Defense against Adversarial Attacks Using High-Level Representation Guided Denoiser

Fangzhou Liao, Ming Liang, Yinpeng Dong, Tianyu Pang, Xiaolin Hu, Jun Zhu
Department of Computer Science and Technology, Tsinghua Lab of Brain and Intelligence, Beijing National Research Center for Information Science and Technology, BNRist Lab
Tsinghua University, 100084 China
{liaofangzhou, liangming.tsinghua}@gmail.com, {dyp17, pty17}@mails.tsinghua.edu.cn, {xlhu, dcszj}@tsinghua.edu.cn

Abstract

Neural networks are vulnerable to adversarial examples, which poses a threat to their application in security sensitive systems. We propose high-level representation guided denoiser (HGD) as a defense for image classification. Standard denoiser suffers from the error amplification effect, in which small residual adversarial noise is progressively amplified and leads to wrong classifications. HGD overcomes this problem by using a loss function defined as the difference between the target model’s outputs activated by the clean image and denoised image. Compared with ensemble adversarial training which is the state-of-the-art defending method on large images, HGD has three advantages. First, with HGD as a defense, the target model is more robust to either white-box or black-box adversarial attacks. Second, HGD can be trained on a small subset of the images and generalizes well to other images and unseen classes. Third, HGD can be transferred to defend models other than the one guiding it. In NIPS competition on defense against adversarial attacks, our HGD solution won the first place and outperformed other models by a large margin.

1. Introduction

As many other machine learning models [2], neural networks are known to be vulnerable to adversarial examples [30, 7]. Adversarial examples are maliciously designed inputs to attack a target model. They have small perturbations on original inputs but can mislead the target model. Adversarial examples can be transferred across different models [30, 21]. This transferability enables black-box adversarial attacks without knowing the weights and structures of the target model. Black-box attacks have been shown to be feasible in real-world scenarios [22], which poses a potential threat to security-sensitive deep learning applications, such as identity authentication and autonomous driving. It is thus important to find effective defenses against adversarial attacks.

Since adversarial examples are constructed by adding noises to original images, a natural idea is to denoise adversarial examples before sending them to the target model (Figure[1]). We explored two models for denoising adversarial examples, and found that the noise level could indeed be reduced. These results demonstrate the feasibility of the de-
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the adversarial noise, such as the median filter, averaging filter and Gaussian low-pass filter. Graese et al. [8] assess the defending performance of a set of preprocessing transformations on MNIST digits [17], including the perturbations introduced by image acquisition process, fusion of crops and binarization. Das et al. [4] preprocess images with JPEG compression to reduce the effect of adversarial noises. Meng and Chen [18] propose a two-step defense model, which detects the adversarial input and then reform it based on the difference between the manifolds of clean and adversarial examples. Our approach distinguishes from these methods by using the reconstruction error of high-level features to guide the learning of denoisers. Moreover, these methods are usually evaluated on small images. As we will show in experiments section, some method effective on small images may not transfer well to large images.

Another family of adversarial defenses is based on the so-called gradient masking effect [22, 23, 31]. These defenses apply some regularizers or smooth labels to make the model output less sensitive to the perturbation on input. Gu and Rigazio [9] propose the deep contrastive network, which uses a layer-wise contrastive penalty term to achieve output invariance to input perturbation. Papernot et al. [24] adapts knowledge distillation [12] to adversarial defense, and uses the output of another model as soft labels to train the target model. Nayebi and Surya [19] use saturating networks for robustness to adversarial noises. The loss function is designed to encourage the activations to be in their saturating regime. The basic problem with these gradient masking approaches is that they fail to solve the vulnerability of the models to adversarial attacks, but just make the construction of white-box adversarial examples more difficult. These defenses still suffer from black-box attacks [22, 31] generated on other models.

3. Methods

3.1. Pixel guided denoiser

In this section, we introduce a set of denoising networks and their motivations. These denoisers are designed in the context of image classification on ImageNet [5] dataset. They are used in conjunction with a pretrained classifier \( f \) (By default Inception V3 [29] in this study). Let \( x \) denote the clean image. The denoising function is denoted as \( D: x^* \rightarrow \hat{x} \), where \( x^* \) and \( \hat{x} \) denote the adversarial image and denoised image, respectively. The loss function is:

\[
L = ||x - \hat{x}||, \tag{3}
\]

where \( || \cdot || \) stands for the \( L_1 \) norm, the following equations also use this notation. Since the loss function is defined at the level of image pixels, we name this kind of denoiser pixel guided denoiser (PGD).

