All-photon Polarimetric Time-of-Flight Imaging

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Abstract

Time-of-flight (ToF) sensors provide an image modality fueling diverse applications, including LiDAR in autonomous driving, robotics, and augmented reality. Conventional ToF imaging methods estimate depth by sending pulses of light into a scene and measuring the ToF of the first-arriving photons directly reflected from a scene surface without any temporal delay. As such, all photons following this first response are typically considered as unwanted noise. In this paper, we depart from the principle of using first-arriving photons and propose an all-photon ToF imaging method that relies on the temporal-polarimetric analysis of first- and late-arriving photons which encode rich scene information in terms of geometry and material. To this end, we propose a novel temporal-polarimetric reflectance model, an efficient capture method, and a reconstruction method that exploits the temporal-polarimetric changes of light reflected by the surface and sub-surface reflection. The proposed all-photon polarimetric ToF imaging method allows us to acquire depth, surface normals, and material parameters of a scene by utilizing all photons captured by the system, whereas conventional ToF imaging only obtains coarse depth from the first-arriving photons. We validate our method in simulation and experimentally with a prototype system.

1. Introduction

Depth cameras have equipped us with the ability to acquire scene geometry that is essential for 3D vision both directly as a geometric input to a perception or reconstruction method, and indirectly, as training data for supervised learning in rich 3D vision datasets \cite{9,11,42}. As such, depth sensor have fueled diverse applications across domains, including autonomous vehicles, virtual and augmented reality, mobile photography, and robotics. A large body of prior work explores different approaches to extract depth, including parallax \cite{37}, defocus \cite{23}, double refraction \cite{4}, and correlation imaging \cite{22}. In particular, pulsed ToF cameras \cite{32} have been rapidly adopted across application domains for their high depth precision, low baseline, long range and robustness to scene texture.

ToF cameras directly measure the round-trip return time of light emitted into a scene. This requires high-speed sensors and electronics that can time-tag photon arrival events, such as single-photon avalanche diode (SPAD) and time-correlated single-photon counting (TSCPC) electronics. By repeating pulses and recording arrival events hundreds of thousands of times per measurement, these pulsed ToF cameras are capable of recording an entire temporal histogram for each pixel, reporting the number of photons detected by the sensor for each travel time bin.

Photons that arrive at different times at a single pixel can be broadly categorized into two temporally distinct components that sum up to the total measured photons. The first group of photons originates from the light directly reflected off from an object surface. Therefore, this surface reflection allows for estimating the object depth directly from its ToF measurement. Surface reflection often has higher intensity in comparison to the other component. As a result, one common practice for ToF depth imaging is to estimate
the ToF through peak-finding over the photon counts. In contrast to the surface reflection, the second group of photons comes from the light that penetrates the object surface, undergoes sub-surface scattering, and leaves the surface towards the detector. This sub-surface scattered light arrives at the sensor with a longer travel time than the light originating from surface reflections. At first glance, sub-surface scattering appears to harm accurate depth estimation as it disturbs the true ToF by an additional unknown scattering time. Existing ToF methods typically discard this sub-surface observation and only rely on the surface reflection.

In this work, we treat this sub-surface scattering component as a signal instead of noise in estimating geometric and material properties of a scene. The proposed all-photon ToF imaging method combines ToF imaging with polarization analysis, exploiting the unique temporal-polarimetric signature of surface and sub-surface reflections, as shown in Figure 1. The proposed method hinges on a novel temporal-polarimetric bidirectional reflectance distribution function (BRDF) model that describes both surface and sub-surface reflections in temporal and polarimetric domains. We implement this BRDF model with differentiable operators allowing us to pose scene reconstruction as an inverse rendering problem. To efficiently acquire high-dimensional polarimetric-temporal data, we also propose a light-efficient temporal-polarimetric acquisition approach that captures the temporal-polarimetric signals of a scene combined with a learned optical ellipsometry. We demonstrate that all-photon polarimetric ToF imaging can record diverse scene information, including depth, normals, and material parameters from temporal-polarimetric measurements – both in simulation and experimentally. Specifically, we make the following contributions.

