Surface Reconstruction from Normals: A Robust DGP-based Discontinuity Preservation Approach

Wuyuan Xie 1, Miaohui Wang 2,*, Mingqiang Wei 3, Jianmin Jiang 1, Jing Qin 4
1 College of Computer and Software Engineering, Shenzhen University (SZU), P. R. China
2 Guangdong Key Laboratory of Intelligent Information Processing, College of Information Engineering, SZU, P. R. China
3 School of Computer Science and Technology, Nanjing University of Aeronautics and Astronautics, P. R. China
4 School of Nursing, Hong Kong Polytechnic University, Hong Kong, P. R. China
{wyxie, mhwang, jianmin.jiang}@szu.edu.cn, mqwei@nuaa.edu.cn, harry.qin@polyu.edu.hk

Abstract

In 3D surface reconstruction from normals, discontinuity preservation is an important but challenging task. However, existing studies fail to address the discontinuous normal maps by enforcing the surface integrability in the continuous domain. This paper introduces a robust approach to preserve the surface discontinuity in the discrete geometry way. Firstly, we design two representative normal incompatibility features and propose an efficient discontinuity detection scheme to determine the splitting pattern for a discrete mesh. Secondly, we model the discontinuity preservation problem as a light-weight energy optimization framework by jointly considering the discontinuity detection and the overall reconstruction error. Lastly, we further shrink the feasible solution space to reduce the complexity based on the prior knowledge. Experiments show that the proposed method achieves the best performance on an extensive 3D dataset compared with the state-of-the-arts in terms of mean angular error and computational complexity.

1. Introduction

Surface reconstruction from normals is driven by several computer vision tasks, such as shape from shading (SfS), deflectometry, and photometric stereo (PS). Given a static scene captured by a camera with fixed viewpoint, PS [15, 16, 20, 21] is widely used to obtain the surface normal orientations. To reconstruct a surface from the estimated normals, the most common way [1, 3, 8, 11, 17] is to conduct integration on the depth gradients which are transformed from the normal orientations. However, the normal map produced by PS may not be uniformly integrable, due to occlusion boundary, sharp surface changes, or computation error. To reconstruct a surface from such a discontinuous and noisy normal map, Terzopoulos et al. [18] provided a compact framework to compute the depth field and surface discontinuity simultaneously, where a rough depth map was needed for initialization. Approaches in [6, 7, 9] used binary weights to indicate the presence of surface discontinuities, so that the integrability constraint can be applied partially. Although these methods can reconstruct surfaces from discontinuous and noisy normals, none of them satisfactorily preserves the discontinuity, where the reconstructed surfaces are somewhat distorted. One key reason is that forming a discontinuity between two adjacent patches requires breaking their connection. The aforementioned approaches assume that the number of total reconstructed vertices is equal to the number of normal orientations, which means every patch is connected, and distortion in the local shape is propagated to the whole surface. Fig. 1 shows an example of reconstructing the boundary vertexes of the Saddle model, the object surface is split and can be separately to form a more accurate shape.

In this paper, we concentrate on addressing the preservation of the discontinuity feature in surface reconstruction...
from normals. The input is a single normal map which can be obtained by PS or point cloud, and the output is a 3D surface with rich discontinuities. We study and model the normal discontinuity in a discrete geometry domain [24] which is used for surface reconstruction. To measure the incompatibility between two adjacent normal orientations, we introduce two new features, including absolute depth difference and normal angle difference. The surface discontinuities are detected by these two normal incompatibility features, and followed by vertex partition and redistribution. We build a geometry-based energy function to optimize the discontinuity and the surface shape simultaneously. Besides, the prior statistical knowledge of the normal incompatibility features greatly facilitates obtaining the optimal result with low computation complexity. Extensive experimental results (e.g., comparisons on 16 different models) validate the efficiency of the proposed method.

