# RGB no more: Minimally-decoded JPEG Vision Transformers Supplementary Material 

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## A. Scaling property of a $8 \times 8$ DCT

Consider an $8 \times 8$ 2D-DCT defined as the following where $\alpha_{i}=1 / \sqrt{2}$ if $i=0$, else $1, u, v, m, n \in[0 . .7]$.

$$
\begin{equation*}
X_{u, v}=\frac{\alpha_{u} \alpha_{v}}{4} \sum_{m, n} x_{m, n} \cos \left[\frac{\pi(2 m+1) u}{16}\right] \cos \left[\frac{\pi(2 n+1) v}{16}\right] \tag{1}
\end{equation*}
$$

We then calculate how much the DCT scales up the $\mathrm{min} / \mathrm{max}$ values considering the following two cases.

- If $u, v=0$

If $u, v=0$ then the resulting coefficient $X_{0,0}$ is simply:

$$
\begin{align*}
X_{0,0} & =\frac{1}{8} \sum_{m=0}^{7} \sum_{n=0}^{7} x_{m, n} \cdot \cos (0) \cos (0)  \tag{2}\\
& =\frac{1}{8} \sum_{m=0}^{7} \sum_{n=0}^{7} x_{m, n} \quad(\because \cos (0)=1) \tag{3}
\end{align*}
$$

Which is minimized/maximized when $x_{m, n}$ is $\mathrm{min} / \mathrm{max}$ :

$$
\begin{align*}
\min \left(X_{0,0}\right) & =\frac{1}{8} \min \left(x_{m, n}\right) \cdot 8 \cdot 8  \tag{4}\\
& =\min \left(x_{m, n}\right) \cdot 8  \tag{5}\\
\max \left(X_{0,0}\right) & =\frac{1}{8} \max \left(x_{m, n}\right) \cdot 8 \cdot 8  \tag{6}\\
& =\max \left(x_{m, n}\right) \cdot 8 \tag{7}
\end{align*}
$$

So applying $8 \times 8 \mathrm{DCT}$ to an input with $\mathrm{min} / \mathrm{max}$ value of [-128, 127] scales the output $\mathrm{min} / \mathrm{max}$ value to:

$$
\begin{align*}
\min \left(X_{0,0}\right) & =-128 \cdot 8=-1024  \tag{8}\\
\max \left(X_{0,0}\right) & =127 \cdot 8=1016 \tag{9}
\end{align*}
$$

- If $u \neq 0$ or $v \neq 0$

In this case, the amplitude of DCT coefficient $X_{u, v}$ will be maximized if the input data sequence resonates with (i.e. match the signs of) the cosine signal of the corresponding DCT bases. We will show that this value is less than or equal to the magnitude when $u, v=0$. We first consider the 1 D case and then use it to calculate the 2D case. The

1D DCT is as follows.

$$
\begin{equation*}
X_{u}=\frac{\alpha_{u}}{2} \sum_{m=0}^{7} x_{m} \times \cos \left[\frac{\pi(2 m+1) u}{16}\right] \tag{10}
\end{equation*}
$$

Where the DCT bases are:

$$
\begin{equation*}
\frac{\alpha_{u}}{2} \cos \left[\frac{\pi(2 m+1) u}{16}\right], \quad m, u \in[0 . .7] \tag{11}
\end{equation*}
$$

This 1D DCT will be maximized when the signs of $x_{m}$ match the signs of the DCT bases. Likewise, it will be minimized when the signs are exactly the opposite. Therefore, we compare the absolute sum of the DCT bases and show that it is less than or equal to the sum when $u=0$. This absolute sum of DCT bases can be interpreted as the scale-up factor as it shows how much the input 1's with matching signs are scaled up. The following values are rounded to the third decimal place.