- We devise an all-photon polarimetric ToF imaging method that combines ToF imaging and polarization analysis to jointly exploit surface and sub-surface reflected photons for scene reconstruction.
- We present the first temporal-polarimetric BRDF model which characterizes surface and sub-surface reflection based on micro-facet theory and the Stokes-Mueller formalism.
- We propose an efficient temporal-polarimetric acquisition approach tailored for polarimetric imaging with polarized-laser illumination.
- We validate our method in simulation and with an experimental prototype for capturing depth, normals, and material parameters.

Limitations As a result of the mechanical rotation of the polarizing optics and sequential scanning, the acquisition of the temporal-polarimetric data takes five hours for each scene. We note that the limited number of temporal-polarimetric photons and low sensor quantum efficiency makes the acquisition challenging. In the future, accelerating the polarimetric capture with electronically-controllable liquid crystal modulators instead of mechanically rotating polarizers, or using a polarization array filters placed on photon-efficient SPAD sensor arrays, may eliminate the need for sequential acquisition. Our experimental prototype employs a laser module with low average power of 0.13 mW available to us. We note that higher-power laser sources are commercially available which could increase the signal-to-noise ratio of the measurements for a given exposure time budget.

2. Related Work

ToF Imaging Modern ToF imaging methods can be broadly categorized into correlation and pulsed approaches. Correlation ToF methods emit intensity-modulated light into a scene and indirectly estimate the round-trip time of the light returned back to the sensor by performing intensity demodulation [22, 49]. In contrast, pulsed ToF methods directly measure ToF of light in an emitted pulse. These methods combine picosecond-pulsed illumination with time-resolved sensors, such as a SPAD, synchronized with the laser using TSCPC electronics [15, 26]. Not only have pulsed ToF approaches been deployed broadly for LiDAR systems in autonomous vehicles [40], robotics [21], and space missions [1], but recently in consumer mobile phones such as the iPhone 12 Pro. Typical LiDAR sensors extract depth by reporting a detection event for the first-arriving photons among all photons reflected from a scene surface. To this end, existing methods implement peak finding via analog thresholding [40], spatial coherence [31], temporal coherence [41], and learned priors [24]. This acquisition principle also means that photons arriving later are ignored, along with rich material and geometric information that these photons carry about the scene. Researchers have attempted to utilize this hidden information by modeling a more comprehensive temporal response of a scene with analytic temporal BRDF models [35, 36, 48]. However, temporal-only analysis restricts them to only extracting scene depth from the fitted first-arriving photons, while the later arriving photons are only used for obtaining a better fit of the first-arriving photons. In contrast, we analyze all detected photons by jointly analyzing their polarization and temporal characteristics to extract geometric and material properties of a scene.

Polarimetric Imaging A rich body of work has explored using polarization of light for various visual-computing tasks. Early works rely on cross-polarization, which equips illumination and detector with orthogonal polarization filters. This allows for separating polarized reflection from
unpolarized reflection, or vice versa [28, 38]. This principle has led to many applications such as seeing through scattering media [44] and diffuse-specular separation [13, 25]. Recently, polarization cameras with spatially multiplexed linear polarizers have been used for the acquisition of surface normals [2, 19]. These methods explicitly or implicitly rely on polarimetric BRDFs that couple local geometry to a polarization response [6, 7]. Combining polarization andToF imaging has largely been an unexplored field. Callenberg et al. [8] investigated polarization-difference imaging by configuring a two-illumination correlation ToF camera in a cross-polarization mode. Most relevant to our work, Baek et al. [5] combine polarization imaging and ToF imaging to capture the temporal-polarimetric response of a scene. Their method is unable to extract geometry and reflectance from the measurements due to the absence of a temporal-polarimetric BRDF model that links the scene parameters to the observation. We close this gap in this work and introduce the first temporal-polarimetric BRDF model, which makes it possible to estimate scene parameters directly from temporal-polarimetric observations.

Polarization LiDAR Interestingly, combining polarization with ToF imaging has been studied for decades in geoscience [34]. Notably, researchers in cloud science have applied polarization analysis to LiDAR systems in order to examine cloud properties and aerosol concentration by sending out polarized laser pulses to the cloud and measure how much of returned light, at a given travel time, is depolarized [14, 33, 47]. This principle, first studied by Schotland et al. [39], has led to remarkable success, not only in cloud analysis but also in other fields, including biology [17] and ocean science [45]. The proposed method shares this motivation in that we combine polarization and ToF imaging, however, we tackle the problem of scene reconstruction.

