Supplementary materials for "Patch SVDD: Patch-level SVDD for Anomaly Detection and Segmentation"

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S1 Pseudo code

A	lgorithm	1	Patch	1 SVDD	(train))
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1: Input normal images $\{\mathbf{x}\}$, hyperparameter λ , encoder f_{θ} , and classifier C_{ϕ} 2: for patch \mathbf{p} in $\{\mathbf{x}\}$ do \triangleright Train the encoder $\mathbf{p}_1 \leftarrow \texttt{RandomJitter}(\mathbf{p})$ 3: 4: $\mathcal{L}_{\text{SVDD}} \leftarrow \|f_{\theta}(\mathbf{p}) - f_{\theta}(\mathbf{p}_1)\|_2$ 5: $\mathbf{p}_2, y \leftarrow \texttt{RandomNeighborhood}(\mathbf{p})$ \triangleright A neighborhood in the 3 \times 3 grid 6: $\mathcal{L}_{SSL} \leftarrow \texttt{Cross-entropy}\left(y, C_{\phi}\left(f_{\theta}(\mathbf{p}), f_{\theta}(\mathbf{p}_{2})\right)\right)$ 7: Backprop $\mathcal{L}_{Patch SVDD} \leftarrow \lambda \mathcal{L}_{SVDD'} + \mathcal{L}_{SSL}$ 8: end for \triangleright Split encoders 9: $f_{\text{big}}, f_{\text{small}} \leftarrow f_{\theta}$ \triangleright Sets of normal features 10: $S_{\text{big}}, S_{\text{small}} \leftarrow \emptyset$ 11: for patch \mathbf{p} in $\{\mathbf{x}\}$ do \triangleright Patch size K with stride S $S_{\text{big}} \leftarrow S_{\text{big}} \cup \{f_{\text{big}}(\mathbf{p})\}$ 12:13: end for 14: for patch \mathbf{p} in $\{\mathbf{x}\}$ do \triangleright Patch size K with stride S 15: $S_{\text{small}} \leftarrow S_{\text{small}} \cup \{f_{\text{small}}(\mathbf{p})\}$ 16: end for 17: return $(S_{\text{big}}, S_{\text{small}}), (f_{\text{big}}, f_{\text{small}})$ \triangleright Normal features and trained encoders

Algorithm 1 trains a hierarchical encoder using $\mathcal{L}_{\text{Patch SVDD}}$. After the training, sets of features of normal patches are extracted using the trained multi-scale encoders. The outputs of Algorithm 1 are the sets of normal features and trained encoders. Algorithm 2 performs inspection on a query image and outputs the anomaly map and anomaly score.

Algorithm 2 Patch SVDD (test)

1:	: Input query image x, normal feature sets $(S_{\text{big}}, S_{\text{small}})$, and encoders $(f_{\text{big}}, f_{\text{small}})$			
2:	Initialize \mathcal{M}_{big} and $\mathcal{M}_{\text{small}}$			
3:	for patch \mathbf{p} in \mathbf{x} do	\triangleright Patch size K with stride S		
4:	$d \leftarrow \min_{h \in S_{\text{big}}} \ f_{\text{big}}(\mathbf{p}) - h\ _2$	\triangleright Anomaly score of a patch		
5:	Distribute d to \mathcal{M}_{big} of each pixel in \mathbf{p}			
6:	end for			
7:	for patch \mathbf{p} in \mathbf{x} do	\triangleright Patch size K with stride S		
8:	$d \leftarrow \min_{h \in S_{\text{small}}} \ f_{\text{small}}(\mathbf{p}) - h\ _2$	\triangleright Anomaly score of a patch		
9:	Distribute d to $\mathcal{M}_{\text{small}}$ of each pixel in \mathbf{p}			
10:	end for			
11:	$\mathcal{M}_{ ext{multi}} \leftarrow \mathcal{M}_{ ext{small}} \odot \mathcal{M}_{ ext{big}}$	\triangleright Element-wise multiplication		
12:	$a \leftarrow \max \mathcal{M}_{\text{multi}}$	\triangleright Anomaly score		
13:	return $\mathcal{M}_{\text{multi}}, a$	\triangleright Anomaly map and anomaly score		

S2 Results

S2.1 Numerical results

Table S1: Anomaly detection (Det.) and segmentation performances (Seg.) of proposed Patch SVDD on MVTec AD [1] dataset. The inspection performances for each class are given in AUROC, and the average values are also reported in Table 1 of the main paper.