3.1.1 Denoising U-net

Denoising autoencoder (DAE) [32] is a popular denoising model. In a previous work [9], DAE in the form of a multi-layer perceptron was used to defend target models against adversarial attacks. However, the experiments were conducted on the relatively simple MNIST [17] dataset. To better represent the high-resolution images in the ImageNet dataset, we use a convolutional version of DAE for the experiments (see Figure 2(left)).

DAE has a bottleneck structure between the encoder and decoder. This bottleneck may constrain the transmission of fine-scale information necessary for reconstructing high-resolution images. To overcome this problem, we modify DAE with the U-net [27] structure and propose the denoising U-net (DUNET, see Figure 2(right)). DUNET is different from DAE in two aspects. First, similar to the Ladder network [25], DUNET adds lateral connections from encoder layers to their corresponding decoder layers in the same scale. Second, the learning objective of DUNET is the adversarial noise (\( d\hat{x} \) in Figure 2), instead of reconstructing the whole image as in DAE. This residual learning [24] is implemented by the shortcut from input to output to additively combine them. The clean image can be readily obtained by subtracting the noise (adding \( -d\hat{x} \)) from the corrupted input.

3.1.2 Network architecture

We use DUNET as an example to illustrate the architecture (Figure 3). DAE can be obtained simply by removing the lateral connections from DUNET. \( C \) is defined as a stack of layer sequences, and each sequence contains a \( 3 \times 3 \) convolution, a batch normalization layer [13] and a rectified linear unit. \( C_k \) is defined as \( k \) consecutive \( C \). The network is composed of a feedforward path and a feedback path. The feedforward path is composed of five blocks, corresponding to one \( C2 \) and four \( C3 \), respectively. The first convolution of each \( C3 \) has \( 2 \times 2 \) stride, while the stride of all other layers is \( 1 \times 1 \). The feedback path receives the image as input, and generates a set of feature maps of increasingly lower resolutions (see the top pathway of Figure 3).

The feedback path is composed of four blocks and a \( 1 \times 1 \) convolution. Each block receives a feedback input from the
feedback path and a lateral input from the feedforward path. It first upsamples the feedback input to the same size as the lateral input using bilinear interpolation, and then processes the concatenated feedback and lateral inputs with a $Ck$. From top to bottom, three $C3$ and one $C2$ are used. Along the feedback path, the resolution of feature maps is increasingly higher. The output of the last block is transformed to the negative noise $-d\hat{x}$ by a $1 \times 1$ convolution (See the bottom pathway of Figure 3). The final output is the sum of the negative noise and the input image:

$$\hat{x} = x^* - d\hat{x}. \quad (4)$$

### 3.2. High-level representation guided denoiser

A potential problem with PGD is the amplification effect of adversarial noise. Adversarial examples have negligible differences from the clean images. However, this small perturbation is progressively amplified by deep neural networks and yields a wrong prediction. Even if the denoiser can significantly suppress the pixel-level noise, the remaining noise may still distort the high-level responses of the target model. Refer to Section 5.1 for details.

To overcome this problem, we replace the pixel-level loss function with the reconstruction loss of the target model’s outputs. More specifically, given a target neural network, we extract its representations at $l$-th layer activated by $x$ and $\hat{x}$, and define the loss function as the $L_1$ norm of their difference:

$$L = ||f_l(\hat{x}) - f_l(x)||. \quad (5)$$

The corresponding model is called HGD, in that the supervised signal comes from certain high-level layers of the target model and carries guidance information related to image classification. HGD uses the same U-net structure as DUNET. They only differ in their loss functions.

