Multispectral and Hyperspectral Image Fusion by MS/HS Fusion Net

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Abstract

Hyperspectral imaging can help better understand the characteristics of different materials, compared with traditional image systems. However, only high-resolution multispectral (HrMS) and low-resolution hyperspectral (LrHS) images can be captured at video rate in practice. In this paper, we propose a model-based deep learning approach for merging an HrMS and LrHS images to generate a high-resolution hyperspectral (HrHS) image. In specific, we construct a novel MS/HS fusion model which takes the observation models of low-resolution images and the low-rankness knowledge along the spectral mode of HrHS image into consideration. Then we design an iterative algorithm to solve the model by exploiting the proximal gradient method. And then, by unfolding the designed algorithm, we construct a deep network, called MS/HS Fusion Net, with learning the proximal operators and model parameters by convolutional neural networks. Experimental results on simulated and real data substantiate the superiority of our method both visually and quantitatively as compared with state-of-the-art methods along this line of research.

1. Introduction

A hyperspectral (HS) image consists of various bands of images of a real scene captured by sensors under different spectrums, which can facilitate a fine delivery of more faithful knowledge under real scenes, as compared to traditional images with only one or a few bands. The rich spectra of HS images tend to significantly benefit the characterization of the imaged scene and greatly enhance performance in different computer vision tasks, including object recognition, classification, tracking and segmentation [10, 37, 35, 36].

In real cases, however, due to the limited amount of incident energy, there are critical tradeoffs between spatial and spectral resolution. Specifically, an optical system usually can only provide data with either high spatial resolution but a small number of spectral bands (e.g., the standard RGB image) or with a large number of spectral bands but reduced spatial resolution [23]. Therefore, the research issue on merging a high-resolution multispectral (HrMS) image and a low-resolution hyperspectral (LrHS) image to generate a high-resolution hyperspectral (HrHS) image, known as MS/HS fusion, has attracted great attention [47].

The observation models for the HrMS and LrHS images are often written as follows [12, 24, 25]:

\[
Y = XR + N_y, \quad (1)
\]

\[
Z = CX + N_z, \quad (2)
\]

where \(X \in \mathbb{R}^{HW \times s}\) is the target HrHS image\(^1\) with \(H, W\) and \(S\) as its height, width and band number, respectively, \(Y \in \mathbb{R}^{HW \times s}\) is the HrMS image with \(s\) as its band number \((s < S)\), \(Z \in \mathbb{R}^{hw \times S}\) is the LrHS image with \(h, w, S\) as its height, width and band number \((h < H, w < W)\), \(R \in \mathbb{R}^{S \times s}\) is the spectral response of the multispectral sensor as shown in Fig. 1 (a), \(C \in \mathbb{R}^{hw \times HW}\) is a linear operator which is often assumed to be composed of a cyclic convolution operator \(\phi\) and a down-sampling matrix \(D\) as shown in Fig. 1 (b), \(N_y\) and \(N_z\) are the noises contained in

\(^1\)The target HS image can also be written as tensor \(X \in \mathbb{R}^{H \times W \times S}\). We also denote the folding operator for matrix to tensor as: fold\((X) = \mathcal{X}\).
HRMS and LRHS images, respectively. Many methods have been designed based on (1) and (2), and achieved good performance [40, 14, 24, 25].

Since directly recovering the HRHS image \( X \) is an ill-posed inverse problem, many techniques have been exploited to recover \( X \) by assuming certain priors on it. For example, [54, 2, 11] utilize the prior knowledge of HRHS that its spatial information could be sparsely represented under a dictionary trained from HRMS. Besides, [27] assumes the local spatial smoothness prior on the HRHS image and uses total variation regularization to encode it in their optimization model. Instead of exploring spatial prior knowledge from HRHS, [52] and [26] assume more intrinsic spectral correlation prior on HRHS, and use low-rank techniques to encode such prior along the spectrum to reduce spectral distortions. Albeit effective for some applications, the rationality of these techniques relies on the subjective prior assumptions imposed on the unknown HRHS to be recovered. An HRHS image collected from real scenes, however, could possess highly diverse configurations both along space and across spectrum. Such conventional learning regimes thus could not always flexibly adapt different HS image structures and still have room for performance improvement.

