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Rethinking Federated Learning with Domain Shift: A Prototype View

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https://github.com/WenkeHuang/RethinkFL

Abstract

Federated learning shows a bright promise as a privacypreserving collaborative learning technique. However, prevalent solutions mainly focus on all private data sampled from the same domain. An important challenge is that when distributed data are derived from diverse domains. The private model presents degenerative performance on other domains (with domain shift). Therefore, we expect that the global model optimized after the federated learning process stably provides generalizability performance on multiple domains. In this paper, we propose Federated Prototypes Learning (FPL) for federated learning under domain shift. The core idea is to construct cluster prototypes and unbiased prototypes, providing fruitful domain knowledge and a fair convergent target. On the one hand, we pull the sample embedding closer to cluster prototypes belonging to the same semantics than cluster prototypes from distinct classes. On the other hand, we introduce consistency regularization to align the local instance with the respective unbiased prototype. Empirical results on Digits and Office Caltech tasks demonstrate the effectiveness of the proposed solution and the efficiency of crucial modules.

1. Introduction

Federated learning is a privacy-preserving paradigm [47, 83], which reaches collaborative learning without leaking privacy. The cornerstone solution, FedAvg [47], aggregates parameters from participants and then distributes the global model (averaged parameters) back for further training, which aims to learn a high-quality model without centralizing private data. However, an inherent challenge in federated learning is data heterogeneity [26, 39, 69, 87]. Specifically, the private data is collected from distinct sources with diverse preferences and presents non-iid (independently and

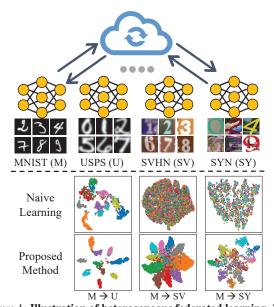


Figure 1. **Illustration of heterogeneous federated learning**. The feature visualization on inter domains (\rightarrow represents testing on target domain *i.e.*, M \rightarrow SV means that local dataset is from MNIST and test model on SVHN). The **top** row indicates that local training results in domain shift. The **bottom** row shows that our method acquires generalizable performance on different domains.

identically distributed) distribution [87]. Each participant optimizes toward the local empirical risk minimum, which is inconsistent with the global direction. Therefore, the averaged global model unavoidably faces a slow convergence speed [40] and achieves limited performance improvement.

A mainstream of subsequent efforts delves into introducing a variety of global signals to regulate private model [13, 28, 38, 40, 51, 66, 70]. These methods focus on label skew, where distributed data are from the **same domain**, and simulate data heterogeneity via imbalanced sampling, *e.g.*, Dirichlet strategy [32] to generate different label distributions. Nonetheless, another noticeable data het-

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erogeneous property in federated learning is domain shift [21,22,41,55,57]. In particular, private data is derived from various domains, leading to distinct feature distributions. In this scenario, we argue that naive learning on private data brings poor generalizable ability in Fig. 1. Specifically, the private model fails to provide discrimination on other domains because it overfits local domain distribution. The aforementioned methods mainly regulate the private model via global knowledge (i.e., the average signals from participants). Therefore, these algorithms share a common weakness: the global information is insufficient to describe diverse domain knowledge, which is magnified under the domain shift and thus hinders the improvement of generalizability. An intuitive solution is to preserve multiple models for distilling respective domain knowledge. However, it incurs a high cost of both communication and computation.

Taking into account both the effectiveness and efficiency, we rethink the prototype [11, 36, 67, 82, 91], which is the mean value of features with identical semantics. It represents class-wise characteristics and is vector type [90]. Given the enormous participant scale in federated learning, it is not efficient and feasible to maintain all prototypes. However, directly averaging all prototypes to get global prototypes would arise the same impediment as global models because averaging operation weakens the domain diversity. Besides, global prototypes probably yield biased to the dominant domain due to the unknown of private domains proportion, which results in disadvantageous performance on minority domains. Driven by these two issues, on the one hand, we find representative prototypes by clustering all prototypes. Therefore, each class is abstracted by a set of diverse prototypes, capturing rich domain variance. On the other hand, we generate unbiased prototypes based on cluster prototypes to construct fair and stable global signals, which avoid optimizing toward the underlying primary domain and thus ensure stability on different domains. Compared with original feature vectors, cluster and unbiased prototypes are privacy-friendly because it experiences twice and third times averaging operation [70]. Hence, it is less feasible to disentangle each raw representation and subsequently reconstruct private data. We analyze the superiority of cluster prototypes and unbiased prototypes in Sec. 3.2.

