

# DualRefine: Self-Supervised Depth and Pose Estimation Through Iterative Epipolar Sampling and Refinement Toward Equilibrium

## Supplementary Material

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### 1. DEQ Framework

We adhere to the general framework of DEQ [2, 3] and employ a quasi-Newton solver to accelerate convergence. In our experiments, we utilize the Anderson solver [1]. A DEQ model computes  $A = I - \frac{\partial U}{\partial z^*}$  at the fixed point  $z^*$  to obtain the gradient. This is typically achieved by performing another fixed-point iteration. However, in line with [2, 5, 8], we approximate  $A = I$  and utilize the inexact gradient for training.

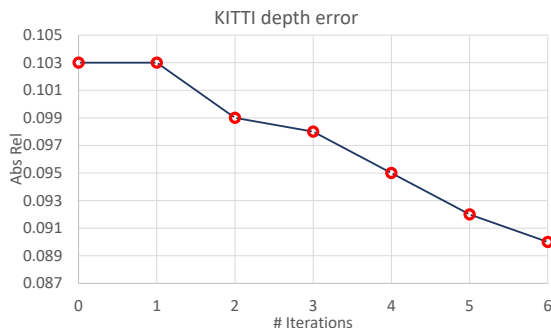


Figure 1. The progression of Abs Rel errors in each DualRefine iteration for KITTI depth.

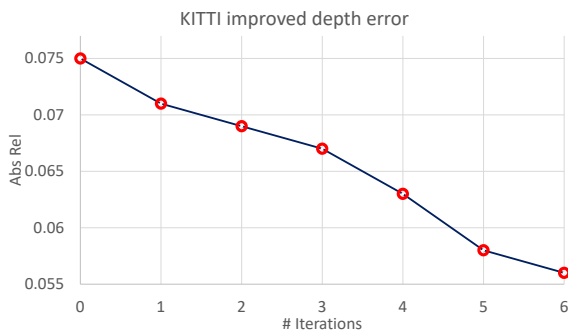


Figure 2. The progression of Abs Rel errors in each DualRefine iteration for KITTI improved depth.

### 2. Training Loss Combinations

Determining the optimal pairings to calculate the self-supervision losses at the refined fixed point is not straightforward. For each refined estimate ( $D^*$  and  $T^*$ ), we can calculate the self-supervision loss using either the detached initial estimates ( $[D^* \leftrightarrow \text{detached } T_0]$  pair and  $[T^* \leftrightarrow \text{detached } D_0]$  pair) or the corresponding refined estimate ( $[D^* \leftrightarrow T^*]$  pair and  $[D^* \leftrightarrow T^*]$ ).

We observe a worse accuracy when both final estimates are paired with the corresponding initial estimates. We infer that, by pairing the final estimates with the initial ones, we impose a strong constraint on the model, limiting the scope of the output. We observe the best results when at least one of the final estimates is paired with the corresponding initial estimate. One example is when the depth loss is computed using the  $[D^* \leftrightarrow \text{detached } T_0]$  pair, while the pose loss is computed using the  $[T^* \leftrightarrow D^*]$  pair. From this experiment, pairing the refined estimates with each other seems to display the best accuracy. However, to ensure scale consistency with the teacher networks, we follow the third loss pairing in the table.

### 3. Additional results on KITTI Depth

#### 3.1. KITTI improved depth

In Tab. 1 we present evaluation results on the improved dense ground truth [19] of the KITTI [7] eigen split [4]. We perform garg cropping [6] and report the error for distances up to 80m. Our refinement module improves the initial estimates and outperforms most previous models while still being competitive with the Transformer [20]-based DepthFormer [12] model.