Methods based on Deep Learning (DL) have outperformed traditional approaches in many computer vision tasks [34] in the past decade, and have been introduced to HS/MS fusion problem very recently [28, 30]. As compared with conventional methods, these DL-based ones are superior in that they need fewer assumptions on the prior knowledge of the to-be-recovered HRHS, while can be directly trained on a set of paired training data simulating the network inputs (LRHS&HRMS images) and outputs (HRHS images). The most commonly employed network structures include CNN [7], 3D CNN [28], and residual net [30]. Like other image restoration tasks where DL is successfully applied to, these DL-based methods have also achieved good resolution performance for MS/MS fusion task.

However, the current DL-based MS/HS fusion methods still have evident drawbacks. The most critical one is that these methods use general frameworks for other tasks, which are not specifically designed for MS/HS fusion. This makes them lack interpretability specific to the problem. In particular, they totally neglect the observation models (1) and (2) [28, 30], especially the operators \( R \) and \( C \), which facilitate an understanding of how LRHS and HRMs are generated from the HRHS. Such understanding, however, should be useful for calculating HRHS images. Besides this generalization issue, current DL methods also neglect the general prior structures of HS images, such as spectral low-rankness. Such priors are intrinsically possessed by all meaningful HS images, which implies that DL-based methods still have room for further enhancement.

In this paper, we propose a novel deep learning-based method that integrates the observation models and image prior learning into a single network architecture. This work mainly contains the following three-fold contributions:

Firstly, we propose a novel MS/HS fusion model, which not only takes the observation models (1) and (2) into consideration but also exploits the approximate low-rankness prior structure along the spectral mode of the HRHS image to reduce spectral distortions [52, 26]. Specifically, we prove that if and only if observation model (1) can be satisfied, the matrix of HRHS image \( X \) can be linearly represented by the columns in HRMS matrix \( Y \) and a to-be-estimated matrix \( \hat{Y} \), i.e., \( X = YA + \hat{Y}B \) with coefficient matrices \( A \) and \( B \). One can see Fig. 1 (d) for easy understanding. We then construct a concise model by combining the observation model (2) and the linear representation of \( X \). We also exploit the proximal gradient method [3] to design an iterative algorithm to solve the proposed model.

Secondly, we unfold this iterative algorithm into a deep network architecture, called MS/HS Fusion Net or MHF-net, to implicitly learn the to-be-estimated \( \hat{Y} \), as shown in Fig. 1 (c). After obtaining \( \hat{Y} \), we can then easily achieve \( X \) with \( Y \) and \( \hat{Y} \). To the best of our knowledge, this is the first deep-learning-based MS/HS fusion method that fully considers the intrinsic mechanism of the MS/HS fusion problem. Moreover, all the parameters involved in the model can be automatically learned from training data in an end-to-end manner. This means that the spatial and spectral responses (\( R \) and \( C \)) no longer need to be estimated beforehand as most of the traditional non-DL methods did, nor to be fully neglected as current DL methods did.

Thirdly, we have collected or realized current state-of-the-art algorithms for the investigated MS/HS fusion task, and compared their performance on a series of synthetic and real problems. The experimental results comprehensively substantiate the superiority of the proposed method, both quantitatively and visually.

In this paper, we denote scalar, vector, matrix and tensor in non-bold case, bold lower case, bold upper case and calligraphic upper case letters, respectively.

2. Related work

2.1. Traditional methods

The pansharpening technique in remote sensing is closely related to the investigated MS/HS problem. This task aims to obtain a high spatial resolution MS image by the fusion of a MS image and a wide-band panchromatic image. A heuristic approach to perform MS/HS fusion is to treat it as a number of pansharpening sub-problems, where each band of the HRMS image plays the role of a panchromatic image. There are mainly two categories of pansharpening methods: component substitution (CS) [5, 17, 1] and multisiresolution analysis (MRA) [20, 21, 4, 33, 6]. These methods always suffer from the high spectral distortion,
since a single panchromatic image contains little spectral information as compared with the expected HS image.

In the last few years, machine learning based methods have gained much attention on MS/HS fusion problem [54, 2, 11, 14, 52, 48, 26, 40]. Some of these methods used sparse coding technique to learn a dictionary on the patches across a HrMS image, which delivers spatial knowledge of HrHS to a certain extent, and then learn a coefficient matrix from LrHS to fully represent the HrHS [54, 2, 11, 40]. Some other methods, such as [14], use the sparse matrix factorization to learn a spectral dictionary for LrHS images and then construct HrMS images by exploiting both the spectral dictionary and HrMS images. The low-rankness of HS images can also be exploited with non-negative matrix factorization, which helps to reduce spectral distortions and enhances the MS/HS fusion performance [52, 48, 26]. The main drawback of these methods is that they are mainly designed based on human observations and strong prior assumptions, which may not be very accurate and would not always hold for diverse real world images.