In this paper, we propose Federated Prototype Learning (FPL), which consists of two components. **First**, in order to improve the generalizability on the premise of discriminability. We introduce Cluster Prototypes Contrastive Learning (CPCL), which leverages cluster prototypes to construct contrastive learning [7,19,79,84,85]. CPCL adaptively enforces the query embedding to be more similar to cluster prototypes from the same class than other prototypes with different semantics. In particular, such an objective encourages instance feature to be close to representative prototypes in the same semantic and separates it away from other

class prototypes, which incorporates diverse domain knowledge and maintains a clear decision boundary. **Second**, we utilize unbiased prototypes to provide a fair and stable convergence point and propose Unbiased Prototypes Consistent Regularization (UPCR). Specifically, we average cluster prototypes to acquire unbiased prototypes. The local instance is required to minimize the feature-level distance with the corresponding unbiased prototype. Therefore, the local model would not be biased toward dominant domains and exhibits stable performance on inferior domains. We conjecture that these two components together make FPL a competitive method for federated learning with domain shift. The main contributions are summarized below.

- We focus on heterogeneous federated learning with domain shift and identify that the inherent limitation of existing methods is that global regularization signal is insufficient to depict diverse domain knowledge and biased toward major domain among participants.
- We propose a simple yet effective strategy to learn a well generalizable global model in federated learning with domain shift. Inspired by the success of prototype learning, we introduce cluster prototypes to provide rich domain knowledge and further construct unbiased prototypes based on the average of cluster prototypes to further offer fair and stable objective signal.
- We conduct extensive experiments on Digits [23, 33, 52, 61] and Office Caltech [16] tasks. Accompanied with a set of ablative studies, promising results validate the efficacy of FPL and the indispensability of each module.

2. Related Work

2.1. Data Heterogeneous Federated Learning

Federated learning is proposed to handle privacy concerns in the distributed learning environment. A pioneering federated method, FedAvg [47] trains a global model by aggregating local model parameters. However, its performance is impeded due to decentralized data, which poses non-i.i.d distribution (called data heterogeneity). Based on FedAvg, existing methods of tackling data heterogeneity problem mainly leverage global penalty term. Fed-Prox [40], FedCurv [66], pFedME [68], and FedDyn [1] calculate global parameter stiffness to control discrepancies. Besides, MOON [38], FedUFO [86], FedProto [70], and FedProc [51] maximize feature-level agreement of local model and global model. Moreover, SCAFFOLD [28] and FedDC [13] leverage global gradient calibration to control local drift. The major limitation of these methods is that they focus on single domain performance under label skew scenario and overlook the problem of domain shift, leading to an unsatisfying generalizable performance on multiple domains. Closely related methods such as FedBN [41], ADCOL [37], FCCL [22] focus on personalized models rather than a shared global model. Besides, the latter two methods require additional discriminator and public data, which incurs a heavy burden for either the participant or the server side. In this paper, we introduce cluster prototypes (diverse domain knowledge) and unbiased prototypes (consistent optimization direction) to learn a generalizable and stable global model during the federated learning process.

2.2. Clustering Federated Learning

Clustered federated learning involves grouping clients with similar data distributions into clusters, such that each client is uniquely associated with a particular data distribution and contributes to the training of a model tailored to that distribution [64, 80]. Existing methods can mainly leverage four types of clustering signals: model parameters [5, 43], gradient information [10, 64], training loss [15, 46] and exogenous information [2, 42]. However, we leverage the clustering strategy to select representative prototypes in order to address the federated learning with domain shift.

2.3. Prototype Learning

Prototype refers to the mean vector of the instances belonging to the identical class [67]. Due to its exemplardriven nature and simpler inductive bias, it has boosted great potential in a variety of tasks. For example, in supervised classification tasks, it labels testing images via calculating its distance with prototypes of each class, which is considered to be more robust and stabler [81] in handling few-shot [48, 67, 75, 81], zero-shot [25]. Moreover, it also has been a surge of interest in semantic segmentation task [35, 77, 90], unsupervised learning [18, 36, 79, 84, 85] and so on. As for federated learning, prototypes can provide diverse abstract knowledge while adhering to privacy protocols. There exist a few works incorporating prototypes to handle data heterogeneous federated learning. PGFL [49] leverages prototypes to construct weight attention parameter aggregation. FedProc [51] and FedProto [70] aim to reach feature-wise alignment with global prototypes. CCVR [44] generates virtual feature based on approximated Gaussian Mixture Model. FedPCL [71] focuses on personalized federated learning and utilizes prototypes to learn personalized models. However, these methods focus on single-domain performance. In domain shift, it is vital to consider generalization on diverse domains. Our work sheds light on leveraging cluster and unbiased prototypes to achieve this goal in federated learning.

