Boosting Standard Classification Architectures Through a Ranking Regularizer Supplementary material

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1. Supplementary Material

The next subsections provide more details about our architecture and training procedure's technicalities. Further quantitative evaluations on fine-grained visual recognition (FGVR) are presented. Finally, we demonstrate the training procedure for the Honda Research Institute Driving Dataset.

1.1. Fine-Grained Visual Recognition

Figure 2 in the main paper presents our two-head architecture. The pre-logit layer x supports the softmax loss. Similarly, triplet loss utilizes h, where x = pool(h). The network outputs, both logits and embedding, are formulated as follows.

$$logits = W_{logits} * flat(x)$$
(1)

$$embedding = W_{emb} * flat(h).$$
(2)

Orderless pooling, like averaging, reduces h dimensionality but loses spatial information. For example, in DenseNet161, $h \in R^{7 \times 7 \times 2208}$ while $x \in R^{1 \times 1 \times 2208}$. Thus, W_{emb} employs h, instead of x, to improve feature embedding. Figure S1 illustrates how h provides a finer control level while learning W_{emb} .

Figure S2 shows a t-SNE visualization for Flowers-102 embedding using 50 random classes, 20 samples per class. In the main paper, the inferior performance of triplet loss with hard-mining is associated with convergence to bad local minima, *i.e.*, a collapsed model (i.e. f(x) = 0) [7]. To examine such assumption, we train a DenseNet for 400K iterations on Stanford Dogs. This large number of iterations increases the chances of a model collapse. Figure S3 presents the performance on the test split after every 50K iterations. Triplet loss with hard-mining is evaluated with both soft and hard margin. Soft margin applies the softplus function $\ln(1 + \exp(\bullet))$ while hard margin uses a fixed margin m = 0.2. The triplet loss with hard-mining deteriorates with soft margin when trained for a large number of iterations. Hard-mining with hard margin is more robust. We found similar behavior on other datasets like Stanford Cars and Aircrafts datasets.

Table 5 in the main paper presents a quantitative analysis for the feature embedding learned by the second head Abhinav Shrivastava¹ Larry Davis¹ ²Honda Research Institute, USA



Figure S1: Orderless pooling reduces dimensionality but loses features spatial information.



Figure S2: t-SNE visualization for Flowers-102 embedding using 50 random classes, 20 samples per class. Best viewed in color.

in our proposed architecture. Similarly, Table S1 presents feature embedding quantitative analysis using the architecture penultimate layer, *i.e.*, layer x (Figure 2 in the main paper). This layer is present in both our proposed two-head and single-head (vanilla softmax) architecture. Similar to Table 5, the triplet loss embedding is superior to the softmax embedding. Triplet loss with hard-mining achieves the best results on ResNet-50 but degrades on Inception-V4 trained for 80K iterations. Center loss achieves good results with DenseNet161 on NABirds but generally fluctuates and suf-



Figure S3: Model collapse study by training DenseNet161 for 400K iterations. Triplet loss with hard-mining evaluated with soft and hard margins.

fers with Inception-V4. Triplet loss with semi-hard margin achieves sub-optimal embedding but maintains the highest stability compared to center and hard-mining approaches.

Figure S4 graphically summarizes Table S1. It provides a comparative embedding evaluation between the singlehead softmax verses the two-head with semi-hard triplet loss using recall@1 metric. Triplet loss improvements, over the softmax model, are reported as (\triangle). The Flowers-102 dataset has the smallest training split with 1020 images only. With this limited data, the head-two architecture achieves marginal improvement if any.

Table S2 compares our proposed two-head architecture, using DenseNet161, with state-of-the-art approaches on the five FGVR datasets. Our two-head architecture with the semi-hard triplet loss regularizer achieves competitive results.

1.2. Autonomous Car Driving

The Honda Research Institute Driving Dataset (HDD) contains 137 sessions S. Each session S_i represents a navigation task performed by a driver. S is divided into 93, 5, and 36 sessions for training, validation and testing splits respectively. Three sessions are removed for missing annotations. HDD has four annotation layers to study the drivers' actions: (1) Goal-oriented, (2) stimulus-driven, (3) cause and (4) attention. The **Goal-oriented** layer, utilized in our experiments, defines drivers' actions to reach their destinations, *e.g.*, *left-turn* and *intersection passing*. Ramanishka *et al.* [6] provides further details for the other three annotation layers.

