

# Supplementary File: Learning the Non-differentiable Optimization for Blind Super-Resolution

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## Abstract

In this supplementary file, we first provide the details of our proposed adaptive modulation generative adversarial network (AMGAN) and then show the training procedure of AMGAN-RL. Finally, we show more visual results.

## 1. AMGAN

**VGG perceptual loss.** The VGG perceptual loss  $\mathcal{L}_{\text{vgg}}$  compares the activation maps in the intermediate layers of well-trained VGG19 [5] network, which can be formulated as

$$\mathcal{L}_{\text{vgg}} = \sum_{l=1}^5 w^l \frac{\|\Psi_{\mathbf{I}^{\text{HR}}}^l - \Psi_{\mathbf{I}^{\text{SR}}}^l\|_1}{N_{\Psi_{\mathbf{I}^{\text{HR}}}^l}},$$

where  $\Psi_{\mathbf{I}^*}^l$  is the activation map of the  $\text{relu}_{-1}$  layer given original input  $\mathbf{I}^*$ ,  $N_{\Psi_{\mathbf{I}^{\text{HR}}}^l}$  is the number of elements in  $\Psi_{\mathbf{I}^{\text{HR}}}^l$ . Following [2], we set  $w^l = \frac{1e3}{\left(C_{\Psi_{\mathbf{I}^{\text{HR}}}^l}\right)^2}$ . Here,  $C$  is the channel size of feature map  $\Psi_{\mathbf{I}^{\text{HR}}}^l$ .

**Realness adversarial loss.** Different from the standard GAN (including relativistic GAN [3]), RealnessGAN [6]’s discriminator outputs a distribution as the measure of realness.

$$\mathcal{L}_{\text{realness}} = \mathbb{E}_{\mathbf{I}^{\text{LR}} \sim p_{\text{LR}}} \left[ \mathcal{D}_{\text{KL}}(\mathcal{A}_1 \parallel \mathcal{D}(G(\mathbf{I}^{\text{LR}}))) \right] - \mathbb{E}_{\mathbf{I}^{\text{LR}} \sim p_{\text{LR}}} \left[ \mathcal{D}_{\text{KL}}(\mathcal{A}_0 \parallel \mathcal{D}(G(\mathbf{I}^{\text{LR}}))) \right],$$

where  $\mathcal{D}_{\text{KL}}(\cdot \parallel \cdot)$  denotes Kullback-Leibler (KL) divergence. Two virtual ground-truth distributions are required to stand for the realness distributions of real and fake images. We refer to these two distributions as  $\mathcal{A}_1$  (real) and  $\mathcal{A}_0$  (fake). Specifically,  $\mathcal{A}_1$  and  $\mathcal{A}_0$  are chosen to resemble

the shapes of a Gaussian distribution  $\mathcal{N}(\mathbf{0}, \mathbf{I})$  and a Uniform distribution  $\mathcal{U}(\mathbf{0}, \mathbf{I})$ , respectively. The architecture of our discriminator is illustrated in Figure 1.

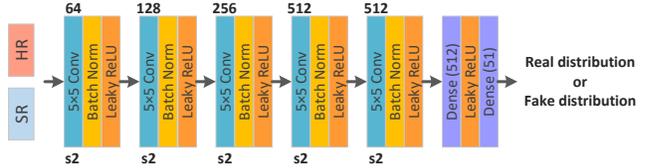


Figure 1. The structure of our discriminator. “s2” denotes the stride as 2.

**Total loss.** With L1 loss, VGG perceptual loss, realness adversarial loss, and DISTS loss [1], our final loss function is defined as

$$\mathcal{L}_{\text{total}} = \mathcal{L}_1 + 15\mathcal{L}_{\text{vgg}} + 0.01\mathcal{L}_{\text{realness}} + 10\mathcal{L}_{\text{DISTS}}.$$

To validate the effectiveness of the introduced *Realness GAN*, we conduct the same model trained with *Relativistic GAN*, denoted by AMGAN\*. As shown in Table 1, AMGAN perform superior performance (PSNR & SSIM) than AMGAN\*.

Table 1. Average LPIPS/PSNR results. The comparison is conducted using kernel widths 0.2, 1.3 and 2.6. Here, AMGAN\* is trained with *Relativistic GAN*.

Dataset	Scores	AMGAN	AMGAN*
Set5	LPIPS↓	<b>0.0707</b>	0.1078
	PSNR↑	<b>31.02</b>	29.29
Set14	LPIPS↓	<b>0.1254</b>	0.2048
	PSNR↑	<b>27.14</b>	26.38
BSD100	LPIPS↓	<b>0.1698</b>	0.2862
	PSNR↑	<b>26.36</b>	25.63
PIRM_Val	LPIPS↓	<b>0.1197</b>	0.2291
	PSNR↑	<b>26.50</b>	25.91

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## 2. The training procedure of AMGAN-RL

The algorithm of the detailed training process is summarized in Algorithm 1.

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**Algorithm 1** Training AMGAN-RL

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**Require:** Critic network  $Q(s, a | \theta^Q)$  (random initialization); Pretrained actor  $\mu(s | \theta^\mu)$ ; Initialize replay buffer  $R$ ; Initialize **Environment** with pre-trained renderer AMGAN.

