Dynamic Traffic Modeling from Overhead Imagery

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Abstract

Our goal is to use overhead imagery to understand patterns in traffic flow, for instance answering questions such as how fast could you traverse Times Square at 3am on a Sunday. A traditional approach for solving this problem would be to model the speed of each road segment as a function of time. However, this strategy is limited in that a significant amount of data must first be collected before a model can be used and it fails to generalize to new areas. Instead, we propose an automatic approach for generating dynamic maps of traffic speeds using convolutional neural networks. Our method operates on overhead imagery, is conditioned on location and time, and outputs a local motion model that captures likely directions of travel and corresponding travel speeds. To train our model, we take advantage of historical traffic data collected from New York City. Experimental results demonstrate that our method can be applied to generate accurate city-scale traffic models.

1. Introduction

Road transportation networks have become extremely large and complex. According to the Bureau of Transportation Statistics [31], there are approximately 6.6 million kilometers of roads in the United States alone. For most individuals, navigating these complex road networks is a daily challenge. A recent study found that the average driver in the U.S. travels approximately 17,500 kilometers per year in their vehicle, which equates to more than 290 hours behind the wheel [33].

As such, traffic modeling and analysis has become an increasingly important topic for urban development and planning. The Texas A&M Transportation Institute [26] estimated that in 2017, considering 494 U.S. urban areas, there were 8.8 billion vehicle-hours of delay and 12.5 billion liters of wasted fuel, resulting in a congestion cost of 179 billion dollars. Given these far-reaching implications, there is significant interest in understanding traffic flow and developing new methods to counteract congestion.

Numerous cities are starting to equip themselves with intelligent transportation systems, such as adaptive traffic control, that take advantage of recent advances in computer vision and machine learning. For example, Pittsburgh recently deployed smart traffic signals at fifty intersections that use artificial intelligence to estimate traffic volume and optimize traffic flow in real-time. An initial pilot study [27] indicated travel times were reduced by 25%, time spent waiting at signals by 40%, number of stops by 30%, and emissions by 20%. Ultimately, interest in applying machine learning to problems in traffic management continues to grow due to its potential for improving safety, decreasing congestion, and reducing emissions.

Direct access to empirical traffic data is useful for planners to analyze congestion in relation to the underlying street network, as well as for validating models and guiding infrastructure investments. Unfortunately, historical information relating time, traffic speeds, and street networks has typically been expensive to acquire and limited to only primary roads. Only very recently has a large corpus of traffic speed data been released to the public. In May of 2019, Uber Technologies, Inc. (an American multinational ridesharing company) announced Uber Movement Speeds [1], a dataset of street speeds collected from drivers of their ridesharing platform. However, even this data has limitations, including: 1) coverage, speed data is only available for 5 large metropolitan cities at the time of release and 2) granularity, not all roads are traversed at all times (or
traversed at all). For example, only 29% of road segments in New York City have historical traffic data for Monday at 12pm, considering every Monday in 2018.

In this work, our goal is to use historical traffic speeds to build a complete model of traffic flow for a given city (Figure 2). Traditional approaches for modeling traffic flow assume that the road network is known (i.e., in the form of a graph reflecting the presence and connectivity of road segments) and model road segments individually. However, this approach is limited in that it cannot generalize to new areas and it gives noisy estimates for road segments with few samples. Instead, we explore how image-driven mapping can be applied to model traffic flow directly from overhead imagery. We envision that such a model could be used by urban planners to understand city-scale traffic patterns when the complete road network is unknown or insufficient empirical traffic data is available.

We propose an automatic approach for generating dynamic maps of traffic speeds using convolutional neural networks (CNNs). We frame this as a multi-task learning problem, and design a network architecture that simultaneously learns to segment roads, estimate orientation, and predict traffic speeds. Along with overhead imagery, the network takes as input contextual information describing the location and time. Ultimately, the output of our method can be considered as a local motion model that captures likely directions of travel and corresponding travel speeds. To support training and evaluating our methods, we introduce a new dataset that takes advantage of a year of traffic speeds for New York City, collected from Uber Movement Speeds.