$$
\begin{aligned}
& \text { - } u=0: X_{0}=\frac{\alpha_{0}}{2} \sum_{m=0}^{7} \operatorname{abs}(1)=2 \sqrt{2}=\mathbf{2 . 8 2 8} \\
& \text { - } u=1: X_{1}=\frac{\alpha_{1}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{\pi(2 m+1)}{16}\right]\right)=2.563 \\
& \text { - } u=2: X_{2}=\frac{\alpha_{2}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{2 \pi(2 m+1)}{16}\right]\right)=2.613 \\
& \text { - } u=3: X_{3}=\frac{\alpha_{3}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{3 \pi(2 m+1)}{16}\right]\right)=2.563 \\
& \text { - } u=4: X_{3}=\frac{\alpha_{4}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{4 \pi(2 m+1)}{16}\right]\right)=2.828 \\
& \text { - } u=5: X_{3}=\frac{\alpha_{5}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{5 \pi(2 m+1)}{16}\right]\right)=2.563 \\
& \text { - } u=6: X_{3}=\frac{\alpha_{6}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{6 \pi(2 m+1)}{16}\right]\right)=2.613 \\
& \text { - } u=7: X_{3}=\frac{\alpha_{7}}{2} \sum_{m=0}^{7} \operatorname{abs}\left(\cos \left[\frac{7 \pi(2 m+1)}{16}\right]\right)=2.563
\end{aligned}
$$

We can see that for all $u$, the absolute sums of DCT bases are less than or equal to the sum when $u=0$. 2D DCT is simply a DCT on each axis (rows and columns), so the

2D scale-up factors will be a pairwise product for any pairs of $u$ with replacement. This will still not exceed the value when we choose $u=0$ twice. Therefore, we can conclude that the minimum and maximum values calculated in the $u, v=0$ case will hold for all $8 \times 8$ DCT coefficients. Thus, $8 \times 8$ DCT will scale up the $\min /$ max value by 8 .

## B. Compute cost to decode JPEG

JPEG is decoded through the following steps.
(a) Decode Huffman codes to RLE symbols
(b) Decode RLE symbols to quantized DCT coefficients
(c) De-quantize the DCT coefficients
(d) Apply inverse-DCT to the DCT coefficients
(e) Shift value from $[-128,127]$ to $[0,255]$
(f) Upsample $\mathrm{Cb}, \mathrm{Cr}$ by $2 \times$ for each dimension
(g) Convert YCbCr to RGB

We count the number of operations (OPs) for each step:
(a) Read $N_{s}$ Huffman codes and recover $N_{s}$ RLE symbols $=N_{s}+N_{s}=2 N_{s} \mathrm{OPs}$
(b) Read $N_{s}$ RLE symbols and recover $8 \times 8$ quantized DCT coefficients $=N_{s}+64$ OPs
(c) Multiply $8 \times 8$ quantization table element-wise with $8 \times 8 \mathrm{DCT}$ coefficients $=64 \mathrm{OPs}$
(d) The $8 \times 8$ inverse DCT is given as:

$$
\begin{equation*}
x_{m, n}=\frac{1}{4} \gamma_{m} \gamma_{n} \sum_{u, v} X_{u, v} \cos \left[\frac{(2 m+1) u \pi}{16}\right] \cos \left[\frac{(2 n+1) v \pi}{16}\right] \tag{12}
\end{equation*}
$$

Where

$$
\gamma_{i}= \begin{cases}\frac{1}{\sqrt{2}} & \text { if } i=0 \\ 1 & \text { otherwise }\end{cases}
$$

- If $m, n \in[1 . .7]$

We need 2 cos $+10 \mathrm{mul}+3$ add +3 div per step as $\gamma_{i}=1$. Number of OPs: $7 \times 7 \times 18=882$

- If $m=0, n \in[1 . .7]$ or $m \in[1 . .7], n=0$

We need 2 cos $+10 \mathrm{mul}+3$ add +4 div +1 sqrt per step. OPs: $7 \times 20 \times 2=280$

- If $m=0, n=0$
$2 \cos +10 \mathrm{mul}+3$ add $+5 \mathrm{div}+2 \mathrm{sqrt}=22 \mathrm{OPs}$
Total OPs per $8 \times 8$ block: $882+280+22=1184$
(e) Add 128 to every elements of $x_{m, n}=64$ OPs
(f) Upsample $8 \times 8 \mathrm{Cb}$ and Cr block to $16 \times 16: 256 \times$ $2=512$ OPs per 6 blocks. This is because 4 Y blocks are paired with 1 Cb and Cr block. Per-block cost: $512 / 6=85.3$ OPs.
(g) YCbCr is converted to RGB using [1]:
$R=Y+1.402\left(C_{r}-128\right)$
$G=Y-0.344136\left(C_{b}-128\right)-0.714136\left(C_{r}-128\right)$
$B=Y+1.772\left(C_{b}-128\right)$