We propose two HGDs with different choices of $l$. For the first HGD, we define $l = -2$ as the index of the topmost convolutional layer. The activations of this layer are fed to the linear classification layer after global average pooling, so it is more related to the classification objective than lower convolutional layers. This denoiser is called feature guided denoiser (FGD) (see Figure 4a). The loss function used by FGD is also known as perceptual loss or feature matching loss\cite{26, 14, 6}. For the second HGD, we define $l = -1$ as the index of the layer before the final softmax function, i.e., the logits. This denoiser is called logits guided denoiser (LGD). In this case, the loss function is the difference between the two logits activated by $\hat{x}$ and $x$ (see Figure 4b). We consider both FGD and LGD for the following reason. The convolutional feature maps provide richer supervised information, while the logits directly represent the classification results.

All PGD and these HGDs are unsupervised models, in that the ground truth labels are not needed in their training process. An alternative is to use the classification loss of the target model as the denoising loss function, which is supervised learning as ground truth labels are needed. This model is called class label guided denoiser (CGD) (see Figure 4c).

### 4. Experimental settings

Throughout experiments, the pretrained Inception v3 (IncV3)\cite{29} is assumed to be the target model that attempts to fool and our denoisers attempt to defend. Therefore this model is used for training the three HGDs illustrated in Figure 4. However, it will be seen that the HGDs trained with this target model can also defend other mod-
els (see Section 5.3). All our experiments are conducted on images from the ImageNet dataset. Although many defense methods have been proposed, they are mostly evaluated on small images and only adversarial training is thoroughly evaluated on ImageNet. We compare our model with ensemble adversarial training, which is the state-of-the-art defense method of defending large images.

4.1. Dataset

For both training and testing of the proposed method, adversarial images are needed. To prepare the training set, we first extract 30K images from the ImageNet training set (30 images per class). Then we use a bunch of adversarial attacking methods to distort these images and form a training set of adversarial images. Different attacking methods including FGSM and IFGSM are applied to the following models: Pre-trained IncV3, InceptionResnet v2 (IncResV2) [28], ResNet50 v2 (Res) [11] individually or in combinations (the same model ensemble as the work of Tramer et al. [31]). For each training sample, the perturbation level \( \epsilon \) is uniformly sampled from integers in \([1, 16]\). See Table 1 for details. As a consequence, we gather 210K images in the training set (TrainSet).

To prepare the validation set, we first extract 10K images from the ImageNet training set (10 images per class), then apply the same method as described above. Therefore the size of the validation set (ValSet) is 70K.

Two different test sets are constructed, one for white-box attacks (WhiteTestSet)\(^2\) and the other for black-box attacks (BlackTestSet). They are obtained from the same clean 10K images from the ImageNet validation set (10 images per class) but using different attacking methods. The WhiteTestSet uses two attacks targeting at IncV3, which is also used for generating training images, and the BlackTestSet uses two attacks based on a holdout model pre-trained Inception V4 (IncV4) [28], which is not used for generating training images. Every attacking method is conducted on two perturbation levels \( \epsilon \in \{4, 16\} \). So both WhiteTestSet and BlackTestSet have 40k images (see Table 1 for details).

4.2. Implementation details

The denoisers are optimized using Adam [15]. The learning rate is initially set to 0.001, and decay to 0.0001 when the training loss converges. The model is trained on six GPUs and the batch size is 60. The number of training epochs ranges from 20 to 30, depending on the convergence speed of the model. The model with the lowest validation loss is used for testing.

5. Results

5.1. PGD and the error amplification effect

The results of DAE and DUNET on the test sets are shown in Table 2. The original IncV3 without any defense is used as a baseline, denoted as NA. For all types of attacks, DUNET has much lower denoising loss than DAE and NA, which demonstrates the structural advantage