Extensive experiments show that our approach is able to capture complex relationships between the underlying road infrastructure and traffic flow, enabling understanding of city-scale traffic patterns, without requiring the road network to be known in advance. This enables our approach to generalize to new areas. The main contributions of this work are summarized as follows:

- introducing a new dataset for fine-grained road understanding,
- proposing a multi-task CNN architecture for estimating a localized motion model directly from an overhead image,
- integrating location and time metadata to enable dynamic traffic modeling,
- an extensive quantitative and qualitative analysis, including generating dynamic city-scale travel-time maps.

Our approach has several potential real-world applications, including forecasting traffic speeds and providing estimates of historical traffic speeds on roads which were not traversed during a specific time period.

2. Related Work

The field of urban planning [15] seeks to understand urban environments and how they are used in order to guide future decision making. The overarching goal is to shape the pattern of growth as a community expands to achieve a desirable land-use pattern. A major factor here is understanding how the environment influences human activity. For example, research has shown how the physical environment is associated with physical activity (walking/cycling) and subsequently impacts health [24].

Transportation planning is a specific subarea of urban planning that focuses on the design of transportation systems. The goal is to develop systems of travel that align with and promote a desired policy of human activity [19]. Decisions might include how and where to place roads, sidewalks, and other infrastructure to minimize congestion. As such, decades of research has focused on understanding traffic flow, i.e., the interactions of travelers and the underlying infrastructure. For example, Krauß [14] proposes a model of microscopic traffic flow to understand different types of traffic congestion. Meanwhile other work focuses on simulating urban mobility [13].
In computer vision, relevant work seeks to infer properties of the local environment directly from imagery. For example, estimating physical attributes like land cover and land use [23, 37], categorizing the type of scene [41], and relating appearance to location [25, 35, 36]. Other work focuses on understanding urban environments. Albert et al. [4] analyze and compare urban environments at the scale of cities using satellite imagery. Dubey et al. [8] explore the relationship between the appearance of the physical environment and the urban perception of its residents by predicting perceptual attributes such as safe and beautiful.

Specific to urban transportation, many studies have explored how to identify roads and infer road networks directly from overhead imagery [5, 17, 18, 20, 32]. Recent methods in this area take advantage of convolutional neural networks for segmenting an overhead image, then generate a graph topology directly from the segmentation output. Mapping roads is an important problem as it can positively impact local communities as well as support disaster response [21, 28]. However, identifying roads is just the first step. Other work has focused on estimating properties of roads, including safety [30].

Understanding how roads are used, in particular traffic speeds, is important for studying driver behavior, improving safety, decreasing collisions, and aiding infrastructure planning. Therefore, several works have tackled the problem of estimating traffic speeds from imagery. Hua et al. [11] detect, track, and estimate traffic speeds for vehicles in traffic videos. Song et al. [29] estimate the free-flow speed of a road segment from a co-located overhead image and corresponding road metadata. Van Etten [9] segments roads and estimates road speed limits. Unlike previous work, our goal is to dynamically model traffic flow over time.

Similarly, traffic forecasting is an important research area. Abadi et al. [3] propose an autoregressive model for predicting the flows of a traffic network and demonstrate the ability to forecast near-term future traffic flows. Zhang et al. [38] predict crowd flows between subregions of a city based on historical trajectory data, weather, and events. Wang et al. [34] propose a deep learning framework for path-based travel time estimation. These methods typically assume prior knowledge of the spatial connectivity of the road network, unlike our work which operates directly on overhead imagery.

### 3. A Large Traffic Speeds Dataset

To support training and evaluating our methods, we introduce the Dynamic Traffic Speeds (DTS) dataset that takes advantage of a year of historical traffic speeds for New York City. Our traffic speed data is collected from Uber Movement Speeds [1], a dataset of publicly available aggregated speed data over road segments at hourly frequencies.

![Figure 3: Example traffic speed data from Uber Movement Speeds for New York City (visualized as free-flow speeds for January 2018).](https://www.openstreetmap.org)

#### 3.1. Uber Movement Speeds

During rideshare trips, Uber (via their Uber Driver application) frequently collects GPS data including latitude, longitude, speed, direction, and time. While this data supports many functionalities, it is also stored for offline processing, where it is aggregated and used to derive speed data. Additionally, Uber uses OpenStreetMap as the source of their underlying map data (i.e., road network).