3. Temporal-polarimetric Light Transport

The proposed method hinges on a novel analytical model for temporal-polarimetric light transport, which we introduce in this section. Our model is the first to describe both surface and sub-surface reflection based on the Stokes-Mueller formalism. We represent polarized light and reflectance with a Stokes vector and a Mueller matrix [10].

3.1. Temporal-polarimetric Reflectance

We introduce a temporal-polarimetric reflectance model $M(\tau, \omega_1, \omega_o)$. This model describes how light polarization and intensity change when impinging on a surface with given incident and outgoing direction of light ($\omega_1$ and $\omega_o$), and with temporal delay upon the arrival of incident light ($\tau$). Specifically, we model reflectance $M$ as a sum of sur-

![Figure 2. We introduce the first temporal-polarimetric reflectance model which explains the total reflection (left) as a sum of the temporal polarization change of surface (middle) and sub-surface reflections (right). Here, we visualize an example reflectance function in the form of a temporal-polarimetric Mueller matrix. Time-varying Mueller matrix elements are shown in the second and third rows for diagonal and non-diagonal elements, respectively.](image-url)
where the GGX normal distribution function [46], we arrive at the proposed temporal-polarimetric surface-reflection model

\[ M_s(\tau, \omega_1, \omega_2) = \frac{D(\theta_h; \sigma)G(\theta_c, \theta_o; m)}{4 \cos \theta_c \cos \theta_o} D^s(\tau) F_R, \quad (2) \]

where \( \theta_h = \cos^{-1}(h \cdot n) \) is the halfway angle, \( n \) is the normal, \( m \) is the roughness, and \( \theta_c = \cos^{-1}n \cdot \omega_1 \) and \( \theta_o = \cos^{-1}n \cdot \omega_2 \) are the incident/outgoing angles.

Sub-surface Reflection The second type of reflection originates from the light transmitted into the object. The transmitted light undergoes sub-surface scattering and eventually leaves the object. The Fresnel-transmission Mueller matrix \( F_T \) [10] describes the polarization change of light passing through the interface between the two mediums (air and bulk material). Back et al. [6] combined this Fresnel matrix with a perfect depolarization Mueller matrix to describe sub-surface reflection with an assumption that light becomes completely unpolarized after sub-surface scattering. However, in reality, depolarization by sub-surface scattering is highly correlated with the path length of light; sub-surface scattering with longer path lengths results in more depolarization [12]. Modeling this behavior is essential for the proposed temporal-polarimetric imaging method because path length determines the temporal delay. To this end, we model sub-surface scattering with time-varying depolarization. We use time-varying Gaussian distributions as the diagonal elements of a depolarization Mueller matrix \( D^s(\tau) \) similar to the surface-reflection model with the parameters \( \mu_s^s, \sigma_s^s \). For sub-surface scattering, we also consider the coordinates of Stokes vectors. As a Stokes vector of light can only be defined in a basis coordinate system [10], we use the halfway coordinate approach [7]. For more details on the coordinate conversion, see the Supplemental Document.

With all components described above, we define our temporal-polarimetric sub-surface reflection model

\[ M_{ss}(\tau, \omega_1, \omega_2) = C_{n \rightarrow s} F_T^s D^s(\tau) F_T^s C_{i \rightarrow n}, \quad (3) \]

where \( C_{i \rightarrow n} \) and \( C_{n \rightarrow s} \) are the coordinate-conversion Mueller matrices from the halfway coordinate of incident and outgoing light to the surface normal coordinate [10]. Here, \( F_T^s \) and \( F_T^s \) are the Fresnel transmission Mueller matrices for the incident and outgoing light which both depend on the refractive index of the material \( \eta \). Note that our surface-reflection model does not require coordinate conversion, as surface reflection is already defined in halfway coordinates following microfacet theory [43].

3.2. Temporal-polarimetric Rendering

The proposed temporal-polarimetric reflectance model returns a Mueller matrix \( M(\tau, \omega_1, \omega_2) \) at a temporal delay \( \tau \) and incident and outgoing directions, \( \omega_1 \) and \( \omega_2 \). Incorporating this Mueller matrix into the rendering equation [20] describes the Stokes vector of the outgoing light at each temporal delay as

\[ s_o(\omega_2, t) = \int_{S_2} \int_{0}^{t} \cos \theta_c M(\tau, \omega_1, \omega_2) s_i(\omega_1, t - \tau) d\tau d\omega_1 \]

where \( H(\tau, \omega_1, \omega_2) = s_i(\omega_1, t - \tau) d\tau d\omega_1, \quad (4) \]

where \( H(\tau, \omega_1, \omega_2) \) is the Mueller matrix scaled by the cosine fore-shorting. As such, the Stokes vector of the outgoing light \( s_o(\tau, t) \) is the function of time and propagation direction.