Comparing to [24], the proposed method accurately reconstructs the surface discontinuities by allowing the mesh node to have multiple vertexes, rather than approximating it in the continuous domain. To the best of our knowledge, this is the first approach to address the discontinuity problem in a discrete geometry way, which has the following main merits:

- **Discontinuity preservation**: As two adjacent facets oriented by incompatible normals are taken to be independent, the discontinuity between them can be formed along the breaking boundary. Meanwhile, as a light-weight least-square optimization is used to compute the depth map, and the surface smoothness on continuous segments is preserved.

- **Robustness to noise**: This research can be applied to the continuous/discontinuous normal maps with noise. Examples with heavy Gaussian noise (e.g., variance up to 8° angle degree) can be successfully reconstructed, where discontinuities are still accurately distinguished from noise and preserved.

- **Parameter-tuning free**: Due to the convexity of the proposed surface energy model, the optimal parameter used for discontinuity detection can be uniquely determined. As a result, the proposed approach can be adaptive to varying continuous/discontinuous normals without parameter tuning.

2. Related Work

This paper aims to reconstruct a surface from normals and allow the normal map to contain occlusion boundary, discontinuities, and noise. Traditional approaches [6, 9, 13] enforce the integrability constraint over the whole normal map to estimate the depths, and can be mainly categorized into regularization-based, weighting-based, and basis function-based methods.

**Regularization-based**: Regularization method attempts to smooth the depth gradients by introducing additional constraints. The most common way [4] is to use the least square energy function which is defined on residuals between the depth difference and the depth gradient. Although it is useful to noisy gradients, its quadratic behavior may over-penalize discontinuities which have higher residuals. Methods in [2, 18] considered the discontinuity through a variational formulation where a rough depth map was needed to estimate discontinuities and depth values simultaneously. Petrovic et al. in [11] used a belief propagation to enforce integrability constraints in Markov Random Field network.

**Weighting-based**: Instead of enforcing the regularization uniformly over the whole gradient field, methods in [6, 7] employed the constraint partially by a weighting map, where the weight values were designed to be inversely proportional to the probability of lying on a discontinuity. An extreme case is Mumford et al. [9], where a binary template was used to indicate the presence of discontinuities. Studies in [12, 14, 19, 23] used an expectation maximization method to estimate a weighted discontinuity map, and then reconstructed the surface in segments according to the discontinuity labels. It is worth noting that all these methods either require manually labeling or thresholding for edge detection, thus cannot guarantee the reconstruction quality for a general surface.

**Basis function-based**: Frankot and Chellappa [3] projected the densely non-integrable gradients onto a set of Fourier basis functions for enforcing surface integrability. Hsieh et al. [5] and Karacali et al. [7] used wavelet basis functions instead. Kovesi et al. [8] computed the correlations of gradients via a bank of shapelets, which could solve the gradients with a certain ambiguity by carefully parameter tuning. One inevitable drawback of all these basis function-based approaches is that the global integrability enforcement constraint on the whole gradient field can smooth out the occlusion boundary. To address this problem, Wu et al. in [10, 22] further developed to introduce the kernel basis function, but these approaches are limited to the normal map of rectangular boundary and bring extremely computational complexity.

3. Discontinuity Detection

This research addresses the discontinuity problem based on a discrete geometry processing (DGP) framework. In this section, we first give a brief review of the DGP deformation method, and discuss the difficulty of reconstructing the surface discontinuities by the state-of-the-art method in a discrete geometry way. Considering the characteristics of DGP, we introduce two new features to measure the incompatibility between normals, and demonstrate how to use these two features to detect discontinuities.
3.1. DGP-based Shape Deformation