Given the map and GPS data as input, an extensive process is used to 1) match the GPS data to locations on the street network, 2) compute segment traversal speeds using the matched data, and 3) aggregate speeds along each segment. Please refer to the whitepaper [2] for a detailed overview of this process. Ultimately, the publicly released data includes the road segment identifier and average speed along that segment at an hourly resolution. Note that bidirectional roads, represented as line strings, are twinned and a speed estimate is provided for each direction.

#### 3.2. Augmenting with Overhead Imagery

To support our methods, we generated an aligned dataset of overhead images, contained road segments, and historical traffic speeds. We started by collecting road geometries and speed data from Uber Movement Speeds for New York City during the 2018 calendar year. This resulted in over 292 million records, or approximately 22GB (not including road geometries). For reference, there are around 290 thousand road segments in NYC when considering bidirectional roads. Figure 3 shows the free-flow speed along these segments for January 2018, where free-flow speed is defined as

\[ 1 \text{https://www.openstreetmap.org} \]
the 85th percentile of all recorded traffic speeds.

Starting from a bounding box around New York City, we generated a set of non-overlapping tiles using the standard XYZ style spherical Mercator tile. For each tile, we identified the contained road segments, extracted the corresponding speed data along those segments, and downloaded an overhead image from Bing Maps (filtering out tiles that do not contain any roads). This process resulted in approximately 12,000,000 1024 × 1024 overhead images at ~0.3 meters/pixel. We partitioned these non-overlapping tiles into 85% training, 5% validation, and 10% testing. The result is a large dataset containing overhead images (over 12 billion pixels), road geometries, and traffic speed data (along with other road attributes).

Figure 4 shows some example data: from left to right, an overhead image, the corresponding road mask, and a mask characterizing the traffic speeds at a given time. Notice that, depending on the time, not all roads have valid speed data. For this visualization, road geometries are buffered (converted to polygons) with two meter half width.

3.3. Aggregating Traffic Speeds

For a single road segment, there are a possible 8,760 (365 × 24) unique recorded speeds for that segment over the course of a year. When considering all roads, this is a large amount of data. For this work, we instead aggregate speed data for each road segment using day of week and hour of day, retaining the number of samples observed (i.e., the number of days per year that traffic was recorded at that time on a particular segment). This reduces the number of possible traffic speeds to 168 (7 × 24) per segment.

3.4. Discussion

While the current version of the dataset includes only New York City, we are actively working towards expanding it to include other cities where traffic speed data is available (e.g., London, Cincinnati). Further, we plan to incorporate other contextual road attributes (e.g., type of road, surface material, number of lanes) so that our dataset is useful for other tasks in fine-grained road understanding. Our hope is that this dataset will inspire further work in computer vision directed towards traffic modeling, with a positive impact on urban planning and minimizing traffic congestion.

4. Modeling Traffic Flow

We propose a novel CNN that fuses high-resolution overhead imagery, location, and time to estimate a dynamic model of traffic flow. We can think of our task as learning a conditional probability distribution over velocity, \( P(\vec{v}|S(l),l,t) \), where \( l \) is a latitude-longitude coordinate, \( S(l) \) is an overhead image centered at that location, and \( t \) represents the time.

4.1. Architecture Overview

We propose a multi-task architecture that simultaneously solves three pixel-wise labeling tasks: segmenting roads, estimating orientation, and predicting traffic speeds. Our network (Figure 5) has three inputs: a location, \( l \), the time, \( t \), and an overhead image, \( S(l) \), centered at \( l \) (of size \( H \times W \times C \)). We build on a modern, lightweight, semantic segmentation architecture, LinkNet [7], that follows an encoder/decoder approach with skip connections between every layer. Specifically, we use LinkNet-34, which is LinkNet with a ResNet-34 [10] encoder. For our purposes, we modify the baseline architecture to a multi-task version, with a shared encoder and separate decoder for each task. Though we use LinkNet, our approach would work with any modern encoder/decoder segmentation architecture.