4. Polarimetric ToF Imaging

We now turn to developing a polarimetric ToF imaging system to capture a temporal-polarimetric scene response.

Coaxial ToF Imaging Although the proposed method is not restricted to a specific time-resolved sensing system, we opt to use a pulsed laser illumination and a synchronized SPAD sensor in a coaxial configuration typical to LiDAR systems [40]. This means that the illumination and detection share the same optical path to optically sample direct illumination with minimal indirect illumination by interference. This allows us to simplify the rendering equation (4) by removing the outer integral over direction, that is

\[ I(t, \omega) = \left[ \int_{0}^{t} H(\tau, \omega, \omega)s_{\text{illum}}(\omega, t' - \tau) d\tau \right]_{0}^{1} \]

where \( I(t, \omega) \) is the captured intensity of light with ToF \( t \) along the direction \( \omega \). The term \( x_0 \) denotes the first element of a Stokes vector \( \mathbf{x} \), \( c \) is the speed of light, and \( s_{\text{illum}}(\omega, t) \) is the Stokes vector of the laser illumination. Here, \( t' \) is the shifted time by the ToF \( t' = t - \frac{2d}{c} \), where \( d \) is the Euclidean distance between the collocated laser at position \( 0 \), set to the origin without loss of generality, and a scene point \( p = 0 + d\omega \). In addition, the second integral over the temporal dimension is simplified as a result of using pulsed laser illumination.

Rotating Ellipsometry for Polarized Illumination Starting with the coaxial ToF imaging systems described above, we acquire the complete polarization change induced by light-matter interaction using rotating optical ellipsometry [10]. Rotating optical ellipsometry commonly incorporates pairs of linear polarizers (LP) and quarter-wave plates (QWP) in front of an unpolarized illumination source and a detector [3, 5]. Multiple intensity measurements \( I_{i \in \{1, \ldots, N\}} \) are then captured by rotating
Alyzing optics and the polarizing optics defined as $A$ where vectors (the Poincaré sphere of the polarizing (c) and analyzing (d) Stokes captures than conventional ellipsometry methods. We visualize which allows us to reconstruct polarimetric reflectance with fewer captures than conventional ellipsometry methods. We visualize the Poincaré sphere of the polarizing (c) and analyzing (d) Stokes vectors ([P]i, [A]i) before and after learning.

Figure 3. Energy-efficient Polarimetric ToF Imaging. (a) For a polarimetric capture, we rotate a HWP instead of a LP to preserve the light intensity of the polarized source. (b) We learn the rotation angles of the polarizing optics with uniform initialization (see text) which allows us to reconstruct polarimetric reflectance with fewer captures than conventional ellipsometry methods. We visualize the Poincaré sphere of the polarizing (c) and analyzing (d) Stokes vectors ([P]i, [A]i) before and after learning.

The proposed temporal-polarimetric image formation model explains how geometric and material parameters of a scene relate to our sensor measurements in the presence of surface and sub-surface reflections. This allows us to solve the corresponding inverse problem: Given the temporal-polarimetric sensor measurements $I_i$, we estimate a set of scene parameters $\Theta$, including travel distance ($d$), surface normals ($n$), refractive index ($\eta$), surface roughness ($m$), and scattering parameters ($a_i^{ss}, a_i^{s/s}, a_i^{s/s}, \mu_i^{s/s}, \sigma_i^{s/s}$): $\Theta = \{d, n, \eta, m, a_i^{ss}, a_i^{s/s}, a_i^{s/s}, \mu_i^{s/s}, \sigma_i^{s/s}\}$. Note that conventional ToF imaging methods estimate travel distance by measuring the round-trip time of the first-returning photons with digital or analog peak-finding methods. In contrast, we do not discard photons that are arriving later and exploit the temporal-polarimetric information in the surface and subsurface reflections to reconstruct a scene.

