siyuan Bian, Lixin Yang, and Cewu Lu. Hybrik: A hybrid analytical-neural inverse kinematics solution for 3d human pose and shape estimation. In *CVPR*, 2021.
- [29] Tsung-Yi Lin, Michael Maire, Serge Belongie, James Hays, Pietro Perona, Deva Ramanan, Piotr Dollár, and C Lawrence Zitnick. Microsoft COCO: Common objects in context. In *ECCV*, 2014.
- [30] Kenkun Liu, Rongqi Ding, Zhiming Zou, Le Wang, and Wei Tang. A comprehensive study of weight sharing in graph networks for 3d human pose estimation, 2020.
- [31] Diogo C Luvizon, Hedi Tabia, and David Picard. Human pose regression by combining indirect part detection and contextual information. *Computers & Graphics*, 2019.
- [32] Julieta Martinez, Rayat Hossain, Javier Romero, and James J Little. A simple yet effective baseline for 3d human pose estimation. In *ICCV*, 2017.
- [33] William McNally, Kanav Vats, Alexander Wong, and John McPhee. Evopose2d: Pushing the boundaries of 2d human pose estimation using neuroevolution. *arXiv preprint arXiv:2011.08446*, 2020.
- [34] Dushyant Mehta, Helge Rhodin, Dan Casas, Pascal Fua, Oleksandr Sotnychenko, Weipeng Xu, and Christian Theobalt. Monocular 3D human pose estimation in the wild using improved cnn supervision, 2017.
- [35] Gyeongsik Moon, Ju Yong Chang, and Kyoung Mu Lee. Camera distance-aware top-down approach for 3D multi-person pose estimation from a single rgb image. In *ICCV*, 2019.
- [36] Gyeongsik Moon, Ju Yong Chang, and Kyoung Mu Lee. Posefix: Model-agnostic general human pose refinement network. In *CVPR*, 2019.

- [37] Natalia Neverova, David Novotny, and Andrea Vedaldi. Correlated uncertainty for learning dense correspondences from noisy labels. In *NeurIPS*, 2019.
- [38] Alejandro Newell, Zhiao Huang, and Jia Deng. Associative embedding: End-to-end learning for joint detection and grouping. In *NeurIPS*, 2017.
- [39] Alejandro Newell, Kaiyu Yang, and Jia Deng. Stacked hourglass networks for human pose estimation. In *ECCV*, 2016.
- [40] Aiden Nibali, Zhen He, Stuart Morgan, and Luke Prendergast. Numerical coordinate regression with convolutional neural networks. *arXiv preprint arXiv:1801.07372*, 2018.
- [41] Aiden Nibali, Zhen He, Stuart Morgan, and Luke Prendergast. 3d human pose estimation with 2d marginal heatmaps. In *WACV*, 2019.
- [42] Xuecheng Nie, Jiashi Feng, Jianfeng Zhang, and Shuicheng Yan. Single-stage multi-person pose machines. In *ICCV*, 2019.
- [43] George Papamakarios, Theo Pavlakou, and Iain Murray. Masked autoregressive flow for density estimation, 2017.
- [44] George Papandreou, Tyler Zhu, Liang-Chieh Chen, Spyros Gidaris, Jonathan Tompson, and Kevin Murphy. Personlab: Person pose estimation and instance segmentation with a bottom-up, part-based, geometric embedding model. In *ECCV*, 2018.
- [45] George Papandreou, Tyler Zhu, Nori Kanazawa, Alexander Toshev, Jonathan Tompson, Chris Bregler, and Kevin Murphy. Towards accurate multi-person pose estimation in the wild. In *CVPR*, 2017.
- [46] Georgios Pavlakos, Xiaowei Zhou, Konstantinos G Derpanis, and Kostas Daniilidis. Coarse-to-fine volumetric prediction for single-image 3d human pose, 2017.
- [47] Dario Pavlo, Christoph Feichtenhofer, David Grangier, and Michael Auli. 3d human pose estimation in video with temporal convolutions and semi-supervised training. In *CVPR*, 2019.
- [48] Leonid Pishchulin, Eldar Insafutdinov, Siyu Tang, Bjoern Andres, Mykhaylo Andriluka, Peter V Gehler, and Bernt Schiele. Deepcut: Joint subset partition and labeling for multi person pose estimation. In *CVPR*, 2016.