	Patch SVDD		
Classes	Det.	Seg.	
bottle	0.986	0.981	
cable	0.903	0.968	
capsule	0.767	0.958	
carpet	0.929	0.926	
grid	0.946	0.962	
hazelnut	0.920	0.975	
leather	0.909	0.974	
$metal_nut$	0.940	0.980	
pill	0.861	0.951	
screw	0.813	0.957	
tile	0.978	0.914	
toothbrush	1.000	0.981	
transistor	0.915	0.970	
wood	0.965	0.908	
zipper	0.979	0.951	
Average	0.921	0.957	

Table S2: **The effect of hierarchical encoding.** Aggregating the results from multi-scale inspection boosts the performance, and adopting hierarchical structure to the encoder is helpful as well. The plot of the data is provided in Fig. 12 of the main paper.

Hierarchical	K	Det.	Seg.
×	64	0.810	0.879
 Image: A second s	64	0.894	0.932
✓	32	0.902	0.957
<u> </u>	Agg. (64 & 32)	0.921	0.957

S2.2 Anomaly maps



Fig. S1: Anomaly maps generated by the proposed method. Patch SVDD generates anomaly maps of the images in each class of MVTec AD [1] dataset. The ground truth defect annotations are depicted as red contours in the image, and the darker heatmap indicates higher anomaly scores. The name of the class is provided at the left of the image, and the type of the defect is indicated below the image.



Fig. S2: Anomaly maps generated by the proposed method. Patch SVDD generates anomaly maps of the images in each class of MVTec AD [1] dataset. The ground truth defect annotations are depicted as red contours in the image, and the darker heatmap indicates higher anomaly scores. The name of the class is provided at the left of the image, and the type of the defect is indicated below the image.



Fig. S3: Anomaly maps generated by the proposed method. Patch SVDD generates anomaly maps of the images in each class of MVTec AD [1] dataset. The ground truth defect annotations are depicted as red contours in the image, and the darker heatmap indicates higher anomaly scores. The name of the class is provided at the left of the image, and the type of the defect is indicated below the image.

S3 Implementation details

S3.1 Dataset

The dataset in the study, MVTec AD [1], consists of 15-class industrial images. Each class is categorized as either an $object^1$ or $texture^2$. Each class contains 60 to 390 normal train images and 40 to 167 test images. Test images include both normal and abnormal examples, and the defects of the abnormal images are annotated at the pixel level in the form of binary masks. We downsampled every image to a resolution of 256×256 . Gray-scale images are converted to RGB images by replicating the single channel to three. No data augmentation method (e.g., horizontal flip, rotation) was used for the training.

S3.2 Networks

Two neural networks are used throughout the study: an encoder and a classifier. The encoder is composed of convolutional layers only. The classifier is a twolayered MLP model having 128 hidden units per layer, and the input to the classifier is a subtraction of the features of the two patches. The activation function for both networks is a LeakyReLU [2] with a $\alpha = 0.1$. Please refer to the code³ for the detailed architecture of the networks.

As proposed in Section 3.3 of the main paper, the encoder has a hierarchical structure. The receptive field of the encoder is K = 64, and that of the embedded smaller encoder is K = 32. Patch SVDD divides the images into patches with a size K and a stride S. The values for the strides are S = 16 and S = 4 for the encoders with K = 64 and K = 32, respectively.

S3.3 Environments

The experiments throughout the study were conducted on a machine equipped with an Intel i7-5930K CPU and an NVIDIA GeForce RTX 2080 Ti GPU. The code is implemented in python 3.7 and PyTorch [3].

References

- 1. Bergmann, P., Fauser, M., Sattlegger, D., Steger, C.: Mvtec ad–a comprehensive real-world dataset for unsupervised anomaly detection. In: CVPR. (2019)
- 2. Maas, A.L., Hannun, A.Y., Ng, A.Y.: Rectifier nonlinearities improve neural network acoustic models. In: ICML. (2013)
- Paszke, A., Gross, S., Chintala, S., Chanan, G., Yang, E., DeVito, Z., Lin, Z., Desmaison, A., Antiga, L., Lerer, A.: Automatic differentiation in pytorch. (2017)

¹ bottle, cable, capsule, hazelnut, metal_nut, pill, screw, toothbrush, transistor, and zipper

 $^{^{2}}$ carpet, grid, leather, tile, and wood

³ https://github.com/nuclearboy95/Anomaly-Detection-PatchSVDD-PyTorch