Integrating Location and Time Context To make location and time-dependent traffic flow predictions, we integrate location and time into the final speed classification layers. We represent location as normalized latitude/longitude coordinates (\( \mu = 0, \sigma^2 = 1 \)). Time is parameterized as day of week (0-6) and hour of day (0-23). Each time dimension is represented as an embedding lookup with an embedding dimension of 3. To form a context feature, we concatenate the parameterized location and time embedding outputs together. The context feature is then tiled and fused in the decoder at each of the final two convolutional layers (concatenated on as additional feature channels).

Loss Function We simultaneously optimize the entire network, in an end-to-end manner, for all three tasks. The
final loss function becomes:
\[ L = L_{\text{road}} + L_{\text{orientation}} + L_{\text{speed}} + \alpha_r L_{\text{reg}}, \]
where \( L_{\text{road}}, L_{\text{orientation}}, \) and \( L_{\text{speed}} \) correspond to the task-specific objective function for road segmentation, orientation estimation, and traffic speed prediction, respectively. Additionally, \( L_{\text{reg}} \) is a regularization term that is weighted by a scalar \( \alpha_r \). In the following sections we detail the specifics of each task, including the architecture and respective loss terms.

### 4.2. Identifying Presence of Roads

The objective of the first decoder is to segment roads in an overhead image. We represent this as a binary classification task (road vs. not road) resulting in a single output per pixel \((H \times W \times 1)\). The output is passed through a sigmoid activation function. We follow recent trends in state-of-the-art road segmentation \([42]\) and formulate the objective function as a combination of multiple individual elements. The objective is:
\[ L_{\text{road}} = L_{\text{bce}} + (1 - L_{\text{dice}}), \]
where \( L_{\text{bce}} \) is binary cross entropy, a standard loss function used in binary classification tasks, and \( L_{\text{dice}} \) is the dice coefficient, which measures spatial overlap.

### 4.3. Estimating Direction of Travel

The objective of the second decoder is to estimate the direction of travel along the road at each pixel. We represent this as a multi-class classification task over \( K \) angular bins, resulting in \( K \) outputs per pixel \((H \times W \times K)\). A softmax activation function is applied to the output. For this task, the per-pixel loss function is categorical cross entropy:
\[ L_{\text{orientation}} = -\log(G(S(l); \Theta)(y)), \]
where \( G(S(l); \Theta) \) represents our CNN as a function that outputs a probability distribution over the \( K \) angular bins and \( y \) indicates the true label. We compute road orientation, \( \theta \), as the angle the road direction vector makes with the positive X axis. The valid range of values is between \(-\pi\) and \(\pi\) and we generate angular bins by dividing this space uniformly.

### 4.4. Predicting Traffic Speeds

The objective of the final decoder is to estimate local traffic speeds, taking into account the imagery, the location, and the time. Instead of predicting a single speed value for each pixel, we make angle-dependent predictions. The road speed decoder has \( K \) outputs per pixel \((H \times W \times K)\) and a softplus output activation, \( \log(1 + \exp(x)) \), to ensure positivity. For a given road angle \( \theta \), we compute the estimated speed as an orientation-weighted average using \( w_\mu = e^{k \cos(\theta - \mu)} \) as the weight for each bin where \( \mu \) is the angle of the corresponding bin and \( k = 25 \) is a fixed smoothing factor. Weights are normalized to sum to one. Note that we can predict angle-dependent speeds using either the true angle if known, or the predicted angle.
For traffic speed estimation, we minimize the Charbonnier loss (also known as the Pseudo-Huber loss):

\[
\mathcal{L}_{\text{speed}} = \delta^2 (\sqrt{1 + (a/\delta)^2} - 1),
\]

where \( y \) and \( \hat{y} \) are the observed and predicted values, respectively, and \( a = y - \hat{y} \) is their residual. The Charbonnier loss is a smooth approximation of the Huber loss, where \( \delta \) controls the steepness. In addition, we add a regularization term, \( \mathcal{L}_{\text{reg}} \), to reduce noise and encourage spatial smoothness. For this we use the anisotropic version of total variation, \( f(x) = (x_{i+1,j} - x_{i,j})^2 + (x_{i,j+1} - x_{i,j})^2 \), averaged over all pixels, \( i,j \), in the raw output.

