## A1. More Technical Details

We summarize the detailed procedures of Aug-NeRF in the Algorithm 1.

```
Algorithm 1 The training pipeline of Aug-NeRF. For sim-
plicity, we assume batch size is 1 .
Initialize: Training view images \(\mathcal{I}=\left\{\boldsymbol{I}_{i} \in \mathbb{R}^{M}\right\}_{i=1}^{N}\) and
    their associated camera poses \(\mathcal{P}=\left\{\phi_{i} \in \mathbb{R}^{3 \times 4}\right\}_{i=1}^{N}\).
    Define neural radiance field \(F_{\Theta}(\boldsymbol{p}, \boldsymbol{\theta})=(g \circ f(\boldsymbol{p}, \boldsymbol{\theta}), h \circ\)
    \(f(\boldsymbol{p})):(\boldsymbol{p}, \boldsymbol{\theta}) \mapsto(\boldsymbol{c}, \sigma)\) as in Sec. 4.2.
    Cast rays for each pixel in each \(I_{i}\) via inverse pro-
    jection with respect to \(\phi_{i}\), and obtain a set of rays
    \(\mathcal{R}=\left\{\left(\boldsymbol{o}_{i}, \boldsymbol{d}_{i}, \boldsymbol{\theta}_{i}, \widehat{\boldsymbol{C}}_{i}\right)\right\}_{i=1}^{N M}\).
    while until convergence do
        Randomly pick a ray \(\left(\boldsymbol{o}_{i}, \boldsymbol{d}_{i}, \boldsymbol{\theta}_{i}, \widehat{\boldsymbol{C}}_{i}\right) \in \mathcal{R}\)
        Generate adversarial perturbations \(\delta_{t}, \boldsymbol{\delta}_{x y z}, \boldsymbol{\delta}_{\theta}, \boldsymbol{\delta}_{f}\),
    \(\boldsymbol{\delta}_{c}, \delta_{\sigma}\) by solving Eqn. 4 using PGD (Eqn. 5) within the
    corresponding search space in Sec. 4.2.
        \# Sample points along rays.
        (Coarse) Sample \(K / 2\) depth intervals \(t_{k}\) along the
    rays uniformly
        (Fine) Sample \(K / 2\) depth intervals \(t_{k}\) via propor-
    tional to coarse sampled densities [29].
        for \(k \in\{1, \cdots, K\}\) do
            \(t_{k}^{\dagger}=t_{k}+\delta_{t, k}, \boldsymbol{\theta}_{i}^{\dagger}=\boldsymbol{\theta}_{i}+\boldsymbol{\delta}_{\theta}\).
            \(\boldsymbol{p}_{k}=\boldsymbol{o}_{i}+t_{k} \boldsymbol{d}_{i}, \boldsymbol{p}_{k}^{\dagger}=\boldsymbol{o}_{i}+t_{k}^{\dagger} \boldsymbol{d}_{i}+\boldsymbol{\delta}_{x y z}\)
            \(\left(\boldsymbol{c}_{k}, \sigma_{k}\right)=g \circ f\left(\boldsymbol{p}_{k}, \boldsymbol{\theta}_{i}\right), h \circ f\left(\boldsymbol{p}_{k}\right)\)
            \(\boldsymbol{c}_{k}^{\dagger}=g\left(f\left(\boldsymbol{p}_{k}^{\dagger}\right)+\boldsymbol{\delta}_{f}, \boldsymbol{\theta}_{i}^{\dagger}\right)+\boldsymbol{\delta}_{c}\)
            \(\sigma_{k}^{\dagger}=h\left(f\left(\boldsymbol{p}_{k}^{\dagger}+\boldsymbol{\delta}_{f}\right)\right)+\boldsymbol{\delta}_{\sigma}\)
        end for
        \# Volumetric rendering.
        \(\left(\Delta t_{k}, \Delta t_{k}^{\dagger}\right)=t_{k}-t_{k-1}, t_{k}^{\dagger}-t_{k-1}^{\dagger}\)
        \(T(k)=\exp \left(-\sum_{l=1}^{k-1} \sigma_{l} \Delta t_{l}\right)\)
        \(T^{\dagger}(k)=\exp \left(-\sum_{l=1}^{k-1} \sigma_{l}^{\dagger} \Delta t_{l}^{\dagger}\right)\)
        \(\boldsymbol{C}_{i}=\sum_{k=1}^{K} T(k)\left(1-\exp \left(-\sigma_{k} \Delta t_{k}\right)\right) \boldsymbol{c}_{k}\)
        \(\boldsymbol{C}_{i}^{\dagger}=\sum_{k=1}^{K} T^{\dagger}(k)\left(1-\exp \left(-\sigma_{k}^{\dagger} \Delta t_{k}^{\dagger}\right)\right) \boldsymbol{c}_{k}^{\dagger}\)
        \# Train network.
        \(\mathcal{L}=\left\|\boldsymbol{C}_{i}-\widehat{\boldsymbol{C}}_{i}\right\|_{2}^{2}+\lambda\left\|\boldsymbol{C}_{i}^{\dagger}-\widehat{\boldsymbol{C}}_{\boldsymbol{i}}\right\|_{2}^{2}\)
        Update network parameter \(\Theta\) via \(\nabla_{\Theta} \mathcal{L}\).
    end while
```