In DGP deformation [24], the surface to be reconstructed is taken as a mesh consisting of a set of micro square facets oriented by the input normal map, and then a local/global deformation is iteratively conducted on the mesh to generate the final shape. Specifically, each pixel \((i,j)\) in a normal map is converted into a facet \(f_{i,j}\) bounded by four vertices \(v_{i,j}, v_{i,j+1}, v_{i+1,j+1},\) and \(v_{i+1,j}\) as shown in Fig. 3 (Left). A vertex \(v_{i,j}\) has its \(x\)- and \(y\)-coordinates fixed, and \(z\)-coordinate (i.e., the depth value \(z_{i,j}\)) as an unknown variable to be determined. In each iteration of the shape deformation, a local shaping step is first performed to determine the position of each facet according to its demanding normal orientation. Meanwhile, a global blending step is applied to generate all facets into a connected mesh surface. The local/global steps can be summarized as a least square formulation:

\[
\Phi (z_{i,j}) = \sum_{f_{i,j}} \|z(f_{i,j}) - p(f_{i,j})\|^2, \tag{1}
\]

where \(z(f_{i,j})\) is a column vector stacking the depth values of four vertexes of \(f_{i,j}\), \(z(f_{i,j}) = [z_{i,j}, z_{i,j+1}, z_{i+1,j+1}, z_{i+1,j}]^T\), and \(p(f_{i,j})\) is the updated depth values of \(z(f_{i,j})\) after employing the local shaping. By iteratively solving Eq. (1), the depth converges to form a surface whose orientations are expected to be the same as the input normals. However, in [24], all facets are supposed to be connected, and the reconstructed shape for the discontinuous normals can be inevitably distorted as shown in Fig. 1.

Actually, for a vertex \(v_{i,j}\) with discontinuity, the \(z\)-coordinate value is not unique. Let us denote it as \([z_{i,j}^{(1)}, ..., z_{i,j}^{(K)}]^T\). The total number \(K\) should be greater than one, and less or equal to the total number of facets around \(v_{i,j}\). We enumerate all possible splittings for \(v_{i,j}\) in Fig. 2, which in general can be grouped into four types: I) \(v_{i,j}\) has a unique depth value, and four facets are connected and continuous; II) \(v_{i,j}\) has two depth values, e.g., the first group separated by dotted line in Fig. 2. There are two cases in this group: 1) Three facets are connected to one split vertex, and the last one independently holds another vertex alone (i.e., the first four graphs); 2) Two pairs of adjacent facets are connected by one split vertex (i.e., the last two graphs of the first group); III) \(v_{i,j}\) has three depth values, e.g., the second group in Fig. 2. A pair of facets is connected to one vertex, and the remaining two facets hold one independent vertex in the rest of this section.

3.2. Absolute Depth Difference Feature

An intuitive way to detect the compatibility between two adjacent normals is to check whether the facets oriented by them can be connected. Let us consider a patch \(P_{i,j}\) consisting of \(2 \times 2\) facets and centering at \(v_{i,j}\) as shown in Fig. 3 (Middle). If there are two adjacent conflicting orientations, the associated two facets are divided along the \(z\)-axis but still hold the joint vertex \(v_{i,j}\) as illustrated in Fig. 4. It is observed that the depth difference between these two split

\[\text{Figure 2. Example of all possible splitting patterns for a vertex with four facets.}\]

\[\text{Figure 3. Example of a discrete mesh consisting of vertexes and facets. (Left): A facet and its four vertexes; (Middle): A vertex and the facets around; (Right): Related normals used to calculate the depth difference along the positive direction of the } y\text{–axis at } v_{i,j}.\]

\[\text{Figure 4. Illustration of the conflicting normals. Arrows in gray are the ground-truth normals, while arrows in black are the reconstructed ones.}\]
facets can be used to measure the degree of incompatibility, and defined as the absolute depth difference (ADD) feature,

$$\delta_{i,j}^l = \left| \frac{\ell \cdot n_l}{k \cdot n_r} - \frac{\ell \cdot n_r}{k \cdot n_l} \right|,$$

where $\ell$ has the four directions in $P_{i,j}$ as shown in Fig. 3 (Right), which is a unit vector of directions of the $x-$ and $y-$ axis in the Cartesian coordinate. $k$ is a unit vector of the positive direction of the $z-$ axis. $n_l$ and $n_r$ are the left and right normal orientations along the direction $\ell$ at $v_{i,j}$.