**Region Aggregation** The target labels for traffic speed are provided as averages over road segments, which means we cannot use a traditional per-pixel loss. The na"ıve approach would be to assume the speed is constant across the entire road segment, which would lead to over-smoothing and incorrect predictions. Instead, we use a variant of the region aggregation layer [12], adapted to compute the average of the per-pixel estimated speeds over the segment. We optimize our network to generate per-pixel speeds such that the segment averages match the true speed. In practice we predict angle-dependent speeds, compute the orientation-weighted average, and then apply region aggregation; finally, computing the average loss over road segments.

4.5. Implementation Details

Our methods are implemented using PyTorch [22] and optimized using RAdam [16] (\( \lambda = 10^{-3} \)) with Lookahead [39] (\( k = 5, \alpha = 0.5 \)). We initialize the encoder with weights from a network pretrained on ImageNet. For fairness, we train all networks with a batch size of 6 for 50 epochs, on random crops of size 640 \( \times \) 640. We use \( K = 16 \) angular bins and set \( \alpha_r = 10^{-2} \), chosen empirically. For this work, we set \( \delta = 2 \). Our networks are trained in a dynamic manner; instead of rendering a segmentation mask at every possible time, for every training image, we sample a time during training and dynamically render the speed mask. The alternative would be to pregenerate over a million segmentation masks. Additionally, we train the orientation and speed estimation decoders in a sparse manner by sampling pixels along road segments (every one meter along the segment and up to two meters on each side, perpendicularly) and computing orientation from corresponding direction vectors. For road segmentation, we buffer the road geometries (two meter half width) and do not sample. Model selection is performed using the validation set.

5. Evaluation

We train and evaluate our method using the dataset described in Section 3. We primarily evaluate our model for traffic speed estimation, but present quantitative and qualitative results for both road segmentation and orientation estimation.

### 5.1. Ablation Study

We conducted an extensive ablation study to evaluate the impact of various components of our proposed architecture. For evaluation, we use the reserved test set, but evaluate on a single timestep per image (randomly selected from the observed traffic speeds using a fixed seed). When computing metrics, we represent speeds using kilometers per hour and average predictions along each road segment before comparing to the ground truth.

#### 5.1.1 Impact of Multi-Task Learning

For our first experiment, we quantify the impact of multi-task learning for estimating traffic speeds. In other words, we evaluate whether or not simultaneously performing the road segmentation and orientation estimation tasks improves the results for estimating traffic speeds. We compare our full method (Section 4) to variants with subsets of the multi-task components. The results of this experiment are shown in Table 1 for three metrics: root-mean-square error (RMSE), mean absolute error (MAE) and the coefficient of determination (\( R^2 \)).

As observed, the multi-task nature of our architecture improves the final speed predictions. Adding the road segmentation and orientation estimation tasks improves results over a baseline that only estimates traffic speed, with the best performing model integrating both tasks. Our results are in line with previous work [40] that demonstrates multi-task learning can be helpful when the auxiliary tasks are related to the primary task. For the remainder of the ablation study, we only consider our full architecture that performs all three tasks.

#### 5.1.2 Impact of Region Aggregation

Next, we consider how region aggregation affects traffic speed estimation. As described in Section 4, the target speeds for the traffic speed estimation task are averages over each road segment. Here we compare two approaches.
for training using these labels: 1) naïvely replicating the target labels spatially across the entire road segment, and 2) our approach that integrates a variant of the region aggregation layer \cite{yolov3}, which enables prediction of per-pixel speeds such that the segment averages match the ground-truth speed label for that segment.

To evaluate both approaches, we average predictions along each road segment and compare to the true traffic speed label. The baseline method achieves an RMSE score of 11.10, which is worse than our method (RMSE = 10.66). Additionally, we show some qualitative results of the two approaches in Figure 6. Our method which incorporates region aggregation (top) is better able to capture real-world properties of traffic speed, such as slowing down at intersections or around corners. For the remainder of the ablation study, we only consider methods which were optimized and evaluated using region aggregation.

