

## A. Appendix

### A.1. Generalized Coordinate Transformation

In Sec. 3.4 we have assumed  $\sigma_{HW}=\hat{\sigma}_{HW}$  and  $\sigma_{VU}=\hat{\sigma}_{VU}$ . Here we relax this condition and only assume  $\sigma_{HW}=\hat{\sigma}_{HW}$ . Again, we still have the following two relations for  $x, u$ :  $x+\alpha u=\hat{x}$  and  $x=\hat{x}-\hat{\alpha}\hat{u}$ . Solving for  $\hat{x}$  and  $\hat{u}$  gives:  $\hat{x}=x+\alpha u$  and  $\hat{u}=\frac{\alpha}{\hat{\alpha}}u$ . Then `align2nat` is:

$$\mathcal{F}(v, u, y, x) = \hat{\mathcal{F}}(\frac{\alpha}{\hat{\alpha}}v, \frac{\alpha}{\hat{\alpha}}u, y+\alpha v, x+\alpha u). \quad (2)$$

More generally, consider arbitrary units  $\sigma_{HW}, \hat{\sigma}_{HW}, \sigma_{VU}$ , and  $\hat{\sigma}_{VU}$ . Then the relations between the natural and aligned representation can be rewritten as:

$$\begin{cases} x \cdot \sigma_{HW} + u \cdot \sigma_{VU} &= \hat{x} \cdot \hat{\sigma}_{HW} \\ x \cdot \hat{\sigma}_{HW} &= \hat{x} \cdot \hat{\sigma}_{HW} - \hat{u} \cdot \hat{\sigma}_{VU} \end{cases} \quad (3)$$

Note that these relations only hold in the image pixel domain (hence the usage of all units). Solving for  $\hat{x}, \hat{u}$  gives:

$$\begin{cases} \hat{x} &= \frac{\sigma_{HW}}{\hat{\sigma}_{HW}}x + \frac{\sigma_{VU}}{\hat{\sigma}_{HW}}u \\ \hat{u} &= \frac{\sigma_{VU}}{\hat{\sigma}_{VU}}u \end{cases} \quad (4)$$

And the `align2nat` transform becomes:

$$\mathcal{F}(v, u, y, x) = \hat{\mathcal{F}}(\frac{\sigma_{VU}}{\hat{\sigma}_{VU}}v, \frac{\sigma_{VU}}{\hat{\sigma}_{VU}}u, \frac{\sigma_{HW}}{\hat{\sigma}_{HW}}y + \frac{\sigma_{VU}}{\hat{\sigma}_{HW}}v, \frac{\sigma_{HW}}{\hat{\sigma}_{HW}}x + \frac{\sigma_{VU}}{\hat{\sigma}_{HW}}u). \quad (5)$$

This version of the coordinate transformation demonstrates the role of units and may enable more general uses.

### A.2. Aligned Representation and InstanceFCN

We prove that the InstanceFCN [7] output behaves as an upscaling aligned head with *nearest-neighbor* interpolation.

In [7], each output mask has  $V \times U$  pixels that are divided into  $K \times K$  bins. A mask pixel is read from the channel corresponding to the pixel's bin. In our notation, [7] predicts  $\mathcal{G}$  which is related to the natural representation  $\mathcal{F}$  by:

$$\mathcal{F}(v, u, y, x) = \mathcal{G}([\frac{K}{V}v], [\frac{K}{U}u], y+v, x+u), \quad (6)$$

where  $[\cdot]$  is a rounding operation and the integers  $[\frac{K}{V}v]$  and  $[\frac{K}{U}u]$  index a bin. Now, define a new function  $\tilde{\mathcal{F}}$  by:

$$\tilde{\mathcal{F}}(v, u, y+v, x+u) \triangleq \mathcal{G}([\frac{K}{V}v], [\frac{K}{U}u], y+v, x+u), \quad (7)$$

and new coordinates:  $\tilde{x}=x+u$  and  $\tilde{u}=u$  (likewise for  $v$  and  $y$ ). Then  $\tilde{\mathcal{F}}$  can be written as:

$$\tilde{\mathcal{F}}(\tilde{v}, \tilde{u}, \tilde{y}, \tilde{x}) \triangleq \mathcal{G}([\frac{K}{V}\tilde{v}], [\frac{K}{U}\tilde{u}], \tilde{y}, \tilde{x}). \quad (8)$$

