A. Implementation details

A.1. Pose Estimation (Section 3.2)

MLP $T_\Theta$ takes the positionally encoded frame id as input and outputs a vector of $9P$ dimensions. The $3P$ dimensions correspond to each element of $t_i$, and the remaining $6P$ dimensions correspond to $R_i$. For the rotation matrix calculation, please refer to Zhou et al. [13], Section B. $T_\Theta$ is a 4-layer MLP with a hidden dimension of 256.

A.2. SDF Computation of an Ellipsoid (Section 3.3)

The merit of using ellipsoids as the representation of the parts is that their SDFs are continuous functions and can be computed cheaply. In this subsection, we explain how to calculate the SDF of an ellipsoid. First, the surface of an ellipsoid of radii $r$ is given by

$$f(x, r) = \frac{x_1^2}{r_1^2} + \frac{x_2^2}{r_2^2} + \frac{x_3^2}{r_3^2} = 1,$$

where position $x = (x_1, x_2, x_3)$ and radii $r = (r_1, r_2, r_3)$. We calculate the SDF of an ellipsoid as follows. First, from the query point $x$, we find the nearest ellipsoid surface point $x_e$. Since this cannot be solved analytically, we use Lagrange’s multiplier method and Newton’s method to find the point. The cost function $\mathcal{L}$ is defined as

$$\mathcal{L} = |x - x_e|^2 - \lambda(f(x_e, r) - 1),$$

and we solve $\frac{\partial \mathcal{L}}{\partial x_e} = \frac{\partial \mathcal{L}}{\partial x} = 0$. This can be transformed into the following equations

$$\begin{align*}
    x_e &= r^2 \odot (r^2 + \lambda) \odot x, \\
    |r \odot (r^2 + \lambda) \odot x|^2 &= 1,
\end{align*}$$

where $\odot$ is element-wise division, $\odot$ is element-wise product, and $a^2 = a \odot a$. We use Newton’s method to find the largest solution for $\lambda$ in Equation 4 and substitute it into Equation 3 to get $x_e$.

The distance between the searched point and the input point $x$ is the absolute value of the SDF, which has a negative sign when $x$ is inside the ellipsoid and a positive sign when it is outside:

$$SDF(x, r) = \text{sign}(f(x, r) - 1)|x - x_e|^2.$$  \hspace{1cm} (5)

However, since $x_e$ is computed numerically, the gradient is not propagated to $r$. Therefore, we re-parametrize $x_e$ using $r$ by projecting $x_e$ onto the surface of the unit sphere and back onto the surface of the ellipsoid.

$$\hat{x}_e = (x_e \odot r)\text{.detach()} \odot r,$$  \hspace{1cm} (6)

where $\odot$ is element-wise division, $\odot$ is element-wise product, and detach() is a stop-gradient operation.

Finally, the differentiable SDF of an ellipsoid is computed as,

$$SDF(x, r) = \text{sign}(f(x, r) - 1)|x - \hat{x}_e|^2.$$  \hspace{1cm} (7)

A.3. Shape and Appearance Decoder (Section 3.3)

MLP $S_\Theta$ takes a feature vector $f$ at a query 3D location $x^q$ and outputs the color $c$ and a residual SDFs $\Delta d$. The color on the surface of real objects changes in complex ways according to the time, pose, and view direction. We simplify the problem by assuming the color depends only on $f$, meaning the color is constant across view and time. $S_\Theta$ is an 8-layer MLP with a hidden dimension of 256.

A.4. Joint Candidates (Section 3.5.1)

In this subsection, we explain the details of the joint candidates defined in the Section 3.5.1 in the main paper. When a point inside one ellipsoid $e_i$ is closed to a point inside another ellipsoid $e_j$ throughout the entire video, the point is considered to be a joint between parts $i$ and $j$. To find these points, we create several joint candidate points $\{\xi^n_i\}_{n=1:N}$ inside the ellipsoids in advance, and minimize the distance between them. We define six candidates inside each ellipsoid in the local coordinate, as follows

$$\hat{\xi}_i^n = r_i \odot \xi^n,$$  \hspace{1cm} (8)

where $\xi^n \in \{(-\frac{3}{4}, 0, 0), (0, \frac{3}{4}, 0), (0, 0, \frac{3}{4})\}$. This is then transformed into the global coordinate system using the rotation and translation of each part

$$\xi_i^n = R_i \xi_i^n + t_i.$$  \hspace{1cm} (9)
A.5. Frame scheduling (Section 3.6)

In order to stabilize the training, we progressively increase the number of frames used for training. First, we use the first $T_0$ frames of data to train for $\tau_0$ iterations. Then, the number of frames used for training is increased linearly so that all frames $T$ of the video are used at $\tau_1$ iteration. After that, all frames are used for training until $\tau_{\text{final}}$. In the experiment using human data, we set $T_0 = 10$, $\tau_0 = 10k$, $\tau_1 = 80k$.