For three blocks - Y, Cb , and Cr - the number of OPs is $64 \times(2 \mathrm{add}+6 \mathrm{sub}+4 \mathrm{mul})=768$. We ignore the cost of rounding and min/max clamping for simplicity. Thus, the per-block cost is $768 / 3=256$ OPs

Recovering DCT coefficients requires going through steps (a)-(c), where the compute cost sums up to $3 N_{s}+128$ OPs. Full decoding requires $3 N_{s}+1717.3$ OPs. We can see that most of the decoding cost comes from the inverse-DCT, which costs 1184 OPs to compute. Note that this result is only an estimate and can vary under different settings.

## C. Conversion matrix for sub-block conversion

The conversion matrix $A$ can be calculated using the basis transform from $L \times M$ number of $N \times N$ DCT bases to $L N \times M N$ DCT bases. Let $T^{N \times N}$ as a 1-D DCT bases of size $N \times N$ then:

$$
T^{N \times N}=\sqrt{\frac{2}{N}}\left[\begin{array}{cccc}
\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \cdots & \frac{1}{\sqrt{2}}  \tag{13}\\
\cos \left[\frac{1 \pi}{2 N}\right] & \cos \left[\frac{3 \pi}{2 N}\right] & \cdots & \cos \left[\frac{(2 N-1) \pi}{2 N}\right] \\
\vdots & \vdots & \ddots & \vdots \\
\cos \left[\frac{(N-1) \pi}{2 N}\right] & \cos \left[\frac{3(N-1) \pi}{2 N}\right] & \cdots & \cos \left[\frac{(2 N-1)(N-1) \pi}{2 N}\right]
\end{array}\right]
$$

$T^{N \times N}$ is an orthogonal matrix [2]. Hence,

$$
\begin{equation*}
T T^{T}=I \quad T^{T}=T^{-1} \tag{14}
\end{equation*}
$$

Define $B_{\text {large }}$ as $T^{L N \times L N}$ and $B_{\text {small }}$ as a block diagonal matrix of $T^{N \times N}$ with size $L N \times L N$ :

$$
B_{\text {small }}=\left[\begin{array}{ccc}
T^{N \times N} & \cdots & 0  \tag{15}\\
\vdots & \ddots & \vdots \\
0 & \cdots & T^{N \times N}
\end{array}\right]
$$

Then the conversion matrix $A_{L, N}$ is [3]:

$$
\begin{align*}
& B_{\text {large }}=A_{L, N} \times B_{\text {small }}  \tag{16}\\
& A_{L, N}=B_{\text {large }} \times B_{\text {small }}^{-1} \tag{17}
\end{align*}
$$

Where $B_{\text {small }}^{-1}=B_{\text {small }}^{T}$ due to Eqs. (14) and (15). Thus,

$$
\begin{equation*}
A_{L, N}=B_{\text {large }} \times B_{\text {small }}^{T} \tag{18}
\end{equation*}
$$

We can also see that $B_{\text {large }}^{-1}=B_{\text {large }}^{T}$. Thus,

$$
\begin{align*}
A_{L, N}^{-1} & =\left(B_{\text {large }} \times B_{\text {small }}^{T}\right)^{-1}  \tag{19}\\
& =\left(B_{\text {small }}^{T}\right)^{-1} \times B_{\text {large }}^{-1}  \tag{20}\\
& =B_{\text {small }} \times B_{\text {large }}^{T}  \tag{21}\\
& =A_{L, N}^{T} \tag{22}
\end{align*}
$$