Fig. 5 shows the statistics of the ADD feature for all continuous $P_{i,j}$ from the Bunny model. One can see that there is about $60\%$ continuous $P_{i,j}$ having a non-zero $\delta$. In addition, the distribution of discontinuities for the non-zero $\delta$ is also shown in Fig. 5 (Right). For a noise-free discontinuous normal map, all facets are supposed to be connected except for the occlusion boundary. In such a case, the normal discontinuities are only caused by the occlusion boundaries, which indicate that detecting the non-zero $\delta$ can be an effective measure to find discontinuities. However, this condition is too strict for a real case where the normal map is obtained by PS or from a set of noisy point cloud. The computational error introduced by PS and the scanning error in the point cloud disturb the normal orientations, and produce the non-zero $\delta$ on the $P_{i,j}$ which is expected to be continuous. It is obvious that the detection method based on a single ADD feature cannot distinguish discontinuity from noise as shown in Fig. 5 (Right). To improve the detection efficiency, a normal orientation feature is introduced in the next section.

### 3.3. Normal Angle Difference Feature

In general, surface discontinuities are mainly caused by the occlusion boundaries, where the ADD features are non-zero, and there exists the sharp orientation changes. Thus, both the non-zero $\delta$ and sharp orientation change are jointly considered to detect the discontinuity. To better quantify the change of orientations, a new feature called normal angle difference (NAD) is defined as the difference of normal orientations within a certain range, as given in Eq. (3):

$$\phi_{i,j}^l = \left\| \frac{\theta_{i,j}^l}{\theta_{i,j}^l} - \frac{\theta_{i,j}^r}{\theta_{i,j}^r} \right\|_\infty,$$

if $\delta_{i,j}^l > 0$, and $\left\| \theta_{i,j}^l \right\|_{\infty} = \theta_{i,j}^l$,

where $\phi_{i,j}^l$ is the NAD value along $\ell$ in $P_{i,j}$, and $\theta_{i,j}^l$ is,

$$\theta_{i,j}^l = [\arccos(n_l, n_{ll}), \arccos(n_l, n_r), \arccos(n_r, n_{rr})]^T,$$

where $n_{ll}$ and $n_{rr}$ are the left-adjacent and right-adjacent normals of $n_l$ and $n_r$, respectively as shown in Fig. 3 (Right). $\cdot \cdot_{\infty}$ is the $\pm\infty$-norm, which can be considered as the maximum/minimum operation.

### 3.4. Overall Detection Algorithm

The discontinuity detection that comprehensively considers both the ADD feature and the NAD feature can be implemented as:

Step 1) If $\delta_{i,j}^l$ is smaller than a given threshold $\tau_3$, then it is needed to check whether $\phi_{i,j}^l$ exists or not. Otherwise, $P_{i,j}$ is discontinuous along the direction $\ell$.

Step 2) If $\phi_{i,j}^l$ exists, it is needed to check the relationship between $\phi_{i,j}^l$ and another threshold $\tau_\phi$. Otherwise, $P_{i,j}$ is continuous along the direction $\ell$.

Step 3) If $\phi_{i,j}^l$ is bigger than $\tau_\phi$, then $P_{i,j}$ is discontinuous along the direction $\ell$. Otherwise, $P_{i,j}$ is continuous along the direction $\ell$.

Step 4) After all four directions are detected, the final splitting pattern of $P_{i,j}$ is determined as follows: If two directions are detected as discontinuities for a $P_{i,j}$, then the splitting pattern is shown in the first group of Fig. 2; Similarly, if three and four directions are detected as discontinuities for a $P_{i,j}$, the associated splitting patterns are shown in the second and third group of Fig. 2, respectively.

