Supplementary Materials for "Counterfactual VQA: A Cause-Effect Look at Language Bias"

This supplementary document is organized as follows:

- Section 1 introduces that RUBi [5] and Learned-Mixin [6] can be unified into our counterfactual inference framework.
- Section 2 provides an analysis of estimating NDE using the learnable parameter.
- Section 3 describes the implementation details.
- Section 4 describes the supplementary quantitative and qualitative results.

1. Revisiting RUBi and Learned-Mixin

As mentioned in Section 4.3, RUBi [5] and Learned-Mixin [6] can be unified into our counterfactual inference framework, which (1) follow a simplified causal graph without the direct path $V \rightarrow A$, and (2) use natural indirect effect (NIE) for inference. The detailed analysis is provided as follows.

1.1. Cause-Effect Look

Recent works RUBi [5] and Learned-Mixin [6] apply an ensemble architecture with a vision-language branch $\mathcal{F}_{\mathcal{VQ}}$ and a question-only branch $\mathcal{F}_{\mathcal{Q}}$, while the direct relation between vision and answer is not formulated. The architecture is shown in Figure 1 (a).

Note that total effect can be decomposed into natural direct effect (NDE) and total indirect effect (TIE). As introduced in the main paper, we remove language bias by subtracting the natural direct effect from the total effect. The TIE is calculated by:

$$TE = Z_{q,k} - Z_{q^*,k^*},$$

$$NDE = Z_{q,k^*} - Z_{q^*,k^*},$$

$$TIE = TE - NDE = Z_{q,k} - Z_{q,k^*},$$

(1)

which corresponds to Eq. (4) in the main paper. An alternative option to reduce language bias is to substract the total direct effect (TDE) of questions on answers from total effect, which is formulated as:

$$TDE = Z_{q,k} - Z_{q^*,k},$$

$$NIE = TE - TDE = Z_{q^*,k} - Z_{q^*,k^*}.$$
(2)

Intuitively, both TIE and NIE reflect the increase of confidence for the answer given the visual knowledge, *i.e.*, from k^* to k. The difference between TIE and NIE is the existence of question q. The question q is block to calculate NIE (*i.e.*, q^*), while q is given to calculate TIE. We use TIE to reserve q as the language context. In addition, both TDE and NDE reflect the increase of confidence for the answer given the question, *i.e.*, from q^* to q. The difference between TDE and NDE is also the existence of question q. Note that we hope to exclude the effect directly caused by question. Therefore, the mediator knowledge should be blocked when estimating the pure language effect, which is captured by NDE.

1.2. Implementation

RUBi [5] and Learned-Mixin (LM) [6] use the following fusion strategies for ensemble-based training:

(RUBi)
$$h(Z_q, Z_k) = Z_k \cdot \sigma(Z_q)$$
 (3)

(LM)
$$h(Z_q, Z_k) = \log \sigma(Z_k) + g(k) \cdot \log \sigma(Z_q)$$
(4)

where $\sigma(\cdot)$ represents the sigmoid function, and $g(\cdot)$ is a learned function $\mathbb{R}^d \to \mathbb{R}^1$ with the knowledge representation $k \in \mathbb{R}^d$ as input and a scalar weight as output. During the test stage, they use Z_k for inference.

Perhaps supering As for RUBi, NIE is calculated as:

$$NIE = \underbrace{z_k \cdot \sigma(c)}_{Z_{q^*,k}} - \underbrace{c \cdot \sigma(c)}_{Z_{q^*,k^*}} \propto z_k \tag{5}$$

As for Learned-Mixin, NIE is calculated as:

$$NIE = \underbrace{(\log \sigma(z_k) + g(k) \cdot \log \sigma(c))}_{Z_{q^*,k}} - \underbrace{(\log \sigma(c) + g(k^*) \cdot \log \sigma(c))}_{Z_{q^*,k^*}} \propto z_k$$
(6)

where c, g(k) and $g(k^*)$ are constants for the same sample. Therefore, we have $NIE \propto z_k$ for both RUBi and Learned-Mixin, which is exactly the output score of the

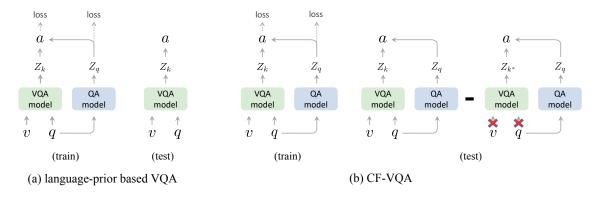


Figure 1: Comparison between our CF-VQA and language-prior based methods [5, 6] based on the simplified causal graph.

