

# Supplementary Materials for LASR: Learning Articulated Shape Reconstruction from a Monocular Video

Table 1. Choices of hyper-parameters for training.

Name	Value
<b>Optimization parameters</b>	
Network architecture of $\phi_w$	ResNet-18 (ImageNet-pretrained) [1]
Optimizer	Adam [2]
Learning rate for $\phi_w$	$1 \times 10^{-4}$
Learning rate for other params.	$5 \times 10^{-3}$
Batch size	8 image pairs
Loss weight $\{\beta_1, \dots, \beta_4\}$	$\{0.5, 0.5, 2, 5 \times 10^{-3}\}$
<b>Measurement pre-processing</b>	
Crop center	Center of object bounding box
Crop size	$1.2 \times$ longest edge
Resized to	$256 \times 256$

## 1. Implementation details

**Training details:** We include details of the hyper-parameters used for training in Tab. 1.

**Video pre-processing:** We provide details for video pre-processing. To ensure enough object motion between adjacent frames, we use a heuristic rule that skips the next frame when the average magnitude of measured flow within the object silhouette is lower than 0.05 in the clip space.

## 2. Notations

A summary of the notations is listed in Tab. 2.

## References

- [1] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *CVPR*, pages 770–778, 2016. 1
- [2] Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014. 1

Table 2. Table of notations used in this work.

Symbol	Description
<b>Numbers</b>	
$T$	Number of frames in the input video
$M$	Number of faces in the mesh
$N$	Number of vertices in the mesh
$B$	Number of bones for LBS
<b>Measurements</b>	
$I_t$	Input RGB image at time $t$
$S_t$	Input or measured object silhouette image at time $t$
$\mathbf{u}_t^+$	Input or measured forward optical flow map from time $t$ to $t + 1$
$\mathbf{u}_t^-$	Input or measured backward optical flow map from time $t$ to $t - 1$
$\mathbf{Y}^*$	Union of all measurements $\{I_t, S_t, \mathbf{u}_t^+, \mathbf{u}_t^-\}$
<b>Renderings</b>	
$\hat{I}_t$	Rendered color image of the object at time $t$
$\hat{S}_t$	Rendered object silhouette image at time $t$
$\hat{\mathbf{u}}_t^+$	Rendered forward optical flow map of the object from time $t$ to $t + 1$
$\hat{\mathbf{u}}_t^-$	Rendered backward optical flow map of the object from time $t$ to $t - 1$
$\mathbf{Y}$	Union of all renderings $\{\hat{I}_t, \hat{S}_t, \hat{\mathbf{u}}_t^+, \hat{\mathbf{u}}_t^-\}$
<b>Variables</b>	
$f_t$	Focal length of the camera at time $t$
$\mathbf{K}_t$	Intrinsic matrix of a simple pinhole camera (with zero skew and square pixel) at time $t$
$\mathbf{R}_{0,t}$	Object-to-camera rotation matrix $\in SO(3)$ at time $t$
$\mathbf{T}_{0,t}$	Object-to-camera translation vector at time $t$
$\mathbf{G}_{0,t}$	Object-to-camera transformation at time $t$ , $\mathbf{G}_{0,t} = (\mathbf{R}_0 \mid \mathbf{T}_0)_t$
$\mathbf{R}_{1\dots B,t}$	Bone rotations from the rest pose to time $t$
$\mathbf{T}_{1\dots B,t}$	Bone translations from the rest pose to time $t$
$\mathbf{G}_{1\dots B,t}$	Bone transformations from the rest pose to time $t$ , $\mathbf{G}_{i,t} = (\mathbf{R}_i \mid \mathbf{T}_i)_t, i \in \{1 \dots, B\}$
$\mathbf{D}_t$	Union of camera and bone transformations $\{\mathbf{G}_{0,t}, \dots, \mathbf{G}_{B,t}\}$
$\mathbf{P}_t$	Projection matrix of the camera at time $t$ , $\mathbf{P}_t = \mathbf{K}_t \mathbf{G}_{0,t}$
$\Delta \mathbf{V}_t$	Vertex motion from the rest shape to time $t$
<b>Parameters</b>	
$(p_x, p_y)$	Principal point of the camera
$\bar{\mathbf{V}}_i$	Position of the $i$ -th vertex of the mesh in the rest pose (or mean shape)
$\bar{\mathbf{C}}_i$	Color of the $i$ -th vertex of the mesh
$\mathbf{S}$	Union of all mesh parameters, $\mathbf{S} = \{\bar{\mathbf{V}}, \bar{\mathbf{C}}, \mathbf{F}\}$
$\mathbf{J}_b$	Position of the center of the $b$ -th bone (or Gaussian component)
$\mathbf{Q}_b$	Precision matrix of $b$ -th bone (or Gaussian component)
$\mathbf{W}$	Skinning weights matrix, $\mathbf{W} = \{\mathbf{J}, \mathbf{Q}\}$
$\phi_w$	Weights of the convolutional camera and pose network
$\mathbf{n}^*$	Normal vector of the symmetry plane in the canonical frame
$\mathbf{X}$	Union of all Parameters
<b>Constants</b>	
$\mathbf{F}$	Faces of the mesh
$\beta$	Weights between the losses
$\mathbf{H}$	Householder transformation matrix describing reflection about the $y$ - $z$ plane
$\mathbf{n}_0$	Unit vector towards to the $x$ axis
<b>Others</b>	
$\mathbf{S0}$	Training stage 0: optimize for $\{\phi_w(f_t, \mathbf{G}_{0,t}), p_x, p_y, \mathbf{n}^*, \bar{\mathbf{V}}, \bar{\mathbf{C}}\}$
$\mathbf{S1-3}$	Training stage 1 to 3: optimize for $\{\phi_w(f_t, \mathbf{G}_{0\dots B,t}), p_x, p_y, \mathbf{n}^*, \bar{\mathbf{V}}, \bar{\mathbf{C}}, \mathbf{J}, \mathbf{Q}\}$