Triplet loss mini-batches require both positive and negative samples. The FGVR datasets have uniform class distribution. Thus, training batches' construction is straightforward by sampling random classes and their corresponding images as outlined in the main paper. On the other hand, HDD suffers class imbalance. A different batch construction procedure is required.

Algorithm 1 outlines our training procedure. First, N_B mini-batches are constructed, each containing *b* random actions. The batches' embeddings are computed using N_B

		NMI	R@1	R@4	R@8	R@16
	Vanilla	0.791	77.88	91.17	94.65	96.9
Core BooNat	CNTR	0.756	77.98	91.12	94.58	96.78
Cars - Resider	SEMI	0.823	81.41	92.79	95.91	97.74
	HARD	0.853	85.31	94.30	96.82	98.07
	Vanilla	0.800	88.76	95.51	97.27	98.49
Element DecNet	CNTR	0.807	88.79	95.58	97.32	98.49
riowers - Keshet	SEMI	0.818	89.48	95.82	97.37	98.37
	HARD	0.742	90.78	95.56	96.93	97.98
	Vanilla	0.587	51.62	74.22	83.02	89.76
Doos DooNot	CNTR	0.526	48.74	71.90	80.92	87.81
Dogs - Resider	SEMI	0.621	54.18	76.39	84.50	91.10
	HARD	0.684	60.37	80.34	87.33	92.26
	Vanilla	0.756	73.42	87.88	92.26	94.90
Ainenefte DecNet	CNTR	0.677	70.84	85.84	90.79	93.91
Aircrans - ResNet	SEMI	0.792	77.26	89.65	93.07	95.29
	HARD	0.829	84.01	91.63	94.21	95.65
	Vanilla	0.669	50.70	71.20	79.48	85.80
MADINI- D. N.4	CNTR	0.623	47.40	68.18	76.56	83.33
NABirds - Resnet	SEMI	0.657	50.05	70.83	78.84	85.52
	HARD	0.723	55.85	75.81	83.26	88.67
	Vanilla	0.660	72.47	86.77	90.55	93.55
	CNTR	0.496	61.55	79.09	85.09	89.69
Cars - Inc-V4	SEMI	0.788	81.46	92.14	94.64	96.37
	HARD	0.566	63.70	82.04	87.54	91.42
	Vanilla	0.778	90.54	96.21	97.63	98.70
T	CNTR	0.707	85.62	93.74	95.95	97.56
Flowers - Inc-V4	SEMI	0.801	89.58	95.23	96.91	97.84
	HARD	0.731	92.68	96.21	97.27	98.32
	Vanilla	0.421	41.11	62.97	72.59	81.13
D 1 111	CNTR	0.453	57.13	68.32	72.35	76.90
Dogs - Inc-V4	SEMI	0.609	55.03	76.50	84.44	90.23
	HARD	0.330	33.89	54.28	65.06	74.98
	Vanilla	0.680	69.79	85.18	89.23	91.93
	CNTR	0.546	61.60	79.75	85.33	89.53
Aircrafts - Inc-V4	SEMI	0.751	78.13	89.20	91.78	94.27
	HARD	0.831	86.26	91.87	93.49	94.72
	Vanilla	0.546	41.03	60.11	68.88	76.71
XY . XX . X XY .	CNTR	0.438	24.30	40.43	49.38	58.78
NABirds - Inc-V4	SEMI	0.638	52.42	72.38	79.57	85.60
	HARD	0.433	23.68	38.95	47.48	57.10
	Vanilla	0.813	85.08	94 49	96.84	98.22
	CNTR	0 787	87 39	93.17	94 64	95.97
Cars - Dense	SEMI	0.875	88.57	96.08	97.66	98.71
	HARD	0.892	89.44	96.38	97.86	98.76
	Vanilla	0.838	95.28	98.23	98.94	99.38
	CNTR	0.812	95.87	98.16	98 75	99.22
Flowers - Dense	SEMI	0.864	95.40	98 39	99.09	99.46
	HARD	0.865	95.79	98.50	99.14	99.50
	Vanilla	0.544	57.06	78 72	85.98	91.84
	CNTR	0.720	70.96	84.00	88 19	91.96
Dogs - Dense	SEMI	0.728	68.55	87.04	92.18	95.83
	HARD	0.756	70.63	87.80	92.95	96.22
	Vanilla	0.768	79.06	91.66	94.66	96.49
	CNTR	0.792	86.20	91.63	93.16	94.48
Aircrafts - Dense	SEMI	0.853	84.49	94.15	95.68	96.97
	HARD	0.856	85.51	93 70	95.83	96.94
	Vanilla	0.606	53.91	73.08	80.70	86 44
	CNTR	0.818	75.28	86.88	90.85	93.69
NABirds - Dense	SEMI	0.677	61.82	80 70	87 07	91.62
	HARD	0.674	61.64	80.21	86.77	91.37
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Table S1: Detailed feature embedding quantitative analysis across the five datasets using ResNet-50, Inception-V4 and DenseNet-161 architectures' penultimate layer x. Triplet with hard mining achieves superior embedding with ResNet-50 trained for 40K iterations. Semi-hard triplet is competitive and stable with Inception-V4 trained for 80K iterations. Center loss suffers a high instability.