Algorithm 1 Improving RUBi [5] using CF-VQA	
1: function RUBI($v, q, \text{ is_Training; } \theta, c$)	
2: $z_q = \mathcal{F}_Q(q)$	
3: $z_k = \mathcal{F}_{VQ}(v, q)$	
4: if is_Training then	
5: $z = z_k \cdot \sigma(z_q)$	
6: updating θ according to \mathcal{L}_{cls}	
7: updating c according to \mathcal{L}_{kl}	
8: else	
9: $\frac{z = z_k}{z = (z_k - c) \cdot \sigma(z_q)}$	
10: end if	
11: return z	
12: end function	

vision-language branch \mathcal{F}_{VQ} . Note that RUBi and Learned-Mixin simply preserve the vision-language branch and uses z_k for inference. From our cause-effect view, *RUBi and* Learned-Mixin use natural indirect effect for inference.

1.3. Improving RUBi [5]

Thanks to our cause-effect look, RUBi [5] can be improved using CF-VQA, *i.e.*, using TIE for inference. Specifically, TIE for RUBi is calculated as:

$$TIE = \underbrace{z_k \cdot \sigma(z_q)}_{Z_{q,k}} - \underbrace{c \cdot \sigma(z_q)}_{Z_{q,k^*}}$$
(7)

where *c* denotes a learnable parameter. Table 5 in the main paper demonstrates that CF-VQA can outperform RUBi by 7% on VQA-CP v2. The red notes in Algorithm 1 show how RUBi is improved by changing several lines of code.

2. Analysis of Estimating NDE

In Section 4.2 in the main paper, we claimed that the learnable parameter c controls the sharpness of Z_{q,v^*,k^*} for estimating NDE. We give an intuitive analysis here.

For Harmonic (HM), we have:

(HM)
$$Z_{q,v^*,k^*} = \log \frac{\sigma(z_q) \cdot c_{\text{HM}}}{1 + \sigma(z_q) \cdot c_{\text{HM}}},$$
 (8)

where $c_{\text{HM}} = (\sigma(c))^2 \in (0, 1)$. We approximate the limits of Z_{q,v^*,k^*} and $TIE = Z_{q,v,k} - Z_{q,v^*,k^*}$ as:

(HM)
$$\lim_{\substack{c_{\mathrm{HM}} \to 0}} Z_{q,v^*,k^*} = -\infty$$
$$\lim_{\substack{c_{\mathrm{HM}} \to 0}} TIE = z_{q,v,k} - C \qquad (9)$$
$$\propto z_{q,v,k},$$

where we use a extremely negative number C to replace $-\infty$ for valid estimation of TIE. In this case, NDE is estimated as the same constant for all the answers, and TIE is dominated by $z_{q,v,k}$, which means that the language bias is not reduced. For $c_{\rm HM} \rightarrow 1$, we have

(HM)
$$\lim_{c_{\rm HM}\to 1} Z_{q,v^*,k^*} = \log \frac{\sigma(z_q)}{1+\sigma(z_q)}$$
$$\lim_{c_{\rm HM}\to 1} TIE = \log \frac{\sigma(z_v)\cdot\sigma(z_k)\cdot(1+\sigma(z_q))}{1+\sigma(z_q)\cdot\sigma(z_v)\cdot\sigma(z_k)}.$$
(10)

For SUM, we have

(SUM)
$$Z_{q,v^*,k^*} = \log \sigma(z_q + 2c),$$
 (11)

where $c \in (-\infty, +\infty)$. We approximate the limits of Z_{q,v^*,k^*} and $TIE = Z_{q,v,k} - Z_{q,v^*,k^*}$ as:

(SUM)
$$\lim_{c \to \infty} Z_{q,v^*,k^*} = -\infty$$
$$\lim_{c \to \infty} TIE = z_{q,v,k} - C \qquad (12)$$
$$\propto z_{q,v,k}.$$

Similar to HM, TIE is dominated by $z_{q,v,k}$. For $c \to +\infty$, we have:

(SUM)
$$\lim_{\substack{c \to +\infty}} Z_{q,v^*,k^*} = 0$$
$$\lim_{\substack{c \to +\infty}} TIE = z_{q,v,k}.$$
(13)