2.2. Deep learning based methods

Recently, a number of DL-based pansharpening methods were proposed by exploiting different network structures [15, 22, 42, 43, 29, 30, 32]. These methods can be easily adapted to MS/HS fusion problem. For example, very recently, [28] proposed a 3D-CNN based MS/HS fusion method by using PCA to reduce the computational cost. This method is usually trained with prepared training data. The network inputs are set as the combination of HrMS/panchromatic images and LrHS/multispectral images (which is usually interpolated to the same spatial size as HrMS/panchromatic images in advance), and the outputs are the corresponding HrHS images. The current DL-based methods have been verified to be able to attain good performance. They, however, just employ networks assembled with some off-the-shelf components in current deep learning toolkits, which are not specifically designed against the investigated problem. Thus the main drawback of this technique is the lack of interpretability to this particular MS/HS fusion task. In specific, both the intrinsic observation model (1), (2) and the evident prior structures, like the spectral correlation property, possessed by HS images have been neglected by such kinds of “black-box” deep model.

3. MS/HS fusion model

In this section, we demonstrate the proposed MS/HS fusion model in detail.

3.1. Model formulation

We first introduce an equivalent formulation for observation model (1). Specifically, we have following theorem\(^2\).

\[ \text{Theorem 1.} \quad \text{For any } X \in \mathbb{R}^{HW \times S} \text{ and } Y \in \mathbb{R}^{HW \times s}, \text{ if } \text{rank}(X) = r > s \text{ and rank}(Y) = s, \text{ then the following two statements are equivalent to each other:} \]

(a) There exists an \( R \in \mathbb{R}^{S \times s} \), subject to,

\[ Y = X R. \quad (3) \]

(b) There exist \( A \in \mathbb{R}^{s \times S} \), \( B \in \mathbb{R}^{(r-s) \times S} \) and \( \tilde{Y} \in \mathbb{R}^{HW \times (r-s)} \), subject to,

\[ X = \tilde{Y} A + \tilde{Y} B. \quad (4) \]

In reality, the band number of an HrMS image is usually not large, which makes it full rank along spectral mode. For example, the most commonly used HrMS images, RGB images, contain three bands, and their rank along the spectral mode is usually also three. Thus, by letting \( \tilde{Y} = Y - N_y \), where \( Y \) is the observed HrMS in (1), it is easy to find that \( Y \) and \( X \) satisfy the conditions in Theorem 1. Then the observation model (1) is equivalent to

\[ X = YA + YB + N_x, \quad (5) \]

where \( N_x = -N_y A \) is caused by the noise contained in the HrMS image. In (5), \([Y, \tilde{Y}]\) can be viewed as \( r \) bases that represent columns in \( X \) with coefficients matrix \([A; B] \in \mathbb{R}^{r \times S}\), where only the \( r - s \) bases in \( \tilde{Y} \) are unknown. In addition, we can derive the following corollary:

\[ \text{Corollary 1.} \quad \text{For any } Y \in \mathbb{R}^{HW \times s}, Z \in \mathbb{R}^{hw \times S}, C \in \mathbb{R}^{hw \times HW}, \text{ if rank}(\tilde{Y}) = s \text{ and rank}(\tilde{Z}) = r > s, \text{ then the following two statements are equivalent to each other:} \]

(a) There exist \( X \in \mathbb{R}^{HW \times S} \) and \( R \in \mathbb{R}^{S \times s} \), subject to,

\[ \tilde{Y} = XR, \quad \tilde{Z} = CX, \quad \text{rank}(X) = r. \quad (6) \]

(b) There exist \( A \in \mathbb{R}^{S \times S}, r > s \), \( B \in \mathbb{R}^{(r-s) \times S} \) and \( \tilde{Y} \in \mathbb{R}^{HW \times (r-s)} \), subject to,

\[ Z = C (\tilde{Y} A + \tilde{Y} B). \quad (7) \]

Let \( \tilde{Z} = Z - N_z \), where \( Z \) is the observed LrHS image in (2). It is easy to find that, when being viewed as equations of the to-be-estimated \( X \), \( R \) and \( C \), the observation model (1) and model (2) are equivalent to the following equation of \( \tilde{Y} \), \( A \), \( B \) and \( C \):

\[ Z = C (YA + YB) + N, \quad (8) \]

where \( N = N_x - C N_y A \) denotes the noise contained in HrMS and LrHS image. Then, we can design the following MS/HS fusion model:

\[ \min_{Y} \left\| C (YA + YB) - Z \right\|_F^2 + \lambda f(Y), \quad (9) \]

\(^2\)All proofs are presented in supplementary material.