A.6. Loss (Section 3.6)

The loss function is a weighted sum of $L_{\text{SDF}}, L_{\text{photo}}, L_\Gamma, L_{\text{merge}}, L_\xi, L_\tau,$ and $L_{\text{separation}}$:

$$L_{\text{total}} = \lambda_{\text{SDF}} L_{\text{SDF}} + \lambda_{\text{photo}} L_{\text{photo}} + \lambda_\Gamma L_\Gamma + \lambda_{\text{merge}} L_{\text{merge}} + \lambda_\xi L_\xi + \lambda_\tau L_\tau + \lambda_{\text{separation}} L_{\text{separation}}.$$  

(10)

We used $\lambda_{\text{SDF}} = 0.2$, $\lambda_{\text{photo}} = 1$, $\lambda_{\text{merge}} = 0$, $\lambda_\xi = 600$, $\lambda_\tau = 1000$, and $\lambda_{\text{separation}} = 1$. We gradually increase $L_\Gamma$ from 2 to 50 until iteration $\tau_0$ for training stability. From iteration $\tau_2$, we set $\lambda_{\text{merge}} = 5$ and train the model until $\tau_{\text{final}}$. We set $\tau_2 = 150k$.

A.7. Other Training Details

The other hyper-parameters were set as $d_{\text{max}} = 0.02$, $\lambda_l = 0.02$, $\lambda_{\text{motion}} = 3$, $D = 0.1$, $\epsilon = 0.01$. For the weighted positional encoding in Equation 4 in the main paper, we apply positional encoding [8] to spatial locations $x_i$ with 6 frequencies following the training setting of NeuS [12].

We used AdamW optimizer [7] with learning rate 0.0003, and $\beta_1 = 0.9$, $\beta_2 = 0.999$, $\lambda = 0.005$. All training images are resized to $512 \times 512$. We train the model up to $\tau_{\text{final}} = 200k$ iterations with a batch size of 16. We randomly sample 384 rays from each image for human data, where $P$ is set to 20. Training takes about 48 hours on a single NVIDIA A100 GPU.

A.8. Pose Manipulation (Section 4.1)

Since our method estimates explicit joint relationships between parts, we can freely manipulate the pose of the object. First, the position of the final joints $\xi_{i,j}$ is defined as the midpoint of the candidate points $\xi_{i,m}^n$ and $\xi_{i,n}^n$ connected in Equations 16 and 17 of the main paper:

$$\xi_{i,j} = \frac{1}{2}(\xi_{i,m}^n + \xi_{i,n}^n) \quad \text{s.t.} \ (m, n) = \arg\min_{m,n} \bar{f}_{i,j}^{m,n}. \ (11)$$

By manually rotating the part $i$ or $j$ and its children parts around this joint $\xi_{i,j}$, the pose of the object can be freely changed, and novel rotations and translations for each part can be obtained $\{R_i, t_i\}_{i=1}^{\text{novel}}$. To render the novel pose image, we directly input $\{R_i, t_i\}_{i=1}^{\text{novel}}$ to the second network $S_\Theta$.

A.9. Baselines (Section 4.3)

Kundu* et al. [6] Their original model estimates SMPL parameters in an unsupervised manner as follows. First, a CNN-based encoder receives an image and estimates the parameters of the SMPL model. Based on the estimated parameters, the SMPL mesh is deformed and a pixel value of the image is assigned to each vertex according to its position in the image. The model is trained to match the colors of the estimated mesh vertices from different images of the same person at different times. By using CNN-based encoder, they can reconstruct the mesh from unseen monocular images. However, our method uses videos of specific scenes from multiple viewpoints, which gives us an unfair advantage. In order to allow for a fair comparison between our method and theirs, we replaced their CNN-based encoder with an MLP $T_{\Theta^*}^{\text{Kundu}}$ that takes frame id as input and estimates SMPL parameters for each frame.

$$T_{\Theta^*}^{\text{Kundu}} : \gamma(t) \rightarrow R(t), t(t), \Theta(t), \beta,$$  

