# Supplementary Material for Exploring and Exploiting Uncertainty for Incomplete Multi-View Classification

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## 1. Large-Scale Multi-view Datasets Experiments

To validate the effectiveness of the proposed method on large-scale datasets, we conduct experiments on two datasets. **Caltech-101** [1] is a 6-view dataset consists of pictures of objects belonging to 101 classes, plus one background clutter class. Each class contains roughly 40 to 800 images, totalling 9144 images. **NUS-WIDE-OBJECT** [2] is a 5-view dataset consists of pictures belonging to 31 classes, totally 30,000 images.

We compare the proposed algorithm with 4 state-of-the-art multi-view classification methods. **CPM-Nets** [3] directly learns the joint latent representations for all views with available data, and maps the latent representation to classification predictions. **DeepIMV** [4] applies the information bottleneck (IB) framework to obtain marginal and joint representations with the available data, and constructs the view-specific and multi-view predictors to obtain the classification predictions. **MMD** [5] models both the feature-level and modality-level dynamicities and introduces a sparse gating strategy to trust-worthily fuse the complete multi-view data. **DCP** [6] provides an information theoretical framework under which the consistency learning and data recovery are treated as a whole. The missing views are recovered by minimizing the conditional entropy through dual prediction. For the MMD method which can not deal with incomplete multi-view data, we first impute the missing views with the corresponding means, and then train MMD to obtain the classification predictions. As shown in Fig. **S1**, our method still achieves the superior performance on large-scale datasets.

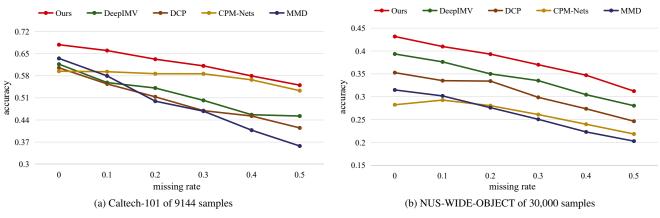


Figure S1. Classification performance with  $\eta = [0, 0.1, 0.2, 0.3, 0.4, 0.5]$ .

#### **2.** Details and Impact of Hypeparameter $\lambda$

**Details.** Same as previous methods [7,8], we set  $\lambda = min(F, e/E)$  where F, e and E denote the final value of  $\lambda$ , iteration epoch and the parameter controlling the decay rate of  $\lambda$ . **Impact.** we conduct experiments on ROSMAP with different missing rates  $\eta$  to investigate the influence of  $\lambda$  in terms of decay rate and the final value. Specifically, we change the final value F or parameter E to control the decay rate. As shown in Fig. S2, our method is robust to the final value and decay rate of  $\lambda$ .

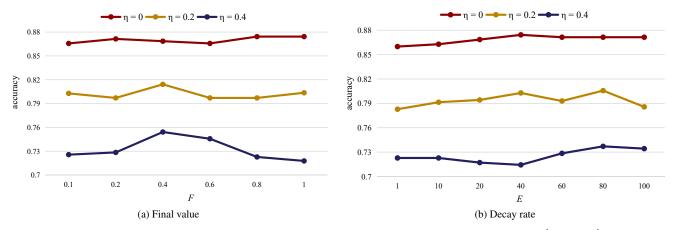


Figure S2. Classification performance with different final values and decay rates of  $\lambda$  on ROSMAP under  $\eta = [0, 0.2, 0.4]$  where we set E = 50 in Fig. S2a and F = 1 in Fig. S2b.

### 3. Details of Constructing the Incomplete Multi-view Data.

Same as previous methods [3,4], we construct the incomplete multi-view data to satisfy the following requirements. 1. Missing at random with the desired missing rate  $\eta$ . 2. Each sample has at least one view that is not missing. Therefore, the following steps are conducted. 1. Calculate how many views are missing with  $N^m = \eta NV$ , where N and V are number of samples and views respectively. 2. Randomly assign  $N^m$  to each sample while ensure that at least one view is available for each sample (i.e.,  $N^m = \sum_{i=1}^N N_i^m$  and  $N_i^m < V$ , where  $N_i^m$  is the number assigned to each sample). 3. Randomly select  $V - N_i^m$  available views for each sample.

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