

# clDice - a Novel Topology-Preserving Loss Function for Tubular Structure Segmentation

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## Abstract

Accurate segmentation of tubular, network-like structures, such as vessels, neurons, or roads, is relevant to many fields of research. For such structures, the topology is their most important characteristic; particularly preserving connectedness: in the case of vascular networks, missing a connected vessel entirely alters the blood-flow dynamics. We introduce a novel similarity measure termed center-lineDice (short clDice), which is calculated on the intersection of the segmentation masks and their (morphological) skeleta. We theoretically prove that clDice guarantees topology preservation up to homotopy equivalence for binary 2D and 3D segmentation. Extending this, we propose a computationally efficient, differentiable loss function (soft-clDice) for training arbitrary neural segmentation networks. We benchmark the soft-clDice loss on five public datasets, including vessels, roads and neurons (2D and 3D). Training on soft-clDice leads to segmentation with more accurate connectivity information, higher graph similarity, and better volumetric scores.

## 1. Introduction

Segmentation of *tubular* and *curvilinear* structures is an essential problem in numerous domains, such as clinical and biological applications (blood vessel and neuron segmentation from microscopic, optoacoustic, or radiology images), remote sensing applications (road network segmentation from satellite images) and industrial quality control, etc. In the aforementioned domains, a topologically accurate segmentation is necessary to guarantee error-free downstream tasks, such as computational hemodynamics, route planning, Alzheimer’s disease prediction [18], or stroke modeling [20]. When optimizing computational algorithms for segmenting curvilinear structures, the two most commonly used categories of quantitative performance measures for evaluating segmentation accuracy of *tubular* struc-

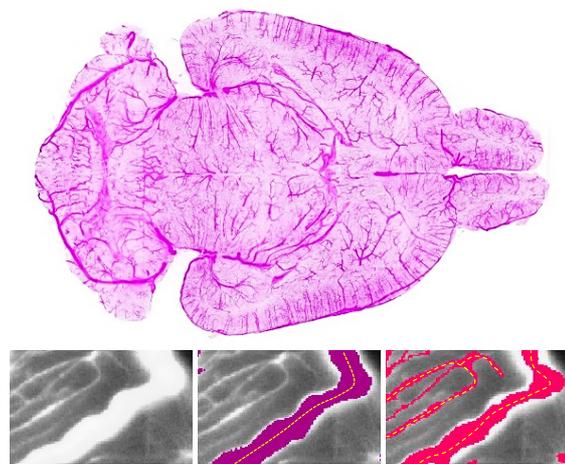


Figure 1. **Motivation:** The figure shows a 3D rendering of a complex, whole brain vascular dataset [48], where an exemplary 2D slice of the data is chosen and segmented by two different models, see purple (middle) and red (right), respectively. The two segmentation results achieve identical quality in terms of the traditional Dice score. Note that the purple segmentation does not capture the small vessels while segmenting the large vessel very accurately; on the other side, the red segmentation captures all vessels in the image while being less accurate on the radius of the large vessel. Skeleta are drawn in yellow. From a topology or network perspective, the red segmentation is evidently preferred.

tures, are 1) overlap based measures such as Dice, precision, recall, and Jaccard index; and 2) volumetric distance measures such as the Hausdorff and Mahalanobis distance [21, 40, 36, 16].

However, in most segmentation problems, where the object of interest is 1) locally a *tubular* structure and 2) globally forms a *network*, the most important characteristic is the connectivity of the global network topology. Note that *network* in this context implies a physically connected structure, such as a vessel network, a road network, etc., which is also the primary structure of interest for the given

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image data. As an example, one can refer to brain vasculature analysis, where a missed vessel segment in the segmentation mask can pathologically be interpreted as a stroke or may lead to dramatic changes in a global simulation of blood flow. On the other hand, limited over- or under-segmentation of vessel radius can be tolerated, because it does not affect clinical diagnosis.

For evaluating segmentations in such tubular-network structures, traditional volume-based performance indices are sub-optimal. For example, Dice and Jaccard rely on the average voxel-wise hit or miss prediction [46]. In a task like network-topology extraction, a spatially contiguous sequence of correct voxel prediction is more meaningful than a spurious correct prediction. This ambiguity is relevant for objects of interest, which are of the same thickness as the resolution of the signal. For them, it is evident that a single-voxel shift in the prediction can change the topology of the whole network. Further, a globally averaged metric does not equally weight tubular-structures with large, medium, and small radii (cf. Fig 1). In real vessel datasets, where vessels of wide radius ranges exist, e.g.  $30\ \mu\text{m}$  for arterioles and  $5\ \mu\text{m}$  for capillaries [48, 9], training on a globally averaged loss induces a strong bias towards the volumetric segmentation of large vessels. Both scenarios are pronounced in imaging modalities, such as fluorescence microscopy [48, 58] and optoacoustics, which focus on mapping small capillary structures.

To this end, we are interested in a topology-aware image segmentation, eventually enabling a correct network extraction. Therefore, we ask the following research questions:

- Q1. What is a good pixelwise measure to benchmark segmentation algorithms for **tubular**, and related linear and curvilinear structure segmentation while guaranteeing the preservation of the **network-topology**?
- Q2. Can we use this *improved measure* as a loss function for neural networks, which is a void in existing literature?

### 1.1. Related Literature

Achieving topology preservation can be crucial to obtain meaningful segmentation, particularly for elongated and connected shapes, e.g. vascular structures or roads. However, analyzing preservation of topology while simplifying geometries is a difficult analytical and computational problem [11, 10].