2.4. Contrastive Learning

Contrastive learning has recently become a promising direction in the self-supervised learning field, achieving competitive performance as supervised learning. The classic methods [7, 19, 53, 79, 84, 85] mainly construct a positive pair and a negative pair for each instance and leverage InfoNCE [54] to contrast positiveness against neg-

ativeness. A major branch of subsequent research focuses on elaborating the selection of the informative positive pairs [3, 12, 30, 31, 34, 56, 59, 65] and negative pairs [8, 14, 24, 27, 50, 60, 72, 88]. Another line explicitly investigates the semantic structure and introduces unsupervised clustering methods to construct fruitful prototypes as representative embeddings for groups of semantically similar instances [6, 18, 36, 73, 89]. Differently, in this work, Cluster Prototypes Contrastive Learning (CPCL) is designed for providing generalization ability in federated learning with domain shift. We leverage the unsupervised clustering algorithm to select representative prototypes for each class and then seek to attract each instance to cluster prototypes in the same semantics while pushing away other cluster prototypes from different classes, which brings both generalizable and discriminative ability.

3. Methodology

3.1. Preliminaries

Following the typical federated learning [40, 47], there are M participants (indexed by m) with respective private data, $D_m = \{x_i, y_i\}_{i=1}^{N_m}$, where N_m denotes the local data scale. Under heterogeneous federated learning, the conditional feature distribution P(x|y) varies across participants even if P(y) is consistent, resulting in **domain shift**:

• Domain shift: $P_m(x|y) \neq P_n(x|y)$ $(P_m(y) = P_n(y))$. There exists domain shift among private data. Specifically, for the same label space, distinctive feature distribution exists among different participants.

Besides, participants agree on sharing a model with the same architecture. We regard the model with two modules: feature extractor and unified classifier. The feature extractor $f : \mathcal{X} \to \mathcal{Z}$, encodes sample x into a compact d dimensional feature vector $z = f(x) \in \mathbb{R}^d$ in the feature space \mathcal{Z} . A unified classifier $g : \mathcal{Z} \to \mathbb{R}^{|I|}$, maps feature z into logits output l = g(z), where I means the classification categories. The optimization direction is to learn a generalizable global model to present favorable performance on multiple domains, through the federated learning process.

3.2. Prototypes Meet Federated Learning

Motivation. Each prototype $c^k \in R^d$ is calculated by the mean vector of the features belonging to same class:

$$e^{k} = \frac{1}{|S^{k}|} \sum_{(x_{i}, y_{i}) \in S^{k}} f(x_{i}),$$
 (1)

where S^k means the set of samples annotated with class k. Prototypes are typical for respective semantic information. Besides, it carries the specific domain style information because the prototypes are not consistent on different domains. Therefore, it motivates us to leverage prototypes from different domains to learn a generalizable model without leaking privacy information. We further define the k^{th}

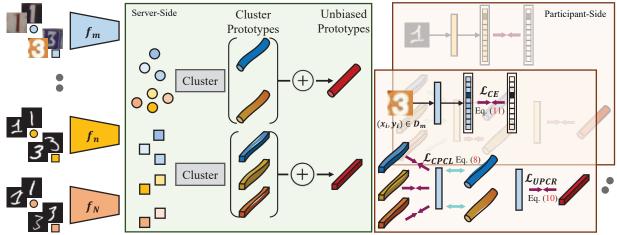


Figure 2. Architecture illustration of Federated Prototypes Learning (FPL). Participants upload local prototypes to server. Based on these prototypes, we introduce cluster prototypes () to construct Cluster Prototypes Contrastive Learning (CPCL in Sec. 3.3.1), bringing diverse domain information. Besides, we acquire unbiased prototypes () and propose Unbiased Prototypes Consistent Regularization (UPCR in Sec. 3.3.2) to provide a stable consistency signal. Best viewed in color. Zoom in for details.

class prototype from the m^{th} participant as:

$$c_{m}^{k} = \frac{1}{|S_{m}^{k}|} \sum_{(x_{i}, y_{i}) \in S_{m}^{k}} f_{m}(x_{i})$$

$$\mathcal{O}_{m} = [c^{1} - c^{k} - c^{|I|}] \in \mathbb{R}^{|I| \times d}$$
(2)

where $S_m^k = \{x_i, y_i | y_i = k\}_{i=1}^{N_m^k} \subset D_m$ represents the private dataset D_m of the k^{th} class for the m^{th} participant.

