ACT-Diffusion: Efficient Adversarial Consistency Training for One-step Diffusion Models

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Abstract

Though diffusion models excel in image generation, their step-by-step denoising leads to slow generation speeds. Consistency training addresses this issue with single-step sampling but often produces lower-quality generations and requires high training costs. In this paper, we show that optimizing consistency training loss minimizes the Wasserstein distance between target and generated distributions. As timestep increases, the upper bound accumulates previous consistency training losses. Therefore, larger batch sizes are needed to reduce both current and accumulated losses. We propose Adversarial Consistency Training (ACT), which directly minimizes the Jensen-Shannon (JS) divergence between distributions at each timestep using a discriminator. Theoretically, ACT enhances generation quality, and convergence. By incorporating a discriminator into the consistency training framework, our method achieves improved FID scores on CIFAR10 and ImageNet 64×64 and LSUN Cat 256×256 datasets, retains zero-shot image inpainting capabilities, and uses less than $1/6$ of the original batch size and fewer than $1/2$ of the model parameters and training steps compared to the baseline method, this leads to a substantial reduction in resource consumption. Our code is available: https://github.com/kong13661/ACT

1. Introduction

Diffusion models, known for their success in image generation [12, 19, 31, 43, 44, 53], utilize diffusion processes to produce high-quality, diverse images. They also perform tasks like zero-shot inpainting [32] and audio generation [24, 25, 36]. However, they have a significant drawback: lengthy sampling times. These models generate target distribution samples by iterative denoising a Gaussian noise input, a process that involves gradual noise reduction until samples match the target distribution. This limitation affects their practicality and efficiency in real-world applications.

The lengthy sampling times of diffusion models have spurred the creation of various strategies to tackle this issue. Several models and techniques have been suggested to enhance the efficiency of diffusion-based image generation [4, 29, 57]. Recently, consistency models [45] have been introduced to speed up the diffusion models' sampling process. A consistency function is one that consistently yields the same output along a specific trajectory. To use consistency models, the trajectory from noise to the target sample must be obtained. By fitting the consistency function, the model can generate data within 1 or 2 steps.

The score-based model [44], an extension of the diffusion model in continuous time, gradually samples from a normal distribution p_T to the sample distribution p_0. In deterministic sampling, it essentially solves an Ordinary Differential Equation (ODE), with each sample representing an ODE trajectory. Consistency models generate samples using a consistency function that aligns every point on the ODE trajectory with the ODE endpoint. However, deriving the true ODE trajectory is complex. To tackle this, consistency models suggest two methods. The first, consistency distillation, trains a score-based model to obtain the ODE trajectory. The second, consistency training, approximates the trajectory using a conditional one. Compared to distillation, consistency training has a larger error, leading to lower sample quality. The consistency function is trained by equating the model's output at time t_{n+1} with its output at time t_n.

Generative Adversarial Networks (GANs) [3, 15, 55],

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unlike consistency training, can directly minimize the distance between the model's generated and target distributions via the discriminator, independent of the model's output at previous time t_{n-1}. Drawing from GANs, we introduce Adversarial Consistency Training. We first theoretically explain the need for large batch sizes in consistency training by showing its equivalence to optimizing the upper bound of the Wasserstein-distance between the model's generated and target distributions. This upper bound consists of the accumulated consistency training loss $\mathcal{L}_{CT}^{t_k}$, the distance between sampling distributions, and the accumulated error, all of which increase with t. Hence, a large batch size is crucial to minimize the error from the previous time t. To mitigate the impact of $\mathcal{L}_{CT}^{t_k}$ and accumulated error, we incorporate the discriminator into consistency training, enabling direct reduction of the JS-divergence between the generated and target distributions at each timestep t. Our experiments on CIFAR10 [26], ImageNet 64×64 [7] and LSUN Cat 256×256 [51] show that ACT significantly surpasses consistency training while needing less than $1/6$ of the original batch size and less than $1/2$ of the original model parameters and training steps, leading to considerable resource savings. For comparison, we use 1 NVIDIA GeForce RTX 3090 for CIFAR10, 4 NVIDIA A100 GPUs for ImageNet 64×64 and 8 NVIDIA A100 GPUs for LSUN Cat 256×256, while consistency training requires 8, 64, 64 A100 GPUs for CIFAR10, ImageNet 64×64 and LSUN Cat 256×256, respectively.

