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# Geometric Visual Similarity Learning in 3D Medical Image Self-supervised Pre-training

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# Abstract

Learning inter-image similarity is crucial for 3D medical images self-supervised pre-training, due to their sharing of numerous same semantic regions. However, the lack of the semantic prior in metrics and the semantic-independent variation in 3D medical images make it challenging to get a reliable measurement for the inter-image similarity, hindering the learning of consistent representation for same semantics. We investigate the challenging problem of this task, i.e., learning a consistent representation between images for a clustering effect of same semantic features. We propose a novel visual similarity learning paradigm, Geometric Visual Similarity Learning, which embeds the prior of topological invariance into the measurement of the interimage similarity for consistent representation of semantic regions. To drive this paradigm, we further construct a novel geometric matching head, the Z-matching head, to collaboratively learn the global and local similarity of semantic regions, guiding the efficient representation learning for different scale-level inter-image semantic features. Our experiments demonstrate that the pre-training with our learning of inter-image similarity yields more powerful inner-scene, inter-scene, and global-local transferring ability on four challenging 3D medical image tasks. Our codes and pre-trained models will be publicly available<sup>1</sup>.

# 1. Introduction

Learning inter-image similarity [26, 33, 44, 47] is crucial for 3D medical image (e.g., CT, MR) self-supervised pretraining (SSP) [20]. As shown in Fig.1, different from natural images which are widely researched in SSP, 3D medical images share numerous same semantic regions due to the consistency of human anatomies [28] and the complete spatial information in 3D vision [35], bringing a strong prior for effective SSP. Therefore, it targets on constrain-



Figure 1. Learning inter-image similarity is crucial for 3D medical image SSP. a) Natural images have large semantic difference between images whose inter-image similarity is weak. b) 3D medical images share numerous same semantic regions between images due to the consistent human anatomies and the complete spatial information in 3D vision, having large inter-image similarity.

ing the pre-training network for a consistent representation of these same semantic regions between images without annotations. Once successful, it will bring great clustering effect for same semantic features, powerful representability of pre-trained network, and effective transferring for potential downstream tasks.

Although the existing SSP works have achieved promising results in their tasks, they are limited in the learning of inter-image similarity in 3D medical images. 1) Clusteringbased SSP methods [2, 24] measure the features' similarity between images for their clustering pattern in an embedding space, and learn to aggregate same cluster's features. However, they simply employ the Mahalanobis or Euclidean distance as the measurement function which is extremely interfered by images' semantics-independent variations (Fig.2). 2) Contrastive learning works [3, 4] directly learn to separate their features for inter-image *dissimilarity*. This violates the learning inter-image *similarity* which is crucial in 3D images and will make the network represent distinct features for same semantic regions. Although some other contrastive learning works [4, 7, 41] have removed the sep-

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<sup>&</sup>lt;sup>1</sup>https://github.com/YutingHe-list/GVSL



Figure 2. It is challenging to measure a reliable inter-image similarity. a) There is a large similarity between the Myo and the RA regions between images A and B. b) Due to the variation of the scanning protocol, RA regions are different in images B and C.

aration learning, they are still unable to learn the consistency of inter-image same semantics. 3) Generation-based methods [23,25,40,48] construct pretext labels via designed transformation methods (e.g., rotation [23]) and train networks to predict these labels. These methods implicitly impose a bias into SSP via manually designing the transformation methods. However, the bias extremely relies on the manual design which makes pre-training networks focus on the biased features of pretext labels and become sensitive to the change of scenario [25].

Thinking the limitations in above existing works, the large-scale mis-measurement for inter-image similarity is the key challenge in 3D medical SSP, interfering the discovery of semantics' correspondence and hindering the learning of consistent representation for same semantic regions. Semantic-independent variations (Fig.2) make the 3D medical images have different appearance. Different semantic regions have similar appearances and same semantic regions have different appearances between images. The direct measurement in the embedding space, like the clustering-based SSP methods [2, 24], is sensitive due to lack of semantic prior in their metrics. Therefore, in the non-supervision situation, once the features changed caused by the variations, these metrics will make mis-measurement of similarities for large-scale semantics, bringing their miscorrespondence. It will train network to aggregate the features with different semantic but similar appearance, causing mis-representation.

Topological invariance [18,27] of the visual semantics in 3D medical images provides a motivation to construct a reliable measurement for inter-image similarity (Fig.3). Due to the consistency of human anatomies [28], 3D medical images have consistent context topology between the visual semantics in image space (e.g., the four chambers of human hearts have a fixed space relationship), and the same semantic regions have similar shapes in different images (e.g., the vessels (AO) have a stable tubular structure), constructing an invariant topology for the visual semantics. Therefore,



Figure 3. The topological invariance of the visual semantics between the 3D medical images provides a motivation to discover their inter-image correspondence.

according to the semantic prior of topological invariance, the semantic regions are able to be transformed to align in the image space via a topology-invariant mapping [10], thus discovering their reliable inter-image correspondence even with large variations in appearance. An intuitive strategy is to use the registration or geometric matching (GM) methods [11, 13, 15, 16, 32] to discover correspondence indexes between images, and use these indexes to constrain the consistent representation for corresponding regions. However, the errors in these indexes will bring mis-correspondence.

In this paper, we propose a novel SSP paradigm, Geometric Visual Similarity Learning (GVSL), to learn the inter-image similarity in 3D medical images. It embeds the prior of topological invariance into the measurement of the similarities, and train network to estimate semantics' correspondence from the represented features in GM. Due to this effective semantic prior, the measurement will consider the semantic-related topology similarity avoiding the large interference of semantic-independent variation. Therefore, when learning to enlarge this similarity between two images for more accurate estimation of correspondence, the gradient in backpropagation will constrain the network to cluster the corresponding features in embedding space for more consistent representation. To drive the GM learning, we further propose a Z-Matching head to explore the global and local collaborative representation learning of inter-image similarity in our GVSL paradigm. It constructs a collaborative learning head with affine (global matching) and deformable (local matching) transformations [13], thus embedding the pre-trained model with a powerful transferring ability for potential downstream tasks.

