

## A. Appendix

### A.1. Methodology

The algorithm for the proposed LSFSL approach is provided in Algorithm 1. The sequential distillation and online self-distillation approach to incorporate shape information is illustrated in Algorithm 2 and Algorithm 3.

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#### Algorithm 2 LSFSL-Distill: Training Algorithm

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**Input:** dataset  $\mathcal{D}$ , fixed LSFSL-trained RIN model  $R_t$  with feature extractor  $f_t$  and classifier  $g_t$ , randomly initialized student RIN model  $R_s$  with feature extractor  $f_s$  and classifier  $g_s$ , epochs  $E$ , softmax operator  $\sigma$ , cross-entropy loss  $CE$ , Kullback-Leibler divergence loss  $KLD$ , cross-entropy loss factor  $\alpha$ , teacher-student decision alignment loss factor  $\beta$

- 1: **for** epoch  $e \in \{1, 2, \dots, E\}$  **do**
  - 2:   sample a mini-batch  $(x, y) \sim \mathcal{D}$
  - 3:    $R_t(x) = g_t(f_t(x))$
  - 4:    $R_s(x) = g_s(f_s(x))$
  - 5:    $\mathcal{L}_{CER} = CE(R_s(x), y)$
  - 6:    $\mathcal{L}_{DA} = KLD(R_t(x), R_s(x))$
  - 7:    $\mathcal{L} = \alpha\mathcal{L}_{CER} + \beta\mathcal{L}_{DA}$
  - 8:   Update parameters of  $R_s$  based on  $\mathcal{L}$  using Stochastic Gradient Descent (SGD)
  - 9: **end for**
  - 10: **return** RIN student model  $R_s$
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### A.2. Analysis Visualizations

The texture bias, spurious correlation, and statistical regularity analysis are performed by applying different textures by stylization, class-specific tints, and radial low-pass Fourier filters at increasing severities as shown in Figure 5, Figure 6 and Figure 7.

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#### Algorithm 3 LSFSL-Online: Training Algorithm

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**Input:** dataset  $\mathcal{D}$ , randomly initialized RIN model  $R$  with feature extractor  $f_\Phi$  and classifier  $g_\Theta$ , randomly initialized SIN model  $S$  with feature extractor  $f_\phi$  and classifier  $g_\omega$ , randomly initialized and fixed teacher RIN model  $R_t$  with feature extractor  $f_{t,\Phi}$  and classifier  $g_{t,\Theta}$ , epochs  $E$ , softmax operator  $\sigma$ , stopgrad operator  $SG$ , cross-entropy loss  $CE$ , Kullback-Leibler divergence loss  $KLD$ , mean square error  $MSE$ , Sobel edge operator  $h$ , feature alignment loss factors  $(\gamma_r, \gamma_s)$ , decision alignment loss factors  $(\lambda_r, \lambda_s)$ , teacher-student decision alignment loss factor  $\beta$

- 1: **for** epoch  $e \in \{1, 2, \dots, E\}$  **do**
  - 2:   sample a mini-batch  $(x, y) \sim \mathcal{D}$
  - 3:    $x_{shape} = h(x)$
  - 4:    $z_\Phi = f_\Phi(x)$
  - 5:    $z_\phi = f_\phi(x_{shape})$
  - 6:    $R(x) = g_\Theta(f_\Phi(x))$
  - 7:    $S(h(x)) = g_\omega(f_\phi(h(x_{shape})))$
  - 8:    $R_t(x) = g_{t,\Theta}(f_{t,\Phi}(x))$
  - 9:    $\mathcal{L}_{CER} = CE(\sigma(R(x)), y)$
  - 10:    $\mathcal{L}_{CES} = CE(\sigma(S(h(x))), y)$
  - 11:    $\mathcal{L}_{FAR} = MSE(z_\Phi, SG(z_\phi))$  ▷ (Eq. 5)
  - 12:    $\mathcal{L}_{FAS} = MSE(SG(z_\Phi), z_\phi)$  ▷ (Eq. 6)
  - 13:    $\mathcal{L}_{FA} = \gamma_r\mathcal{L}_{FAR} + \gamma_s\mathcal{L}_{FAS}$  ▷ (Eq. 7)
  - 14:    $\mathcal{L}_{DAR} = KLD(\sigma(R(x)), SG(\sigma(S(h(x))))$  ▷ (Eq. 8)
  - 15:    $\mathcal{L}_{DAS} = KLD(SG(\sigma(R(x))), \sigma(S(h(x))))$  ▷ (Eq. 9)
  - 16:    $\mathcal{L}_{DA} = \lambda_r\mathcal{L}_{DAR} + \lambda_s\mathcal{L}_{DAS}$  ▷ (Eq. 10)
  - 17:    $\mathcal{L}_{TS} = KLD(\sigma(R(x)), \sigma(R_t(x)))$
  - 18:    $\mathcal{L} = \mathcal{L}_{CER} + \mathcal{L}_{CES} + \mathcal{L}_{FA} + \mathcal{L}_{DA} + \beta\mathcal{L}_{TS}$
  - 19:   Update parameters of  $R$  and  $S$  based on  $\mathcal{L}$  using Stochastic Gradient Descent
  - 20:   Update  $R_t$  as EMA of  $R$
  - 21: **end for**
  - 22: **return** RIN student model  $R$
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Figure 5. An illustration of the various stylized miniImageNet images generated for varying stylization intensities to perform the texture bias analysis in Section 6.1.

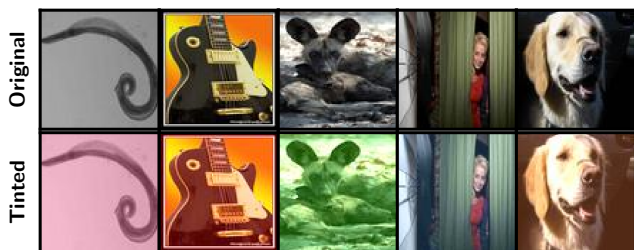


Figure 6. An illustration of class-specific tinted images generated for spurious correlation analysis is provided in Section 6.2.

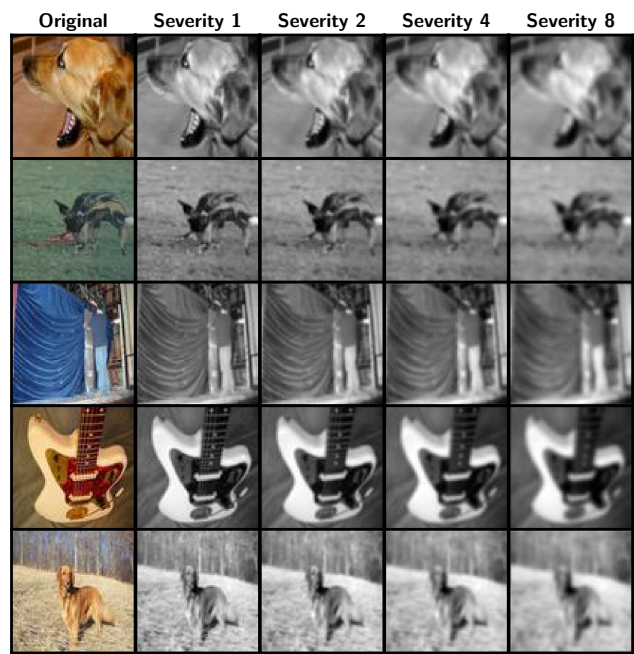


Figure 7. An illustration of low-pass filtered images generated for statistical regularity analysis in Section 6.3.