Global Prototypes. Considering that number of participants is large-scale in federated learning, the straightforward solution to leverage prototypes is the global prototypes (G) via directly averaging operation akin to the global model. Hence, the global prototypes are formulated into:

$$\mathcal{G}^{k} = \frac{1}{N} \sum_{m=1}^{N} c_{m}^{k} \in \mathbb{R}^{d}$$

$$\mathcal{G} = [\mathcal{G}^{1}, \dots, \mathcal{G}^{k}, \dots, \mathcal{G}^{|I|}].$$
(3)

However, global prototypes mainly suffer from two notable problems. • Global prototype unavoidably faces the same dilemma as the global model. In detail, it depicts each class signal by only one prototype, bearing no domain variation under heterogeneous federated learning with domain shift. • Moreover, due to the unknown of participants data distribution in federated learning, global prototypes would be biased toward the dominant domain distribution, leading to a skewed optimization objective during federated process.

Cluster Prototypes. Inspired by such limitations, we first propose cluster prototypes. Compared with global prototypes, we select representative prototypes rather than single one via unsupervised clustering method, FINCH [63]. Compared with well-known clustering techniques such as Kmeans [4, 45] and HAC [78], FINCH is parameter-free and thus suitable for federated learning with uncertain participants scale. Specifically, FINCH views that the nearest neighbor of each sample is a sufficient support for grouping.

It implicitly picks characteristic prototypes because prototypes from different domains are less likely to be the first neighbor. Therefore, prototypes from different domains probably fail to merge together, while prototypes from similar domains fall into the same group, conversely. Specifically, we leverage cosine similarity to evaluate the distance between any two prototypes and view the prototype with minimum distance as its 'neighbor', sorted into the same set. We define the k^{th} class prototype adjacency matrix as:

$$A^{k}(m,n) = \begin{cases} 1, & \text{if } n = v_{m}^{k} \text{ or } m = v_{n}^{k} \text{ or } v_{m}^{k} = v_{n}^{k}; \\ 0, & \text{otherwise,} \end{cases}$$
(4)

where v_m^k denotes the first neighbor (largest cosine similarity) of the class k prototype from the m^{th} participant, c_m^k . Then, we select several representative prototypes in the embedding space based on the clustering results via Eq. (4). Thus, the cluster prototypes (\mathcal{P}) are denoted as:

$$\mathcal{P}^{k} = \{c_{m}^{k}\}_{m=1}^{N} \underbrace{\text{Cluster}}_{m} \{c_{m}^{k}\}_{m=1}^{J} \in \mathbb{R}^{J \times d}$$

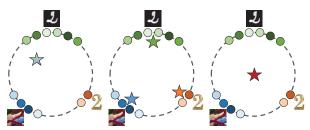
$$\mathcal{P} = \{\mathcal{P}^{1}, \dots, \mathcal{P}^{k}, \dots, \mathcal{P}^{|I|}\}.$$
(5)

We cluster N prototypes into J representatives of class k, which effectively addresses the aforementioned problem **①**. **Unbiased Prototypes**. Nevertheless, the scale of cluster prototypes is variant because the unsupervised clustering methods generate them after each communication, which can not ensure a stable and fair convergent point. Thus, we further average cluster prototypes to get a consistent signal: unbiased prototypes (\mathcal{U}), which is calculated as follows:

$$\mathcal{U}^{k} = \frac{1}{J} \sum_{c^{k} \in \mathcal{P}^{k}} c^{k} \in \mathbb{R}^{d}$$

$$\mathcal{U} = [\mathcal{U}^{1}, \dots, \mathcal{U}^{k}, \dots, \mathcal{U}^{|I|}].$$
(6)

Note that compared with global prototypes (\mathcal{G}), unbiased prototypes (\mathcal{U}) largely avoid being biased toward dominant domains in heterogeneous federated learning and provide a stable optimization target. Thus, we hypothesize that unbi-



Global Prototype Cluster Prototype Unbiased Prototype Figure 3. **Illustration of different prototypes**. Global prototype (\bigstar) fails to describe diverse domains information and is biased toward the underlying dominant domain. Cluster prototype ($\bigstar \bigstar$) and unbiased prototype (\bigstar) carry multiple domain knowledge and stable optimization signal. See details in Sec. 3.2.

ased prototypes could depict the considerably fair convergent point and further leverage them to conduct consistent regularization, which productively handles the problem \boldsymbol{Q} . Discussion. We further explain the difference of these three kinds of prototypes in Fig. 3. Global prototypes inherently present limited domain knowledge and show skewed feature space toward the potentially dominant domains in heterogeneous federated learning. Cluster and unbiased prototypes complementarily handle these two problems because the former provides fruitful domain knowledge and the latter represents an ideal optimization target, collaboratively ensuring both generalization and stability. Compared with existing methods that leverage the global model to construct regularization term, prototypes are substantially smaller in size than model parameters, which bring less computation cost for participants. Besides, cluster prototypes and unbiased prototypes are privacy-safe because they experience twice and third times averaging operations through unsupervised clustering. Therefore, leveraging these two kinds of prototypes: cluster prototypes and unbiased prototypes is not only a computation-friendly media but also a privacypreserving solution in heterogeneous federated learning.