Our contributions are summarized as follows: 1) Our work advances the learning of inter-image similarity in 3D medical image SSP, and pre-trains the network to learn a consistent representation for same visual semantics between images without annotation, pushing the representability of pre-trained models. 2) We propose the Geometric Visual Similarity Learning (GVSL) that embeds the prior of topological invariance into the metric for a reliable measurement of inter-image similarity, learning a consistent representation for same semantic regions between images. 3) We present a novel GM head, Z-Matching head, for simultaneously powerful global and local representation. It collaboratively learns the affine and deformable matching, realizing an effective optimization for the representation of different semantic granularity in our GVSL, and finally achieving a powerful transferring ability.

## 2. Related work

Learning similarity in self-supervised pre-training: Learning similarity [26, 43, 46] targets on learning consistent representation for similar visual objects and distinguished representation for dissimilarity objects, which is a fundamental task in visual SSP [20]. As illustrated in Sec.1, it has three main paradigms. Contrastive learning [3, 4, 14, 39, 44, 45] which constrains the representation of same image to be consistent and different images to be separated. However, they are unable to learn the inter-images similarity, and the learning of separation will extremely interfere the representation of the 3D medical images. Clustering-based methods [2, 24] are able to learn interimage similarity, but their large-scale mis-measurement for similarities interferes the learning for consistent representation. Generation-based methods [8,9,23,25,40,48] generate pretext labels manually and constrain networks to predict these labels. However, it implicitly embeds bias from manual design into the learning which will make network ignore some potential aspects and limit in the representation in some specific scenario.

Geometric matching & Registration: Geometric matching (GM, or named registration) [11, 13, 16, 17, 32, 36] aligns images' semantic regions to a same spatial coordinate system, thus providing correspondence indexes between two images. It has two level transformations: 1) Affine matching [13, 42] aligns images in global. It calculates a transformation matrix that consists of the rotation, scaling, translation, and shearing operations between images and transforms the images to align in a global view. 2) Deformable matching [13, 15, 16, 36] aligns images in local. It calculates a voxel-wise displacement vector field (DVF) which indicates the correspondence of the voxels between two images, and aligns the images via a spatial transformation operation [19]. Recently, due to the development of deep learning (DL), the DL-based GM [13, 16, 32] learns the representation driven by learning correspondence prediction, which provides us a potential solution.

# 3. Methodology

Our framework (Fig.4) learns from scratch on unlabeled 3D medical images, yielding a common visual representa-

tion with inter-image similarity.

#### **3.1. GVSL for inter-image similarity**

The proposed GVSL (Fig.4 a)) models the learning of inter-image similarity as the estimation of inter-image correspondence from represented features which embeds the prior of topological invariance into the measurement, thus utilizing the gradient in backpropagation to train the network to represent consistent features on same semantics.

**3.1.1 Description of GVSL** GVSL's goal is to learn a representation that has a powerful clustering effect of the same semantic features even in different images. As shown in Fig.4, it uses two shared-weight neural networks  $\mathcal{N}_{\theta}$  with weights  $\theta$  to represent the features  $f_A$ ,  $f_B$  from two images  $x_A, x_B$ . These features are put into a GM head  $\mathcal{G}_{\xi}$  (our Z-matching head in our framework, Sec.3.2), to learn the correspondence of the semantic regions between images, thus driving the consistent representation in  $\mathcal{N}_{\theta}$  for these same semantics.

Given a set of 3D medical images  $\mathcal{D}$ , two images  $x_A, x_B \sim \mathcal{D}$  are sampled uniformly from  $\mathcal{D}$  (A and B refer to different images), and one transformation operation  $t \sim \mathcal{T}$  is sampled from a transformation set  $\mathcal{T}$ . GVSL produce a transformed view  $x_A^t \triangleq t(x_A)$  from  $x_A$  by applying the transformation t to improve the diversity of the images. The network outputs global and local representations  $\{f_A^g, f_A^l\} \triangleq \mathcal{N}_{\theta}(x_A^t), \{f_B^g, f_B^l\} \triangleq \mathcal{N}_{\theta}(x_B)$  of  $x_A^t$  and  $x_B$ . The head for GM  $\mathcal{G}_{\xi}$  further outputs a displacement vector field (DVF)  $\psi_{AB} \triangleq \mathcal{G}_{\xi}(f_A^l, f_B^l, f_A^g, f_B^g)$  which indicates the correspondence of the voxels between two images. The spatial coordinate system of the image  $x_A$  is transformed to the image  $x_B$  for a geometric matched image  $x_{AB} \triangleq \psi_{AB}(x_A)$  via spatial transformation [19]. We utilize the in-painting, local-shuffling, and non-linear as the transformation set  $\mathcal{T}$ .

We calculate a normalized cross-correlation (NCC) to evaluate the alignment degree between two images which indirectly evaluates the accuracy of the predicted correspondence. We train the framework to minimize this loss  $\mathcal{L}^{NCC}$ , thus driving the learning of correspondence,

$$\mathcal{L}_{\theta,\xi}^{NCC} \triangleq (1) \\ \sum_{p \in \Omega} \frac{(\sum_{p_i} (x_B(p_i) - \hat{x_B}(p))(x_{AB}(p_i) - x_{\hat{A}B}(p)))^2}{(\sum_{p_i} (x_B(p_i) - \hat{x_B}(p))^2)(\sum_{p_i} (x_{AB}(p_i) - x_{\hat{A}B}(p))^2)}$$

where the p is the position of the voxels in the image space  $\Omega$ , and the i is the index of p. The  $\hat{x}_B(p)$  is the local mean intensity images:  $\hat{x}_B(p) = \frac{1}{n^3} \sum_{p_i} x_B(p_i)$  (the same as  $\hat{x}_{AB}(p)$ ). To keep the topology invariant in GM, we further calculate a smooth loss  $\mathcal{L}^{smooth}$  on the DVF, constraining the network to perceive the correspondence of semantic regions under the condition of their topology,

$$\mathcal{L}^{smooth}_{\theta,\xi} \triangleq \sum_{p \in \Omega} \| \bigtriangledown \psi_{AB}(p) \|^2.$$
<sup>(2)</sup>



Figure 4. The framework of our GVSL: **a**) Our GVSL learns the GM from the representation of the semantics in images, thus driving the learning of inter-image similarity via the gradient in backpropagation. **b**) Our Z-Matching head learns affine and deformable matchings simultaneously for powerful global and local representations. **c**) For efficient learning, it also takes a fundamental pretext task, the self-restoration, for a basic representation of semantics, thus giving a warm-up for GM learning.