5. All-photon Scene Reconstruction

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Ellipsometric Reconstruction We first convert the temporal measurements $I_i$ for all the rotation angles of the polarizing optics into a time-varying Mueller matrix $H_{\text{meas}}$. To this end, we invert the image formation model of Equation (6) in a least-squares manner following Baek et al. [7], solving the following optimization problem for each spatio-temporal pixel

$$\minimize_{H_{\text{meas}}} \sum_{i=1}^{N} (I_i - [A_i H_{\text{meas}} P_i s_{\text{illum}}]_0)^2.$$
Scene Reconstruction

Once we have obtained the Mueller matrix $H_{\text{meas}}$ for each temporal bin $t$ and coaxial incident/outgoing direction $\omega$, we estimate the scene parameters $\Theta$ best explaining the Mueller matrix $H_{\text{meas}}$, that is

$$\min_{\Theta} \| W_p \odot (f(\Theta) - H_{\text{meas}}) \|_1 + \| W_d \odot \nabla n \|_1,$$  (8)

where $x$ is the stacked vector of pixel quantities of variable $x$ for each temporal bin, spatial direction, and Mueller matrix element. Here, $\odot$ is the Hadamard product, and $\nabla$ is the spatial gradient operator. The data term evaluates the predicted Mueller matrix using the forward rendering function $f(\Theta) = H(\tau, \omega, \omega, \Theta)$. The matrix $W_p$ weights the diagonal/non-diagonal Mueller matrix elements due to their different scales, see Supplemental Document for details. The regularization term penalizes steep surface normal changes in the spatial dimension. The matrix $W_d$ is a weighting matrix that penalizes the occlusion edges. With the objective in Equation (8) being differentiable with respect to the scene parameters $\Theta$, we solve it using the first-order Adam optimization [30].

To circumvent the ill-posedness of Equation (8), we propose the three following modifications. First, we take a regional approach commonly used in inverse rendering methods [6, 27]. That is, while surface normals and travel distance are per-pixel quantities, we define refractive index, surface roughness, and scattering parameters as per-material quantities specified by a given cluster map. This reduces the total parameter count. We compute the cluster map based on the per-pixel average intensity using $k$-means clustering. Second, we incorporate the unit-norm and range constraints of each scene parameter to reduce the parameter search space with vector normalization and scaled sigmoid functions, see Supplemental Document for details. Third, we initialize the travel distance $d$ and surface normals $n$ with conventional peak-finding outputs from the unpolarized ToF measurements corresponding to the first element of the Mueller matrix $|H_{\text{meas}}|_{00}$.

6. Experimental Setup

Figure 4 shows our experimental prototype. We use a picosecond pulsed laser of optical wavelength 635 nm (Edinburgh Instruments EPL-635) and a SPAD sensor (MPD Series) with 25 ps temporal resolution. A time-correlation circuit (PicoQuant TimeHarp 260 PICO) synchronizes the laser and the SPAD. Light emitted from the laser passes through a half-wave plate (Thorlabs AHWP10M-600) and a quarter-wave plate (Thorlabs AQWP10M-580). A galvo mirror (Thorlabs GVS012) redirects the beam to a scene. We use a non-polarizing beamsplitter (Thorlabs BS013) to implement a coaxial configuration. Another quarter-wave plate and a linear polarizer (Newport 10LP-VIS-B) modulate the returning light. We use a 50 mm objective lens for the SPAD sensor, and mount the polarizing optics on motorized rotary stages (Thorlabs KPRM1E). We implement capture and reconstruction in Matlab and Pytorch.
7. Assessment

Temporal-polarimetric BRDF  To evaluate the representation capacity of our temporal-polarimetric BRDF model, we capture a spherical object and reconstruct its corresponding Mueller matrix for each time bin: \( \mathbf{H}_{\text{meas}}(t, \omega, \omega') \). We then find the scene parameters \( \Theta \) of a spherical object, which best explains the observed temporal Mueller matrices, resulting in the reconstructed Mueller matrix \( \mathbf{H}(t, \omega, \omega'; \Theta) \). We further convert \( \mathbf{H} \) to another Mueller matrix \( \mathbf{H}' \) so that it follows similar noise statistics of the measured Mueller matrix \( \mathbf{H}_{\text{meas}} \) by simulating the sensor measurements \( I'_i \) with the reconstructed Mueller matrix \( \mathbf{H} \) and again reconstructing this Mueller matrix. The experiment in Figure 5 validates that the measured temporal-polarimetric data from our prototype matches simulated data from the proposed BRDF model. In particular, our model predicts the normal-dependent temporal-polarimetric structure of sub-surface reflection at the boundaries of the spherical object in \( \mathbf{H}'_{\{i,0\},\{0,i\},v_1} \). We also see the sign changes of the circular polarimetric sub-surface and surface reflection in \( \mathbf{H}_{3,3} \).