3.3. Federated Prototypes Learning

For generalizability and stability in heterogeneous federated learning with domain shift, we leverage cluster prototypes and unbiased prototypes to obtain fruitful domain knowledge and stable consistency signal. The proposed method comprises two key components: Cluster Prototypes Contrastive Learning (CPCL in Sec. 3.3.1) and Unbiased Prototypes Consistent Regularization (UPCR in Sec. 3.3.2).

3.3.1 Cluster Prototypes Contrastive Learning

We deem that a well-generalizable representation should not only be discriminative to provide a clear decisional boundary for different classes but also be as invariant as possible to diverse domain distortions that are applied to this sample. Specifically, for instance $(x_i, y_i) \in D_m$, we feed it into network and acquire its feature vector z_i = $f(x_i)$. Then, we enforce the instance feature to be similar to respective semantic prototypes (\mathcal{P}^k) and dissimilar to different semantic prototypes $(\mathcal{N}^k = \mathcal{P} - \mathcal{P}^k)$. We define the similarity of the query sample embedding z_i with corresponding cluster prototypes $c \in \mathcal{P}$ as follows:

$$s(z_i, c) = \frac{z_i \cdot c}{||z_i|| \times ||c||/\tau},$$
(7)

where temperature hyper-parameter, τ controls the concentration strength of representations [76]. Thus, we expect to enlarge the similarity with semantic coincident cluster prototypes than other different cluster prototypes, which aims to maintain a clear class-wise decision boundary. In our work, we introduce Cluster Prototypes Contrastive Learning (CPCL) to contrast cluster prototypes with the same class for each query sample against other remainder of cluster prototypes with different semantics. It is natural to derive the following optimization objective term:

$$\mathcal{L}_{CPCL} = -\log \frac{\sum_{c \in \mathcal{P}^k} \exp(s(z_i, c))}{\sum_{c \in \mathcal{P}^k} \exp(s(z_i, c)) + \sum_{c \in \mathcal{N}^k} \exp(s(z_i, c))}$$
$$= \log(1 + \frac{\sum_{c \in \mathcal{N}^k} \exp(s(z_i, c))}{\sum_{c \in \mathcal{P}^k} \exp(s(z_i, c))}),$$
(8)

We give a detailed optimization direction analysis of Eq. (8) and thus reformulate the CPCL loss function as follows: $\min \mathcal{L}_{CPCL}$

$$\equiv \log(\frac{\sum_{c \in \mathcal{N}^k} \exp(s(z_i, c))}{\sum_{c \in \mathcal{P}^k} \exp(s(z_i, c))})$$

$$\equiv \underbrace{\log(\sum_{c \in \mathcal{N}^k} \exp(s(z_i, c)))}_{\text{Discriminative}} - \underbrace{\log(\sum_{c \in \mathcal{P}^k} \exp(s(z_i, c)))}_{\text{Generalizable}}.$$
(9)

Note that minimizing Eq. (8) equally requires pulling embedding vector z_i closely to its assigned positive cluster prototypes (\mathcal{P}^k) and pushing z_i far away from others negative prototypes (\mathcal{N}^k), which not only aims to be invariant to diverse domain distortions but also enhances the semantic spread-out property, promising both generalizable and discriminative property of feature space and thus acquiring satisfying generalizable performance in federated learning.

3.3.2 Unbiased Prototypes Consistent Regularization

Although cluster prototypes bring diverse domain knowledge for the sake of plasticity under domain shift, the cluster prototypes are dynamically generated at each communication and its scale is changing due to the unsupervised clustering method. Therefore, cluster prototypes could not offer a stable convergence direction at different communication epochs. We assume that unbiased prototypes (\mathcal{U} in Eq. (6)) based on averaged cluster prototypes, could provide a relatively fair and stable optimization point and thus cope with the problem of convergence instability. Thus, in this paper, we purpose Unbiased Prototypes Consistent Regularization (UPCR) to leverage unbiased prototypes. Specifically, we utilize a consistency regularization term to pull the feature vector z_i closer to the respective unbiased prototype, U^k as:

$$\mathcal{L}_{UPCR} = \sum_{v=1}^{d} (z_{i,v} - \mathcal{U}_v^k)^2, \tag{10}$$

where v indexes the dimension of feature output. We expect to achieve feature-level alignment between query embedding and the corresponding unbiased prototype. Besides, we construct CrossEntropy [9] loss and use the logits output $(l_i = g(z_i))$ with original annotation signal (y_i) to maintain local domain discriminative ability via:

$$\mathcal{L}_{CE} = -\mathbf{1}_{y_i} \log(\sigma(l_i)), \tag{11}$$

where σ denotes softmax. Finally, we carry out the following optimization objective in local updating phase:

$$\mathcal{L} = \mathcal{L}_{CPCL} + \mathcal{L}_{UPCR} + \mathcal{L}_{CE}. \tag{12}$$

The overall federated learning algorithm is shown in Algorithm 1. In each communication epoch, the server distributes the cluster prototypes and unbiased prototypes to participants. In local updating, each participant optimizes on local data, while the objective is defined in Eq. (12).