Figure 5. Intuitions on GVSL's behavior: The prior of topological invariance in GM embeds a topology manifold into the metric, thus bringing an efficient measurement for inter-image similarity and guiding the clustering effect of same semantic features.

At each training step, we perform a stochastic optimization step to minimize  $\mathcal{L}_{\theta,\xi}^{GVSL} = \mathcal{L}_{\theta,\xi}^{NCC} + \mathcal{L}_{\theta,\xi}^{smooth}$  with the weights of  $\theta$  and  $\xi$ . Therefore, the framework's dynamics are summarized as  $\{\theta,\xi\} \leftarrow optimizer(\{\theta,\xi\}, \nabla_{\theta,\xi}\mathcal{L}_{\theta,\xi}^{GVSL}, \eta)$ , where the *optimizer* is an optimizer in training and  $\eta$  is a learning rate.

**3.1.2 Intuitions on GVSL's behavior** The GM head together with the loss for similarity ( $\mathcal{L}^{NCC}$ ) and the loss for topology-preservation ( $\mathcal{L}^{smooth}$ ) in our GVSL is an implicit metric [1] with the prior of topological invariance. As shown in Fig.5 a), metrics determine the similarity between images. The GM limits the measurement of inter-image visual similarity under the condition of the invariant topology in the image space, avoiding mis-measurement caused by the appearance (Fig.2).

$$\min_{\theta,\xi} \mathcal{L}(\mathcal{G}_{\xi}(\mathcal{N}_{\theta}(x_A), \mathcal{N}_{\theta}(x_B)); \{x_A, x_B\})$$
(3)

It implicitly embeds a topology manifold inner the images  $\{x_A, x_B\}$  into the measurement process, and measure the similarity ( $\mathcal{L}^{NCC}$ ) on this topology manifold (Fig.5 b), Equ.3). The  $x_A^{RA}$ ,  $x_B^{RA}$  and  $x_A^{Myo}$  are the potential RA regions on images  $x_A, x_B$  and the potential Myo region on

image  $x_A$ . In embedding space, due to the similarity in appearance, the distance between the features of RA in image B  $\mathcal{N}_{\theta}(x_B^{RA})$  and the features of Myo in image A  $\mathcal{N}_{\theta}(x_A^{Myo})$  is closer than that between the features of RA regions in image A  $\mathcal{N}_{\theta}(x_A^{RA})$  and B  $\mathcal{N}_{\theta}(x_B^{RA})$ . This will bring miscorrespondence via some direct metrics, e.g., Euclidean distance. The GM  $\mathcal{G}_{\xi}$  in our GVSL maps these represented features ( $\mathcal{N}_{\theta}(x_A^{RA}), \mathcal{N}_{\theta}(x_B^{RA}), \mathcal{N}_{\theta}(x_A^{Myo})$ ) in the embedding space to the topology manifold inner the images  $\{x_A, x_B\}$  in image space. Therefore, due to the prior of the topological invariance, the distance between the RA regions will be closer than that between the  $x_B^{RA}$  and  $x_A^{Myo}$  and bring efficient learning of inter-image similarity via the gradient, thus learning efficient clustering effect.

Throughout the whole training process, the learning of representation for inter-image similarity in the network  $\mathcal{N}_{\theta}$ and the correspondence in the GM head  $\mathcal{G}_{\xi}$  is a two-player game [34]. The GM head  $\mathcal{G}_{\xi}$  learns to estimate the correspondence of semantic regions from the represented features  $f_A$ ,  $f_B$  and measure their voxel displacement in image space. The network  $\mathcal{N}_{\theta}$  learns to provide features of visual semantic regions to the GM head  $\mathcal{G}_{\xi}$  for their correspondence. To achieve more accurate correspondence, the GM head has to drive the pre-training network to output more consistent and representative features in turn for same semantic regions via the gradient in backpropagation. Therefore, under this interaction, the network  $\mathcal{N}_{\theta}$  will provide more representative features for the GM head for better correspondence estimation, and the GM head  $\mathcal{G}_{\xi}$  will have a more powerful ability to learn the inter-image similarity.

#### 3.2. Z-Matching for Global-Local Representations

The proposed Z-Matching  $\mathcal{G}_{\xi}$  (Fig.4 b)) is a novel GM head that collaboratively learns affine and deformable matching for simultaneous global and local representation. It has two sub-head including the affine head  $\mathcal{G}_{\xi}^{g}$  for global similarity and the deformable head  $\mathcal{G}_{\xi}^{l}$  for local similarity.

**3.2.1 Affine head for global visual similarity** It concatenates the global features  $(f_A^g, f_B^g)$  of two images from the encoder part of the network  $\mathcal{N}_{\theta}$ , and puts these features into the affine head  $\mathcal{G}_{\xi}^g$  to predict the affine values. 15 values (3 for rotation  $(\theta_x, \theta_y, \theta_z)$ , 3 for translation  $(t_x, t_y, t_z)$ , 3 for scaling  $(s_x, s_y, s_z)$ , and 6 for shearing  $(sh_{xy}, sh_{xz}, sh_{yx}, sh_{yz}, sh_{zx}, sh_{zy})$ ) are estimated to calculate the affine matrix  $\psi_{AB}^g \triangleq \mathcal{G}_{\xi}^g(f_A^g, f_B^g)$  which indicates the global transformation target in the spatial coordinate system of  $x_A$  to align the  $x_B$  in global. Therefore, to percept the global correspondence, the optimizer will constrain the encoder to extract consistent and representative features for same global semantic regions.

**3.2.2 Deformable head for local visual similarity** It takes the affine matrix  $\psi_{AB}^g$  to transform the global spatial coordinate system of the local features (from the decoder of the network  $\mathcal{N}_{\theta}$ )  $f_A^l$  to the  $f_B^l$  for a global matching, thus the local features are globally aligned. It further concatenates the local features and puts them into the deformable head  $\mathcal{G}_{\xi}^l$  to predict a deformable map  $\psi_{AB}^l \triangleq \mathcal{G}_{\xi}^l(\psi_{AB}^g(f_A^l), f_B^l)$  that will deform the voxels in the image A to align their corresponding voxels in image B. Therefore, to achieve this voxel-wise alignment, the optimizer will constrain the whole network to extract consistent and representative features for same local visual semantic regions. Finally, the affine matrix  $\psi_{AB}^g$  and the deformable map  $\psi_{AB}^l$  are fused ( $\odot$ ) for the DVF  $\psi_{AB} \triangleq \psi_{AB}^l \odot \psi_{AB}^g$ . (Details of  $\odot$  are in *Supplementary Material.*)

Therefore, the correspondence of the visual semantic regions between two images is predicted in  $\psi_{AB}$ , and the learning of correspondence will constrain the network  $\mathcal{N}_{\theta}$ to extract more consistent and representative features for same visual semantics, thus driving the head  $\mathcal{G}_{\xi}$  to have more powerful ability to discover their correspondence.