(12)

where $R(t)$ is a global orientation, $t(t)$ is a global translation, $\Theta(t)$ is joint poses, and $\beta$ is a shape parameters. An overview of the method is visualized in Figure A (a). This MLP allows Kundu* et al. to overfit to the specific video sequence, like our method does. Please note that $\beta$ is not time dependent. The structure of the MLP $T_{\Theta^*}^{\text{Kundu}}$ is the same as that of $T_{\Theta^*}$ used in the proposed method except for the output dimension. Since the authors do not publish their training implementation, all modules and loss functions are our replicated implementation. For the human pose prior, instead of training the adversarial auto-encoder, we used the pre-trained human pose prior from Bogo et al. [1]. Also, since our experimental setup uses multi-view videos and overfits to a single subject, we do not use reflectional symmetry or shape-consistency loss. Please refer to Kundu et al. [6] for more details. In addition, since human foreground masks are available in our experimental setup, we use a differentiable renderer [10] to render the mask of the mesh and train it so that the L2 norm with the GT foreground mask is small. We apply the same frame scheduling as in Section A.5 for training stabilization.

After training the model, we assign colors to the vertices of the SMPL mesh for novel view and pose synthesis, where we average the estimated vertex color for various frame ids and viewpoints using the learned SMPL poses.

Schmidtke* et al. [11] Their original model trains the deformation of a 2D template of a person’s structure in an unsupervised manner using image reconstruction. They use a CNN-based encoder to estimate the 2D deformation parameters. To extend the method to 3D, we replaced the 2D templates with 3D templates, where the shape is approximated with 3D gaussians. For a fair comparison, we also
replaced the CNN-based encoder with an MLP $T^\text{Schmidtke*}_\Theta$ that takes a frame id as input and outputs the deformation parameters of the template in the global coordinate, as in Kundu* et al.

$$T^\text{Schmidtke*}_\Theta : \gamma(t) \rightarrow \{R_i(t), t_i(t), s_i\}_{i=1:18},$$  

where $R_i(t)$ and $t_i(t)$ are rotation and translation for each part, and $s_i$ is 3D scale parameters for each part. An overview of the method is visualized in Figure A (b). We replace the affine transformation $\Theta_i$ defined in Equation 3 in Schmidtk et al. [11] with a physically meaningful transformation

$$\Theta = \begin{bmatrix} s_1 R_{1,1} & s_1 R_{1,2} & s_1 R_{1,3} & t_1 \\ s_2 R_{2,1} & s_2 R_{2,2} & s_2 R_{2,3} & t_2 \\ s_3 R_{3,1} & s_3 R_{3,2} & s_3 R_{3,3} & t_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}. $$  

(14)

Please note that $s_i$ is not time dependent. The deformed 3D template is projected onto a 2D heatmap using the viewpoint of the training image, and then transformed into an RGB image using a second CNN-based network. Since the model is overfitted on a single scene, we do not input the reference frame to the second network, but only the 2D heatmap. We modified the implementation based on their public training code\footnote{https://github.com/lschmidtke/shape_templates}, and the loss function used for training is exactly the same as the original. Please refer to Schmidtk et al. [11] for more details.

We apply the same frame scheduling as in Section A.5 for training stabilization.

A.10. Regression of GT SMPL Pose (Section 4.2, 4.4)

For human re-posing we learn a linear mapping from the GT SMPL poses to estimated joints and for joint evaluation we learn a mapping from the estimated joints to the GT SMPL poses.

Mapping from SMPL For re-posing, we perform a regression from the GT SMPL mesh to our part pose $R_i$ and $t_i$. First, for all frames of the training data, we optimize the linear transformation $X$ from the mesh vertices $V(t)$ to the concatenation of the learned part centers and the candidate points $P(t) = \text{CAT}\{t_i, \xi_i^1, \ldots, \xi_i^N\}_{i=1:P}(t)$ using the least-squares method

$$\min_X \left( \sum_t |XV(t) - P(t)|_F + \frac{1}{2} \lambda |X|_F^2 \right).$$  

(15)

When re-posing with SMPL meshes, we compute the part centers and candidate points $P^\text{new} = \text{CAT}\{t_i, \xi_i^1, \ldots, \xi_i^N\}_{i=1:P}^\text{new}$ corresponding to the novel pose SMPL mesh $V^\text{new}$ using the learned linear transformation $X$.

$$P^\text{new} = XV^\text{new}. $$  

(16)

The part centers $t_i^\text{new}$ of the new pose are obtained by extracting the corresponding elements of $P_i^\text{new}$. The rotation matrix $R_i^\text{new}$ is obtained by solving the following optimization:

$$\min_{R_i^\text{new}} |R_i^\text{new} \hat{\xi}_i - \Xi_i|_F \quad \text{s.t.} \quad (R_i^\text{new})^\top R_i^\text{new} = I, $$  

(17)

where $\hat{\xi}_i = [\xi_i^1, \ldots, \xi_i^N]$, $\Xi_i = [\xi_i^1 - t_i, \ldots, \xi_i^N - t_i]$. By using the resulting $t_i^\text{new}$ and $R_i^\text{new}$ into the second network $S_\Theta$ directly, we can re-pose the object.