## A2. More Experiment Results

Qualitative results on NeRF-Synthetic $\mathbf{3 6 0}{ }^{\circ}$ dataset. We present the constructed test views in Fig. A8 and the learned depth maps in Fig. A9. As shown in Fig. A8, we find that the vanilla NeRF fails to capture the fine-grained details of objects, such as the "ship net", while Aug-NeRF demonstrates substantially improved visual qualities.

In the meantime, from the depth maps in Fig. A9, NeRF


Figure A8. Comparisons on test-set views for scenes from the NeRF-Synthetic $360^{\circ}$ dataset generated with a physics-based renderer [29].
baseline suffers from severe noises. On the contrary, AugNeRF enjoys much more smooth depth maps, which suggests that our proposed triple-level robust augmentations indeed enhance the NeRF's continuity and generate smooth geometry representations.


Figure A9. Comparisons of learned depth maps from NeRF and our Aug-NeRF on scenes from NeRF-Synthetic $360^{\circ}$ dataset.

Benefits in overfitting vs underfitting cases. We take the scene "chair" as an example, and investigate three combinations of different model sizes and data scales as below Tab. A5: ( $i$ ) big NeRF (512) on small images ( $\frac{1}{2}$ Res.); (ii) normal NeRF (256) on small images ( $\frac{1}{2}$ Res.); (iii) small NeRF (128) on large images (Full Res.). We show that in all settings of overfitting / normal case / underfitting, our
proposed augmentations are consistently beneficial.

Table A5. Performance of Aug-NeRF on different backbone and data size combinations.

| Setting | Model | PSNR $\uparrow$ | SSIM $\uparrow$ | LPIPS $\downarrow$ | Average $\downarrow$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| Big NeRF (512) | NeRF | 33.56 | 0.968 | 0.043 | 0.015 |
| $+\frac{1}{2}$ Res. | Aug-NeRF (Ours) | $\mathbf{3 4 . 2 6}$ | $\mathbf{0 . 9 7 3}$ | $\mathbf{0 . 0 3 8}$ | $\mathbf{0 . 0 1 3}$ |
| Big NeRF (256) | NeRF | 33.27 | 0.968 | 0.045 | 0.016 |
| + $\frac{1}{2}$ Res. | Aug-NeRF (Ours) | $\mathbf{3 3 . 9 2}$ | $\mathbf{0 . 9 7 1}$ | $\mathbf{0 . 0 3 8}$ | $\mathbf{0 . 0 1 3}$ |
| Small NeRF (128) | NeRF | 33.00 | 0.967 | 0.046 | 0.016 |
| + Full Res. | Aug-NeRF (Ours) | $\mathbf{3 3 . 8 6}$ | $\mathbf{0 . 9 7 0}$ | $\mathbf{0 . 0 4 1}$ | $\mathbf{0 . 0 1 4}$ |