\(^3\)We say two equation are equivalent to each other if the solution of one equation can easily achieve by solving the other one.
where $\lambda$ is a trade-off parameter, and $f(\cdot)$ is a regularization function. We adopt regularization on the to-be-estimated bases in $Y$, rather than on $X$ as in conventional, to facilitate an entire preservation of spatial details contained in the known HrMS bases ($Y$) for representing $X$.

It should be noted that for data obtained with the same sensors, $A$, $B$ and $C$ are fixed. This means that they can be learned from the training data. In the later sections we will show how to learn them with a deep network.

3.2. Model optimization

We now solve (9) using a proximal gradient algorithm [3], which iteratively updates $Y$ by calculating

$$
\hat{Y}^{(k+1)} = \arg\min_Y Q(\hat{Y}, \hat{Y}^{(k)}),
$$

(10)

where $\hat{Y}^{(k)}$ is the updating result after $k - 1$ iterations, $k = 1, 2, \cdots, K$, and $Q(\hat{Y}, \hat{Y}^{(k)})$ is a quadratic approximation [3] defined as:

$$
Q(\hat{Y}, \hat{Y}^{(k)}) = g(\hat{Y}^{(k)}) + \left\langle \hat{Y} - \hat{Y}^{(k)}, \nabla g(\hat{Y}^{(k)}) \right\rangle + \frac{1}{2\eta} \left\| \hat{Y} - \hat{Y}^{(k)} \right\|_F^2 + \lambda f(\hat{Y}),
$$

(11)

where $g(\hat{Y}^{(k)}) = \left\| C(YA + \hat{Y}^{(k)}B) - Z \right\|_F^2$ and $\eta$ plays the role of stepsize.

It is easy to prove that the problem (10) is equivalent to:

$$
\min_Y \frac{1}{2} \left\| \hat{Y} - \hat{Y}^{(k)} - \eta \nabla g(\hat{Y}^{(k)}) \right\|_F^2 + \lambda f(\hat{Y}).
$$

(12)

For many kinds of regularized terms, the solution of Eq. (12) is usually in closed-form [8], written as:

$$
\hat{Y}^{(k+1)} = \text{prox}_{\lambda f}(\hat{Y}^{(k)} - \eta \nabla g(\hat{Y}^{(k)})),
$$

(13)

where prox$_{\lambda f}(\cdot)$ is the proximal operator dependent on $f(\cdot)$. Since $\nabla g(\hat{Y}^{(k)}) = C^T(C(YA + \hat{Y}^{(k)}B) - Z)B^T$, we can obtain the final updating rule for $Y$:

$$
\hat{Y}^{(k+1)} = \text{prox}_{\lambda f}(\hat{Y}^{(k)} - \eta C^T(C(YA + \hat{Y}^{(k)}B) - Z)B^T).
$$

(14)

We can then unfold this algorithm into a deep network.

4. MS/HIS fusion net

Based on the above algorithm, we build a deep neural network for MS/HIS fusion by unfolding all steps of the algorithm as network layers. This technique has been widely utilized in various computer vision tasks and has been substantiated to be effective in compressed sensing, dehazing, deconvolution, etc. [44, 45, 53]. The proposed network is a