## D. Sub-band approximation

Define $x(m, n)$ as the 2D image data, and $X(k, l)$ as the 2D DCT coefficient of $x(m, n)$ where $m, n, k, l \in[0 . . N-$ 1]. Then, define $x_{L L}\left(m^{\prime}, n^{\prime}\right)$ as the $2 \times$ downsized image of $x(m, n)$. Then $x_{L L}$ is given as:

$$
\begin{gather*}
x_{L L}\left(m^{\prime}, n^{\prime}\right)=\frac{1}{4}\left\{x\left(2 m^{\prime}, 2 n^{\prime}\right)+x\left(2 m^{\prime}+1,2 n^{\prime}\right)+\right. \\
\left.x\left(2 m^{\prime}, 2 n^{\prime}+1\right)+x\left(2 m^{\prime}+1,2 n^{\prime}+1\right)\right\} \tag{23}
\end{gather*}
$$

where $m^{\prime}, n^{\prime}, k^{\prime}, l^{\prime} \in\left[0, \ldots \frac{N}{2}-1\right]$. Similarly, define $\overline{X_{L L}}\left(k^{\prime}, l^{\prime}\right)$ as the 2D DCT coefficient of $x_{L L}\left(m^{\prime}, n^{\prime}\right)$. Mukherjee and Mitra's work [4] shows that $X(k, l)$ can be represented in terms of $\overline{X_{L L}}(k, l)$ :

$$
X(k, l)= \begin{cases}2 \cos \left(\frac{\pi k}{2 N}\right) \cos \left(\frac{\pi l}{2 N}\right) \overline{X_{L L}}(k, l) & 0 \leq k, l \leq \frac{N}{2}-1  \tag{24}\\ 0 & \text { otherwise }\end{cases}
$$

Which can be further simplified assuming that $k, l$ are negligible compared to $2 N: \frac{\pi k}{2 N}, \frac{\pi l}{2 N} \approx 0$

$$
X(k, l) \approx \begin{cases}2 \overline{X_{L L}}(k, l) & 0 \leq k, l \leq \frac{N}{2}-1  \tag{25}\\ 0 & \text { otherwise }\end{cases}
$$

We can follow the same process for $L \times M$ downsampling from $L N \times M N$ DCT coefficient to $N \times N$ DCT [4]:

$$
X(k, l) \approx \begin{cases}\sqrt{L M} \overline{X_{L L}}(k, l) & 0 \leq k, l \leq N-1  \tag{26}\\ 0 & \text { otherwise }\end{cases}
$$

Thus, Eq. (26) implies the approximate up and downsampling formula as:

- Upsampling:

$$
X_{L N \times M N} \approx\left[\begin{array}{cc}
\sqrt{L M} X_{N \times N} & \mathbf{0}_{N \times(M N-N)}  \tag{27}\\
\mathbf{0}_{(L N-N) \times N} & \mathbf{0}_{(L N-N) \times(M N-N)}
\end{array}\right]
$$

- Downsampling:

$$
\begin{equation*}
X_{N \times N} \approx \frac{1}{\sqrt{L M}} X_{L N \times M N}[0: N, 0: N] \tag{28}
\end{equation*}
$$

## E. Fourier transform's rotational property

The proof of the Fourier transform's rotational property is as follows. Define $g(\mathbf{x})$ as a function of $x$ where $\mathbf{x} \in \mathbb{R}^{d}$. The Fourier transform of $g$ is:

$$
\begin{equation*}
\mathcal{F}[g(\mathbf{x})]=G(\mathbf{X})=\int g(\mathbf{x}) e^{-j 2 \pi \mathbf{x}^{T} \mathbf{x}} d \mathbf{x} \tag{29}
\end{equation*}
$$

We can describe the rotated version of $\mathbf{x}$ as $\mathbf{u}=\mathbf{A x}$ where $\mathbf{A}$ is a rotation matrix in which

$$
\begin{align*}
\mathbf{A}^{T} & =\mathbf{A}^{-1}  \tag{30}\\
\mathbf{x}=\mathbf{A}^{-1} \mathbf{u} & =\mathbf{A}^{T} \mathbf{u} \tag{31}
\end{align*}
$$