Since $v_{i,j}$ can be split according to the discontinuity detection condition, $z(f_{i,j})$ in Eq. (1) is updated as $z(f_{i,j}) = [z_{i,j}, z_{i,j+1}, z_{i+1,j+1}, z_{i+1,j+1}]^T$. The superscript $k$ represents the $k$th depth value along the $z$-axis.

### 4. Discontinuity Preservation

This section details the proposed DGP-based discontinuity preservation scheme for surface reconstruction from normals. A new lightweight energy model jointly considers the discontinuity detection parameters $(\tau_8, \tau_\phi)$ and the
overall surface reconstruction error. We also discuss how to efficiently compute the optimal detection parameters based on the prior knowledge.

4.1. Surface Reconstruction Optimization

In practice, it is infeasible to specify a different \((\tau_3, \tau_\phi)\) for each \(P_{i,j}\). For instance, considering that for a normal map with resolution of \(W \times H\), the total number of unknown detection parameters is \(2 \times (W \times H)\). To compute these unknown parameters, it greatly complicates the reconstruction process. Thus, we propose to uniformly apply \((\tau_3, \tau_\phi)\) to the whole normal field, and the reconstruction energy model with respect to \(\tau_3\) and \(\tau_\phi\) can be formulated as,

\[
\arg\min_{\{x_{i,j}\}} E(M(\tau_3, \tau_\phi)) \quad \text{s.t.} \quad n(f_{i,j}) \equiv n_{i,j},
\]

where \(M(\tau_3, \tau_\phi)\) is the reconstructed mesh surface by Eq. (1), with the input normals whose discontinuities have been detected and meshed by \(\tau_3\) and \(\tau_\phi\) (e.g., see Section 3.4). \(E(M)\) is a function measuring the shape variation, and \(n(\cdot)\) returns the normal vector of a facet.

Fig. 6 shows the energy surfaces of four discontinuous models with the original normals and the noisy normals, respectively. It can be seen that a large \((\tau_3, \tau_\phi)\) results in a big reconstruction error. The reason is that when there are no discontinuities detected under the large detection parameters, \(M(\cdot)\) is taken to be continuous. Strictly speaking, Xie et al. [24] is a special case of this research with infinite \((\tau_3, \tau_\phi)\). In addition, the result of a small \((\tau_3, \tau_\phi)\) is another extreme case where every \(P_{i,j}\) is determined to be discontinuous, and every \(f_{i,j}\) is separated. In this case, the total number of unknown depth values is larger than the total number of normals, and Eq. (5) has no feasible solution. Consequently, the reasonable \((\tau_3, \tau_\phi)\) candidates are located in the middle range as shown in Fig. 6.

4.2. Determination of the Feasible Solution Space

The conventional way to compute the optimal \((\tau_3^*, \tau_\phi^*)\) is to use Newton’s method for all possible values of \(\delta\) and \(\varphi\). However, it is time-consuming and easy to be stuck in a local minimum in the practical reconstruction, especially for the noisy normal map. Considering that a given surface to be reconstructed commonly has more continuities than discontinuities, the scope of searching \((\tau_3^*, \tau_\phi^*)\) can be shrunk based on the prior statistical knowledge of \(\delta\) and \(\varphi\).

The histogram statistics of the ADD feature \(\delta = \{\delta_{i,j}\}\), which is computed by Eq. (2). An example of the histogram of \(\delta\) for the Bunny model is given in Fig. 7. It can be seen that the ADD values are mainly concentrated in a narrow range with the mean value close to zero, and the rest are randomly distributed in a wide range with the upper limit approaching to the largest depth of the ground-truth. Supposing the ADD value with the largest probability is denoted as \(\delta_0\) (i.e. the \(x\)- coordinate of the first bar in Fig. 7). A reasonable \(\tau_3\) is expected to be capable of filtering every \(P_{i,j}\) of \(\delta_0\) to avoid being disconnected. As a result, \(\tau_3\) can only be the value bigger than \(\delta_0\).