#### 3.2. DEQ results

In Tab. 2 we present the error for the output of our model in each DEQ iteration. Iteration 0 corresponds to the depth

	Method	Test frames	$W \times H$	Abs Rel ↓	Sq Rel ↓	RMSE ↓	RMSE log ↓	$\delta_1 \uparrow$	$\delta_2 \uparrow$	$\delta_3 \uparrow$
Low & mid res	Ranjan [17]	1	$832 \times 256$	0.123	0.881	4.834	0.181	0.860	0.959	0.985
	EPC++ [15]	1	$832 \times 256$	0.120	0.789	4.755	0.177	0.856	0.961	0.987
	Johnston [13] <i>et al.</i>	1	$640 \times 192$	0.081	0.484	3.716	0.126	0.927	0.985	0.996
	Monodepth2 [9]	1	$640 \times 192$	0.090	0.545	3.942	0.137	0.914	0.983	0.995
	PackNet-SFM [11]	1	$640 \times 192$	0.078	0.420	3.485	0.121	0.931	0.986	0.996
	<b>DualRefine-initial (<math>D_0</math>)</b>	1	$640 \times 192$	0.075	0.379	3.490	0.117	0.936	0.989	<u>0.997</u>
	Patil <i>et al.</i> [16]	$N^\dagger$	$640 \times 192$	0.087	0.495	3.775	0.133	0.917	0.983	0.995
	Wang <i>et al.</i> [21]	2 (-1, 0)	$640 \times 192$	0.082	0.462	3.739	0.127	0.923	0.984	0.996
	ManyDepth [22]	2 (-1, 0)	$640 \times 192$	0.064	0.320	3.187	<u>0.104</u>	0.946	0.990	0.995
	DepthFormer [12]	2 (-1, 0)	$640 \times 192$	<b>0.055</b>	<b>0.271</b>	<b>2.917</b>	<b>0.095</b>	<u>0.955</u>	<u>0.991</u>	<b>0.998</b>
<b>DualRefine-refined (<math>D^*</math>)</b>	2 (-1, 0)	$640 \times 192$	<u>0.056</u>	<u>0.281</u>	<u>3.040</u>	<b>0.095</b>	<b>0.960</b>	<b>0.992</b>	<b>0.998</b>	
High res	DRO [10]	2 (-1, 0)	$960 \times 320$	<u>0.057</u>	<u>0.342</u>	3.201	0.123	0.952	0.989	0.996
	ManyDepth (HR ResNet50) [22]	2 (-1, 0)	$1024 \times 320$	0.062	0.343	<u>3.139</u>	0.102	<u>0.953</u>	<u>0.991</u>	0.997
	<b>DualRefine-refined (<math>D^*</math>)</b>	2 (-1, 0)	$960 \times 288$	<b>0.052</b>	<b>0.282</b>	<b>2.880</b>	<b>0.090</b>	<b>0.966</b>	<b>0.993</b>	<b>0.998</b>

Table 1. Results and comparison with other state-of-the-arts models on the KITTI [7] Eigen split [4] with improved depth maps [19]. **Bold**: Best, Underscore: Second best.  $\dagger$ : evaluated on whole sequences

# iters	Abs Rel ↓	Sq Rel ↓	RMSE ↓	RMSE log ↓	$\delta_1 \uparrow$	$\delta_2 \uparrow$	$\delta_3 \uparrow$
0	0.103	0.726	4.497	0.181	0.893	0.965	0.983
1	0.103	0.702	4.360	0.179	0.900	0.967	0.984
2	0.099	0.700	4.321	0.174	0.906	0.968	0.984
3	0.098	0.695	4.318	0.175	0.905	0.968	0.984
4	0.095	0.690	4.308	0.174	0.908	0.967	0.984
5	0.092	0.673	4.264	0.172	0.911	0.968	0.984
6	0.090	0.658	4.237	0.171	0.912	0.967	0.984
7	0.089	0.653	4.23	0.172	0.912	0.967	0.983
8	0.090	0.653	4.234	0.173	0.910	0.967	0.983
9	0.091	0.655	4.251	0.174	0.909	0.966	0.983

Table 2. The progression of the errors on the KITTI [7] Eigen split in each DualRefine iteration.