For binary geometries, various algorithms based on thinning and medial surfaces have been proven to be topology-preserving according to varying definitions of topology [23, 25, 26, 35]. For non-binary geometries, existing methods applied topology and connectivity constraints onto variational and Markov random field-based methods: tree shape priors for vessel segmentation [44], graph representation

priors to natural images [2], higher-order cliques which connect superpixels [53] and adversarial learning for road segmentation [51], integer programming to general curvilinear structures [49], and proposed a tree-structured convolutional gated recurrent unit [22], morphological optimization [14], among others [3, 15, 32, 31, 33, 37, 41, 52, 57, 56]. Further, topological priors of containment were applied to histology scans [5], a 3D CNN with graph refinement was used to improve airway connectivity [19], and recently, Mosinska et al. trained networks which perform segmentation and path classification simultaneously [30]. Another approach enables the predefinition of Betti numbers and enforces them on the training[8].

The aforementioned literature has advanced the communities understanding of topology-preservation, but critically, they do not possess end-to-end loss functions that optimize topology-preservation. In this context, the literature remains sparse. Recently, Mosinska et al. suggested that pixel-wise loss-functions are unsuitable and used selected filter responses from a VGG19 network as an additional penalty [29]. Nonetheless, their approach does not prove topology preservation. Importantly, Hu et al. proposed the first continuous-valued loss function based on the Betti number and persistent homology [17]. However, this method is based on matching critical points, which, according to the authors makes the training very expensive and error-prone for real image-sized patches [17]. While this is already limiting for a translation to large real world data set, we find that none of these approaches have been extended to three dimensional (3D) data.

### 1.2. Our Contributions

The objective of this paper is to identify an efficient, general, and intuitive loss function that enables topology preservation while segmenting tubular objects. We introduce a novel connectivity-aware similarity measure named *clDice* for benchmarking tubular-segmentation algorithms. Importantly, we provide theoretical guarantees for the topological correctness of the *clDice* for binary 2D and 3D segmentation. As a consequence of its formulation based on morphological skeletons, our measure pronounces the network's topology instead of equally weighting every voxel. Using a differentiable soft-skeletonization, we show that the *clDice* measure can be used to train neural networks. We show experimental results for various 2D and 3D network segmentation tasks to demonstrate the practical applicability of our proposed similarity measure and loss function.

## 2. Let's Emphasize *Connectivity*

We propose a novel connectivity-preserving metric to evaluate tubular and linear structure segmentation based on intersecting skeletons with masks. We call this metric *centerlineDice* or *clDice*.

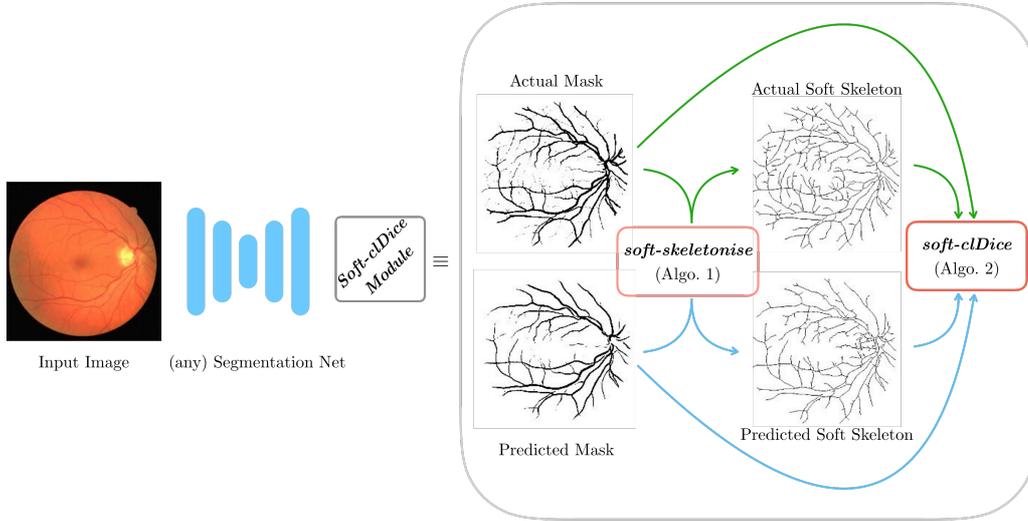


Figure 2. **Schematic overview of our proposed method:** Our proposed *clDice* loss can be applied to any arbitrary segmentation network. The soft-skeletonization can be easily implemented using pooling functions from any standard deep-learning toolbox.

We consider two binary masks: the ground truth mask ( $V_L$ ) and the predicted segmentation masks ( $V_P$ ). First, the skeletons  $S_P$  and  $S_L$  are extracted from  $V_P$  and  $V_L$  respectively. Subsequently, we compute the fraction of  $S_P$  that lies within  $V_L$ , which we call *Topology Precision* or  $T_{\text{prec}}(S_P, V_L)$ , and vice-a-versa we obtain *Topology Sensitivity* or  $T_{\text{sens}}(S_L, V_P)$  as defined below;

$$T_{\text{prec}}(S_P, V_L) = \frac{|S_P \cap V_L|}{|S_P|}; \quad T_{\text{sens}}(S_L, V_P) = \frac{|S_L \cap V_P|}{|S_L|} \quad (1)$$