4. Experiments

4.1. Experimental Setup

Datasets. We evaluate methods on two classification tasks:

- Digits [23, 33, 52, 61] includes four domains: MNIST (M), USPS (U), SVHN (SV) and SYN (SY) with 10 categories (digit number from 0 to 9).
- Office Caltech [16] consists four domains: Caltech (C), Amazon (A), Webcam (W) and DSLR (D), which is formed of ten overlapping classes between Office31 [62] and Caltech-256 [17].

We initialize 20 and 10 participants for Digits and Office Caltech tasks and randomly allocate domains for participants. In detail, the Digits task is MNIST: 3, USPS: 7, SVHN: 6 and SYN: 4. The Office Caltech is Caltech: 3, Amazon: 2, Webcam: 1 and DSLR: 4. For each participant, local data is randomly selected from these domains with different proportions (*i.e.*, 1 % in Digits and 20 % in Office Caltech), based on the difficulty and scale of the tasks. We fix the seed to ensure reproduction of our results.

Model. For these two classification tasks, we conduct experiment with ResNet-10 [20]. The feature vector dimension is 512. Note that all methods use the same network architecture for fair comparison in different tasks.

Counterparts. We compare ours against several sota federated methods focusing on **learning a shared global model**: FedAvg (AISTATS'17 [47]), FedProx (arXiv'18 [40]), MOON (CVPR'21 [38]), FedDyn (ICLR'21 [1]), FedOPT (ICLR'21 [58]), FedProc (arXiv'21 [51]) and FedProto (AAAI'22 [70] with parameter averaging).

Algorithm 1: FPL

Input: Communication epochs *E*, local rounds *T*, number of participants *M*, m^{th} participant private data $D_m(x, y)$, private model θ_m **Output:** The final global model θ^E

for e = 1, 2, ..., E do Participant Side; for m = 1, 2, ..., N in parallel do $\[\[\] \theta_m^e, \mathcal{O}_m \leftarrow \text{LocalUpdating}(\theta^e, \mathcal{P}, \mathcal{U}) \]$ Server Side; $\theta^{e+1} \leftarrow \sum_{m=1}^{N} \frac{|D_m|}{|D|} \theta_m^e$ /* Cluster prototypes */ $\mathcal{P}^k = \{c_m^k\}_{m=1}^{N} \underbrace{\text{Cluster}}_{m=1} \{c_m^k\}_{m=1}^{J} \text{ via Eq. (5)}$ /* Unbiased prototypes */ $\mathcal{U}^k = \frac{1}{J} \sum_{c^k \in \mathcal{P}^k} c^k \text{ by Eq. (6)}$

LocalUpdating(θ^e , \mathcal{P} , \mathcal{U}):

```
\theta^e_m \leftarrow \bar{\theta}^e ; // Distribute global parameter for t=1,2,...,T do
```

```
for (x_i, y_i) \in D_m do
           z_i = f_m^e(x_i)
            l_i = g_m^e(z_i)
             /* Cluster Prototypes Contrastive
                   Learning */
             \mathcal{L}_{CPCL} \leftarrow (z_i, \mathcal{P}) \text{ in Eq. (8)}; // \text{Sec. 3.3.1}
             /* Unbiased Prototypes Consistent
                   Regularization */
            \mathcal{L}_{UPCR} \leftarrow (z_i, \mathcal{U}) \text{ in Eq. (10)}; // \text{ Sec. 3.3.2}
            \mathcal{L}_{CE} \leftarrow (l_i, y_i) in Eq. (11)
            \mathcal{L} = \mathcal{L}_{CPCL} + \mathcal{L}_{UPCR} + \mathcal{L}_{CE}
           \theta_m^e \leftarrow \theta_m^e - \eta \nabla \mathcal{L}
\mathcal{O}_m = \{\};
                        // Initialize local prototypes
/* Local prototypes */
for k = 1, 2, ..., |I| do
     \begin{split} S_m^k &= \{x_i, y_i | y_i = k\}^{N_m^k} \subset D_m \\ c_m^k &= \frac{1}{N_m^k} \sum_{(x_i, y_i) \in S_m^k} f_m(x_i) \end{split}
    \mathcal{O}_m = \mathcal{O}_m \cup \{c_m^k\} in Eq. (2)
return \theta_m^e, \mathcal{O}_m
```

Implement Details. To enable a fair comparison, we follow the same setting in [22,38]. We conduct communication epoch for E = 100 and local updating round T = 10, where all federated learning approaches have little or no accuracy gain with more communications. We use the SGD optimizer with the learning rate lr = 0.01 for all approaches. The corresponding weight decay is 1e - 5 and momentum is 0.9. The training batch size is 64. The hyper-parameter setting for FPL presents in the next Sec. 4.2.