# iters	Abs Rel ↓	Sq Rel ↓	RMSE ↓	RMSE log ↓	$\delta_1 \uparrow$	$\delta_2 \uparrow$	$\delta_3 \uparrow$
0	0.075	0.379	3.490	0.117	0.936	0.989	0.997
1	0.071	0.329	3.186	0.108	0.950	0.991	0.997
2	0.069	0.324	3.143	0.105	0.953	0.991	0.997
3	0.067	0.319	3.135	0.104	0.953	0.991	0.997
4	0.063	0.307	3.098	0.101	0.956	0.992	0.998
5	0.058	0.291	3.050	0.097	0.959	0.992	0.998
6	0.056	0.281	3.040	0.095	0.960	0.992	0.998
7	0.055	0.278	3.041	0.095	0.960	0.992	0.998
8	0.055	0.279	3.056	0.096	0.958	0.992	0.998
9	0.057	0.283	3.091	0.097	0.957	0.992	0.998

Table 3. The progression of the errors on the KITTI [7] Eigen split [4] with improved depth maps [19] in each DualRefine iteration.

	Loss pairs		Abs Rel ↓	Sq Rel ↓	RMSE ↓	$\delta_1 \uparrow$
	$D^*$	$T^*$				
1	$T_0$	$D_0$	0.99	0.765	4.449	0.898
2	$T^*$	$D_0$	0.093	0.698	4.342	0.907
3	$T_0$	$D^*$	0.092	0.657	4.34	0.908
4	$T^*$	$D^*$	0.089	0.632	4.305	0.907

Table 4. Ablation experiment for the effect of pose updates and self-supervision pairings on the KITTI [7] Eigen split. **Bold**: Best.

estimates produced by the initial depth estimator. We can see that our model converges around the 6<sup>th</sup> iteration. We also plot the Abs Rel error on Fig. 1

### 3.3. KITTI improved depth DEQ results

We also present detailed DEQ errors in Tab. 3 and plot the Abs Rel error in each iteration on Fig. 2 for the KITTI improved depth ground truth. Similarly, our model converges around the 6<sup>th</sup> iteration.

### 3.4. Additional qualitative results

We illustrate through Figs. 3 and 4 additional results in the KITTI dataset. An interesting observation is how the model learns to give low confidence to vehicles and texture-less image regions. We also show in Fig. 4 how the epipolar geometry differs between the initial estimates and the refined estimates, which may cause inaccurate photometric losses

Methods	$t_{err}(\%) \downarrow$	$r_{err}(\circ/100m) \downarrow$	ATE (m) $\downarrow$
ORB-SLAM2 [61]	12.96	<b>0.7</b>	44.09
Monodepth2 [22]	12.28	3.1	99.36
Zou <i>et al.</i> [102]	7.28	1.4	71.63
<b>DualRefine-initial (<math>T_0</math>)</b>	12.50	4.04	118.29
<b>DualRefine-refined (<math>T^*</math>)</b>	<b>5.82</b>	1.51	<b>17.27</b>

Table 5. Additional results on KITTI odometry test split (Seq. 11 ~ 21) using ORB-SLAM2 stereo as pseudo-GT. We provide a comparison with representative state-of-the-art self-supervised depth and odometry methods. ORB-SLAM2 is included as a representative non-learning based method.

as well as matching costs.

#### 4. Additional results on KITTI odometry

We perform an additional evaluation on Seq. 11-21 of the KITTI odometry dataset, using the stereo version of ORB-SLAM2 as a pseudo-GT following Zou *et al.* [23] We present the average results in Tab. 5 The refinement greatly improves over the initial predictions and also displays better ATE even in comparison to ORB-SLAM2 with loop closure.

#### 5. Conv-GRU Update Implementation

In our approach, we use the standard Conv-GRU block [18] to compute the updates as follows:

$$\begin{aligned}
 z_{k+1} &= \sigma(\text{CNN}_z([h_k, x_k])) \\
 r_{k+1} &= \sigma(\text{CNN}_r([h_k, x_k])) \\
 \tilde{h}_{k+1} &= \tanh(\text{CNN}_{\tilde{h}}([r_{k+1} \odot h_k, x_k])) \\
 h_{k+1} &= (1 - z_{k+1}) \odot h_k + z_{k+1} \odot \tilde{h}_{k+1}
 \end{aligned} \tag{1}$$

where  $\sigma$  represents the sigmoid activation function. Exploring other variants of the Conv-GRU block will be considered in the future.