We observe that the measure  $T_{\text{prec}}(S_P, V_L)$  is susceptible to false positives in the prediction while the measure  $T_{\text{sens}}(S_L, V_P)$  is susceptible to false negatives. This explains our rationale behind referring to the  $T_{\text{prec}}(S_P, V_L)$  as topology's precision and to the  $T_{\text{sens}}(S_L, V_P)$  as its sensitivity. Since we want to maximize both precision and sensitivity (recall), we define *clDice* to be the harmonic mean (also known as F1 or Dice) of both the measures:

$$\text{clDice}(V_P, V_L) = 2 \times \frac{T_{\text{prec}}(S_P, V_L) \times T_{\text{sens}}(S_L, V_P)}{T_{\text{prec}}(S_P, V_L) + T_{\text{sens}}(S_L, V_P)} \quad (2)$$

Note that our *clDice* formulation is not defined for  $T_{\text{prec}} = 0$  and  $T_{\text{sens}} = 0$ , but can easily be extended continuously with the value 0.

### 3. Topological Guarantees for *clDice*

The following section provides general theoretical guarantees for the preservation of topological properties

achieved by optimizing *clDice* under mild conditions on the input. Roughly, these conditions state that the object of interest is embedded in  $S^3$  in a non-knotted way, as is typically the case for blood vessel and road structures.

Specifically, we assume that both ground truth and prediction admit *foreground and background skeleta*, which means that both foreground and background are homotopy-equivalent to topological graphs, which we assume to be embedded as *skeleta*. Here, the voxel grid is considered as a cubical complex, consisting of elementary cubes of dimensions 0, 1, 2, and 3. This is a special case of a *cell complex* (specifically, a *CW complex*), which is a space constructed inductively, starting with isolated points (0-cells), and gluing a collection of topological balls of dimension  $k$  (called *k-cells*) along their boundary spheres to a  $k - 1$ -dimensional complex. The voxel grid, seen as a cell complex in this sense, can be completed to an ambient complex that is homeomorphic to the 3-sphere  $S^3$  by attaching a single exterior cell to the boundary. In order to consider foreground and background of a binary image as complementary subspaces, the foreground is now assumed to be the union of closed unit cubes in the voxel grid, corresponding to voxels with value 1; and the background is the complement in the ambient complex. This convention is commonly used in digital topology [24, 23]. The assumption on the background can then be replaced by a convenient equivalent condition, stating that the foreground is also homotopy equivalent to a subcomplex obtained from the ambient complex by only removing 3-cells and 2-cells. Such a subcomplex is then clearly homotopy-equivalent to the complement

of a 1-complex.

We will now observe that the above assumptions imply that the foreground and the background are connected and have a free fundamental group and vanishing higher fundamental groups. In particular, the homotopy type is already determined by the first Betti number <sup>1</sup>; moreover, a map inducing an isomorphism in homology is already a homotopy equivalence. To see this, first note that both foreground and background are assumed to have the homology of a graph, in particular, homology is trivial in degree 2. By Alexander duality [1], then, both foreground and background have trivial reduced cohomology in degree 0, meaning that they are connected. This implies that both have a free fundamental group (as any connected graph) and vanishing higher homotopy groups. In particular, since homology in degree 1 is the Abelianization of the fundamental group, these two groups are isomorphic. This in turn implies that in our setting a map that induces isomorphisms in homology already induces isomorphisms between all homotopy groups. By Whitehead’s theorem [54], such a map is then a homotopy equivalence.

The following theorem shows that under our assumptions on the images admitting foreground and background skeleta, the existence of certain nested inclusions already implies the homotopy-equivalence of foreground and background, which we refer to as *topology preservation*.

**Theorem 1.** *Let  $L_A \subseteq A \subseteq K_A$  and  $L_B \subseteq B \subseteq K_B$  be connected subcomplexes of some cell complex. Assume that the above inclusions are homotopy equivalences. If the subcomplexes also are related by inclusions  $L_A \subseteq B \subseteq K_A$  and  $L_B \subseteq A \subseteq K_B$ , then these inclusions must be homotopy equivalences as well. In particular,  $A$  and  $B$  are homotopy-equivalent.*

*Proof.* An inclusion of cell complexes map is a homotopy equivalence if and only if it induces isomorphisms on all homotopy groups. Since the inclusion  $L_A \subseteq B \subseteq K_A$  induces an isomorphism, the inclusion  $L_A \subseteq B$  induces a left-inverse, and since  $B \subseteq K_B$  induces an isomorphism, the inclusion  $L_A \subseteq K_B$  also induces a left-inverse. At the same time, since the inclusion  $L_B \subseteq A \subseteq K_B$  induces an isomorphism, the inclusion  $A \subseteq K_B$  induces a left-inverse, and since  $L_A \subseteq A$  induces an isomorphism, the inclusion  $L_A \subseteq K_B$  also induces a right-inverse. Together, this implies that the inclusion  $L_A \subseteq K_B$  induces an isomorphism.

Together with the isomorphisms induced by  $L_A \subseteq A$  and  $B \subseteq K_B$ , we obtain isomorphisms induced by  $L_A \subseteq B$  and by  $A \subseteq K_B$ , which compose to an isomorphism between the homotopy groups of  $A$  and  $B$ .  $\square$

<sup>1</sup>Betti numbers:  $\beta_0$  represents the number of distinct *connected components*,  $\beta_1$  represents the number of *circular holes*, and  $\beta_2$  represents the number of *cavities*, for depictions see Supplementary material

**Corollary 1.1.** *Let  $V_L$  and  $V_P$  be two binary masks admitting foreground and background skeleta, such that the foreground skeleton of  $V_L$  is included in the foreground of  $V_P$  and vice versa, and similarly for the background. Then the foregrounds of  $V_L$  and  $V_P$  are homotopy equivalent, and the same is true for their backgrounds.*

Note that the inclusion condition in this corollary is satisfied if and only if *clDice* evaluates to 1 on both foreground and background of  $(V_L, V_P)$ .