#### 3.3. Fundamental pretext task for warm-up

The initial basic representation for visual semantics is important in our GVSL, so that we utilize self-restoration [48] as the fundamental pretext task (fundament) in our framework. During the learning of GM, the learning of correspondence  $\mathcal{G}_{\xi}$  relies on the represented features of two images from the network  $\mathcal{N}_{\theta}$ . The initial network  $\mathcal{N}_{\theta}$  with weak representability will limit the discovery of the correspondence between potential visual semantics, making it challenging to find a reliable optimization target to align same semantic regions, hindering the inter-image similarity learning. Therefore we construct a self-restoration [48] task in the framework for a warm-up of the GVSL.

As shown in Fig.4 c), it randomly transforms the appearance of an image  $(x_A)$  via a sampled transformation operation  $(t' \sim T)$  for a transformed image  $(x_A^{t'} \triangleq t'(x_A))$  and put it into the network  $\mathcal{N}_{\theta}$  to represent its local feature  $f_A^{l'}$  from the decoder. (To save computing re-

sources, we share this operation with GVSL in our experiment, i.e.,  $\mathcal{N}_{\theta}(x_A^{t'}) = \mathcal{N}_{\theta}(x_A^t)$ .) Then, the feature  $f_A^{l'}$  is put into a restoration head  $\mathcal{R}_{\iota}$  for a restored image  $(x_A')$ , and calculates mean sequence error losses  $\mathcal{L}_{\theta,\iota}^{MSE} = \|\mathcal{R}_{\iota}(\mathcal{N}_{\theta}(t'(x_A))) - x_A\|^2$  [48] with the original image  $x_A$  to learn the restoration of the visual semantics from a transformed context. Therefore, the network will learn a basic representation of semantics for warm-up in dynamics, i.e.,  $\{\theta, \iota\} \leftarrow optimizer(\{\theta, \iota\}, \nabla_{\theta, \iota} \mathcal{L}_{\theta, \iota}^{MSE}, \eta)$ , avoiding the weak optimization in GVSL.

### 4. Experiments and Results

#### **4.1. Experiment protocol**

1) Materials: Five datasets are used in our experiments. a) Pre-training dataset: Cardiac CT images from 302 patients are used as the self-supervised pre-training dataset without annotations. These images were acquired on a SO-MATOM Definition Flash and the contrast media was injected during the CT image acquisition. The x/y-resolution of these CT images is between 0.25 to 0.57 mm/voxel and the slice thickness is between 0.75 to 3 mm/voxel. The x/y-size of the images is 512 voxels and the z-size is between 128 to 994 voxels. b) Downstream datasets: Four public available datasets (MM-WHS-CT [49], ASOCA [6], CANDI [21], STOIC [31]) are used to demonstrate the superiorities of our framework. According to their data kinds, we use them for inner-scene and inter-scene evaluations. For inner-scene evaluation, it utilizes the Segmentation of seven Heart structures on cardiac CT images (SHC) [49], Segmentation of coronary Artery on cardiac CT images (SAC) [6], and diagnosis (Classification) of COVID-19 on chest CT images (CCC) [31] to evaluate the adaptability for same scenes (Cardiac or chest CT) as the source dataset. For inter-scene evaluation, it utilizes the Segmentation of 28 Brain tissues on MR images (SBM) [21] to evaluate the adaptability for *different* scenes (Brain MR) as the source dataset. More details are in our Supplementary Material.

**2) Comparisons:** We take eight works to benchmark our framework, including the generation-based methods [23, 30, 40, 48] and contrast-based methods [2–4, 7]. Therefore, the superiority of our GVSL will be demonstrated. We take 3D U-Net [5] as the backbone network for all methods (the global prediction methods use the encoder part of the backbone) for a fair comparison and use both fine-tuning and linear evaluations for a comprehensive demonstration.

**3) Evaluation metrics:** We use the mean Dice coefficient (DSC) to evaluate the segmentation tasks, and the Area Under the Curve (AUC) to evaluate the classification task following [37].

**4) Implementation:** All tasks are implemented by Py-Torch [29] on NVIDIA GeForce RTX 3090 GPUs with 24 GB memory, optimized by Adam [22] whose learning rate