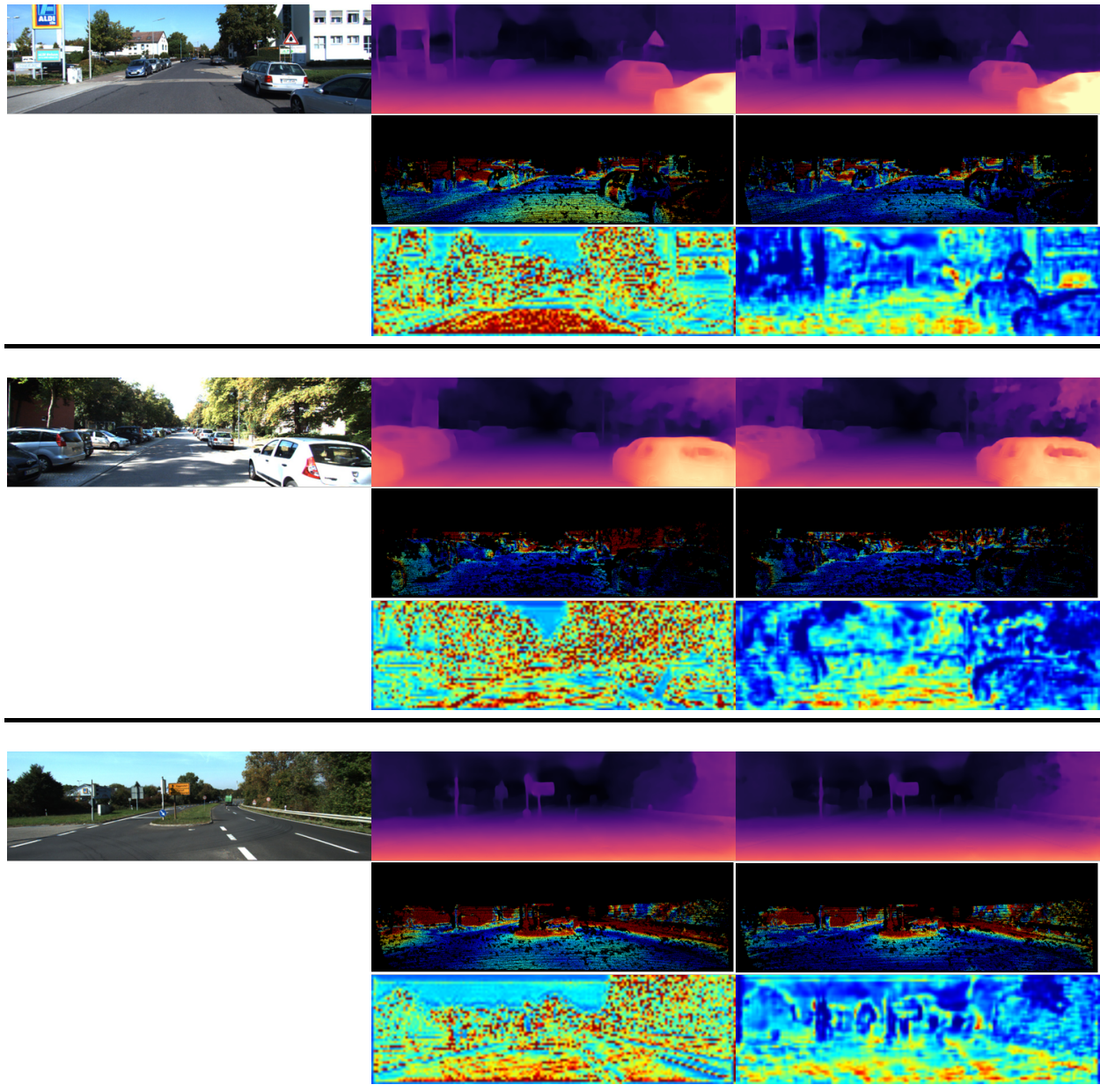


Figure 3. Qualitative results in the KITTI [7] dataset. top left: input image, top center: initial disparity, top right: refined disparity, middle center: initial error map, middle right: refined error map, bottom center: fixed confidence weights, bottom right: 6<sup>th</sup> iter confidence weights.