- 1: **for**  $t_{steps} < maxsteps$  **do**
  - 2:   Receive initial observation state  $s_t$
  - 3:   Select action  $a_t = \mu(s_t | \theta^\mu)$  according to the current policy
  - 4:   Execute action  $a_t$  and observe reward  $r_t$  and observe rendered result  $s'_t$
  - 5:   Store transition  $(s_t, a_t, r_t, s'_t)$  in  $R$
  - 6:   Sample a random minibatch of  $N$  transitions  $(s_t, a_t, r_t, s'_t)$  from  $R$
  - 7:   Update critic by minimizing the loss:  $L(\theta^Q) = \frac{1}{N} \sum_i \max(0, -\gamma * Q(s_i, a_i | \theta^Q)) + (r_i - Q(s_i, a_i | \theta^Q))$
  - 8:   Update the actor policy using the policy gradient:  $\nabla_{\theta^\mu} J = \frac{1}{N} \sum_i \nabla_a Q(s, a | \theta^Q) |_{s=s_i, a=\mu(s_i)} \nabla_{\theta^\mu} \mu(s | \theta^\mu) |_{s=s_i}$
  - 9: **return**  $\mathbf{I}^{SR} = \text{AMGAN}(\mathbf{I}^{LR}, \mu(\mathbf{I}^{LR} | \theta^\mu))$  (Output the final SR result)
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## 3. Visual results

We give more comparisons with methods of DAN [4] (blind) and USRGAN [7] (non-blind) on PIRM\_Val (Figure 2), BSD100, and Set5 (Figure 3). It can be found that our AMNet-RL and AMNet.L-RL shows a little bit sharper than DAN. AMGAN produces texture naturally images, and AMGAN-RL generates sharper details.

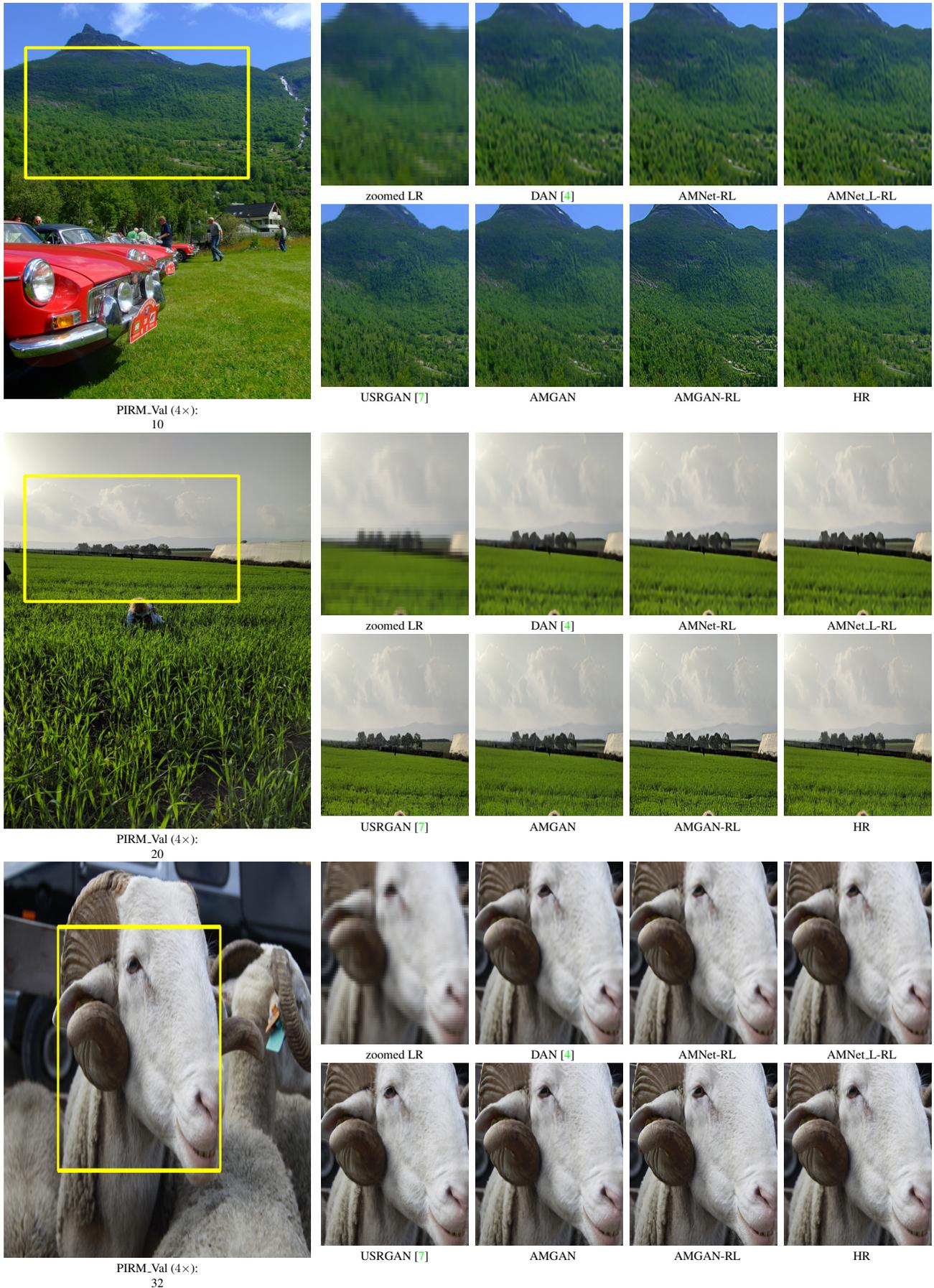


Figure 2. Visual results of various methods at scaling factor of 4. Note that USRGAN [7] adopts direct downsampling instead of *bicubic* downsampling, which is more simple than DAN [4] and our proposed method.



Figure 3. Visual results of various methods at scaling factor of 4. Note that USRGAN [7] adopts direct downsampling instead of *bicubic* downsampling, which is more simple than DAN [4] and our proposed method.

## References

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