Synthetic Evaluation  We evaluate the proposed method on three synthetic scenes shown in Figure 6. As ground-truth scene parameters \( \Theta \) for the synthetic scenes are known, we simulate the synthetic sensor measurements \( I_i \) using the image formation model from Equation (6). Here, we add Gaussian noise with a standard deviation of \( 10^{-4} \) to simulate measurement noise. With the simulated observations in hand, we solve Equation (8) by performing the proposed all-photon scene reconstruction, that is ellipsometric reconstruction of the temporal-polarimetric Mueller matrix \( \mathbf{H}_{\text{meas}} \) and scene reconstruction. Figure 6 validates that our reconstruction approach estimates geometric and material parameters accurately, both qualitatively and quantitatively. For additional results, we refer to the Supplemental Document.

Experimental Evaluation  Next, we validate the proposed method on the additional real-world scenes shown in Figures 7 and 8. We reconstruct the temporal-polarimetric Mueller matrix \( \mathbf{H}_{\text{meas}} \) from experimental measurements \( I_i \), followed by finding the optimal scene parameters \( \Theta \). Our all-photon polarimetric ToF imaging reconstructs travel distance estimates that correspond to per-point depth and surface normals. We also acquire scattering parameters of the scene. Together with the obtained geometry, the proposed method accurately reconstructs the original measurements.
Figure 7. Experimental Validation. We validate our all-photon polarimetric ToF imaging on real-world scenes. (a) Conventional peak-finding ToF imaging methods acquire scene depth from first-reflected photons only, resulting in inaccurate geometry reflected in imperfect depth and surface normals estimates. In contrast, the proposed method relies on all photons, enabling (b) accurate geometry reconstruction and the recovery of material parameters by (c) decomposing light transport into surface and sub-surface components.

Figure 8. Material Editing. We edit the material parameters reconstructed from our polarimetric ToF imaging. Specifically, we change the scattering parameters of sub-surface and surface reflection as well as the surface roughness. We refer to the text for details.

Figure 7 shows the rendered measurements with our estimated parameters $\Theta$ and the corresponding sensor measurements. Our scene reconstructions and the proposed reflectance model also facilitate material editing, which we demonstrate with three editing examples in each column of Figure 8. Specifically, we first change the sub-surface scattering parameters by boosting $a_i \leftarrow 3a_i$, and changing its polarization-dependent temporal shift to $\mu \leftarrow [0.1\mu_0, 2\mu_1, 2\mu_2, 2\mu_3]$. This results in stronger sub-surface scattering. We then edit the surface scattering parameters in the same fashion, but only doubling $a_i \leftarrow 2a_i$. This mimics a material with stronger surface reflection. Lastly, increasing the surface roughness provides the appearance of rough surface with a dominating sub-surface reflection.

8. Conclusion

We introduce an all-photon polarimetric ToF imaging method, which extracts information from both surface and sub-surface reflection for acquiring geometry and scattering parameters. To this end, we propose the first temporal-polarimetric BRDF model, which relates sensor measurements to geometric and scattering parameters of a scene. The proposed learned ellipsometric ToF imaging system permits the acquisition of temporal-polarimetric data with energy-efficient polarimetric modulation. We reconstruct scene parameters from all photons instead of the first reflected ones. We validate the proposed method in simulation and experimentally. Although we validate the utility of temporal-polarimetric measurements, our experimental setup is restricted to sequential scanning by the mechanical rotation of the polarization optics available to us. Exciting future directions include the extension of the proposed system with electronically-controllable liquid crystal modulators, or combining SPAD array sensors with polarization filter arrays, which may pave the way towards single-shot temporal-polarimetric acquisition. Aside from making a step towards high-dimensional computational imaging, the approach may also pave the way for practical implementation such as gated imaging with polarization cues as a low-cost automotive imaging modality.

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References