To specify the mathematical expression of the range of
\( \phi \), we then fit the histogram \( h_\delta \) by a Gaussian function \( g_\delta \). If the peaks of \( h_\delta \) and \( g_\delta \) are close, the optimal \( \tau^*_\omega \) should be larger than the mean value \( \mu_\delta \) of \( g_\delta \). If the peaks of \( h_\delta \) and \( g_\delta \) are far away from each other, it implies that the normal map contains heavy noise, which causes the distribution of \( \delta \) diverging. Thus, in this research, the search range of the optimal \( \tau^*_\omega \) starts from \( \mu_\delta + \frac{d_\delta}{2} \), where \( d_\delta \) is the variance of \( g_\delta \). Eq. (6) gives the search range of \( \tau^*_\omega \),

\[
\Omega_\delta = \left\{ (\mu_\delta, ||\delta||_\infty), \ h_\delta(\mu_\delta) \approx \max h_\delta, \ (\mu_\delta + \frac{d_\delta}{2}, ||\delta||_\infty), \ otherwise \right\}.
\tag{6}
\]

The distribution of the NAD feature is similar to that of the ADD feature, i.e., mainly concentrated near small \( \phi \). Thus, the search range of the optimal \( \tau^*_\phi \) can be derived in a similar way. The difference is that we do not make analysis on all values of \( \phi = \{\phi_{i,j}\} \) to compute the histogram \( h_\phi \). As we know that the patch, \( P_{i,j} \), having the largest probability \( \delta_{i,j} \), must be continuous, and the associated NAD feature \( \varphi_{i,j} \) rarely contains the optimal \( \tau^*_\phi \). That is, the optimal \( \tau^*_\phi \) is impossible to be \( \phi \) with the largest probability over the range of \( \varphi_{i,j} \). Eq. (7) gives the mathematical formulation of the search range of \( \tau^*_\phi \),

\[
\Omega_\phi = \left\{ (\mu_\phi, ||\varphi_{i,j}||_\infty), \ h_\phi(\mu_\phi) \approx \max h_\phi, \ (\mu_\phi + \frac{d_\phi}{2}, ||\varphi_{i,j}||_\infty), \ otherwise \right\},
\tag{7}
\]

where \( h_\phi \) is the histogram of \( \varphi_{i,j} \), \( \mu_\phi \) and \( d_\phi \) are the mean and variance of the Gaussian function \( g_\phi \), which is fitted from \( h_\phi \).

To illustrate the effectiveness of \( \Omega_\delta \) and \( \Omega_\phi \), we define the range reduction ratio as \( \lambda = \frac{||\Omega_\delta||_\infty}{||\Omega_\phi||_\infty} \times \frac{||\Omega_\delta||_\infty}{||\Omega_\phi||_\infty} \), and test the proposed scheme on the Face model containing different noisy levels, and under the normals of 16 different models. The optimal detection parameters \( \tau^*_\omega \) and \( \tau^*_\phi \) are efficiently computed by the Monte Carlo method. As shown in Fig. 8, the searching scope can be shrunk to about 15% of the original one, even for the Face normals containing Gaussian noise of variance up to 8°. The corresponding reconstruction error is provided in Fig. 9 and Fig. 10, where the mean angular error is close to 0°.

Figure 8. Average time cost and the reduction rate of searching range of \( \langle \tau^*_\omega, \tau^*_\phi \rangle \) for all 16 models, and for the Face model containing the Gaussian noise with variance ranging from 0° to 8°.

Figure 9. Reconstruction error rate of the Face model containing the Gaussian noise with variance ranging from 0° to 8°. The indicating percentage is the ratio of the total number of reconstructed normals with angular error greater than 20° to the total number of input normals.

Figure 10. Average reconstruction error rate of the original/noisy normal maps of all 16 models. Results from the original normal maps are plotted by solid lines, while the noisy counterparts are denoted by dot lines.