<table>
<thead>
<tr>
<th>Attacking method</th>
<th>Attacked model</th>
<th>( \epsilon )</th>
</tr>
</thead>
<tbody>
<tr>
<td>FGSM</td>
<td>IncV3</td>
<td></td>
</tr>
<tr>
<td>FGSM</td>
<td>IncResV2</td>
<td></td>
</tr>
<tr>
<td>FGSM</td>
<td>Res</td>
<td></td>
</tr>
<tr>
<td>FGSM</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>FGSM</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>FGSM</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>FGSM</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>IFGSM2</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>IFGSM3</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>IFGSM5</td>
<td>IncV3/IncResV2/Res</td>
<td>[1, 16]</td>
</tr>
<tr>
<td>WhiteTestSet</td>
<td>FGSM</td>
<td>{4, 16}</td>
</tr>
<tr>
<td>WhiteTestSet</td>
<td>IFGSM4</td>
<td>{4, 16}</td>
</tr>
<tr>
<td>BlackTestSet</td>
<td>FGSM</td>
<td>{4, 16}</td>
</tr>
<tr>
<td>BlackTestSet</td>
<td>IFGSM4</td>
<td>{4, 16}</td>
</tr>
</tbody>
</table>

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\( ^2\)The white-box attacks defined in this paper should be called oblivious attacks according to Carlini and Wagner’s definition [3].

\(^3\)For detailed results of each attack in Table 2-5, please refer to the supplementary material.
Table 2: Denosing loss and classification accuracy of different PGD methods on the test sets. Denosing loss is the $L_1$ distance between the input image and the denoised image. NA means no defense. Clean stands for original images.

<table>
<thead>
<tr>
<th>Defense</th>
<th>Clean</th>
<th>WhiteTestSet $\epsilon = 4$</th>
<th>WhiteTestSet $\epsilon = 16$</th>
<th>BlackTestSet $\epsilon = 4$</th>
<th>BlackTestSet $\epsilon = 16$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NA</td>
<td>0.0000</td>
<td>0.0177</td>
<td>0.0437</td>
<td>0.0176</td>
<td>0.0451</td>
</tr>
<tr>
<td>DAE</td>
<td>0.0360</td>
<td>0.0359</td>
<td>0.0360</td>
<td>0.0360</td>
<td>0.0369</td>
</tr>
<tr>
<td>DUNET</td>
<td>0.0150</td>
<td>0.0140</td>
<td>0.0164</td>
<td>0.0140</td>
<td>0.0181</td>
</tr>
</tbody>
</table>

Table 3: The classification accuracy on test sets obtained by different defenses. NA means no defense.

<table>
<thead>
<tr>
<th>Defense</th>
<th>Clean</th>
<th>WhiteTestSet $\epsilon = 4$</th>
<th>WhiteTestSet $\epsilon = 16$</th>
<th>BlackTestSet $\epsilon = 4$</th>
<th>BlackTestSet $\epsilon = 16$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NA</td>
<td>76.7%</td>
<td>14.5%</td>
<td>14.4%</td>
<td>61.2%</td>
<td>41.0%</td>
</tr>
<tr>
<td>PGD</td>
<td>75.3%</td>
<td>20.0%</td>
<td>13.8%</td>
<td>67.5%</td>
<td>55.7%</td>
</tr>
<tr>
<td>ensV3 $^{[31]}$</td>
<td>76.9%</td>
<td>69.8%</td>
<td>58.0%</td>
<td>72.4%</td>
<td>62.0%</td>
</tr>
<tr>
<td>FGD</td>
<td>76.1%</td>
<td>73.7%</td>
<td>67.4%</td>
<td>74.3%</td>
<td>71.8%</td>
</tr>
<tr>
<td>LGD</td>
<td>76.2%</td>
<td>75.2%</td>
<td>69.2%</td>
<td>75.1%</td>
<td>72.2%</td>
</tr>
<tr>
<td>CGD</td>
<td>74.9%</td>
<td>75.8%</td>
<td>73.2%</td>
<td>74.5%</td>
<td>71.1%</td>
</tr>
</tbody>
</table>

Figure 5: Layerwise perturbation levels of the target model. Adversarial, Random noise, PGD and LGD correspond to the $E_l$ for adversarial images, Gaussian noise perturbed images, PGD denoised images, and LGD denoised images, respectively.

of DUNET. DAE does not perform well on encoding the high-resolution images, as its accuracy on clean images significantly drops. DUNET slightly decreases the accuracy of clean images, but significantly improves the robustness of the target model to black-box attacks. In what follows, DUNET is used as the default PGD method.