Define the rotated version of $g$ as $h$ where $g(\mathbf{A x})=h(\mathbf{x})$. Then, the Fourier transform of $g(\mathbf{A x})$ becomes:

$$
\begin{align*}
\mathcal{F}[g(\mathbf{A x})]= & \mathcal{F}[h(\mathbf{x})]=\int h(\mathbf{x}) e^{-j 2 \pi \mathbf{x}^{T} \mathbf{x}} d \mathbf{x}  \tag{32}\\
= & \int g(\mathbf{A x}) e^{-j 2 \pi \mathbf{x}^{T} \mathbf{x}} d \mathbf{x}  \tag{33}\\
= & \int g(\mathbf{u}) e^{-j 2 \pi\left(\mathbf{A}^{T} \mathbf{u}\right)^{T} \mathbf{x}} d \mathbf{u}  \tag{34}\\
& (\because d \mathbf{u}=|\operatorname{det}(\mathbf{A})| d \mathbf{x}, \quad|\operatorname{det}(\mathbf{A})|=1)  \tag{35}\\
= & \int g(\mathbf{u}) e^{-j 2 \pi \mathbf{u}^{T} \mathbf{A} \mathbf{x}} d \mathbf{u}  \tag{36}\\
\mathcal{F}[g(\mathbf{A x})]= & \int g(\mathbf{u}) e^{-j 2 \pi \mathbf{u}^{T} \mathbf{A x}} d \mathbf{u}=G(\mathbf{A X}) \tag{37}
\end{align*}
$$

Thus, the Fourier transform of the rotated $g(\mathbf{x})$ is equal to rotating the Fourier transform $G(\mathbf{X})$.

## F. DCT to DFT sub-block conversion

If we define $\omega=\exp (-j 2 \pi / N)$ then the $N \times N$ 1-D DFT bases matrix $W^{N \times N}$ is given as:

$$
W^{N \times N}=\frac{1}{\sqrt{N}}\left[\begin{array}{ccccc}
1 & 1 & 1 & \cdots & 1  \tag{38}\\
1 & \omega & \omega^{2} & \cdots & \omega^{N-1} \\
1 & \omega^{2} & \omega^{4} & \cdots & \omega^{2(N-1)} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \omega^{N-1} & \omega^{2(N-1)} & \cdots & \omega^{(N-1)(N-1)}
\end{array}\right]
$$

Setting $D_{N \times M}$ as the DFT coefficient block of size $N \times M$, the conversion formula becomes:

$$
D_{L N \times M N}=\hat{A}_{L, N}\left[\begin{array}{ccc}
X_{N \times N}^{0,0} & \cdots & X_{N \times N}^{0, M-1}  \tag{39}\\
\vdots & \ddots & \vdots \\
X_{N \times N}^{L-1,0} & \cdots & X_{N \times N}^{L-1, M-1}
\end{array}\right] \hat{A}_{M, N}^{T}
$$

The corresponding decomposition is then:

$$
\left[\begin{array}{ccc}
X_{N \times N}^{0,0} & \cdots & X_{N \times N}^{0, M-1}  \tag{40}\\
\vdots & \ddots & \vdots \\
X_{N \times N}^{L-1,0} & \cdots & X_{N \times N}^{L-1, M-1}
\end{array}\right]=\hat{A}_{L, N}^{-1} D_{L N \times M N} \hat{A}_{M, N}^{-1^{T}}
$$

Where $\hat{A}$ denotes the DCT to DFT conversion matrix. This can be calculated by following the same process from Eq. (18) with replacing $B_{\text {large }}$ as $W$ of appropriate size.

## G. Resize strategy for DCT

While it is possible to do an arbitrary resize of $\frac{P}{Q} \times \frac{R}{S}$ by first upsampling $P \times R$ times and downsampling by $Q \times S$, it is preferable to avoid it due to the compute cost of an additional resize. Therefore, we utilize a different strategy. During random resized crop, we fuse the cropping and resize together in a way that the crop size is limited to the factors of a resize target. For example, if we are resizing to $28 \times 28 \times 8 \times 8$, then the height and width of the crop window are selected from the set: $\{1,2,4,7,14,28,56, \ldots\}$. This way, we can reduce computation as upsampling or downsampling is limited to an integer multiple. This strategy has been used throughout our experiments.