This proof lays the ground for a general interpretation of *clDice* as a topology preserving metric. Additionally, we provide an elaborate explanation of *clDice* topological properties, using concepts of applied digital topology in the theory section of the Supplementary material [24, 23].

## 4. Training Neural Networks with *clDice*

In the previous section we provided general theoretic guarantees how *clDice* has topology preserving properties. The following chapter shows how we applied our theory to efficiently train topology preserving networks using the *clDice* formulation. <sup>2</sup>

### 4.1. Soft-*clDice* using Soft-skeletonization:

Extracting accurate skeletons is essential to our method. For this task, a multitude of approaches has been proposed. However, most of them are not fully differentiable and therefore unsuited to be used in a loss function. Popular approaches use the Euclidean distance transform or utilize repeated morphological thinning. Euclidean distance transform has been used on multiple occasions [42, 55], but remains a discrete operation and, to the best of our knowledge, an end-to-end differentiable approximation remains to be developed, preventing the use in a loss function for training neural networks. On the contrary, morphological thinning is a sequence of dilation and erosion operations [c.f. Fig. 3].

Importantly, thinning using morphological operations (skeletonization) on curvilinear structures can be topology-preserving [35]. Min- and max filters are commonly used as the grey-scale alternative of morphological dilation and erosion. Motivated by this, we propose ‘soft-skeletonization’, where an iterative min- and max-pooling is applied as a proxy for morphological erosion and dilation. The Algorithm 1 describes the iterative processes involved in its computation. The hyper-parameter  $k$  involved in its computation represents the iterations and has to be greater than or equal to the maximum observed radius. In our experiments, this parameter depends on the dataset. For example, it is  $k = 5 \dots 25$  in our experiments, matching the pixel radius of the largest observed tubular structures. Choosing a larger  $k$  does not reduce performance but increases computation

<sup>2</sup><https://github.com/jocpae/clDice>

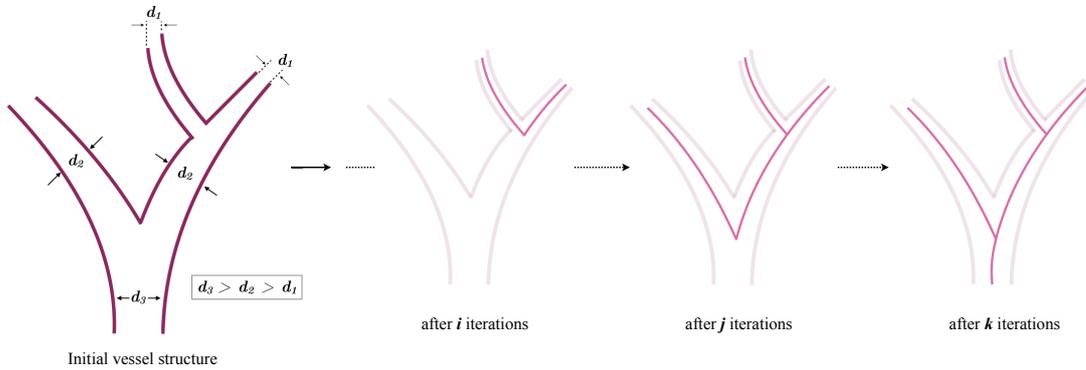


Figure 3. Based on the initial vessel structure (purple), sequential bagging of skeleton voxels (red) via iterative skeletonization leads to a complete skeletonization, where  $d$  denotes the diameter and  $k > j > i$  iterations.

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**Algorithm 1: *soft-skeleton***

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**Input:**  $I, k$   
 $I' \leftarrow \text{maxpool}(\text{minpool}(I))$   
 $S \leftarrow \text{ReLU}(I - I')$

**for**  $i \leftarrow 0$  **to**  $k$  **do**  
 $I \leftarrow \text{minpool}(I)$   
 $I' \leftarrow \text{maxpool}(\text{minpool}(I))$   
 $S \leftarrow S + (1 - S) \circ \text{ReLU}(I - I')$

**end**  
**Output:**  $S$

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**Algorithm 2: *soft-clDice***

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**Input:**  $V_P, V_L$   
 $S_P \leftarrow \text{soft-skeleton}(V_P)$   
 $S_L \leftarrow \text{soft-skeleton}(V_L)$   
 $T_{\text{prec}}(S_P, V_L) \leftarrow \frac{|S_P \circ V_L| + \epsilon}{|S_P| + \epsilon}$   
 $T_{\text{sens}}(S_L, V_P) \leftarrow \frac{|S_L \circ V_P| + \epsilon}{|S_L| + \epsilon}$   
 $\text{clDice} \leftarrow$   
 $2 \times \frac{T_{\text{prec}}(S_P, V_L) \times T_{\text{sens}}(S_L, V_P)}{T_{\text{prec}}(S_P, V_L) + T_{\text{sens}}(S_L, V_P)}$

**Output:**  $\text{clDice}$

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Figure 4. **Algorithm 1** calculates the proposed *soft-skeleton*, here  $I$  is the mask to be *soft-skeletonized* and  $k$  is the number of iterations for skeletonization. **Algorithm 2**, calculates the *soft-clDice* loss, where  $V_P$  is a real-valued probabilistic prediction from a segmentation network and  $V_L$  is the true mask. We denote Hadamard product using  $\circ$ .

time. On the other hand, a too low  $k$  leads to incomplete skeletonization.