A notable result is that the denoising loss and classification accuracy of PGD are not so consistent. For white-box attacks, DUNET has much lower denoising loss than DAE, but its classification accuracy is significantly worse. To investigate this inconsistency, we analyze the layer-wise perturbations of the target model activated by PGD denoised images. Let $x_p$ denote a perturbed image. The perturbation level at layer $l$ is computed as:

$$E_l(x_p, x) = \frac{||f_l(x_p) - f_l(x)||}{||f_l(x)||}.$$  

The $E_l$ for PGD denoised images, adversarial images, and Gaussian noise perturbed images are shown in Figure 5. The latter two are used as baselines. The curves are the averaged results on 30 randomly picked adversarial images generated by the ensemble attack "IFGSM4 x IncV3/IncResV2/Res ($\epsilon = 16$)". For convenience, these $E_l$ are abbreviated as PGD perturbation, adversarial perturbation, and random perturbation. Although the pixel-level PGD perturbation significantly suppressed, the remaining perturbation is progressively amplified along the layer hierarchy. At the top layer, PGD perturbation is much higher than random perturbation and close to adversarial perturbation. Because the classification result is closely related to the top-level features, this large perturbation well explains the inconsistency between the denoising performance and classification accuracy of PGD.

5.2. Evaluation results of HGD

Compared to PGD, LGD strongly suppress the error amplification effect (Figure 5). LGD perturbation at the final layer is much lower than PGD and adversarial perturbations and close to random perturbation.

HGD is more robust to white-box and black-box adversarial attacks than PGD and ensV3 (Table 3). All three HGD methods significantly outperform PGD and ensV3 for all types of attacks. The accuracy of clean images only slightly decreases (by 0.5% for LGD). The difference between these HGD methods is insignificant. In later sections, LGD is chosen as our default HGD method for it achieves a good balance between accuracy on clean and adversarial images. When facing powerful ensemble black-box attacks, LGD also significantly outperforms ensV3 (see supplementary material).

Compared to adversarial training, HGD only uses a small fraction of training images and is efficient to train. Only 30K clean images are used to construct our training set, while all 1.2M clean images of the ImageNet dataset are used for training ensV3. HGD is trained for less than 30 epochs on 210K adversarial images, while ensV3 is trained for about 200 epochs on 1.2M images $^{[31]}$.

To summary, with less training data and time, HGD significantly outperforms adversarial training on defense against adversarial attacks. These results suggest that learning to denoise only is much easier than learning the coupled task of classification and defense.
5.3. Transferability of HGD

The learning objective of HGD is to remove the high-level influence of adversarial noises. In other words, HGD works by producing anti-adversarial perturbations on input images. From this point of view, we expect that HGD can be transferred to defend other models and images.

To evaluate the transferability of HGD over different models, we use the IncV3 guided LGD to defend Resnet. As expected, this LGD significantly improves the robustness of Resnet to all attacks. Furthermore, it achieves very close defending performance as the Resnet guided LGD. (Table 4)

To evaluate the transferability of HGD over different classes, we build another dataset. Its key difference from the original dataset is that there are only 750 classes in the TrainSet, and the other 250 classes are put in ValSet and TestSets. The number of original images in each class in all datasets are changed to 40 to keep the size of dataset unchanged. It is found that although the 250 classes in the test set are never trained, the LGD still learns to defend against the attacks targeting at them (Table 5).

5.4. HGD as an anti-adversarial transformer

HGD is derived from a denoising motivation. However, HGD denoised images have larger pixel-level noise than adversarial images (see Figure 5), indicating that HGD even elevates the overall noise level. This is also confirmed by the qualitative result in Figure 6. LGD does not suppress the total noise as PGD does, but adds more perturbations to the image.

To further investigate this issue, we plot the 2D histogram of the adversarial perturbation ($dx^* = x^* - x$) and the predicted perturbation ($d\hat{x} = x^* - \hat{x}$) by PGD and LGD (Figure 7), where $x$, $x^*$ and $\hat{x}$ denote the clean, adversarial and denoised images, respectively. The ideal result should be $d\hat{x} = dx^*$, which means the adversarial perturbations are completely removed.

Two lines $d\hat{x} = kdx^*$ are fit for PGD and LGD, respectively (the red lines in Figure 7). The slope of PGD’s line is lower than 1, indicating that PGD only removes a portion of the adversarial noises. In contrast, the slope of LGD’s line is even larger than 1. Moreover, the estimation is very noisy, which leads to high pixel-level noise.