					VQA v2		
			val (in-	domain)		test (OOD)	val (in-domain)
	Base.	All	Y/N	Num.	Other	All	All
GRLS [8]	-	56.90	69.23	42.50	49.36	42.33	51.92
GradSup[10]	_	62.4	77.8	43.8	53.6	46.8	-
RandImg [12]	UpDn	54.24	64.22	34.40	50.46	55.37	57.24
CF-VQA (HM)	UpDn	65.47	79.09	45.86	57.86	49.74	63.73
CF-VQA (SUM)	UpDn	60.29	66.32	47.48	57.96	51.27	62.49
CF-VQA (HM)	S-MRL	63.08	75.76	44.88	55.99	53.55	63.54
CF-VQA (SUM)	S-MRL	57.86	66.24	44.98	53.38	55.05	60.94

Table 1: Comparison on VQA-CP v2 val set. "Base." indicates the VQA base model.

Also, TIE is dominated by $z_{q,v,k}$. In both cases, the language bias cannot be excluded. This analysis shows that a extremely large or small c will fail to estimate NDE and TIE, and it is necessary to control the sharpness of NDE by selecting a optimal c. In the main paper, we use a KLdivergence in Eq. (17) to force the sharpness of NDE similar to that of TE.

3. Implementation Details

We use the same implementation of RUBi [5] for fair comparison, including feature representation, baseline architectures, and optimization.

Image Representation. Following the popular bottom-up attention mechanism [2], we use a Faster R-CNN based framework to extract visual features. We select top-K region proposals for each image, where K is fixed as 36.

Question Representation. Following [4, 5], we first lowercase all the questions and remove the punctuation, and then use the pretrained Skip-thought encoder [9] with finetuning. The size of final embedding is set as 4800.

Vision-Language Branch. The vision-language branch consists of the image representation, question representation, and a visual knowledge encoder. The baseline models for encoding visual knowledge includes SAN [13], UpDn [2], and a simplified version of the recent architecture MUREL [4] (S-MUREL) proposed in [5]. In short, S-MUREL consists of a BLOCK [3] bilinear fusion between image and question representations for each region, and a MLP classifier composed of three fully connected layers with ReLU activations. The dimension are 2,048, 2,048, and 3,000. More details can be found in [5].

Language-Only Branch. The language-only branch consists of the question representation and a question-only classifier. The question-only classifier is implemented by a MLP with three fully connect layers with ReLU activations. Note that this MLP has the same structure with the classifier for vision-language branch with different parameters.

Vision-Only Branch. The vision-only branch is composed of the question representation and a vision-only classifier. The vision-only classifier has the same structure as the language-only classifier with different parameters.

Optimization. All the experiments are conducted with the Adam optimizer for 22 epochs. The learning rate linearly increases from 1.5×10^{-4} to 6×10^{-4} for the first 7 epochs, and decays after 14 epochs by multiplying 0.25 every two epochs. The batch size is set as 256.

Datasets. The experiments are conducted on VQA-CP [1] and VQA [7] datasets. VQA-CP v1 and v2 are created by re-organizing the train and val splits of the VQA v1 and v2 datasets, respectively [1].

4. Supplementary Experimental Results

We have conducted the ablation study and compared CF-VQA with state-of-the-art methods in the main paper. In this section, we show supplementary experimental results.

4.1. Quantitative Results

As suggested by [12, 8, 10, 11], we further hold out 8,000 instances from the training set (*i.e.*, VQA-CP v2 val) to measure the in-domain performance. Note that the results on VQA v2 val set also measure the in-domain performance. The results are given in Table 1. Compared to GRLS [8], all of our variants outperform GRLS by large margins for both in-domain and out-of-distribution (OOD) settings. Compared tp GradSup [10], CF-VQA (HM) achieves better results on both VQA-CP val set and test set. Compared to RandImg [12], CF-VQA (SUM) achieves competitive results on VQA-CP v2 test set, and outperforms RandImg on in-domain settings by over 3%. These results demonstrate that CF-VQA not only effectively reduces language bias, but also performs robustly.

Table 2 shows the ablation study on VQA-CP v1 test split. As shown in Table 2, CF-VQA is general to both *base-line VQA architectures* and *fusion strategies*, which is also demonstrated by the results on VQA-CP v2. Table 3 shows the ablation study on VQA-CP v1 test split using the simplified causal graph. Similarly, CF-VQA achieves significant improvement for different baseline VQA architectures and fusion strategies.