Eqn.(8) says that  $\tilde{\mathcal{F}}$  is the *nearest-neighbor* interpolation of  $\mathcal{G}$  on  $(\tilde{V}, \tilde{U})$ . Eqn.(7), (6), and the new coordinates show that  $\mathcal{F}$  is computed from  $\tilde{\mathcal{F}}$  by the `align2nat` transform with  $\alpha=1$ . Thus, InstanceFCN masks can be constructed in the TensorMask framework by predicting  $\mathcal{G}$ , performing nearest-neighbor interpolation of  $\mathcal{G}$  on  $(\tilde{V}, \tilde{U})$  to get  $\tilde{\mathcal{F}}$ , and then using `align2nat` to compute natural masks  $\mathcal{F}$ .

### A.3. Object Detection Results

In Tab. 4 we show the associated *bounding-box* (bb) object detection results. Overall, TensorMask has a comparable box AP with Mask R-CNN and outperforms RetinaNet.

method	aug	epochs	AP <sup>bb</sup>	AP <sup>bb</sup> <sub>50</sub>	AP <sup>bb</sup> <sub>75</sub>
RetinaNet, <i>ours</i>		24	37.1	55.0	39.9
RetinaNet, <i>ours</i>	✓	72	39.3	57.2	42.4
Faster R-CNN, <i>ours</i>	✓	72	40.6	61.4	44.2
Mask R-CNN, <i>ours</i>	✓	72	41.7	62.5	45.7
TensorMask, <i>box-only</i>	✓	72	40.8	60.4	43.9
TensorMask	✓	72	41.6	61.0	45.1

Table 4. **Object detection box AP on COCO test-dev.** All models use ResNet-50-FPN. ‘TensorMask, *box-only*’ is our model without the mask head: it resembles RetinaNet but with the mask-driven assignment rule and only 2 window sizes instead of 9 [23].

### A.4. Mask-Only TensorMask

One intriguing property of TensorMask is that *masks are not dependent on boxes*. This not only opens up new model designs that are mask-specific, but also allows us to investigate whether *box predictions improve masks in a multi-task setting*. Here, we conduct experiments *without* the use of a box head. Note that although we predict masks densely, we still need to perform NMS for post-processing. If regressed boxes are absent, we simply use the bounding boxes of the masks as a substitute (and also to report box AP).

Tab. 5 gives the results. We observe a slight degradation switching from the default setting which uses original boxes (row 1) for NMS to using mask bounding boxes (row 2). After accounting for this, TensorMask *without a box head* (row 3) has nearly equal mask AP to the mask+box variant (row 2). These results indicate that the role of the box head is auxiliary in our system, in contrast to Mask R-CNN.

box head	NMS	AP	AP <sub>50</sub>	AP <sub>75</sub>	AP <sup>bb</sup>	AP <sup>bb</sup> <sub>50</sub>	AP <sup>bb</sup> <sub>75</sub>
✓	bb	35.2	56.4	37.0	41.6	60.8	44.8
✓	mask-bb	34.9	56.0	36.7	39.7	59.1	41.8
	mask-bb	34.8	56.1	36.7	39.4	58.8	41.6

Table 5. **Multi-task benefits** of box training for mask prediction on COCO val2017 with our final ResNet-50-FPN model.

### A.5. Qualitative Comparisons and Calibration

We show more results in Figs. 10 and 11. For these, and all visualizations in the main text, we display all detections that have a *calibrated* score  $\geq 0.6$ . We use a simple calibration that maps uncalibrated detector scores to precision values: for each model and for each category, we compute its precision-recall (PR) curve on val2017. As a PR curve is parameterized by score, we can map an uncalibrated score for the detector-category pair to its corresponding precision value. Score-to-precision calibration enables a fair visual comparison between methods using a fixed threshold.