Evaluation Metric. Following [40, 47], Top-1 accuracy is adopted for fair evaluation in these two classification tasks. We conduct experiments for three times and utilize the last five communication epochs accuracy as final performance.

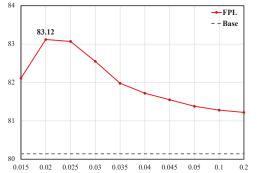


Figure 4. Analysis of FPL with different temperature (Eq. (7)). "Base" denotes FedAvg. See details in Sec. 4.2.

CDCI	UPCR	Digits							
CICL		MNIST	USPS	SVHN	SYN	AVG			
		98.14	90.85	76.56	55.01	80.14			
\checkmark		98.03	91.13	79.76	56.84	81.44			
	1	98.23	93.12	81.18	55.40	81.98			
1	1	98.31	92.71	80.27	61.20	83.12			
CDCI			Offi	ce Caltech	ı				
CPCL	UPCR	Caltech		ce Caltech Webcam	-	AVG			
CPCL	UPCR	Caltech 60.15			-	AVG 54.36			
CPCL	UPCR		Amazon	Webcam	DSLR				
CPCL	UPCR	60.15	Amazon 75.44	Webcam 45.86	DSLR 36.00	54.36			

Table 1. **Ablation study of key components** of our method in Digits and Office Caltech task. Please see Sec. **4.2** for details.

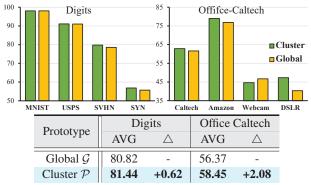


Figure 5. Comparison of cluster (\mathcal{P} in Eq. (5)) and global prototypes (\mathcal{G} in Eq. (3)) for CPCL (Sec. 3.3.1) on each domain (Top Row) and overall performance (Bottom Row) in Digits and Office Caltech tasks with $\tau = 0.02$. See details in Sec. 4.2.1.

4.2. Diagnostic Analysis

For thoroughly analyzing the efficacy of essential modules in our approach, we perform an ablation study on Digits and Office Caltech to investigate: Cluster Prototypes Contrastive Learning (CPCL) and Unbiased Prototypes Consistent Regularization (UPCR). We firstly present the overall performance with different contrastive temperature (τ in Eq. (8)). The Fig. 4 reveals that a smaller temperature benefits training more than higher ones, but extremely low temperatures are harder to train due to numerical instability ($\mathcal{L} = NaN$ in Eq. (12) when $\tau = 0.01$), corroborating relevant observations reported in [7, 29, 74, 76]. Specifically, the accuracy progressively increases as τ enlarges, and the amelioration becomes marginal when $\tau = 0.02$. Hence, we choose $\tau = 0.02$ by default. We further give a quantitative result on these two components in Tab. 1. The first row refers to the FedAvg which directly averages model parameter without extra operation. Three crucial conclusions can be drawn. First, CPCL leads to significant performance improvements against the baseline on different tasks. This evidences that CPCL strategy is able to produce generalizable feature space. Second, we notice gains by incorporating UPCR into the baseline. This proves the importance of considering consistent regularization. Third, combining CPCL and UPCR achieves better performance, which supports our motivation of exploiting joint generalization and stability in heterogeneous federated learning.

4.2.1 Cluster Prototypes Contrastive Learning

To prove the superiority of cluster prototypes (\mathcal{P} in Eq. (5)) in providing generalizable and discriminative ability, we compare them with global prototypes (\mathcal{G} in Eq. (3)) on Office Caltech task under contrastive temperature $\tau = 0.02$ in Fig. 5. The results reveal that leveraging cluster prototypes performs better than global prototypes and thus confirm our motivation of leveraging multiple prototypes to capture diverse domain knowledge. For example, in Office Caltech task, cluster prototypes achieve 2.08% overall performance gain compared with global prototypes.

4.2.2 Unbiased Prototypes Consistent Regularization

Note that both global prototypes (\mathcal{G}) and unbiased prototypes (\mathcal{U}) are able to offer consistent regularization. We conduct experiments on Digits and Office Caltech in Tab. 3. These results confirm the superiority of utilizing unbiased prototypes to offer consistent signal. As seen, the unbiased prototypes provide a better convergence signal than global prototypes and present the increased performance on different tasks *i.e.*, Digits (+0.82) and Office Caltech (+0.73).