Table 2: **Ablation of CF-VQA** on VQA-CP v1 test set. "SAN/UpDn/S-MRL" denotes the baseline VQA model. "HM/SUM" represents the strategies that train the ensemble model and test with only the vision-language branch following ensemble-based method [5, 6]. * represents the reproduced results.

	All	Y/N	Num.	Other		All	Y/N	Num.	Other		All	Y/N	Num.	Other
SAN*	32.50	36.86	12.47	36.22	UpDn*	37.08	42.46	12.76	41.50	S-MRL*	36.68	42.72	12.59	40.35
Harmonic	49.29	72.73	20.57	37.51	Harmonic	55.75	80.65	24.72	43.46	Harmonic	53.55	79.38	17.39	42.38
+ CF-VQA	52.06	80.38	16.88	38.04	+ CF-VQA	55.16	82.27	16.14	43.87	+ CF-VQA	55.26	82.13	18.03	43.49
SUM	38.34	49.88	15.82	35.91	SUM	52.78	78.71	14.30	42.45	SUM	49.44	76.49	16.23	35.90
+ CF-VQA	52.87	84.94	14.85	36.26	+ CF-VQA	57.39	88.46	14.80	43.61	+ CF-VQA	57.03	89.02	17.08	41.27

Table 3: Ablation of CF-VQA with the simplified causal graph on VQA-CP v1 test set. "SAN/UpDn/S-MRL" denotes the baseline VQA model. "HM/SUM" represents the strategies that train the ensemble model and test with only the vision-language branch following ensemble-based method [5, 6]. * represents the reproduced results.

	All	Y/N	Num.	Other		All	Y/N	Num.	Other		All	Y/N	Num.	Other
SAN*	32.50	36.86	12.47	36.22	UpDn*	37.08	42.46	12.76	41.50	S-MRL*	36.68	42.72	12.59	40.35
Harmonic	46.83	66.64	19.45	38.13	Harmonic	54.13	80.60	15.75	43.24	Harmonic	54.51	80.82	17.30	43.29
+ CF-VQA	54.48	83.73	22.73	38.15	+ CF-VQA	56.19	85.08	16.00	43.61	+ CF-VQA	56.82	86.01	17.38	43.63
SUM	40.08	54.15	15.53	35.95	SUM	51.20	74.70	13.61	42.94	SUM	52.54	78.42	16.77	41.18
+ CF-VQA	52.73	84.64	16.02	35.75	+ CF-VQA	56.80	87.76	13.89	43.25	+ CF-VQA	57.07	89.28	17.39	41.00

4.2. Qualitative Results

Figure 2 illustrates examples to show how CF-VQA improves RUBi by simply replacing natural indirect effect with total indirect effect for inference following Algorithm 1. The examples show that CF-VQA benefits from language context, *e.g.*, "large or small", "deep or shallow", and "real or a statue" in the first row. Some failure cases are shown in the last two rows. First, CF-VQA may tend to generate broad answers, *e.g.*, "houses" v.s "church", and "vegetables" v.s "peas". Second, CF-VQA may ignore visual content like traditional likelihood strategy. Therefore, there remains the challenge about how to balance visual understanding and language context.

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Is	this	area	large	or	small?

	RUBi + C	F-VQA
	small	94.6%
	large	3.5%
	big	1.5%
1 10	medium	0.3%
	huma	0.10/





····			
	RUBi + C	F-VQA	RUBi
	natural	50.4%	no
	yes	25.6%	yes
	both	7.7%	none
	curved	4.8%	old
	main	3.9%	unknown

94.6% 3.5% old

0.3% 0.1%

yes no

both

RUB

36.3% 32.8%

18.7%

5.8% 3.0%

72.6% 18.5% 3.2% 1.3% 1.3%

25.7%

15.7% 14.3% 13.7%

8.7%

42.8%

19.1% 12.1% 6.6% 4.1%

83.0%

6.5% 4.8%

2.8%

0.8%

92.5%

6.1%

0.6%

0.1%

RUB

adidas

wilson nike

w white

baseball

ves

pink

baseball cap don't know

RUBi

RUBi

90.0%

8.6%

0.6%

0.1%







RUBi CF-VQA

wilson

nike prince head

adidas







F-VQA	RU	JBi
52.1%	orange	73.7%
9.2%	red	18.6%
6.0%	none	2.7%
5.7%	white	1.7%
2.8%	yellow	0.9%
	9.2% 6.0% 5.7%	52.1% orange 9.2% red 6.0% none 5.7% white