5.1.3 Impact of Location and Time Context

Finally, we evaluate how integrating location and time context impacts our traffic speed predictions. For this experiment, we compare against several baseline methods that share many low-level components with our proposed architecture. Our full model includes all three components image, loc, and time. For the metadata only approaches, those without image, we use our proposed architecture, but omit all layers prior to concatenating in the context feature.

The results of this experiment are shown in Table 2. Both location and time improve the resulting traffic speed predictions. Our method, which integrates overhead imagery, location, and time, outperforms all other models. Additionally, we show results for road segmentation (F1 score) and orientation estimation (top-1 accuracy). These tasks do not rely on location and time, so their performance is comparable, but our method still performs best.

<table>
<thead>
<tr>
<th></th>
<th>Road (F1 Score)</th>
<th>Orientation (Accuracy)</th>
<th>Speed (RMSE)</th>
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<tr>
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<td>–</td>
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<tr>
<td>time</td>
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<td><strong>10.66</strong></td>
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</tbody>
</table>

Figure 7: Estimating directions of travel. (left) An overhead image and estimated orientation represented as a flow field. (right) Predicted distributions over orientation for corresponding dots in the image. (top, right) The predicted distribution for the green dot correctly identifies multiple possible directions of travel. This makes sense as the location in the image is at an intersection.

5.2. Visualizing Traffic Flow

In this section, we qualitatively evaluate our proposed methods ability to capture spatial and temporal patterns in traffic flow. First, we examine how well our approach is able to estimate directions of travel. Figure 7 (left) visualizes the predicted per-pixel orientation for an overhead image, overlaid as a vector field (colored by predicted angle). As observed, our method is able to capture primary directions of travel, including differences in one way and bidirectional roads. Additionally, Figure 7 (right) shows radial histograms representing the predicted distributions over orientation for corresponding color-coded dots in the overhead image. For example, the predicted distribution for the green dot (top, right), which represents an intersection in the image, correctly identifies several possible directions of travel. Alternatively, the predicted distribution for the yellow dot is more uniform, which makes sense as the location is not a road.

Next, we examine how our model captures temporal trends in traffic flow. Figure 9 visualizes traffic speed pre-
predictions for a residential road segment colored in red. Figure 9 (right) shows the predicted speeds for this segment versus the day of the week, with each day representing twenty four hours. As observed, the predicted speeds capture temporal trends both daily, and over the course of the full week. Finally, Figure 1 shows predicted traffic speeds for The Bronx, New York City for Monday at 4am (left) versus Monday at 8am (right). As expected, there is a large slow down likely corresponding to rush hour. These results demonstrate that our model is capturing meaningful patterns in both space and time.

5.3. Application: Generating Travel Time Maps

Our approach can be used to generate dynamic traffic maps at the scale of a city. To demonstrate this, we generate travel time maps at different times. We use OSMnx [6], a library for modeling street networks from OpenStreetMap, to represent the underlying street network topology for New York City as a graph. Our approach is as follows. For each image in our dataset, we estimate traffic speeds at a given time. Then we update the edge weights of the graph (corresponding to each road segment) to represent travel times using the length of each segment in meters and our traffic speed predictions. For any road segment not represented in our dataset, we use the average predicted traffic speed for that time. Figure 8 shows several results, visualized as isochrone maps that depict areas of equal travel time.

6. Conclusion

Understanding traffic flow is important and has many potential implications. We developed a method for dynamically modeling traffic flow using overhead imagery. Though our method incorporates time, a unique overhead image is not required for every timestamp. Our model is conditioned on location and time metadata and can be used to render dynamic city-scale traffic maps. To support our efforts, we introduced a novel dataset for fine-grained road understanding. Our hope is that this dataset will inspire further work in the area of image-driven traffic modeling. By simultaneously optimizing for road segmentation, orientation estimation, and traffic speed prediction, our method can be applied for understanding traffic flow patterns in novel areas. Potential applications of our method include assisting urban planners, augmenting routing engines, and for providing a general understanding of how to traverse an environment.

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