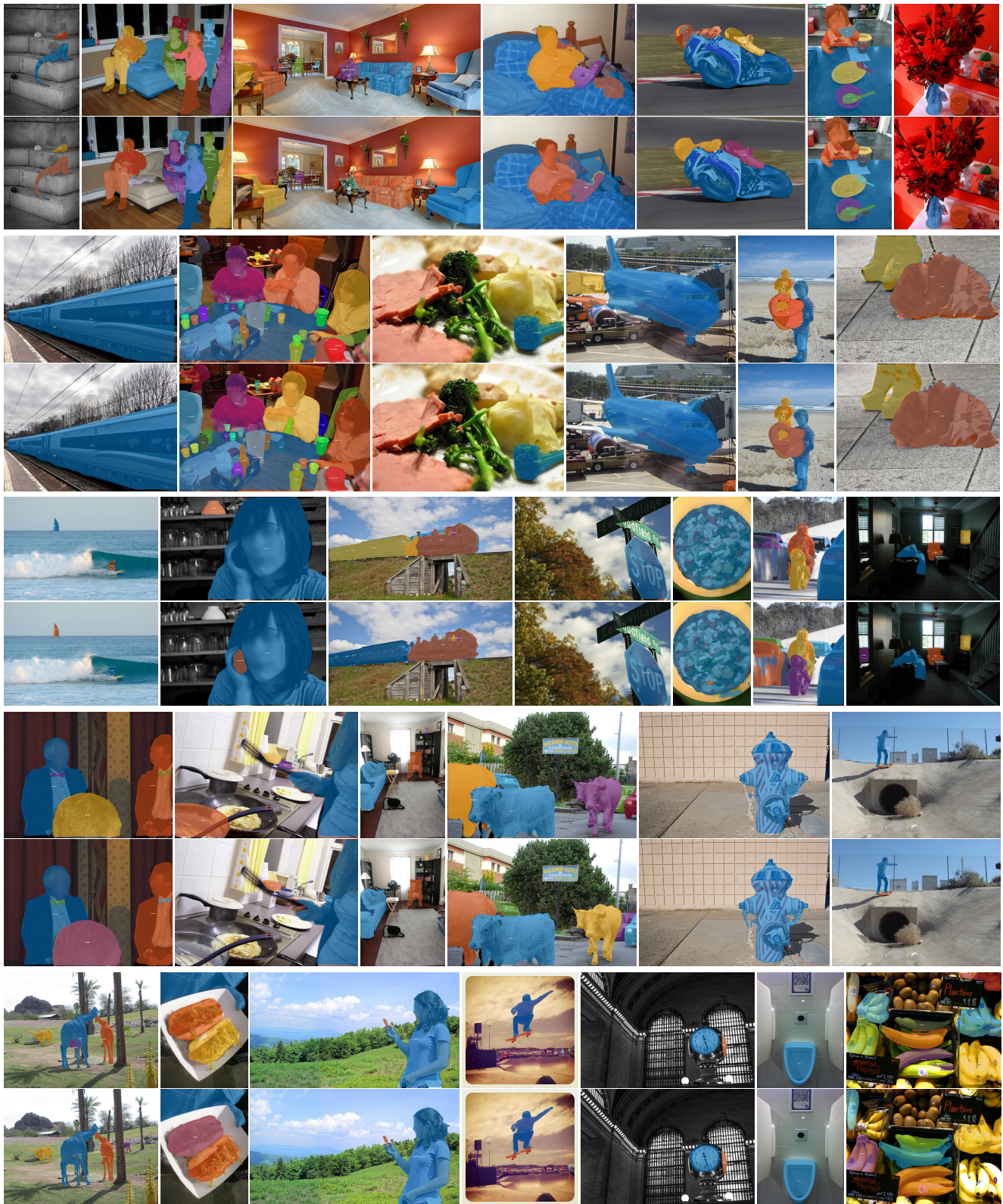


Figure 11. More results of Mask R-CNN [17] (top row per set) and TensorMask (bottom row per set) continued from Fig. 10.



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