- [49] Danilo Rezende and Shakir Mohamed. Variational inference with normalizing flows. In *ICML*, 2015.
- [50] Gregory Rogez, Philippe Weinzaepfel, and Cordelia Schmid. Lcr-net: Localization-classification-regression for human pose. In *CVPR*, 2017.
- [51] Gregory Rogez, Philippe Weinzaepfel, and Cordelia Schmid. Lcr-net++: Multi-person 2d and 3d pose detection in natural images. *TPAMI*, 2019.
- [52] Ke Sun, Bin Xiao, Dong Liu, and Jingdong Wang. Deep high-resolution representation learning for human pose estimation. In *CVPR*, 2019.
- [53] Xiao Sun, Jiaxiang Shang, Shuang Liang, and Yichen Wei. Compositional human pose regression. In *ICCV*, 2017.
- [54] Xiao Sun, Bin Xiao, Fangyin Wei, Shuang Liang, and Yichen Wei. Integral human pose regression. In *ECCV*, 2018.
- [55] Zhi Tian, Hao Chen, and Chunhua Shen. Directpose: Direct end-to-end multi-person pose estimation. *arXiv preprint arXiv:1911.07451*, 2019.
- [56] Jonathan Tompson, Ross Goroshin, Arjun Jain, Yann LeCun, and Christoph Bregler. Efficient object localization using convolutional networks. In *CVPR*, 2015.
- [57] Jonathan J Tompson, Arjun Jain, Yann LeCun, and Christoph Bregler. Joint training of a convolutional network and a graphical model for human pose estimation. *NeurIPS*, 2014.
- [58] Alexander Toshev and Christian Szegedy. Deeppose: Human pose estimation via deep neural networks. In *CVPR*, 2014.
- [59] Can Wang, Jiefeng Li, Wentao Liu, Chen Qian, and Cewu Lu. Hmor: Hierarchical multi-person ordinal relations for monocular multi-person 3d pose estimation. In *ECCV*, 2020.
- [60] Luyang Wang, Yan Chen, Zhenhua Guo, Keyuan Qian, Mude Lin, Hongsheng Li, and Jimmy S Ren. Generalizing monocular 3d human pose estimation in the wild, 2019.
- [61] Fangyun Wei, Xiao Sun, Hongyang Li, Jingdong Wang, and Stephen Lin. Point-set anchors for object detection, instance segmentation and pose estimation. In *ECCV*, 2020.
- [62] Shih-En Wei, Varun Ramakrishna, Takeo Kanade, and Yaser Sheikh. Convolutional pose machines. In *CVPR*, 2016.
- [63] Lijun Wu, Fei Tian, Yingce Xia, Yang Fan, Tao Qin, Jianhuang Lai, and Tie-Yan Liu. Learning to teach with dynamic loss functions. In *NeurIPS*, 2018.
- [64] Bin Xiao, Haiping Wu, and Yichen Wei. Simple baselines for human pose estimation and tracking. In *ECCV*, 2018.
- [65] Hongyi Xu, Eduard Gabriel Bazavan, Andrei Zanfir, William T Freeman, Rahul Sukthankar, and Cristian Sminchisescu. Ghum & ghuml: Generative 3d human shape and articulated pose models. In *CVPR*, 2020.
- [66] Andrei Zanfir, Eduard Gabriel Bazavan, Hongyi Xu, Bill Freeman, Rahul Sukthankar, and Cristian Sminchisescu. Weakly supervised 3d human pose and shape reconstruction with normalizing flows. *ECCV*, 2020.
- [67] Ailing Zeng, Xiao Sun, Fuyang Huang, Minhao Liu, Qiang Xu, and Stephen Lin. Srnet: Improving generalization in 3d human pose estimation with a split-and-recombine approach. In *ECCV*, 2020.
- [68] Long Zhao, Xi Peng, Yu Tian, Mubbasir Kapadia, and Dimitris N. Metaxas. Semantic graph convolutional networks for 3d human pose regression. In *CVPR*, 2019.
- [69] Kun Zhou, Xiaoguang Han, Nianjuan Jiang, Kui Jia, and Jiangbo Lu. Hemlets pose: Learning part-centric heatmap triplets for accurate 3d human pose estimation. In *ICCV*, 2019.
- [70] Xingyi Zhou, Dequan Wang, and Philipp Krähenbühl. Objects as points. *arXiv preprint arXiv:1904.07850*, 2019.