Pre-training	a) Linear: powerful representation				b) Fine-tuning: great transferring			
	SHC <sub>DSC%</sub>	$SAC_{DSC\%}$	$\text{CCC}_{AUC\%}$	$\text{SBM}_{DSC\%}$	$SHC_{DSC\%}$	$SAC_{DSC\%}$	$\text{CCC}_{AUC\%}$	$\text{SBM}_{DSC\%}$
		Inner scene		Inter scene		Inner scene		Inter scene
Scratch	21.9	10.0	52.7	56.4	87.8	80.4	74.4	89.7
Denosing [40]	31.4(+9.5)	$9.3_{(-0.7)}$	57.9 <sub>(+5.2)</sub>	$28.3_{(-28.1)}$	$90.3_{(+2.5)}$	80.5 (+0.1)	75.6 <sub>(+1.2)</sub>	89.7
In-painting [30]	$32.3_{(+10.4)}$	$5.9_{(-4.1)}$	$57.1_{(+4.4)}$	$25.0_{(-31.4)}$	$90.4_{(+2.6)}$	$80.3_{(-0.1)}$	$79.9_{(+5.5)}$	89.9 <sub>(+0.2)</sub>
Models Genesis [48]	$47.4_{(+25.5)}$	$22.5_{(+12.5)}$	$60.4_{(+7.7)}$	$44.9_{(-11.5)}$	$90.3_{(+2.5)}$	$79.9_{(-0.5)}$	$80.7_{(+6.3)}$	$89.4_{(-0.3)}$
Rotation [23]	$56.1_{(+34.2)}$	$21.9_{(+11.9)}$	$62.1_{(+9.4)}$	$54.1_{(-2.3)}$	90.6(+2.8)	$81.1_{(+0.7)}$	$77.1_{(+2.7)}$	$89.6_{(-0.1)}$
DeepCluster [2]	55.9(+34.0)	$4.4_{(-5.6)}$	$57.9_{(+5.2)}$	$67.5_{(+11.1)}$	$85.4_{(-2.4)}$	$80.5_{(+0.1)}$	$59.9_{(-14.5)}$	$89.1_{(-0.6)}$
SimSiam [4]	$56.5_{(+34.6)}$	$9.7_{(-0.3)}$	$61.0_{(+8.3)}$	66.2 <sub>(+9.8)</sub>	$87.5_{(-0.3)}$	$80.1_{(-0.3)}$	$73.6_{(-0.8)}$	$89.8_{(+0.1)}$
BYOL [7]	$46.9_{(+25.0)}$	$8.6_{(-1.4)}$	$53.7_{(+1.0)}$	$52.7_{(-3.7)}$	88.6 <sub>(+0.8)</sub>	80.7 (+0.3)	$76.5_{(+2.1)}$	$89.5_{(-0.2)}$
SimCLR [3]	$48.7_{(+26.8)}$	$15.5_{(+5.5)}$	$61.3_{(+8.6)}$	$58.7_{(+2.3)}$	86.9 (-0.9)	$79.9_{(-0.5)}$	$74.3_{(-0.1)}$	$89.3_{(-0.4)}$
w/o Z-Matching	$49.1_{(+27.2)}$	$21.1_{(+11.1)}$	55.8 <sub>(+3.4)</sub>	$45.1_{(-11.3)}$	88.3 <sub>(+0.5)</sub>	81.2(+0.8)	81.3 <sub>(+6.9)</sub>	89.7
w/o Fundament	$45.3_{(+23.4)}$	$0.0_{(-10.0)}$	$58.8_{(+6.4)}$	$48.5_{(-7.9)}$	$87.0_{(-0.8)}$	$79.5_{(-0.9)}$	$76.6_{(+2.2)}$	$89.0_{(-0.7)}$
w/o Affine head	57.7(+35.8)	$17.9_{(+7.9)}$	$57.6_{(+4.9)}$	$53.4_{(-3.0)}$	89.4(+1.6)	<b>82.3</b> (+1.9)	$79.8_{(+5.4)}$	$89.8_{(+0.1)}$
Our GVSL (Whole)	$68.4_{(+46.5)}$	$28.7_{(+18.7)}$	$60.8_{(+8,1)}$	$79.9_{(+23,5)}$	$91.2_{(+3,4)}$	$81.3_{(+0,9)}$	$82.2_{(+7,8)}$	$90.0_{(\pm 0.3)}$

Table 1. The linear (a) and fine-tuning (b) evaluations demonstrate our powerful representation and great transferring ability. The cells with a pink background are the top value in the columns. The red or blue values are the improvement or reduction compared with the "Scratch".

is  $10^{-4}$ . The pretext task is trained with  $2 \times 10^5$  iterations. The downstream tasks are trained with  $4 \times 10^4$  iterations and validated every 200 iterations to save the best models on their validation sets. For a fair comparison, all methods in our experiment take the same basic training setting.

#### 4.2. Comparison study shows our superiority

As demonstrated in Tab.1, our linear (a) and fine-tuning (b) evaluations demonstrate our power representation ability and great transferring ability.

4.2.1 Powerful inner-scene transferring for both large and small structures Our powerful inner-scene transferring ability shows the great application potential of our GVSL in big-data but low-label scenarios of medical images. It achieves the highest performance both in large and small structures in the same scene of the pre-training dataset. 1) Large structures: In the SHC task which segments large cardiac structures, our GVSL achieves the highest DSC (68.4%) in linear evaluation which is 11.9% higher than the second-highest method [4]. This is because our learning of inter-image similarity promotes the representation of consistent features. Especially for the large anatomies which have clear visual semantics, our GM brings a much more efficient representation. 2) Small structures: In the SAC task which segments the small coronary arteries, numerous pre-training methods [3, 4, 7, 30] mislead the model to ignore such small features, resulting in even lower performance than the "Scratch", especial for those methods [3, 4, 7] designed for global prediction. Our learning of the deformable transformation and the self-restoration teaches the pre-trained network consistent and effective representation for small visual semantics, achieving the highest DSC in linear (28.7%) evaluation. It is also interesting that when removing the affine head in our

Z-matching head, our GVSL achieves the best fine-tuning performance (82.3%). This further demonstrates the importance of learning dense representation for small objects.

4.2.2 Effective inter-scene transferring Our effective inter-scene transferring ability demonstrates our superiority as the initiation for deep networks. The SBM task uses brain MR images which have different modality and context (body range) with the pre-training dataset, making a challenging inter-scene transferring. In linear evaluation, a lot of compared methods [7, 7, 23, 48] are unable to bring promotion in this task and achieves even worse performance than "Scratch" due to the large difference between the source (brain MR) and target (cardiac CT) tasks. Our framework which is pre-trained on cardiac CT images is able to efficiently adapt to the segmentation task on brain MR images. Therefore, it achieves the highest 79.9% DSC (23.5%) improvement). This is because the inter-image similarity brings the pre-trained network a better clustering effect for same semantic features even in different images, making the representation easier to be transferred to the target scene integrally. It is worth noting that in the fine-tuning evaluation, all methods only have similar even worse [2,3,7,23,48] performance as the "Scratch". This is because the large distribution gap between brain MR and cardiac CT images (different modalities and body ranges) makes the pre-trained representability unable to achieve valid transferring. Our GVSL still achieves the highest 0.3% improvement.