## H. Comparison with Pillow-SIMD

Pillow-SIMD [5] is a highly optimized version of Pillow [6]. It allows faster resizing using CPU SIMD instructions. The main bottleneck of our pipeline is resizing. If we reduce resizing by pre-resizing the data to $256 \times 256$, then our method shows $9.1 \%$ and $29.2 \%$ faster training and evaluation versus Pillow-SIMD as shown in Tab. 1. We believe our method could be further sped up given analogous optimization efforts.

|  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Method | Img. size | Model | Train Data | Fwd/Bwd | Train | Eval Data | Fwd | Eval |
| SIMD | $512^{2}$ | ViT-Ti | 1043.3 | 835.2 | 724.7 | 1743.9 | 2832.5 | 1630.8 |
| Ours | $512^{2}$ | ViT-Ti | 816.2 | 857.2 | 687.6 | 775.3 | 2847.5 | 752.3 |
|  |  | $(-21.8 \%)$ | $(+2.6 \%)$ | $(-5.1 \%)$ | $(-55.5 \%)$ | $(+0.5 \%)$ | $(-53.9 \%)$ |  |
| SIMD | $256^{2}$ | ViT-Ti | 1176.4 | 839.6 | 722.4 | 2232.0 | 2832.6 | 1893.9 |
| Ours | $256^{2}$ | ViT-Ti | 1530.9 | 854.2 | 788.0 | 3070.6 | 2842.9 | 2447.1 |
|  |  |  | $(+30.1 \%)$ | $(+1.7 \%)$ | $(+9.1 \%)$ | $(+37.6 \%)$ | $(+0.4 \%)$ | $(+29.2 \%)$ |

Table 1. Comparison with Pillow-SIMD. Our pipeline shows faster training and evaluation if we reduce resizing.

## I. Training settings

The hyperparameter settings and augmentation subset we used for training are reported in Tables 2 and 3. RGB models used the recipe given in [7], including the SwinV2 models [8], for a fair comparison.

| Model | Learning <br> Rate | Weight <br> Decay | RandAug. <br> Magnitude | Input <br> Size | Epochs |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ViT-Ti | $1 \mathrm{e}-3$ | $1 \mathrm{e}-4$ | 10 | $224^{2}$ | 300 |
| ViT-S | $1 \mathrm{e}-3$ | $1 \mathrm{e}-4$ | 10 | $224^{2}$ | 90 |
| SwinV2-T (RGB) | $1 \mathrm{e}-3$ | $1 \mathrm{e}-4$ | 10 | $256^{2}$ | 300 |
| JPEG-Ti | $3 \mathrm{e}-3$ | $1 \mathrm{e}-4$ | 3 | $224^{2}$ | 300 |
| JPEG-S | $3 \mathrm{e}-3$ | $3 \mathrm{e}-4$ | 3 | $224^{2}$ | 90 |
| SwinV2-T (DCT) | $1 \mathrm{e}-3$ | $1 \mathrm{e}-4$ | 3 | $256^{2}$ | 300 |

Table 2. Hyperparameter settings of the trained models.

| Models | Subset |
| :---: | :---: |
| JPEG-Ti | Brightness, Contrast, Color, AutoContrast, <br> AutoSaturation, MidfreqAug, Posterize, SolarizeAdd, <br> Grayscale, ChromaDrop, Translate, Cutout, Rotate90 |
| JPEG-S <br> Srightness, Contrast, Color, AutoContrast, |  |
| RGB2-T (DCT) | AutoSaturation, MidfreqAug, Sharpness, Posterize, <br> Grayscale, ChromaDrop, Translate, Cutout, Rotate90 |
| Brightness, Contrast, Equalize, Color, |  |
| Rodels [7] | AutoContrast, Sharpness, Invert, Posterize, Solarize, <br> SolarizeAdd, Translate, Cutout, Rotate, Shear |

Table 3. Augmentation subset of RandAugment for the models.

## J. Smaller patch sizes

SwinV2 [8] uses a patch size of $4.8 \times 8$ JPEG DCT blocks can be adapted to support this by decomposing them into sixteen $2 \times 2$ blocks using sub-block conversion (Sec 5.2.). Then, we can use any of the embedding strategies discussed in Sec. 4. In general, for a desired patch size $p$, we need to decompose the DCT blocks to be at most $\frac{p}{2} \times \frac{p}{2}$.