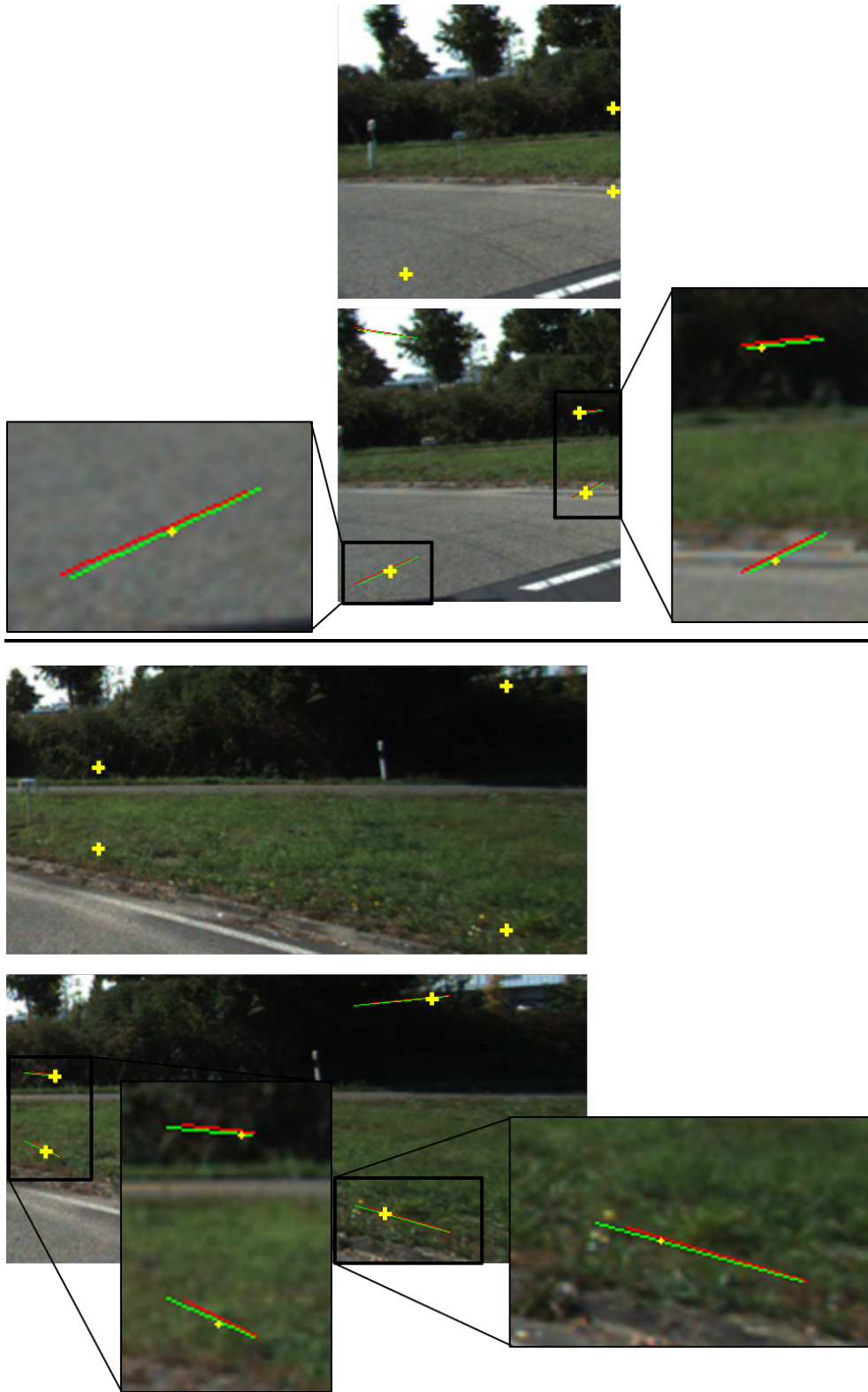


Figure 4. The epipolar line in the source image, calculated from yellow points in the target image, for the PoseNet [14] initial pose (red) and our refined pose (green). The yellow point in the source image is calculated based on our final depth and pose estimates.



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