In Figure 3, the successive steps of our skeletonization are intuitively represented. In the early iterations, the structures with a small radius are skeletonized and preserved until the later iterations when the thicker structures become skeletonized. This enables the extraction of a parameter-

free, morphologically motivated soft-skeleton. The aforementioned soft-skeletonization enables us to use *clDice* as a fully differentiable, real-valued, optimizable measure. The Algorithm 2 describes its implementation. We refer to this as the *soft-clDice*.

For a single connected foreground component and in the absence of knots, the homotopy type is specified by the number of linked loops. Hence, if the reference and the predicted volumes are not homotopy equivalent, they do not have pairwise linked loops. To include these missing loops or exclude the extra loops, one has to add or discard deformation retracted skeleta of the solid foreground. This implies adding *new correctly predicted voxels*. In contrast to other volumetric losses such as Dice, cross-entropy, etc., *clDice* only considers the deformation-retracted graphs of the solid foreground structure. Thus, we claim that *clDice* requires the least amount of *new correctly predicted voxels* to guarantee the homotopy equivalence. Along these lines, Dice or cross-entropy can only guarantee homotopy equivalence if every single voxel is segmented correctly. On the other hand, *clDice* can guarantee homotopy equivalence for a broader combinations of connected-voxels. Intuitively, this is a very much desirable property as it makes *clDice* robust towards outliers and noisy segmentation labels.

## 4.2. Cost Function

Since our objective here is to preserve topology while achieving accurate segmentations, and not to learn skeleta, we combine our proposed *soft-clDice* with *soft-Dice* in the following manner:

$$\mathcal{L}_c = (1 - \alpha)(1 - \text{softDice}) + \alpha(1 - \text{softclDice}) \quad (3)$$

where  $\alpha \in [0, 0.5]$ . In stark contrast to previous works, where segmentation and centerline prediction has been learned jointly as multi-task learning [50, 47], we are not interested in learning the centerline. We are interested in

learning a topology-preserving segmentation. Therefore, we restrict our experimental choice of alpha to  $\alpha \in [0, 0.5]$ . We test *clDice* on two state-of-the-art network architectures: i) a 2D and 3D U-Net[38, 6], and ii) a 2D and 3D fully connected networks (FCN) [47, 13]. As baselines, we use the same architectures trained using *soft-Dice* [27, 45].

### 4.3. Adaption for Highly Imbalanced Data

Our theory (Section 3), describes a two-class problem where *clDice* should be computed on both the foreground and the background channels. In our experiments, we show that for complex and highly imbalanced dataset it is sufficient to calculate the **clDice** loss on the underrepresented foreground class. We attribute this to the distinct properties of tubularness, sparsity of foreground and the lack of cavities (Betti number 2) in our data. An intuitive interpretation how these assumptions are valid in terms of digital topology can be found in the supplementary material.

## 5. Experiments

### 5.1. Datasets

We employ five public datasets for validating *clDice* and *soft-clDice* as a measure and an objective function, respectively. In 2D, we evaluate on the DRIVE retina dataset [43], the Massachusetts Roads dataset [28] and the CREMI neuron dataset [12]. In 3D, a synthetic vessel dataset with an added Gaussian noise term [39] and the Vessap dataset of multi-channel volumetric scans of brain vessels is used [48, 34]. For the Vessap dataset we train different models for one and two input channels. For all of the datasets, we perform three fold cross-validation and test on held-out, large, and highly-variant test sets. Details concerning the experimental setup can be found in the supplementary material.

### 5.2. Evaluation Metrics

We compare the performance of various experimental setups using three types of metrics: volumetric, topology-based, and graph-based.

1. Volumetric: We compute volumetric scores such as Dice coefficient, Accuracy, and the proposed *clDice*.
2. Topology-based: We calculate the mean of absolute Betti Errors for the Betti Numbers  $\beta_0$  and  $\beta_1$  and the mean absolute error of Euler characteristic,  $\chi = V - E + F$ , where  $V$ ,  $E$ , and  $F$  denotes number of vertices, edges, and faces.
3. Graph-based: we extract random patch-wise graphs for the 2D/3D images. We uniformly sample fixed number of points from the graph and compute the StreetmoverDistance (SMD) [4]. SMD captures a Wasserstein distance between two graphs. Additionally we compute the F1 score of junction-based metric [7].

### 5.3. Results and Discussion

We trained two segmentation architectures, a U-Net and an FCN, for the various loss functions in our experimental setup. As a baseline, we trained the networks using *soft-dice* and compared it with the ones trained using the proposed loss (Eq. 3), by varying  $\alpha$  from (0.1 to 0.5).

**Quantitative:** We observe that including *soft-clDice* in any proportion ( $\alpha > 0$ ) leads to improved topological, volumetric and graph similarity for all 2D and 3D datasets, see Table 1. We conclude that  $\alpha$  can be interpreted as a hyper parameter which can be tuned *per-dataset*. Intuitively, increasing the  $\alpha$  improves the *clDice* measure for most experiments. Most often, *clDice* is high or highest when the graph and topology based measures are high or highest, particularly the  $\beta_1$  Error, Streetmover distance and Opt-J F1 score; quantitatively indicating that topological properties are indeed represented in the *clDice* measure.