50.2% 24.1% 9.1% 8.5%

5.6%

RUBi + CF-VQA

40.7%

10.9% cleats

8.6%

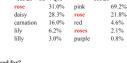
5.9% 5.7%

olaying in?
+ CF-VQA
40.79
10.9
shoes 8.6%
se 5.9%
5.7%
i s

What type of flower is in the vase?



What ar











city







0.9%

89.6%

5.1%

What brand is the box?				
	RUBi + 6	CF-VQA	RU	Bi
	hp	32.2%	dell	64.2%
	canon	21.5%	hp	26.5%
	dell	15.1%	windows	6.9%
THE DOCUMENT COLOR	toshiba	13.4%	adidas	0.9%
E	head	8.0%	toshiba	0.6%





e b	RUBi + C	F-VQA	RU	Bi
	pedestal	49.6%	bathroom	48.5%
	bathroom	10.3%	pedestal	40.0%
1 - 1	porcelain	8.0%	white	5.6%
	ceramic	7.1%	ceramic	5.2%
1. 1. 1. 1. A.	white	4.1%	porcelain	1.0%









40.3%

35.7% 12.1%

and the second second	RUBi + C	F-VQA	RUB	i
	coke	42.2%	none	45.2%
	coca cola	38.9%	nothing	34.5%
	coca-cola	8,9%	unknown	9.0%
	starbucks	1.6%	not possible	3.3%
	fanta	1.6%	white	1.5%
brand is shown?				
brand is shown?	RUBi + C	F-VQA	RUB	i
brand is shown?	RUBi + C harley	F-VQA 55.7%	RUB yamaha	i 34.8%
brand is shown?				
brand is shown?	harley	55.7%	yamaha	34.8%
brand is shown?	harley yamaha	55.7% 20.6%	yamaha harley	34.8% 33.9%
brand is shown?	harley yamaha	55.7% 20.6%	yamaha harley harley	34.8% 33.9%
brand is shown?	harley yamaha honda	55.7% 20.6% 7.8%	yamaha harley harley davidson	34.8% 33.9% 18.2%

RUBi + CF-VOA

RUBi + CF-VOA

90.8% 5.9%

2.7%

0.2%

0.1%

93.1% 6.2% 0.5%

0.1%

F-VQA

58.5% 9.0% 8.8% 5.4%

4.0% old

no

yes

none

neithe

New York

unknown

not sure no

yes

no

yes unknown

expert

statue

node

toy

real

big

itry'

city

yes both

country

United States 0.1%

RUBi

ford

volvo

dodge

chevy

RUR

RUB

RUB

RUB

26.2%

14.1%

11.7%

10.0%

3.9% 3.5%

76.8%

6.5%

3.0%

2.9%

2.5%

97.3%

1.2% 1.2%

0.1%

0.1%

RUBi

RUBi

striped curly

stripes

blue

sweater

0.6%

84.8%

13.0%

1.0%

0.5%

0.4%

25.3%

22.7%

18.4%

7.9%

6.6%

29.2%

27.7%

10.9%

6.2%

5.0%



91.0%

3.7% 3.0%

0.7% 0.5%

73.1%

8.4% 5.5%

1.8%

1.6%

40.3%

27.1%

12.2%

9.3% 7.2%

RUBi

	bob	8.6%	sweater	5.2%
Vhat type of RUBi + CF-VC		CT VO		
iis man	RUBi + 0		RU	
	bow tie	74.7%	striped	50.6%
	bow	15.1%	curly	21.1%
	bowtie	8.0%	stripes	7.8%
	regular	0.8%	blue	3.9%

horizontal

Where on the cow's body	is there a tag?			
-	RUBi + CF-VQA			
1000	ear	48.8%	yes	
	yes	17.3%	no	
and a second	back	9.3%	left	
A CONT	head	5.0%	unkn	
and the second sec	legs	3.2%	bowl	





Figure 2: Qualitative comparison of RUBi and RUBi+CF-VQA on VQA-CP v2 test split. Red bold answer denotes the ground-truth one.

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Is this horse real or a statue?