## K. Measurement process

Latency measurements to decode and augment follow Algorithms 1 and 2. Data Loading throughputs for both train and evaluation is measured using Algorithm 3. Model Fwd/Bwd measures the throughput of model forward and backward pass using Algorithm 4. Model Fwd measures the throughput of the model forward pass using Algorithm 5. Train Pipeline and Eval Pipeline throughput is measured using Algorithms 6 and 7.

```
Algorithm 1 Decoding latency measurement
    latency \(\leftarrow 0\)
    for \(i=0 . . N\) do
        start_time \(\leftarrow\) time ()
        data \(\leftarrow\) decode(Filename)
        end_time \(\leftarrow\) time()
        latency \(\leftarrow\) latency + (end_time - start_time \()\)
    end for
    return latency \(/ N\)
```

```
Algorithm 2 Augment latency measurement
    latency \(\leftarrow 0\)
    for \(i=0 . . N\) do
        data \(\leftarrow\) decode(Filename)
        start_time \(\leftarrow\) time ()
        data \(\leftarrow\) augment(data)
        end_time \(\leftarrow\) time()
        latency \(\leftarrow\) latency + (end_time - start_time)
    end for
    return latency \(/ N\)
```

```
Algorithm 3 Data Loading throughput measurement
    start_time \(\leftarrow\) time()
    for \(i=0 . . N\) do
        data, label \(\leftarrow\) to_gpu(next(data_loader))
    end for
    end_time \(\leftarrow\) time()
    latency \(\leftarrow\) end_time - start_time
    return \((N \cdot \operatorname{len}(\) data \()) /\) latency
```

```
Algorithm 4 Model Fwd/Bwd throughput measurement
    dummy_data, dummy_label \(\leftarrow\) to_gpu(random(data_shape))
    start_time \(\leftarrow\) time()
    for \(i=0 . . N\) do
        data, label \(\leftarrow\) copy(dummy_data, dummy_label)
        mixup(data, label)
        output \(\leftarrow\) model(data)
        loss \(\leftarrow\) criterion(output, label)
        backward(loss)
        step(optimizer)
    end for
    end_time \(\leftarrow\) time()
    latency \(\leftarrow\) end_time - start_time
    return \((N \cdot\) len(dummy_data)) \(/\) latency
```

```
Algorithm 5 Model Fwd throughput measurement
    dummy_data, dummy_label \(\leftarrow\) to_gpu(random(data_shape))
    start_time \(\leftarrow\) time()
    for \(i=0 . . N\) do
        output \(\leftarrow\) model(dummy_data)
        loss \(\leftarrow\) criterion(output, dummy_label)
    end for
    end_time \(\leftarrow\) time()
    latency \(\leftarrow\) end_time - start_time
    return \((N \cdot \operatorname{len}(\) dummy_data) \() /\) latency
```

```
Algorithm 6 Train Pipeline throughput measurement
    start_time \(\leftarrow\) time()
    for \(i=0 . . N\) do
        data, label \(\leftarrow\) to_gpu(next(data_loader))
        mixup(data, label)
        output \(\leftarrow\) model(data)
        loss \(\leftarrow\) criterion(output, label)
        backward(loss)
        step(optimizer)
    end for
    end_time \(\leftarrow\) time()
    latency \(\leftarrow\) end_time - start_time
    return \((N \cdot \operatorname{len}(\) data \()) /\) latency
```

```
Algorithm 7 Eval Pipeline throughput measurement
```

Algorithm 7 Eval Pipeline throughput measurement
start_time $\leftarrow$ time()
start_time $\leftarrow$ time()
for $i=0 . . N$ do
for $i=0 . . N$ do
data, label $\leftarrow$ to_gpu(next(data_loader))
data, label $\leftarrow$ to_gpu(next(data_loader))
output $\leftarrow$ model(data)
output $\leftarrow$ model(data)
loss $\leftarrow$ criterion(output, label)
loss $\leftarrow$ criterion(output, label)
end for
end for
end_time $\leftarrow$ time()
end_time $\leftarrow$ time()
latency $\leftarrow$ end_time - start_time
latency $\leftarrow$ end_time - start_time
return $(N \cdot \operatorname{len}($ data $)) /$ latency

```
    return \((N \cdot \operatorname{len}(\) data \()) /\) latency
```


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