In spite of not optimizing for a high *soft-clDice* on the background class, all of our networks converge to superior segmentation results. This not only reinforces our assumptions on dataset-specific necessary conditions but also validates the practical applicability of our loss. Our findings hold for the different network architectures, for 2D or 3D, and for tubular or curvilinear structures, strongly indicating its generalizability to analogous binary segmentation tasks.

Observe that CREMI and the synthetic vessel dataset (see Supplementary material) appear to have the smallest increase in scores over the baseline. We attribute this to them being the least complex datasets in the collection, with CREMI having an almost uniform thickness of radii and the synthetic data having a high signal-to-noise ratio and insignificant illumination variation. More importantly, we observe larger improvements for all measures in case of the more complex Vessap and Roads data see Figure 5. In direct comparison to performance measures reported in two recent publications by Hu et al. and Mosinska et al. [17, 29], we find that our approach is on par or better in terms of Accuracy and Betti Error for the Roads and CREMI dataset. It is important to note that we used a smaller subset of training data for the Road dataset compared to both while using the same test set.

Hu et al. reported a Betti error for the DRIVE data, which exceeds ours; however, it is important to consider that their approach explicitly minimizes the mismatch of the persistence diagram, which has significantly higher computational complexity during training, see the section below. We find that our proposed loss performs superior to the baseline in almost every scenario. The improvement appears to be pronounced when evaluating the highly relevant graph and topology based measures, including the recently

Table 1. Quantitative experimental results for the Massachusetts road dataset (Roads), the CREMI dataset, the DRIVE retina dataset and the Vessap dataset (3D). Bold numbers indicate the best performance. The performance according to the  $clDice$  measure is highlighted in rose. For all experiments we observe that using  $soft-clDice$  in  $\mathcal{L}_c$  results in improved scores compared to  $soft-Dice$ . This improvement holds for almost  $\alpha > 0$ ;  $\alpha$  can be interpreted as a dataset specific hyper-parameter.