Geometry extraction. To obtain geometric visualization in Fig. 5, we first query the network $F_{\Theta}$ with a regular lattice defined over $[-1,1]^{3}$, and export a discretized density field volume. The absolute voxel size is $2 / 512$. Then we employ marching cube algorithm [22] provided in UCSF Chimera ${ }^{2}$ to extract the surface. We set the threshold to 25 and 1 for chairs and drums, respectively. The step size is chosen as 1 . In order to numerically assess the quality of reconstructed geometries, we introduce Chamfer Distance (CD) to measure the difference between reconstructed geometries and groundtruth models:
$d_{C D}=\frac{1}{\left|\mathcal{S}_{1}\right|} \sum_{\boldsymbol{x} \in \mathcal{S}_{1}} \min _{\boldsymbol{y} \in \mathcal{S}_{2}}\|\boldsymbol{x}-\boldsymbol{y}\|_{2}+\frac{1}{\left|\mathcal{S}_{2}\right|} \sum_{\boldsymbol{x} \in \mathcal{S}_{2}} \min _{\boldsymbol{y} \in \mathcal{S}_{1}}\|\boldsymbol{x}-\boldsymbol{y}\|_{2}$,
where $\mathcal{S}_{1}$ and $\mathcal{S}_{2}$ are point sets sampled from the extracted surfaces and ground-truth models, respectively. On scene chair, our AugNeRF achieves $1.04 \times 10^{-2} \mathrm{CD}$ which is $29.25 \%$ lower than vanilla $\operatorname{NeRF}\left(1.47 \times 10^{-2}\right)$.

Different types of noise and inaccurate camera poses. As shown in Tab. 3 and Fig. 6, we experiment on two kinds of corruptions, i.e., Gaussian and Shot noises. In this paragraph, we add extra results of training with Pepper noise and inaccurate camera poses are collected in below Tab. A6. The results consistently demonstrate the superiority of AugNeRF. We note that our main goal is to endow NeRF with smoothness-aware geometry reconstruction, enhanced generalization to synthesizing unseen views, while the improved tolerance of noisy supervisions is a by-product bonus.

Table A6. Additional results of Aug-NeRF trained on images corrupted by pepper noise and inaccurate camera poses.

| Noise Type | "fern" | PSNR $\uparrow$ | SSIM $\uparrow$ | LPIPS $\downarrow$ | Average $\downarrow$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| Pepper Noise | NeRF | 19.01 | 0.401 | 0.546 | 0.174 |
|  | Aug-NeRF (Ours) | $\mathbf{1 9 . 9 6}$ | $\mathbf{0 . 5 6 8}$ | $\mathbf{0 . 4 0 3}$ | $\mathbf{0 . 1 3 8}$ |
| Inaccurate Pose | NeRF | 12.31 | 0.253 | 0.725 | 0.333 |
|  | Aug-NeRF (Ours) | $\mathbf{1 3 . 5 4}$ | $\mathbf{0 . 3 6 5}$ | $\mathbf{0 . 8 1 1}$ | $\mathbf{0 . 3 0 6}$ |

Implementation of explicit regularization. We investigate three types of explicit regularizations: $\ell_{1}$ sparsity, total

[^0]variation (TV), and Laplacian. The TV regularization is defined as:
$$
R_{\mathrm{TV}}(\Theta)=\int_{[-1,1]^{3}}\left|\nabla_{\boldsymbol{x}} \sigma_{\Theta}(\boldsymbol{x})\right| d \boldsymbol{x}
$$
where $\sigma_{\Theta}$ denotes the density branch of the function $F_{\Theta}$. However, evaluating this integral is implausible. Instead, we discretize the integral interval into regular grids and conducting quadrature rule for estimating TV regularization:
$$
R_{\mathrm{TV}}(\Theta)=\sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N}\left|\nabla_{\boldsymbol{x}} \sigma_{\Theta}(\delta i, \delta j, \delta k)\right| \delta^{3},
$$
where we utilize auto-differentiation provided in PyTorch Library to calculate $\nabla_{\boldsymbol{x}} \sigma_{\Theta}$. Similarly, we can approximate $\ell_{1}$ sparsity and Laplacian regularization by:
\[

$$
\begin{aligned}
R_{\ell_{1}}(\Theta) & =\int_{[-1,1]^{3}}\left|\sigma_{\Theta}(\boldsymbol{x})\right| d \boldsymbol{x} \\
& \approx \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N}\left|\sigma_{\Theta}(\delta i, \delta j, \delta k)\right| \delta^{3} \\
R_{\mathrm{Lap}}(\Theta) & =\int_{[-1,1]^{3}}\left|\Delta_{\boldsymbol{x}} \sigma_{\Theta}(\boldsymbol{x})\right| d \boldsymbol{x} \\
& \approx \sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N}\left|\Delta_{\boldsymbol{x}} \sigma_{\Theta}(\delta i, \delta j, \delta k)\right| \delta^{3}
\end{aligned}
$$
\]

where $\Delta=\operatorname{div} \cdot \nabla$ denotes the Laplacian operator.


[^0]:    ${ }^{2}$ https://www.cgl.ucsf.edu/chimera/