**4.2.3 Superiority in** *global* and *dense* prediction tasks Our superiority in both global and dense prediction tasks shows its great adaptability to potential downstream tasks. **1)** Dense prediction tasks (SHC, SAC, SBM): Our GVSL has the highest DSC for all three tasks owing to our deformable head and self-restoration head which learns representative and consistent features extraction ability for de-



Figure 6. Our GVSL has powerful representability in linear evaluation and faster convergence ability in fine-tuning evaluation. In b), the thick part of the lines mean the useful training process, and at the end of the thick parts are the saved best models on validation set.

tails. The SimSiam, BYOL, SimCLR, and DeepCluster only learn global representation in their pretext tasks, having very poor performance in the SAC which focuses on detail features. **2**) Global prediction tasks (CCC): The medical images are similar globally and their lesions are on the local regions. Our GVSL utilizes our Z-Matching head to simultaneously learn the global and local visual similarity for global-local representation, achieving the highest AUC (82.2%) in the fine-tuning evaluation and illustrating our superiority in the transferring of global prediction tasks. Although our GVSL has 60.8% AUC in linear evaluation which is 1.3% lower than the highest method (Rotation), it is still higher than the Denoising, In-painting, and Model Genesis which pre-train network via dense prediction tasks.

#### 4.3. Ablation study and model analysis

**4.3.1 Ablation study** We compare our GVSL with the only fundamental pretext task (self-restoration), the only Z-Matching for GM learning, and the fundament + only deformable matching, three observations can be found in Tab.1. 1) When only learning the GM (Z-Matching), its initial weak representability makes the pre-trained model have inefficient optimization and brings poor representation. Especially in the linear evaluation of the SAC task, it is unable to segment the extremely small structures due to the single GM's poor representation. 2) When adding the fundamental task, our GVSL has better performance than the single two sub-pretext tasks on all four downstream tasks, showing the importance of the basic representation from self-restoration and the large contribution of our inter-image similarity from our GM. 3) When removing the Affine head in the Z-Matching head, it reduces 3.2% and 2.4% AUC in the linear and fine-tuning evaluations of CCC task due to the lack of global representation learning. However, it achieves the highest DSC in the fine-tuning of the SAC task, because the targeted learning of deformable matching will promote the representation of thin structures in local features.

**4.3.2 Our promotion for the learning efficiency** As shown in Fig.6, we analyze the learning of the models which are initialized from scratch, by our GVSL, and by

the Model Genesis in the SAC and SBM tasks, demonstrating our powerful representability and much faster convergence ability. In the linear evaluation, our GVSL improves more than 20% DSC compared with the 'scratch' or Model Genesis, owing to our effective learning for details in localwise visual similarity. In the fine-tuning evaluation, our GVSL also greatly improves the convergence speed which achieves more than 30% improvement, illustrating its great convergence ability and great potential for saving computing resources. Although in the fine-tuning of the SBM task, the "scratch" has faster convergence, it quickly falls into over-fitting, and its performance is extremely limited.

4.3.3 The fundament's necessity for our GM learning The self-restoration learns a basic representation for visual semantic regions, thus driving the learning of inter-image similarity in our GM. As demonstrated in Fig.8, when only learning our GM task, the network's initial weak representation makes inefficient optimization of the GM task, so the NCC loss  $\mathcal{L}^{NCC}$  does not converge and is unable to learn the correspondence of semantic regions. When adding the fundamental pretext task, driven by the basic representation of visual semantic regions from the self-restoration, the NCC loss is successfully converging to learn the correspondence of semantic regions for a better clustering effect of same visual semantics inter images.

4.3.4 Our GVSL's promotion for clustering effect As shown in Fig.7, the local features  $f^l$  from the pre-trained models in the SHC task demonstrate our GVSL's promotion for the clustering effect. The random initialization mixes the different semantics, so it is unable to extract representative features and distinguish the potential visual semantics. When only learning the self-restoration, it learns basic representation for visual semantics, but is still limited by the constraint for inter-image similarity. Therefore, the local features  $f^{l}$  are still mixed. When only learning our Z-Matching head for the GM task, the features have a significantly better clustering effect, showing the importance of inter-image similarity. However, the features of some semantics are still mixed. When the above two sub-pretext tasks are used simultaneously in our GVSL, the basic representation from the fundament promotes the learning of GM,



Figure 7. Our GVSL's promotion for clustering effect. We draw the local features  $f^l$  of seven semantic regions (AO, RA, RV, LV, PA, LA, and Myo) from the pre-trained network in the SHC task and compress them to 2 values by t-SNE [38]. Our GVSL shows a great clustering effect for these semantics, while the features from other methods are mixed.



Figure 8. The necessity of the fundament in our GM learning. a) When only training the GM task, the NCC loss  $\mathcal{L}^{NCC}$  does not converge and is unable to learn the correspondence of semantic regions. b) When adding the fundament (self-restoration), warm-up from the basic representation of semantic regions drives the GM for efficient optimization.

so the clustering effect is more obvious and the features of different visual semantics are representative and distinguishing. Although the yellow points show three parts in our GVSL, each part is clustered, also showing that the representation of internal semantics of this region is consistent.

# 5. Conclusion and Discussion

In this paper, we have advanced the inter-image similarity learning in 3D medical image SSP, and proposed the *Geometric Visual Similarity Learning (GVSL)* for the representation of inter-image similarity, achieving powerful representability for the transfer learning in downstream application-specific tasks. While its unique properties of learning consistent representation for same semantics have bright powerful performance in inner-scene, inter-scene, and global-local transferring tasks for 3D images (CT, MR), an important future work is to expand the learning of interimage similarity to some images without topological invariance, i.e., whole slide imaging [12]. We believe that our GVSL in SSP will promote the research of efficient learning in medical image analysis, and our GVSL is able to serve as a primary source of transfer learning for downstream tasks.

**Discussion for impact** The proposed method demonstrates an effective and reasonable potential in medical imaging analysis, showing great potential impact. Especially for the widely used 3D medical images, their *spatial completeness* of 3D structures [35] avoids the spatial projection (e.g., X-ray images) and spatial occlusion (e.g., natural images) of 2D images. The consistency in human bodies also brings the *topological invariance* of the content in these 3D images. Therefore, the geometric relationship between these images is able to be effectively used to drive the measurement of visual similarity. The spatial completeness and topological invariance of 3D structure in images will further inspire researchers to do more research on SSP.

**Discussion for limitation** There are still some limitations in our GVSL. 1) The additional calculation in the Z-Matching head and the fundamental self-restoration learning makes larger GPU memory requirement and more computing costs. 2) The inter-scene transferring is still a large challenge for medical image pre-training models due to the large gap between the source and target scenes. Fortunately, these limitations are gradually being solved due to the development of GPU and enlarging of medical datasets (provides more possibilities for inner-scene transferring).