| Dataset      | Network         | Loss                          | Dice         | Accuracy     | $clDice$     | $\beta_0$ Error | $\beta_1$ Error | SMD [4]        | $\chi_{error}$ | Opt-J F1 [7] |
|--------------|-----------------|-------------------------------|--------------|--------------|--------------|-----------------|-----------------|----------------|----------------|--------------|
| Roads        | FCN             | <i>soft-dice</i>              | 64.84        | 95.16        | 70.79        | 1.474           | 1.408           | 0.1216         | 2.634          | 0.766        |
|              |                 | $\mathcal{L}_c, \alpha = 0.1$ | 66.52        | 95.70        | 74.80        | 0.987           | 1.227           | 0.1002         | 2.625          | 0.768        |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | <b>67.42</b> | <b>95.80</b> | 76.25        | <b>0.920</b>    | 1.280           | <b>0.0954</b>  | 2.526          | 0.770        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | 65.90        | 95.35        | 74.86        | 0.974           | 1.197           | 0.1003         | 2.448          | 0.775        |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | 67.18        | 95.46        | <b>76.92</b> | 0.934           | <b>1.092</b>    | 0.0991         | <b>2.183</b>   | <b>0.803</b> |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 65.77        | 95.09        | 75.22        | 0.947           | 1.184           | 0.0991         | 2.361          | 0.782        |
|              | U-NET           | <i>soft-dice</i>              | 76.23        | 96.75        | 86.83        | 0.491           | 1.256           | 0.0589         | 1.120          | 0.881        |
|              |                 | $\mathcal{L}_c, \alpha = 0.1$ | <b>76.66</b> | <b>96.77</b> | 87.35        | 0.359           | <b>0.938</b>    | 0.0457         | 0.980          | 0.878        |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | 76.25        | 96.76        | <b>87.29</b> | <b>0.312</b>    | 1.031           | <b>0.0415</b>  | 0.865          | 0.900        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | 74.85        | 96.57        | 86.10        | 0.322           | 1.062           | 0.0504         | 0.827          | 0.913        |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | 75.38        | 96.60        | 86.16        | 0.344           | 1.016           | 0.0483         | <b>0.755</b>   | <b>0.916</b> |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 76.45        | 96.64        | <b>88.17</b> | 0.375           | 0.953           | 0.0527         | 1.080          | 0.894        |
|              | Mosinska et al. | [29, 17]                      | -            | 97.54        | -            | -               | 2.781           | -              | -              | -            |
|              | Hu et al.       | [17]                          | -            | 97.28        | -            | -               | 1.275           | -              | -              | -            |
| CREMI        | U-NET           | <i>soft-dice</i>              | 91.54        | 97.11        | 95.86        | 0.259           | 0.657           | 0.0461         | 1.087          | 0.904        |
|              |                 | $\mathcal{L}_c, \alpha = 0.1$ | 91.76        | <b>97.21</b> | 96.05        | 0.222           | 0.556           | <b>0.0395</b>  | 1.000          | 0.900        |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | 91.66        | 97.15        | 96.01        | 0.231           | 0.630           | 0.0419         | 0.991          | 0.902        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | <b>91.78</b> | 97.18        | <b>96.21</b> | <b>0.204</b>    | <b>0.537</b>    | 0.0437         | <b>0.919</b>   | <b>0.913</b> |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | 91.56        | 97.12        | 96.09        | 0.250           | 0.630           | 0.0444         | 0.995          | 0.902        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 91.66        | 97.16        | 96.16        | 0.231           | 0.620           | 0.0455         | 0.991          | 0.907        |
|              | Mosinska et al. | [29, 17]                      | 82.30        | 94.67        | -            | -               | 1.973           | -              | -              | -            |
|              | Hu et al.       | [17]                          | -            | 94.56        | -            | -               | 1.113           | -              | -              | -            |
| DRIVE retina | FCN             | <i>soft-Dice</i>              | 78.23        | 96.27        | 78.02        | 2.187           | 1.860           | 0.0429         | 3.275          | 0.773        |
|              |                 | $\mathcal{L}_c, \alpha = 0.1$ | 78.36        | 96.25        | 79.02        | 2.100           | 1.610           | 0.0393         | 3.203          | 0.777        |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | <b>78.75</b> | 96.29        | 80.22        | 1.892           | 1.382           | 0.0383         | 2.895          | 0.793        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | 78.29        | 96.20        | 80.28        | 1.888           | <b>1.332</b>    | <b>0.0318</b>  | 2.918          | <b>0.798</b> |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | 78.00        | 96.11        | 80.43        | 2.036           | 1.602           | 0.0423         | 3.141          | 0.764        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 77.76        | 96.04        | <b>80.95</b> | <b>1.836</b>    | 1.408           | 0.0394         | <b>2.848</b>   | 0.794        |
|              | U-Net           | <i>soft-Dice</i>              | 74.25        | 95.63        | 75.71        | 1.745           | 1.455           | 0.0649         | 2.997          | 0.760        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | <b>75.21</b> | <b>95.82</b> | <b>76.86</b> | <b>1.538</b>    | <b>1.389</b>    | <b>0.0586</b>  | <b>2.737</b>   | <b>0.767</b> |
|              | Mosinska et al. | [29, 17]                      | -            | 95.43        | -            | -               | 2.784           | -              | -              | -            |
|              | Hu et al.       | [17]                          | -            | 95.21        | -            | -               | 1.076           | -              | -              | -            |
| Vessap data  | FCN, 1 ch       | <i>soft-dice</i>              | 85.21        | <b>96.03</b> | 90.88        | 3.385           | 4.458           | 0.00459        | 5.850          | 0.862        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | <b>85.44</b> | 95.91        | <b>91.32</b> | <b>2.292</b>    | <b>3.677</b>    | <b>0.00417</b> | <b>5.620</b>   | <b>0.864</b> |
|              |                 | <i>soft-dice</i>              | 85.31        | 95.82        | 90.10        | 2.833           | 4.771           | 0.00629        | 6.080          | 0.849        |
|              | FCN, 2 ch       | $\mathcal{L}_c, \alpha = 0.1$ | 85.96        | 95.99        | 91.02        | 2.896           | <b>4.156</b>    | 0.00447        | 5.980          | 0.860        |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | <b>86.45</b> | <b>96.11</b> | 91.22        | 2.656           | 4.385           | 0.00466        | 5.530          | 0.869        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | 85.72        | 95.93        | 91.20        | 2.719           | 4.469           | <b>0.00423</b> | 5.470          | 0.866        |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | 85.65        | 95.95        | <b>91.65</b> | 2.719           | 4.469           | <b>0.00423</b> | 5.670          | 0.869        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 85.28        | 95.76        | 91.22        | <b>2.615</b>    | 4.615           | 0.00433        | <b>5.320</b>   | <b>0.870</b> |
|              |                 | <i>soft-dice</i>              | 87.46        | 96.35        | 91.18        | 3.094           | 5.042           | 0.00549        | 5.300          | 0.863        |
|              | U-Net, 1 ch     | $\mathcal{L}_c, \alpha = 0.5$ | <b>87.82</b> | <b>96.52</b> | <b>93.03</b> | <b>2.656</b>    | <b>4.615</b>    | <b>0.00533</b> | <b>4.910</b>   | <b>0.872</b> |
|              |                 | <i>soft-dice</i>              | 87.98        | 96.56        | 90.16        | 2.344           | 4.323           | 0.00507        | 5.550          | 0.855        |
|              | U-Net, 2 ch     | $\mathcal{L}_c, \alpha = 0.1$ | 88.13        | 96.59        | 91.12        | 2.302           | 4.490           | 0.00465        | 5.180          | <b>0.872</b> |
|              |                 | $\mathcal{L}_c, \alpha = 0.2$ | 87.96        | 96.74        | 92.52        | 2.208           | <b>3.979</b>    | 0.00342        | <b>4.830</b>   | 0.861        |
|              |                 | $\mathcal{L}_c, \alpha = 0.3$ | 87.70        | 96.71        | 92.56        | <b>2.115</b>    | 4.521           | <b>0.00309</b> | 5.260          | 0.858        |
|              |                 | $\mathcal{L}_c, \alpha = 0.4$ | <b>88.57</b> | <b>96.87</b> | <b>93.25</b> | 2.281           | 4.302           | 0.00327        | 5.370          | 0.868        |
|              |                 | $\mathcal{L}_c, \alpha = 0.5$ | 88.14        | 96.74        | 92.75        | 2.135           | 4.125           | 0.00328        | 5.390          | 0.864        |

introduced OPT-Junction F1 by Citraro et al. [7]. Our results are consistent across different network architectures, indicating that  $soft-clDice$  can be deployed to any network architecture.