Similarly, for the re-posing of the baseline Schmidtk* et al. [11], the part center $t_i$ of the 3D template and the points around it

$$\xi_i^j \in \{t_i \pm r R_i^1, t_i \pm r R_i^2, t_i \pm r R_i^3\}$$  

(18)

are used to learn the same linear mapping, where $R_i = [R_i^1, R_i^2, R_i^3]$ and $r = 0.1$.

Mapping to SMPL To evaluate the joint, we regress the translation $J(t) = \text{CAT}\{j_i\}_{i=1:23}(t)$ of the GT SMPL joints at frame $t$ from the learned object poses at $t$, where

Figure A: Baselines used for comparison. The * indicates that these are adaptations of the original methods.
CAT is the concatenation operator. We obtain a linear mapping $X$ from the learned poses to the SMPL joints by solving the following optimization problem:

$$\min_X \left( \sum_{t \in T_{train}} |XP(t) - J(t)|_F + \frac{1}{2} \lambda |X|_F \right),$$

where $T_{train}$ is the set of frames used for this optimization, which are uniform sample of 10% of the available frames.

For joint evaluation, a learned linear transformation $X$ was applied to the remaining frames to compute the mean per joint position error (MPJPE) [4] between the regressed joint position and the GT joint position.

Similarly, for the baseline Schmidtke* et al. [11], we learn a linear mapping from the part center $t_i$ of the 3D template and the points around it $\xi_n$ defined in Equation 18 to the GT SMPL joints.

For the evaluation of Kundu* et al. [6], we learn a linear regression $X$ from the learned SMPL mesh vertices $V_{Kundu}$ to the GT SMPL joints

$$\min_X \left( \sum_{t \in T_{train}} |XV_{Kundu}(t) - J(t)|_F + \frac{1}{2} \lambda |X|_F \right).$$

We evaluated both models in the same way as ours.

### A.11. Effect of $L_t$ (Section 4.5)

Qualitative results with and without $L_t$ are shown in Figure C. We can see that the parts sometimes do not cover the entire object or go outside of the object without $L_t$. This result demonstrates the effectiveness of $L_t$.

### B. Training on the RGBD-Dog Dataset

We used RGBD-Dog dataset [5] for training the dog model. We apply off-the-shelf instance segmentation model [2] to obtain the ground truth masks. In this dataset, it is not possible to isolate the exact region of the dog due to occlusion by a person or overlapping background objects.

Therefore, we modified the loss function to ignore occluded regions and regions where the estimated mask is unreliable. Specifically, when calculating $L_{photo}$, $L_E$, and $L_t$, we replace the loss values with 0 for elements that use unreliable pixels in their calculations.

### C. Robot dataset

In order to demonstrate the applicability of our method to objects with various structures, we created a dataset of robots with seven different structures, see Figure B. The dataset consists of 1000 frames of synchronized video with 20 viewpoints per robot. We sampled five of these views and trained on the first 300 frames of each video.

In order to generate the dataset we use a recent python-based renderer, NViSII [9]. We use robots that are freely available and have URDF associated with 3D meshes. In order to animate the robot, we use PyBullet [3]. The robot is given random joint goals, and once it reaches these goals, we repeat the process of giving it random joint goals. We place 20 fixed cameras on the hemisphere at a fixed distance from the robot, and we add a warm sunlight to add more light to the scene. Each frame is rendered with 2000 samples per pixel at 512×512 resolution. We use the OptiX denoiser to clean the final renders to provide noise free images. Both the datasets and the scripts to generate the multiview animated objects will be available at [https://github.com/NVlabs/watch-it-move](https://github.com/NVlabs/watch-it-move).

### D. Additional Results for Parts Merging

Additional results of parts merging are shown in Figure D (a). The results confirm that meaningful parts and the structure are obtained by merging. To show the effect of $L_{merge}$, we show the merging results when it is disabled in Figure D (b). It can be seen that by using $L_{merge}$, we can appropriately pull parts together that have the same relative motion, and learn more meaningful decomposition of parts.
Figure D: (a) Additional results for part merging. From left to right, we show the initial joints and structure, the joints and structure after merging, and the connection between the centers of the parts. Since there is no joint at the endpoint, the center of the part is connected instead (red lines). A polygonal path indicates a part that is connected to multiple parts. The centers of the parts are shown for clarity. (b) Joints and part centers obtained when $L_{\text{merge}}$ is disabled.

References


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