<table>
<thead>
<tr>
<th>Iterative optimization algorithm</th>
<th>Network design</th>
</tr>
</thead>
<tbody>
<tr>
<td>For $k = 1: K$ do:</td>
<td>In stage $k = 1: K$ of the network do:</td>
</tr>
<tr>
<td>$X^{(k)} = YA + \hat{Y}^{(k)}B$</td>
<td>$X^{(1)} = \gamma X + A^T + \tilde{g}^{(k)} \times_3 B^T$</td>
</tr>
<tr>
<td>$E^{(k)} = CX^{(k)} - Z$</td>
<td>$E^{(1)} = \text{downSample}_{\theta^{(k)}}(X^{(1)}) - Z$</td>
</tr>
<tr>
<td>$G^{(k)} = \eta CT E^{(k)} B^T$</td>
<td>$G^{(k)} = \eta \cdot \text{upSample}_{\theta^{(k)}}(E^{(k)}) \times_3 B$</td>
</tr>
<tr>
<td>$Y^{(k+1)} = \text{prox}_{\lambda f}(\hat{Y}^{(k)} - G^{(k)})$</td>
<td>$\hat{Y}^{(k+1)} = \text{proxNet}_{\theta^{(k)}}(\tilde{g}^{(k)} - G^{(k)})$</td>
</tr>
</tbody>
</table>

Figure 2. An illustration of relationship between the algorithm with matrix form and the network structure with tensor form.

structure of $K$ stages, corresponding to $K$ iterations in the iterative algorithm for solving Eq. (9), as shown in Fig. 3 (a) and (b). Each stage takes the HrMS image $Y$, LrHS image $Z$, and the output of the previous stage $Y$, as inputs, and outputs an updated $Y$ to be the input of next layer.

4.1. Network design

**Algorithm unfolding.** We first decompose the updating rule (14) into the following equivalent four sequential parts:

$$
X^{(k)} = YA + \hat{Y}^{(k)}B,
$$

(15)

$$
E^{(k)} = CX^{(k)} - Z,
$$

(16)

$$
G^{(k)} = \eta CT E^{(k)} B^T,
$$

(17)

$$
Y^{(k+1)} = \text{prox}_{\lambda f}(\hat{Y}^{(k)} - G^{(k)}).
$$

(18)

In the network framework, we use the images with their tensor formulations ($X \in \mathbb{R}^{H \times W \times S}$, $Y \in \mathbb{R}^{H \times W \times S}$ and $Z \in \mathbb{R}^{h \times w \times S}$) instead of their matrix forms to protect their spatial structure knowledge and make the network structure (in tensor form) easily designed. We then design a network to approximately perform the above operations in tensor version. Refer to Fig. 2 for easy understanding.

In tensor version, Eq. (15) can be easily performed by the two multiplications between a tensor and a matrix along the 3rd mode of the tensor. Specifically, in the TensorFlow framework, multiplying a tensor with an matrix in $\mathbb{R}^{m \times n}$ along the channel mode can be easily performed by using the 2D convolution function with a associated $1 \times 1 \times m \times n$ tensor. Thus, we can perform the tensor version of (15) by:

$$
X^{(k)} = Y \times_3 A^T + \hat{Y}^{(k)} \times_3 B^T,
$$

(19)

where $\times_3$ denotes the mode-3 multiplication for tensor.

In Eq. (16), the matrix $C$ represents the spatial downsampling operator, which can be decomposed into 2D convolutions and down-sampling operators [12, 24, 25]. Thus, we perform the tensor version of (16) by:

$$
E^{(k)} = \text{downSample}_{\theta^{(k)}}(X^{(k)}) - Z,
$$

(20)

---

4 For a tensor $U \in \mathbb{R}^{I \times J \times K}$ with $u_{ijk}$ as its elements, and $V \in \mathbb{R}^{M \times K}$ with $v_{k\ell}$ as its elements, let $W = U \times_3 V$, the elements of $W$ are $w_{ij\ell} = \sum_{k=1}^{K} u_{ijk} v_{k\ell}$. Besides, $W = U \times_3 V \iff W = UV^T$. 

5 https://tensorflow.google.cn/
where $E^{(k)}$ is denoted as $S_k$, $(k = 1, 2, \ldots, K)$. In the first stage, we simply set $Y^{(0)} = X$. In this way, we design an end-to-end training architecture, called MS/HS fusion net or MHFnet. We denote the function of entire net as $\hat{X} = \text{MHFnet}(Y, \Theta)$, where $\Theta$ represents all parameters involved in the network. Please refer to supplementary material for more details.

### 4.2. Network training

**Training loss.** As shown in Fig. 3 (e), the training loss for each training image is defined as following:

$$L = \|\hat{X} - \mathcal{X}\|_F^2 + \alpha \sum_{k=1}^{K} \|\mathcal{X}^{(k)} - \hat{X}\|_F^2 + \beta \|E^{(k)}\|_F^2,$$  \hspace{1cm} (24)

where $\hat{X}$ and $\mathcal{X}^{(k)}$ are the final and per-stage outputs of the proposed network, $\alpha$ and $\beta$ are two trade-off parameters\(^7\.\)

\(^7\)We set $\alpha$ and $\beta$ with small values (0.1 and 0.01, respectively) in all experiments, to make the first term play a dominant role.
Figure 4. Illustration of how to create the training data when HrHS images are unavailable.

