# Extracurricular Learning: Knowledge Transfer Beyond Empirical Distribution (Supplementary Material)

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### A. Training details

### A.1. Gaze Estimation

We used the MPIIGaze dataset [19, 20] that contains 45,000 annotated eye images of 15 persons (3,000 images per person divided equally between left and right eyes). We followed the leave-one-person-out evaluation process similar to the original works [19, 20]. We split the data to 20% validation and 80% training sets (3 randomly selected persons are held-out for validation and 12 persons for training). We run each experiment three times with a different random seed and report average error. We followed the implementation of original works [19, 20] for training, and used two existing architectures for student and teacher: the student is a 4-layer LeNet [9] and the teacher is a 9-layer PreAct-ResNet [5] trained with MixUp. The models output a two-dimensional vector that predicts the gaze vector. When estimating the uncertainty, we use an isotropic Gaussian  $\mathcal{N}(\mu, \sigma \mathbb{I})$  to model the output distribution. Therefore, the network output is three-dimensional. We set weight decay to  $10^{-4}$ , learning rate to  $10^{-4}$  for LeNet and  $10^{-3}$  for ResNet that is decayed by a factor of 10 after 30 and 36 epochs. All models are trained using ADAM optimizer [8] for 40 epochs with 0.9 momentum and batch-size of 32.

#### A.2. ResNet-18 on CIFAR100

We followed the same setup as [3] to train the ResNet-18 model [5]. Weight decay is  $5 \times 10^{-4}$ , learning rate is 0.1, and is decayed by a factor of 5 after 120, 240, and 320 epochs and the model is trained for 400 epochs. For all experiments, we use standard random cropping and horizontal flipping augmentations, and train with Nesterov [12] accelerated SGD with 0.9 momentum and batch-size of 128.

### A.3. PyramidNet-200 on CIFAR100

We use the same training setup as in [17], namely, PyramidNet [4] initialized with depth 200 and  $\tilde{\alpha} = 240$ , weight decay of  $10^{-4}$ , learning rate of 0.25 that is decayed by a factor of 10 after 150 and 225 epochs. For all experiments we use standard random cropping and horizontal flipping augmentations and train with Nesterov accelerated SGD for 300 epochs with 0.9 momentum and batch-size of 64.

#### A.4. BinaryNet on CIFAR100

We implemented Binary-Weight [2, 14] ResNet-18 architecture, where all weights (with the exception of the first and the last layers) are represented with 1-bit. We use the binary architecture in [14], and training setup in [10], namely, weight decay is zero, learning rate is  $2 \times 10^{-4}$  that is decayed by a factor of 10 after 150 and 250 epochs. For all experiments, we use standard random cropping and horizontal flipping augmentations and train with ADAM optimizer [8] for 350 epochs with 0.9 momentum and batchsize of 128. The implementation is the same as [13].

#### A.5. ResNet on ImageNet

We use the training setup introduced in [6]: the weight decay is  $10^{-4}$  and learning rate is linearly warmed-up during the first 5 epochs from 0.1 to 0.4, and then decayed to 0 by a cosine function. For all experiments, we use SGD with Nesterov with batch-size of 1024, and apply standard data augmentations during training: random crop and resize to  $224 \times 224$ , random horizontal flipping, color jittering, and lightening. We resize the images to  $256 \times 256$  followed by a center cropping to  $224 \times 224$  during test. We use 300 epochs to train all models similar to [17]. We use regular ResNet-50 and ResNet-101 architectures [5] (not the D variant introduced in [6]). To reduce under-fitting for XCL, we used  $10 \times$  smaller weight decay ( $10^{-5}$ ). Note that using a reduced weight decay did not help for other methods.

#### A.6. XCL with GAN-Generated Synthetic Data

Transfer-set using GAN can be generated online or offline. In the online setting, in every batch, we generate a new set of images via GAN. This setting is used when GPU memory

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is sufficient to generate a batch of samples in parallel with distillation (e.g. for CIFAR100 benchmark). In the offline setting, we sample a large dataset using GAN, use the teacher to obtain soft labels, and store the extended transfer-set to be used in distillation.

For the XCL-GAN in 2D gaze estimation experiment, we used the conditional GAN in [15] to sample eye images with random orientations in offline setting, adding  $\sim 485$ k examples to the original transfer-set.

For the classification tasks, we used BigGAN [1] to generate samples when using XCL-GAN. BigGAN architecture is a conditional GAN, where an embedding vector  $v_i$  is trained for each class *i*. At inference time, the generative model *G* gets a latent variable z and an embedding vector  $v_i$  to generate a random sample  $G(z; v_i)$  from class *i*. To sample with mixed class vectors (between two classes *i* and *j*) as in Section 4.2, we interpolate the embedding vectors:  $v = \lambda v_i + (1 - \lambda)v_j$ . We then generate a mixed sample G(z; v).

In CIFAR100 experiments, we used the online setting. In ImageNet experiments, we used the offline setting and sampled a transfer-set of 1M images using mixed-class labels. At each iteration of the training we sample half of the samples from the generated transfer-set and the other half from the original data points.