These observations suggest that HGD defends the target model by two mechanisms. First, HGD indeed reduces the adversarial noise level, which is revealed by the strong correlation between adversarial noise $dx^*$ and HGD induced perturbation $d\hat{x}$ (Figure 7). Second, HGD adds to the image some favorable perturbation which defends the target model. In this sense, HGD can also be seen as an anti-adversarial transformer, which does not necessarily remove all the pixel-level noises but transforms the adversarial example to some easy-to-classify example.

5.5. Results in NIPS adversarial defenses competition

In NIPS 2017 competition track, Google Brain organized competition on adversarial attacks and defenses. The dataset used in this competition contains 5000 ImageNet-compatible clean images unknown to the teams. In the defenses competition, each team submits one solution, which are then evaluated on the attacks submitted by all teams. In total there are 91 non-targeted attacks and 65 targeted attacks. The evaluation is conducted on the cloud by organizers, and a normalized score is calculated based on the accuracy on all attacks.

We used a FGD based solution. To train FGD, we gathered 14 kinds of attacks, all with $\epsilon = 16$. Most of them were iterative attacks on an ensemble of many models (for details, please refer to supplementary file). We chose four pre-trained models (ensV3[31], ensIncResV2[31], Resnet152[10], ResNetX101[33]) and trained a FGD for each one. The logits output of the four defended models were averaged, and the class with the highest score was chosen as the classification result.

Our solution won the first place among 107 teams and significantly outperformed other methods (Table 6). Moreover, our model is much faster than the other top methods, measured by average evaluation time.

6. Conclusion

In this study, we discovered the error amplification effect of adversarial examples in neural networks and proposed to use the error in the top layers of the neural network as loss.

Table 4: The transferability of HGD to different model. Resnet is used as the target model.

<table>
<thead>
<tr>
<th>Denoiser for Resnet</th>
<th>Clean</th>
<th>WhiteTestSet $\epsilon = 4$</th>
<th>WhiteTestSet $\epsilon = 16$</th>
<th>BlackTestSet $\epsilon = 4$</th>
<th>BlackTestSet $\epsilon = 16$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NA</td>
<td>78.5%</td>
<td>63.3%</td>
<td>38.4%</td>
<td>67.8%</td>
<td>48.6%</td>
</tr>
<tr>
<td>IncV3 guided LGD</td>
<td>77.4%</td>
<td>75.8%</td>
<td>71.7%</td>
<td>76.1%</td>
<td>72.7%</td>
</tr>
<tr>
<td>Resnet guided LGD</td>
<td>78.4%</td>
<td>76.1%</td>
<td>72.9%</td>
<td>76.5%</td>
<td>74.6%</td>
</tr>
</tbody>
</table>

Table 5: The transferability of HGD to different classes. The 1000 ImageNet classes are separated in training and test test.

<table>
<thead>
<tr>
<th>Defense</th>
<th>Clean</th>
<th>WhiteTestSet $\epsilon = 4$</th>
<th>WhiteTestSet $\epsilon = 16$</th>
<th>BlackTestSet $\epsilon = 4$</th>
<th>BlackTestSet $\epsilon = 16$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NA</td>
<td>76.6%</td>
<td>15.4%</td>
<td>15.3%</td>
<td>61.5%</td>
<td>41.7%</td>
</tr>
<tr>
<td>LGD</td>
<td>76.3%</td>
<td>73.9%</td>
<td>65.7%</td>
<td>74.8%</td>
<td>72.2%</td>
</tr>
</tbody>
</table>
functions to guide the training of an image denoiser. This method turned to be very robust against both white-box and black-box attacks. The proposed HGD has simple training procedure, good generalization, and high flexibility.

In future work, we aim to build an optimal set of training attacks. The denoising ability of HGD depends on the representability of the training set. In current experiments, we used FGSM and iterative attacks. Incorporating other different attacks, such as the attacks generated by adversarial transformation networks, probably improves the performance of HGD. It is also possible to explore an end-to-end training approach, in which the attacks are generated online by another neural network.

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