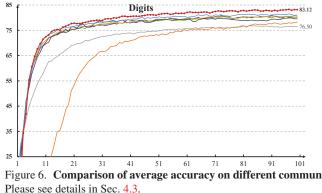
4.3. Comparison to State-of-the-Arts

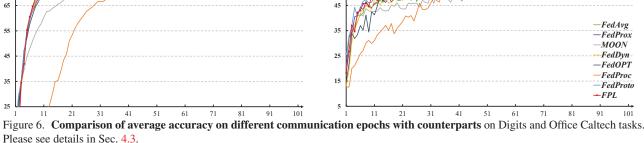
The Tab. 2 plots the final accuracy metric by the end of federated learning process with popular sota methods. It clearly depicts that our method performs significantly better than counterparts, which confirms that FPL can acquire well generalizable ability and thus effectively boost performance on different domains. Take the result of Office Caltech as an example, our method outperforms the best counterpart with a gap of 4.59%. We visualize the t-SNE visualization analysis of FPL at different communication epochs in Fig. 7,

Methods	Digits				Office Caltech							
wiethous	MNIST	USPS	SVHN	SYN	AVG	\bigtriangleup	Caltech	Amazon	Webcam	DSLR	AVG	\bigtriangleup
FedAvg [ASTAT17] [47]	98.14	90.85	76.56	55.01	80.14	-	60.15	75.44	45.86	36.00	54.36	-
FedProx [arXiv18] [40]	98.11	90.24	77.01	56.66	80.50	+0.36	60.21	77.44	48.62	37.33	55.90	+1.54
MOON [CVPR21] [38]	97.44	92.15	77.62	38.79	76.50	-3.64	56.19	71.54	41.04	30.22	49.74	-4.62
FedDyn [ICLR21] [1]	98.01	91.00	78.95	54.22	80.54	+0.40	61.64	75.54	48.28	35.56	55.25	+0.89
FedOPT [ICLR21] [58]	96.23	91.80	73.03	57.85	79.72	-0.42	56.31	56.74	63.33	48.89	56.31	+1.95
FedProc [arXiv21] [51]	97.86	88.99	78.90	45.84	77.89	-2.25	58.07	73.65	42.76	30.22	51.17	-3.19
FedProto [AAAI22] [70]	98.30	92.44	80.35	53.58	<u>81.16</u>	<u>+1.02</u>	64.02	79.37	50.17	40.33	<u>58.47</u>	<u>+4.11</u>
FPL	98.31	92.71	80.27	61.20	83.12	+2.98	63.39	79.26	55.86	48.00	61.63	+7.27

Table 2. Comparison with the sota methods on Digits and Office Caltech tasks. AVG denotes average accuracy calculated on all domains. See details in Sec. 4.3. Best in bold and second with underline. These notes are the same to others.

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Digits Prototype MNIST USPS SVHN SYN AVG \wedge G 98.30 92.44 80.35 53.58 81.16 U 98.23 93.12 81.18 55.40 81.98 +0.82Office Caltech Amazon Webcam DSLR AVG Caltech \wedge G 64.02 79.37 58.47 50.17 40.33 64.26 79.54 48.39 44.67 59.21 +0.73 \mathcal{U}

Table 3. Comparison of consistent regularization with global prototypes (\mathcal{G} in Eq. (3)) and unbiased prototypes (\mathcal{U} in Eq. (6)) on Digits and Office Caltech tasks. See details in Sec. 4.2.2.

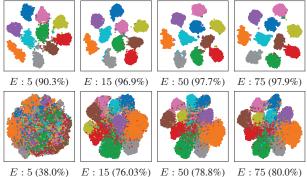


Figure 7. t-SNE Visualization of FPL at different communication epoch on randomly participants from MNIST (Top Row) and SVHN (Bottom Row). Please refer to Sec. 4.3 for details.

which depicts that FPL is feasible to learn a generalizable decision boundary. We draw the the average accuracy metric in each communication epoch during training phase in Fig. 6. We observe that FPL presents faster and stabler convergence speed than other methods in these two tasks.

Offfice-Caltech

5. Conclusion

In this paper, we explore the generalizability and stability problem under domain shift in heterogeneous federated learning. Our work introduces a simple yet effective federated learning algorithm, Federated Prototypes Learning (FPL). We leverage prototypes (class prototypical representation) to tackle these two problems by enjoying the complementary advantages of cluster prototypes and unbiased prototypes: diverse domain knowledge and stable convergence signal. The effectiveness of FPL has been thoroughly validated with many popular counterparts over various classification tasks. We wish this work to pave the way for future research on heterogeneous federated learning.

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