feed forward passes. The 2D matrix D_{ϕ} stores the pairwise distance between the $N_B \times b$ actions. All positive

Flowers-102	2	Aircrafts		NABirds	is Cars I		Dogs		
Method	Acc	Method	Acc	Method	Acc	Method	Acc	Method	Acc
Det.+Seg. [1]	80.66	LRBP [2]	87.30	Branson et al. [9]	35.70	Liu et al. [5]	86.80	Zhang et al. [9]	80.43
Overfeat [8]	86.80	Liu et al. [4]	88.50	Van <i>et al</i> . [3]	75.00	Liu et al. [4]	92.00	Krause et al. [3]	80.60
Softmax	92.56	Softmax	89.13	Softmax	78.69	Softmax	91.64	Softmax	81.58
Two-Head (Semi)	93.65	Two-Head (Semi)	89.64	Two-Head (Semi)	79.57	Two-Head (Semi)	92.36	Two-Head (Semi)	80.89

Table S2: Quantitative evaluation on the five FGVR datasets using DenseNet161. Our two-head architecture with semi-hard triplet loss regularizer compares favorably with state-of-the-art results.



Figure S4: Comparative embedding evaluation between single-head softmax and two-head with semi-hard triplet loss using the penultimate layer in ResNet-50, Inception-V4 and DenseNet161 respectively. Triplet loss semi-hard improvements over the softmax model are reported as (\triangle) .

pairs (a, p) and their corresponding semi-hard negatives n are identified. For a fair comparison with vanilla softmax approach, only (b//3) random triplets (a, p, n) are utilized for back-propagation. This process repeats for N training iterations.

Algorithm 1 HDD training procedure. In our experiments, $b = \{33, 36\}$ is the mini-batch size, $N_B = 3$ is the number of mini-batches, and N = 10K is number of training iterations.

for all iteration <i>i</i> in N do
$S_{\phi} = \Phi$
for all j in N_B do
Add a random batch, of size b, to S_{ϕ}
end for
Compute action embeddings E_{ϕ} for S_{ϕ}
Compute pairwise distance matrix D_{ϕ} using E_{ϕ}
$T_{tri} = \Phi$
Construct all positive pairs (a, p)
for all (a, p) in positive pairs do
Find nearest semi-hard negative n using D_{ϕ}
append (a, p, n) to T_{tri}
end for
if $len(T_{tri}) > b//3$ then
$T_{tri} = \text{shuffle}(T_{tri})[0:b//3]$
end if
// T_{tri} contains b actions
Feed-forward T_{tri}
compute softmax + triplet losses and back-propagate.
end for

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