**Qualitative:** In Figure 5, typical results for our datasets are depicted. Our networks trained on the proposed loss term recover connections, which were false negatives when trained with the soft-Dice loss. These missed connections

appear to be particularly frequent in the complex road and DRIVE dataset. For the CREMI dataset, we observe these situations less frequently, which is in line with the very high quantitative scores on the CREMI data. Interestingly, in the real 3D vessel dataset, the soft-Dice loss oversegments vessels, leading to false positive connections. This is not the case when using our proposed loss function, which we attribute to its topology-preserving nature. Additional

qualitative results can be inspected in the supplementary.

**Computational Efficiency:** Naturally, inference times of CNNs with the same architecture but different training losses are identical. However, during training, our soft-skeleton algorithm requires  $O(kn^2)$  complexity for an  $n \times n$  2D image where  $k$  is the number of iterations. As a comparison, [17] needs  $O(c^2m \log(m))$  (see [15]) complexity to compute the 1d persistent homology where  $d$  is the number of points with zero gradients in the prediction and  $m$  is the number of simplices. Roughly,  $c$  is proportional to  $n^2$ , and  $m$  is of  $O(n^2)$  for a 2D Euclidean grid. Thus, the worst complexity of [17] is  $O(n^6 \log(n))$ . Additionally, their approach requires an  $O(c \log(c))$  complexity to find an optimal matching of the birth-death pairs. We note that the total run-time overhead for soft-clDice compared to soft-Dice is marginal, i.e., for batch-size of 4 and 1024x1024 image resolution, the former takes 1.35s while the latter takes 1.24s on average (<10% increase) on an RTX-8000.

**Future Work:** Although our proposed soft-skeleton approximation works well in practice, a better differentiable skeletonization can only improve performance, which we reserve for future research. Any such skeletonization can be readily plugged into our approach. Furthermore, theoretical and experimental multi-class studies would sensibly extend our study.

## 6. Conclusive Remarks

We introduce *clDice*, a novel topology-preserving similarity measure for tubular structure segmentation. Importantly, we present a theoretical guarantee that *clDice* enforces topology preservation up to homotopy equivalence. Next, we use a differentiable version of the *clDice*, *soft-clDice*, in a loss function, to train state-of-the-art 2D and 3D neural networks. We use *clDice* to benchmark segmentation quality from a topology-preserving perspective along with multiple volumetric, topological, and graph-based measures. We find that training on *soft-clDice* leads to segmentations with more accurate connectivity information, better graph-similarity, better Euler characteristics, and improved Dice and Accuracy. Our *soft-clDice* is computationally efficient and can be readily deployed to any other deep learning-based segmentation tasks such as neuron segmentation in biomedical imaging, crack detection in industrial quality control, or remote sensing.

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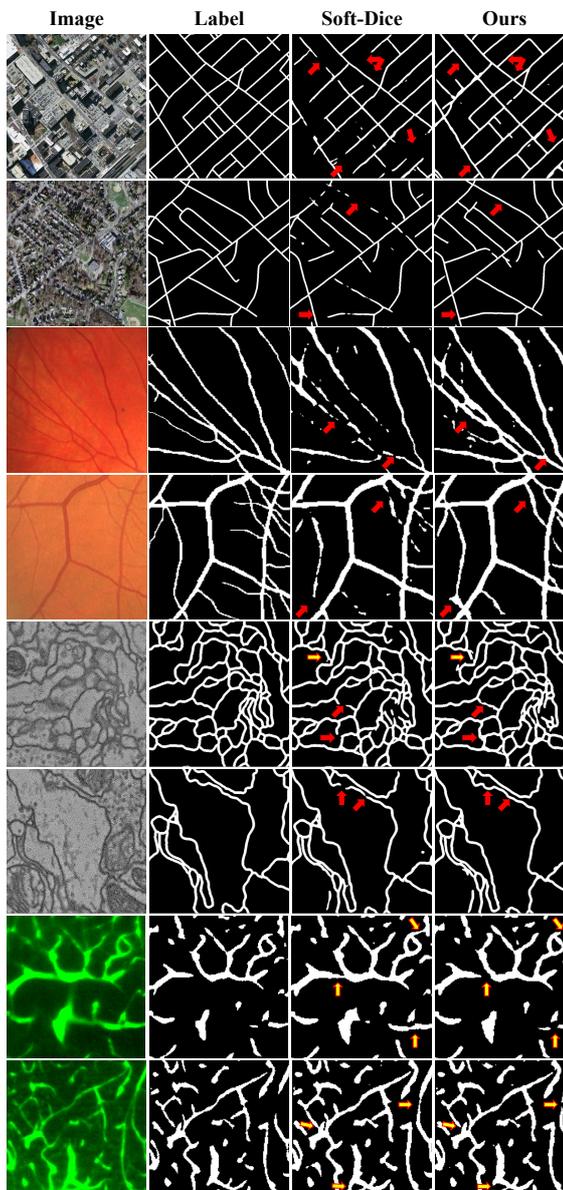


Figure 5. Qualitative results: from top to bottom we show two rows of results for: the Massachusetts road dataset, the DRIVE retina dataset, the CREMI neuron data and 2D slices from the 3D Vessap dataset. From left to right, the real image, the label, the prediction using soft-Dice and the U-Net predictions using  $\mathcal{L}_c(\alpha = 0.5)$  are shown, respectively. The images indicate that *clDice* segments road, retina vessel connections and neuron connections which the soft-Dice loss misses, but also does not segment false-positive vessels in 3D. Some, but not all, missed connections are indicated with solid red arrows, false positives are indicated with red-yellow arrows. More qualitative results can be found in the Supplementary material.

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