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# References

- [1] Aurélien Bellet, Amaury Habrard, and Marc Sebban. Metric learning. *Synthesis lectures on artificial intelligence and machine learning*, 9(1):1–151, 2015. 4
- [2] Mathilde Caron, Piotr Bojanowski, Armand Joulin, and Matthijs Douze. Deep clustering for unsupervised learning of visual features. In *Proceedings of the European conference on computer vision (ECCV)*, pages 132–149, 2018. 1, 2, 3, 5, 6
- [3] Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In *International conference on machine learning*, pages 1597–1607. PMLR, 2020. 1, 3, 5, 6
- [4] Xinlei Chen and Kaiming He. Exploring simple siamese representation learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition* (CVPR), pages 15750–15758, June 2021. 1, 3, 5, 6
- [5] Özgün Çiçek, Ahmed Abdulkadir, Soeren S Lienkamp, Thomas Brox, and Olaf Ronneberger. 3d u-net: learning dense volumetric segmentation from sparse annotation. In *International conference on medical image computing and computer-assisted intervention*, pages 424–432. Springer, 2016. 5
- [6] Ramtin Gharleghi, Dona Adikari, Katy Ellenberger, Sze-Yuan Ooi, Chris Ellis, Chung-Ming Chen, Ruochen Gao, Yuting He, Raabid Hussain, Chia-Yen Lee, et al. Automated segmentation of normal and diseased coronary arteries-the asoca challenge. *Computerized Medical Imaging and Graphics*, page 102049, 2022. 5
- [7] Jean-Bastien Grill, Florian Strub, Florent Altché, Corentin Tallec, Pierre Richemond, Elena Buchatskaya, Carl Doersch, Bernardo Pires, Zhaohan Guo, Mohammad Azar, et al. Bootstrap your own latent: A new approach to self-supervised learning. In *Neural Information Processing Systems*, 2020. 1, 5, 6
- [8] Fatemeh Haghighi, Mohammad Reza Hosseinzadeh Taher, Zongwei Zhou, Michael B Gotway, and Jianming Liang. Learning semantics-enriched representation via selfdiscovery, self-classification, and self-restoration. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, pages 137–147. Springer, 2020. 3
- [9] Fatemeh Haghighi, Mohammad Reza Hosseinzadeh Taher, Zongwei Zhou, Michael B Gotway, and Jianming Liang. Transferable visual words: Exploiting the semantics of anatomical patterns for self-supervised learning. *IEEE transactions on medical imaging*, 2021. 3
- [10] Joon Hee Han and Jong Seung Park. Contour matching using epipolar geometry. *IEEE Transactions on Pattern Analysis* and Machine Intelligence, 22(4):358–370, 2000. 2
- [11] Kai Han, Rafael S Rezende, Bumsub Ham, Kwan-Yee K Wong, Minsu Cho, Cordelia Schmid, and Jean Ponce. Scnet: Learning semantic correspondence. In *Proceedings of the IEEE international conference on computer vision*, pages 1831–1840, 2017. 2, 3
- [12] Matthew G Hanna, Anil Parwani, and Sahussapont Joseph Sirintrapun. Whole slide imaging: technology and appli-

cations. *Advances in Anatomic Pathology*, 27(4):251–259, 2020. 8

- [13] Grant Haskins, Uwe Kruger, and Pingkun Yan. Deep learning in medical image registration: a survey. *Machine Vision* and Applications, 31(1):1–18, 2020. 2, 3
- [14] Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. Momentum contrast for unsupervised visual representation learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR)*, June 2020. 3
- [15] Yuting He, Rongjun Ge, Xiaoming Qi, Yang Chen, Jiasong Wu, Jean-Louis Coatrieux, Guanyu Yang, and Shuo Li. Learning better registration to learn better few-shot medical image segmentation: Authenticity, diversity, and robustness. *IEEE Transactions on Neural Networks and Learning Systems*, 2022. 2, 3
- [16] Yuting He, Tiantian Li, Rongjun Ge, Jian Yang, Youyong Kong, Jian Zhu, Huazhong Shu, Guanyu Yang, and Shuo Li. Few-shot learning for deformable medical image registration with perception-correspondence decoupling and reverse teaching. *IEEE Journal of Biomedical and Health Informatics*, 2021. 2, 3
- [17] Yuting He, Tiantian Li, Guanyu Yang, Youyong Kong, Yang Chen, Huazhong Shu, Jean-Louis Coatrieux, Jean-Louis Dillenseger, and Shuo Li. Deep complementary joint model for complex scene registration and few-shot segmentation on medical images. In *Computer Vision–ECCV 2020: 16th European Conference, Glasgow, UK, August 23–28, 2020, Proceedings, Part XVIII 16*, pages 770–786. Springer, 2020. 3
- [18] Tobias Heimann and Hans-Peter Meinzer. Statistical shape models for 3d medical image segmentation: a review. *Medical image analysis*, 13(4):543–563, 2009. 2
- [19] Max Jaderberg, Karen Simonyan, Andrew Zisserman, et al. Spatial transformer networks. Advances in neural information processing systems, 28, 2015. 3
- [20] Longlong Jing and Yingli Tian. Self-supervised visual feature learning with deep neural networks: A survey. *IEEE transactions on pattern analysis and machine intelligence*, 2020. 1, 3
- [21] David N Kennedy, Christian Haselgrove, Steven M Hodge, Pallavi S Rane, Nikos Makris, and Jean A Frazier. Candishare: A resource for pediatric neuroimaging data. *Neuroinformatics*, 10(3):319, 2012. 5
- [22] Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. arXiv preprint arXiv:1412.6980, 2014. 5
- [23] Nikos Komodakis and Spyros Gidaris. Unsupervised representation learning by predicting image rotations. In *International Conference on Learning Representations (ICLR)*, 2018. 2, 3, 5, 6
- [24] Xiaoni Li, Yu Zhou, Yifei Zhang, Aoting Zhang, Wei Wang, Ning Jiang, Haiying Wu, and Weiping Wang. Dense semantic contrast for self-supervised visual representation learning. In Proceedings of the 29th ACM International Conference on Multimedia, pages 1368–1376, 2021. 1, 2, 3
- [25] Xiao Liu, Fanjin Zhang, Zhenyu Hou, Li Mian, Zhaoyu Wang, Jing Zhang, and Jie Tang. Self-supervised learning:

Generative or contrastive. *IEEE Transactions on Knowledge* and Data Engineering, 2021. 2, 3

- [26] Timo Milbich. Visual Similarity and Representation Learning. PhD thesis, 2021. 1, 3
- [27] Michael I. Miller and Laurent Younes. Group actions, homeomorphisms, and matching: A general framework. *International Journal of Computer Vision*, 41(1):61–84, 2001. 2
- [28] Frank H Netter. Atlas of human anatomy, Professional Edition E-Book: including NetterReference. com Access with full downloadable image Bank. Elsevier health sciences, 2014. 1, 2
- [29] Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, et al. Pytorch: An imperative style, high-performance deep learning library. Advances in neural information processing systems, 32, 2019.
- [30] Deepak Pathak, Philipp Krahenbuhl, Jeff Donahue, Trevor Darrell, and Alexei A Efros. Context encoders: Feature learning by inpainting. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 2536–2544, 2016. 5, 6
- [31] Marie-Pierre Revel, Samia Boussouar, Constance de Margerie-Mellon, Inès Saab, Thibaut Lapotre, Dominique Mompoint, Guillaume Chassagnon, Audrey Milon, Mathieu Lederlin, Souhail Bennani, et al. Study of thoracic et in covid-19: The stoic project. *Radiology*, 301(1):E361–E370, 2021. 5
- [32] Ignacio Rocco, Relja Arandjelovic, and Josef Sivic. Convolutional neural network architecture for geometric matching. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 6148–6157, 2017. 2, 3
- [33] Karsten Roth, Timo Milbich, and Bjorn Ommer. Pads: Policy-adapted sampling for visual similarity learning. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 6568–6577, 2020. 1
- [34] Walid Saad, Zhu Han, Mérouane Debbah, Are Hjorungnes, and Tamer Basar. Coalitional game theory for communication networks. *Ieee signal processing magazine*, 26(5):77– 97, 2009. 4
- [35] Chaman L Sabharwal and Jennifer L Leopold. A completeness of metrics for topological relations in 3d qualitative spatial reasoning. *Polibits*, 52:5–15, 2015. 1, 8
- [36] Jiacheng Shi, Yuting He, Youyong Kong, Jean-Louis Coatrieux, Huazhong Shu, Guanyu Yang, and Shuo Li. Xmorpher: Full transformer for deformable medical image registration via cross attention. arXiv preprint arXiv:2206.07349, 2022. 3
- [37] Abdel Aziz Taha and Allan Hanbury. Metrics for evaluating 3d medical image segmentation: analysis, selection, and tool. *BMC medical imaging*, 15(1):1–28, 2015. 5
- [38] Laurens Van der Maaten and Geoffrey Hinton. Visualizing data using t-sne. *Journal of machine learning research*, 9(11), 2008. 8
- [39] Wouter Van Gansbeke, Simon Vandenhende, Stamatios Georgoulis, and Luc V Gool. Revisiting contrastive methods for unsupervised learning of visual representations. In

M. Ranzato, A. Beygelzimer, Y. Dauphin, P.S. Liang, and J. Wortman Vaughan, editors, *Advances in Neural Information Processing Systems*, volume 34, pages 16238–16250. Curran Associates, Inc., 2021. 3

- [40] Pascal Vincent, Hugo Larochelle, Isabelle Lajoie, Yoshua Bengio, Pierre-Antoine Manzagol, and Léon Bottou. Stacked denoising autoencoders: Learning useful representations in a deep network with a local denoising criterion. *Journal of machine learning research*, 11(12), 2010. 2, 3, 5, 6
- [41] Zhaoqing Wang, Qiang Li, Guoxin Zhang, Pengfei Wan, Wen Zheng, Nannan Wang, Mingming Gong, and Tongliang Liu. Exploring set similarity for dense self-supervised representation learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 16590–16599, 2022. 1
- [42] Eric W Weisstein. Affine transformation. https://mathworld. wolfram. com/, 2004. 3
- [43] Ke Yan, Jinzheng Cai, Dakai Jin, Shun Miao, Dazhou Guo, Adam P Harrison, Youbao Tang, Jing Xiao, Jingjing Lu, and Le Lu. Sam: Self-supervised learning of pixel-wise anatomical embeddings in radiological images. *IEEE Transactions* on Medical Imaging, 41(10):2658–2669, 2022. 3
- [44] Chenyu You, Weicheng Dai, Fenglin Liu, Haoran Su, Xiaoran Zhang, Lawrence Staib, and James S Duncan. Mine your own anatomy: Revisiting medical image segmentation with extremely limited labels. arXiv preprint arXiv:2209.13476, 2022. 1, 3
- [45] Chenyu You, Weicheng Dai, Yifei Min, Fenglin Liu, Xiaoran Zhang, Chen Feng, David A Clifton, S Kevin Zhou, Lawrence Hamilton Staib, and James S Duncan. Rethinking semi-supervised medical image segmentation: A variancereduction perspective. arXiv preprint arXiv:2302.01735, 2023. 3
- [46] Chenyu You, Yuan Zhou, Ruihan Zhao, Lawrence Staib, and James S Duncan. Simcvd: Simple contrastive voxel-wise representation distillation for semi-supervised medical image segmentation. *IEEE Transactions on Medical Imaging*, 41(9):2228–2237, 2022. 3
- [47] Borui Zhang, Wenzhao Zheng, Jie Zhou, and Jiwen Lu. Attributable visual similarity learning. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 7532–7541, 2022. 1
- [48] Zongwei Zhou, Vatsal Sodha, Md Mahfuzur Rahman Siddiquee, Ruibin Feng, Nima Tajbakhsh, Michael B Gotway, and Jianming Liang. Models genesis: Generic autodidactic models for 3d medical image analysis. In *International conference on medical image computing and computer-assisted intervention*, pages 384–393. Springer, 2019. 2, 3, 5, 6
- [49] Xiahai Zhuang, Lei Li, Christian Payer, Darko Štern, Martin Urschler, Mattias P Heinrich, Julien Oster, Chunliang Wang, Örjan Smedby, Cheng Bian, et al. Evaluation of algorithms for multi-modality whole heart segmentation: an open-access grand challenge. *Medical image analysis*, 58:101537, 2019. 5