The first term is the pixel-wise $L_2$ distance between the output of the proposed network and the ground truth $X$, which is the main component of our loss function. The second term is the pixel-wise $L_2$ distance between the output $X^{(k)}$ and the ground truth $X$ in each stage. This term helps find the correct parameters in each stage, since appropriate $Y^{(k)}$ would lead to $X^{(k)} \approx X$. The final term is the pixel-wise $L_2$ distance of the residual of observation model (1) to address this problem, where the Wald protocol [50] is used to create the training data as shown in Fig. 4. We downsample both HrHS images and LrHS images in space, so that the original LrHS images can be taken as references for the downsampled data. Please refer to supplementary material for more details.

Implementation details. We implement and train our network using TensorFlow framework. We use Adam optimizer to train the network for 50000 iterations with a batch size of 10 and a learning rate of 0.0001. The initializations of the parameters and other implementation details are listed in supplementary materials.

5. Experimental results

We first conduct simulated experiments to verify the mechanism of MHF-net quantitatively. Then, experimental results on simulated and real data sets are demonstrated to evaluate the performance of MHF-net.

Evaluation measures. Five quantitative picture quality indices (PQI) are employed for performance evaluation, including peak signal-to-noise ratio (PSNR), spectral angle mapper (SAM) [49], erreur relative globale adimensionnelle de synthèse (ERGAS [38]), structure similarity (SSIM [39]), feature similarity (FSIM [51]). SAM calculates the average angle between spectrum vectors of the target MSI and the reference one across all spatial positions and ERGAS measures fidelity of the restored image based on the weighted sum of MSE in each band. PSNR, SSIM and FSIM are conventional PQIs. They evaluate the similarity between the target and the reference images based on MSE and structural consistency, perceptual consistency, respectively. The smaller ERGAS and SAM are, and the larger PSNR, SSIM and FSIM are, the better the fusion result is.

### Table 1. Average performance of the competing methods over 12 testing samples of CAVE data set with respect to 5 PQIs.

<table>
<thead>
<tr>
<th></th>
<th>ResNet</th>
<th>MHF-net with $(K, L)$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$(4, 9)$</td>
<td>$(7, 5)$</td>
</tr>
<tr>
<td>PSNR</td>
<td>32.25</td>
<td>36.15</td>
</tr>
<tr>
<td>ERGAS</td>
<td>141.28</td>
<td>92.94</td>
</tr>
<tr>
<td>SSIM</td>
<td>0.865</td>
<td>0.948</td>
</tr>
<tr>
<td>FSIM</td>
<td>0.966</td>
<td>0.974</td>
</tr>
</tbody>
</table>

5.1. Model verification with CAVE data

To verify the efficiency of the proposed MHF-net, we first compare the performance of MHF-net with different settings on the CAVE Multispectral Image Database [46]. The database consists of 32 scenes with spatial size of $512 \times 512$, including full spectral resolution reflectance data from 400nm to 700nm at 10nm steps (31 bands in total). We generate the HrMS image (RGB image) by integrating all the ground truth HrHS bands with the same simulated spectral response $R$, and generate the LrHS images via downsampling the ground-truth with a factor of 32 implemented by averaging over $32 \times 32$ pixel blocks as [2, 16].

To prepare samples for training, we randomly select 20 HS images from CAVE database and extract $96 \times 96$ overlapped patches from them as reference HrHS images for training. Then the utilized HrHS, HrMS and LrHS images are of size $96 \times 96 \times 31, 96 \times 96 \times 3$ and $3 \times 3 \times 31$, respectively. The remaining 12 HS images of the database are used for validation, where the original images are treated as ground truth HrHS images, and the HrMS and LrHS images are generated similarly as the training samples.