5. Experimental Results

We implement the proposed approach in MATLAB under Intel i7 CPU with 3.40GHz and 8GB RAM, and compare the performance with five existing methods as mentioned in [13], including Quadratic [4], Fourier [3], Mumford Shah [9], Shapelet [8], and DGP shaping [24]. All the test examples are downloaded from Aim@Shape, and TurboSquid. For each 3D model, we first sample the normal vectors, render them via OpenGL, and then read back the associated depth map and the sampled normal map. To introduce the discontinuous artifacts into the tested examples, we simply introduce \( [0, 0, 1]^T \) as surface normals in the regions where orientations are missing. For comparison, the input normal map serves as the ground-truth, where the angular errors between the input normals and the reconstructed ones are computed to measure the quality of reconstruction. Experimental results show that our approach is efficient and outperforms the other five methods. Detailed comparison and analysis are discussed as below.

Firstly, our approach is robust not only for the original normal maps, but also for the noisy ones. As shown in Fig. 9, the Face model containing the Gaussian noise with different variances ranging from 0° to 8° is used to test the
robustness of our method\(^2\). It can be seen that when the variance is increasing but less than 6°, the reconstruction error rate and mean angular error (MAE) are kept below 5\% and 5°, respectively. When the variance increases to 8°, the error rate and MAE are still below 10\% and 10° respectively, which are much smaller than the other five methods. The related reconstructed surfaces are rendered in Fig. 12. It is clearly shown that all noisy cases of Face are satisfactorily separated from the background and accurately reconstructed.

Secondly, we also validate our approach on the Bunny and the Hand models as shown in Fig. 11 and Fig. 14, respectively. Each example is conducted on two types of inputs, the original normal map and the noisy one. It is obvious that all the other compared methods fail to break the discontinuous patches, thereby distort the reconstructed surface. We also observe that some methods are very sensitive to noise. For example, the reconstructed surfaces by Shapelete [8] fail to be rendered in the comparison as the errors are too large (see Fig. 9). In addition, we show more comparisons on 16 different models in Fig. 10. Obviously, the proposed method achieves the best performance. For the original normal maps, the reconstruction error rate and MAE are close to 0\% and 0°, respectively. For the noisy counterparts, the reconstruction error rate and MAE are below 5\% and 5°. All the other reconstruction results of our method are rendered and shown in Fig. 15.

Thirdly, we qualitatively evaluate our approach on three real-world PS normal models, including Turtle from the Harvard dataset, Cat and Bear from the DiLiGenT dataset, as shown in Fig. 13. The reconstructed mean angular errors are 2.16°, 4.13°, and 6.01°, respectively. It is worth noting that it is usually to remove the dark background to guarantee the reconstruction quality of computing normal by the traditional methods. Here, we still use the noisy (non-Gaussian) and unreliable background in the reconstructions of Cat and Bear.

Last but not the least, the proposed scheme can be efficiently solved. The reason is that Eq. (6) and Eq. (7) define an effective feasible solution space of \((\tau^*, \psi^*)\) for different normals. Especially, for a noisy normal map, the solution space is shrinking along with the increasing Gaussian variance. It means our approach can guarantee the reconstruc-

---

\(^2\)Note that the maximum noise value can reach 30° with the Gaussian variance of 8°.
Figure 14. The Hand model reconstructed by five different methods. (Top): Results from original normal map; (Bottom): Results from normal map containing the Gaussian noise with variance of 6°.

Figure 15. Reconstructed surfaces of different models by the proposed method, where the ground-truth under the same view are framed in a green box at the bottom-right corner.

6. Conclusion

In this paper, we present an approach to address the problem of discontinuity preservation based on a discrete framework in surface reconstruction from normals. To determine the appropriate splittings of a discrete mesh, we introduce two new normal incompatibility features and design an efficient discontinuity detection scheme. In addition, we model the discontinuity preservation as a light-weight energy optimization problem, and shrink the feasible solution space to reduce the computation complexity based on the prior knowledge. Extensive experimental results show that the proposed method reconstructs various discontinuous surfaces efficiently and robustly.
References