#### **B. Results of ResNet-50 Training on ImageNet**

The results are shown in Table 1. Compared to the standard KD we observe that XCL obtains 33% reduction in the teacher-student accuracy gap.

method	val	val	val	V2-A	V2-B	V2-C
	top-1	top-1 gap	top-5	top-1	top-1	top-1
ERM	77.3		93.6	74.5	65.6	79.4
+MixUp [18]	77.8	N/A	93.9	74.9	66.4	79.7
+CutMix [17]	78.7		94.3	75.5	66.9	80.2
KD [7]	79.2	2.4 (-)	94.3	75.6	67.3	80.6
XCL-Mix	80.0	1.6 (-33%)	95.0	77.2	68.2	81.3

Table 1: Accuracies (%) of the ResNet-50 model trained on the ImageNet dataset. Teacher is a ResNet-152-D model trained with CutMix (top-1 acc. = 81.6%). The std of XCL val top-1 is  $\simeq 0.1$ .

## C. Effect of Teacher Model

In this section, we explore alternative choices of the teacher  $\tau$ . We use XCL-Mix with the same training setup as Section 5.2. We compare alternative choices of teacher in Table 2. Each teacher is an ensemble of 8 instances of the given model, trained with different initializations. We observe a general trend that a more accurate teacher results in a more accurate student. [11] observed that when teacher

teacher	Ĥ (%)	teacher top-1 (%)	student top-1 (%)
ResNet-18	23.4	81.4	$80.2\pm0.1$
+LS ε=0.1	44.9	82.5	$80.9\pm0.2$
+MixUp	31.0	83.1	$81.1\pm0.2$
+CutMix	28.2	84.6	$83.1\pm0.2$
Pyr.+CutMix	15.1	87.5	$83.8\pm0.1$

Table 2: Analysis of different teachers. Each teacher is an ensemble of 8 models shown in each row.

is trained with Label Smoothing (LS), it is more accurate, but can transfer less knowledge to the student. We observe that using XCL, a teacher trained with LS not only is more accurate but also trains a more accurate student.

#### **D.** Analysis of Student Size

We investigate the effect of student size on the performance of XCL and other baseline methods. Figures 1a and 1b show the student model accuracy as a function of model size (changed by scaling the channel widths) for both a full precision student and a binary quantized student, respectively. As seen, XCL consistently outperforms ERM and MixUp augmentation, as well as the standard KD which uses the empirical distribution as the transfer-set. It is also worth mentioning that the binary model has a better errorsize trade-off curve compared to the full precision model.

### E. Label Smoothing

Label smoothing (LS) [16] with parameter  $\varepsilon$  replaces ground truth labels with:

$$y^{j} = 1 - \varepsilon$$
 if: *j* is the correct class else:  $\frac{\varepsilon}{c-1}$  (1)

This method artificially increases label entropy. The results of ERM training with LS are reported in Table 3. For all experiments we use the CIFAR100 dataset and ResNet18 architecture as described in Section 5.2. Using  $\epsilon =$ 0.1, LS achieves 1.5% improvement over the baseline. Note that, finding an optimal  $\epsilon$  requires extensive hyperparameter tuning. XCL naturally obtains smooth labels, and without hyper-parameter tuning obtains significant accuracy improvement (by 3.8%) compared to the best LS.

# F. Knowledge Distillation with Temperature Scaling

In KD [7], logits of the student and the teacher are inversely scaled by a temperature parameter T before softmax probabilities are computed. This smoothing strategy can slightly improve the knowledge distillation accuracy (+1.2% compared to KD without temperature scaling). We

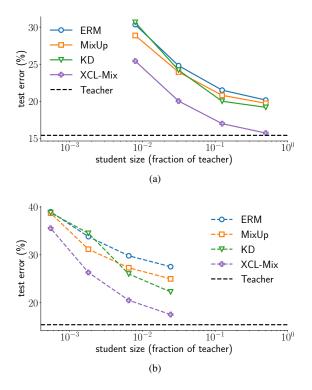


Figure 1: Test error as a function of student model size for (a) full-precision and (b) binary training.

ε	$\hat{H}$ (%)	top-1 (%)
0.1	17.0	$79.3\pm0.3$
0.18	28.2	$78.8\pm0.2$
0.4	54.5	$78.0\pm0.3$
0.8	90.7	$78.3\pm0.2$

Table 3: Effect of label smoothing on ERM.

Т	Ĥ (%)	top-1 (%)
1	10.5	$80.0\pm0.2$
1.5	52.8	$79.9\pm0.3$
2	81.2	$80.2\pm0.1$
5	99.2	$81.2\pm0.3$
10	99.9	$81.1\pm0.3$

Table 4: Effect of temperature on KD.

use the CIFAR100 dataset and ResNet18 architecture as described in Section 5.2. Results are reported in Table 4.

We observe that XCL is not sensitive to temperature (Table 5). Note that finding an optimal T requires extensive hyper-parameter tuning. XCL does not require hyper-parameter tuning, and compared to the best KD with temperature scaling reduces the accuracy gap by 59%.

Т	$\hat{H}$ (%)	top-1 (%)
1	28.2	$83.1\pm0.2$
1.5	65.0	$83.0\pm0.1$
2	85.8	$83.1\pm0.2$
5	99.2	$83.2\pm0.2$
10	99.9	$83.1\pm0.1$

Table 5: Effect of temperature on XCL.

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