We compare the performance of the proposed MHF-net under different stage number $K$. In order to make the competition fair, we adjust the level number $L$ of the ResNet used in proxNet $u_k^b$ for each situation, so that the total level number of the network in each setting is similar to each other. Moreover, to better verify the efficiency of the proposed network, we implement another network for competition, which only uses the ResNet in (22) and (23) without using other structures in MHF-net. This method is simply denoted as “ResNet”. In this method, we set the input as $[Y, Z_{up}]$, where $Z_{up}$ is obtained by interpolating the LrHS image $Z$ (using a bicubic filter) to the dimension of $Y$ as did. We set the level number of ResNet to be 30.

Table 1 shows the average results over 12 testing HS images of two DL methods in different settings. We can observe that MHF-net with more stages, even with fewer net levels in total, can significantly lead to better performance. We can also observe that the MHF-net can achieve better...
results than ResNet (about 5db in PSNR), while the main difference between MHF-net and ResNet is our proposed stage structure in the network. These results show that the proposed stage structure in MHF-net, which introduces interpretability specifically to the problem, can indeed help enhance the performance of MS/HS fusion.

5.2. Experiments with simulated data

We then evaluate MHF-net on simulated data in comparison with state-of-art methods. The comparison methods include: FUSE [41], ICCV 15 [18], GLP-HS [31], SFIM-HS [19], GSA [11], CNMF [48], M-FUSE [40], SASFM [14], and 3D-CNN [28], representing the state-of-the-art traditional methods; PNN [30] and 3D-CNN [28] representing the state-of-the-art DL-based methods. We also compare the proposed MHF-net with the implemented ResNet method.

Performance comparison with CA VE data. The CA VE data set [15] is an airborne HS image taken over Chikusei, Ibaraki, Japan, on 29 July 2014. The data set is of size $2517 \times 2335 \times 128$ with the spectral range from 0.36 to 1.018. We view the original data as the HRHS image and simulate the HRMS (RGB image) and LRMS (with a factor of 32) image in the similar way as the previous section.

We select a $500 \times 2210$-pixel-size image from the top area of the original data for training, and extract $96 \times 96$ overlapped patches from the training data as reference HRHS images for training. The input HRHS, HRMS and LRMS samples are of sizes $96 \times 96 \times 128$, $96 \times 96 \times 3$ and $3 \times 3 \times 128$, respectively. Besides, from remaining part of the original image, we extract 16 non-overlap $448 \times 544 \times 128$ images as testing data. More details about the experimental setting are introduced in supplementary material.

Table 3 shows the average performance over 16 testing images of all competing methods. It is easy to observe that the proposed method performs better than other competing ones, in the better recovery of both finer-grained textures and coarser-grained structures. More results are depicted in the supplementary material.

Performance comparison with Chikusei data. The Chikusei data set [47] is an airborne HS image taken over Chikusei, Ibaraki, Japan, on 29 July 2014. The data set is of size $2517 \times 2335 \times 128$ with the spectral range from 0.36 to 1.018. We view the original data as the HRHS image and simulate the HRMS (RGB image) and LRMS (with a factor of 32) image in the similar way as the previous section.

![Figure 5: (a) The simulated RGB (HRMS) and LRHS (left bottom) images of chart and stuffed toy, where we display the 10th (490nm) band of the HS image. (b) The ground-truth HRHS image. (c)-(n) The results obtained by 12 comparison methods, with two demarcated areas zoomed in 4 times for easy observation.](http://naotoyokoya.com/Download.html)

![Table 2: Average performance of the competing methods over 12 testing images of CA VE data set with respect to 5 PQIs.](http://naotoyokoya.com/Download.html)

![Table 3: Average performance of the competing methods over 12 testing images of Chikusei data set with respect to all evaluation measures.](http://naotoyokoya.com/Download.html)

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9[http://weil.perso.enseeiht.fr/publications.html](http://weil.perso.enseeiht.fr/publications.html)
10[http://github.com/Ianha/SupResPalm](http://github.com/Ianha/SupResPalm)
13[https://github.com/qw245/BlindFuse](https://github.com/qw245/BlindFuse)
14We write the code by ourselves.

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Figure 6. (a) The simulated RGB (HrMS) and LrHS (left bottom) images of a test sample in Chikusei data set. We show the composite image of the HS image with bands 70-100-36 as R-G-B. (b) The ground-truth HrHS image. (c)-(n) The results obtained by 10 comparison methods, with two demarcated areas zoomed in 4 times for easy observation.

Figure 7. (a) and (b) are the HrMS (RGB) and LrHS images of the left bottom area of Roman Colosseum acquired by World View-2 (WV-2). We show the composite image of the HS image with bands 5-3-2 as R-G-B. (c)-(n) The results obtained by 10 comparison methods, with a demarcated area zoomed in 5 times for easy observation.

