Wavelet-based Mamba with Fourier Adjustment for Low-light Image Enhancement (Supplementary Materials)

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1 Additional Ablation Studies

1.1 Width and Depth Ablation.

The width and depth of the model refer to embedding dimension and the number of iterations for each stage module, respectively. $[D_1]$, $[D_2]$, $[D_3]$ respectively indicates number of iterations for the WMB. The depth of [2, 3, 4] used for WalMaFa achieves the best performance as well as fewer parameters.

Why larger models seem to perform worst? LOL-v1 dataset only consists of 485 train images and 15 test images, which inevitably leads to overfitting. Besides, we speculate that the deeper model will greatly overfit the global brightness due to D_1 , D_2 , D_3 indicating the number of iteration for WMB in the encoder-decoder, which will undermine the global and local balance.

1.2 Why Encoder-Latent-Decoder?

In this work, Encoder mainly aims at the coarse-grained global multi-scale brightness extraction (thanks to the low-frequency component of the WMB). Then, Latent fine-tines the fine-grained local details (thanks to the Phase component of the FFAB). However, we found that this coarse-to-fine pipeline exists a local overexposure problem (i.e., color distortion) caused by local texture smoothing, as shown in Figure [1.](#page-1-0) So the extra coarse-grained Decoder is adopted to further balance the global brightness.

Code is available at:<https://github.com/mcpaulgeorge/WalMaFa>

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$W D_1 D_2 D_3 $ Params (M) PSNR/SSIM									
16 ¹				8.92	22.15/0.825				
16	$\overline{2}$	3		11.09	23.27/0.851				
16	4			12.49	22.60/0.831				
16	4			20.16	22.99/0.850				
32	$\overline{2}$	3		41.86	22.12/0.842				

Table 1: Width and depth ablation on LOL-v1 dataset.

Fig. 1: The visual comparisons with coarse-to-fine pipeline.

Model	LOLv1	LOLv2-real LOLv2-syn $ Flops(G) $		
Unet		$21.18/0.833$ $20.80/0.821$ $23.18/0.898$		11.94
Unet-skip-connection	$21.92/0.825$ $21.85/0.812$ $23.76/0.925$			4.24
Channel-wise Self-Attention Simplified Channel Attention	21.71/0.832 22.16/0.843	22.02/0.851 22.32/0.863	24.61/0.927 25.02/0.935	6.52 5.39
Ours	$\left 23.27/0.851\right 22.49/0.869\left 25.56/0.945\right $			14.41

Table 2: Structure ablation on LOL datasets.

1.3 Supplementary Structure Abaltion.

As shown in Table [2,](#page-1-1) we have experimented the Unet (Encoder with WMB and Decoder with FFAB) to verify the efficiency of Encoder-Latent-Decoder. We replace SSM with Unet-skip-connection between Encoder and Decoder to verify the efficiency of SSM. We also replace Channel-wise Mamba with Channel-wise Self-Attention (Restormer [\[2\]](#page-2-0)) and Simplified Channel Attention (NAFNet [\[1\]](#page-1-2)) to verify the efficiency of Channel-wise Mamba.

References

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