Table 3. Average performance of the competing methods over 16 testing samples of Chikusei data set with respect to 5 PQIs.

<table>
<thead>
<tr>
<th>Method</th>
<th>PSNR</th>
<th>SAM</th>
<th>ERGAS</th>
<th>SSIM</th>
<th>FSIM</th>
</tr>
</thead>
<tbody>
<tr>
<td>FUSE</td>
<td>26.59</td>
<td>7.92</td>
<td>272.43</td>
<td>0.718</td>
<td>0.860</td>
</tr>
<tr>
<td>ICCV15</td>
<td>27.77</td>
<td>3.98</td>
<td>178.14</td>
<td>0.799</td>
<td>0.870</td>
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<tr>
<td>GLP-HS</td>
<td>28.85</td>
<td>4.17</td>
<td>163.60</td>
<td>0.796</td>
<td>0.903</td>
</tr>
<tr>
<td>SFIM-HS</td>
<td>28.50</td>
<td>4.22</td>
<td>167.85</td>
<td>0.793</td>
<td>0.900</td>
</tr>
<tr>
<td>GSA</td>
<td>27.08</td>
<td>5.39</td>
<td>238.63</td>
<td>0.673</td>
<td>0.835</td>
</tr>
<tr>
<td>CNMF</td>
<td>28.78</td>
<td>3.84</td>
<td>173.41</td>
<td>0.780</td>
<td>0.898</td>
</tr>
<tr>
<td>M-FUSE</td>
<td>24.85</td>
<td>6.62</td>
<td>282.02</td>
<td>0.642</td>
<td>0.849</td>
</tr>
<tr>
<td>SASFM</td>
<td>24.93</td>
<td>7.95</td>
<td>369.35</td>
<td>0.636</td>
<td>0.845</td>
</tr>
<tr>
<td>PNN</td>
<td>24.30</td>
<td>4.26</td>
<td>157.49</td>
<td>0.717</td>
<td>0.807</td>
</tr>
<tr>
<td>3D-CNN</td>
<td>30.51</td>
<td>3.02</td>
<td>129.11</td>
<td>0.869</td>
<td>0.930</td>
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<tr>
<td>ResNet</td>
<td>28.95</td>
<td>3.69</td>
<td>144.12</td>
<td>0.866</td>
<td>0.930</td>
</tr>
<tr>
<td>MHF-net</td>
<td>32.26</td>
<td>3.02</td>
<td>109.55</td>
<td>0.890</td>
<td>0.946</td>
</tr>
</tbody>
</table>

5.3. Experiments with real data

In this section, sample images of Roman Colosseum acquired by World View-2 (WV-2) are used in our experiments. This data set contains an HrMS image (RGB image) of size 1676 x 2632 x 3 and an LrHS image of size 419 x 658 x 8, while the HrHS image is not available. We select the top half part of the HrMS (836 x 2632 x 3) and LrHS (209 x 658 x 8) image to train the MHF-net, and exploit the remaining parts of the data set as testing data. We first extract the training data into 144 x 144 x 3 overlapped HrMS patches and 36 x 36 x 3 overlapped LrHS patches and then generate the training samples by the method as shown in Fig. 4. The input HrHS, HrMS and LrHS samples are of size 36 x 36 x 8, 36 x 36 x 3 and 9 x 9 x 8, respectively.

Fig. 6 shows a portion of the fusion result of the testing data (left bottom area of the original image). Visual inspection evidently shows that the proposed method gives the better visual effect. By comparing with the results of ResNet, we can find that the results of both methods are clear, but the color and brightness of result of the proposed method are much closer to the LrHS image.

6. Conclusion

In this paper, we have provided a new MS/HS fusion network. The network takes the advantage of deep learning that all parameters can be learned from the training data with fewer prior pre-assumption on the data, and furthermore takes into account the generation mechanism underlying the MS/HS fusion data. This is achieved by constructing a new MS/HS fusion model based on the observation models, and unfolding the algorithm into an optimization-inspired deep network. The network is thus specifically interpretable to the task, and can help discover the spatial and spectral response operators in a purely end-to-end manner. Experiments implemented on simulated and real MS/HS fusion cases have substantiated the superiority of the proposed MHF-net over the state-of-the-art methods.

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References