Our contributions are summarized as follows:

- We demonstrate that consistency training is equivalent to optimizing the upper bound of the W-distance. By analyzing this upper bound, we have identified one reason why consistency training requires a larger batch size.
- Following our analysis, we propose Adversarial Consistency Training (ACT) to directly optimize the JS divergence between the sampling distribution and the target distribution at each timestep t, by incorporating a discriminator into the consistency training process.
- Experimental results demonstrate that the proposed ACT significantly outperforms the original consistency training with only less than $1/6$ of the original batch size and less than $1/2$ of the training steps. This leads to a substantial reduction in resource consumption.

2. Related works

Generative Adversarial Networks GANs have achieved tremendous success in various domains, including image generation [15, 52, 54] and audio synthesis [10]. However, GAN training faces challenges such as instability and mode collapse, where the generator fails to capture the diversity of the training data. To address these issues, several methods have been proposed. For example, spectral normalization, gradient penalty, and differentiable data augmentation techniques have been developed. Spectral normalization [33] constrains the Lipschitz constant of the discriminator, promoting more stable training. Gradient penalty, as employed in the WGAN-GP [17], utilizes the gradient penalty to discriminator to limit the range of gradient, so as to avoid the tend of concentrating the weights around extreme values, when using weight clipping in WGAN [1]. [48] introduces the concept of zero centered gradient penalty, and StyleGAN2 [47] introduces lazy regularization which performs multiple steps of iteration before computing the gradient penalty to improve the efficiency. Moreover, differentiable data augmentation techniques [56] have been introduced to enhance the diversity and robustness of GAN models during training. StyleGAN2-ADA [46] improves GAN performance on small datasets by employing adaptive differentiable data augmentation techniques.

Diffusion Models Diffusion models have emerged as highly successful approaches for generating images [37, 38]. In contrast to the traditional approach of Generative Adversarial Networks (GANs), which involve a generator and a discriminator, diffusion models generate samples by modeling the inverse process of a diffusion process from Gaussian noise. Diffusion models have shown superior stable training process compared to GANs, effectively addressing issues such as checkerboard artifacts [11, 13, 40]. The diffusion process is defined as follows: $\boldsymbol{x}_t = \sqrt{\alpha_t}\boldsymbol{x}_{t-1} + \sqrt{\beta_t}\boldsymbol{\epsilon}_t, \boldsymbol{\epsilon}_t \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$. As t increases, β_t gradually increases, causing $\boldsymbol{x}_t$ to approximate random Gaussian noise. In the reverse diffusion process, $\boldsymbol{x}'_t$ follows a Gaussian distribution, assuming the same variance as in the forward diffusion process. The mean of $\boldsymbol{x}'_t$ is defined as: $\tilde{\boldsymbol{\mu}}_t = \frac{1}{\sqrt{\alpha_t}}\left(\boldsymbol{x}_t - \frac{\beta_t}{\sqrt{1-\bar{\alpha}_t}}\bar{\boldsymbol{\epsilon}}_\theta(\boldsymbol{x}_t, t)\right)$, where $\bar{\alpha}_t = \prod_{k=0}^{t} \alpha_k$ and $\bar{\alpha}_t + \bar{\beta}_t = 1$. The reverse diffusion process becomes: $\boldsymbol{x}_{t-1} = \tilde{\boldsymbol{\mu}}_t + \sqrt{\beta_t}\boldsymbol{\epsilon}, \boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$. The loss function is defined as $\mathbb{E}_{x_0, \bar{\boldsymbol{\epsilon}}_t}\left[\left\|\bar{\boldsymbol{\epsilon}}_t - \boldsymbol{\epsilon}_\theta\left(\sqrt{\bar{\alpha}_t}x_0 + \sqrt{1-\bar{\alpha}_t}\bar{\boldsymbol{\epsilon}}_t, t\right)\right\|^2\right]$. Score-based models [44] transforms the discrete-time diffusion process into a continuous-time process and employs Stochastic Differential Equations (SDEs) to express the diffusion process. Moreover, the forward and backward processes are no longer restricted to the diffusion process. They employ the forward process defined as $d\boldsymbol{x} = \left(\boldsymbol{f}_t(\boldsymbol{x}) - \frac{1}{2}\left(g_t^2 - \sigma_t^2\right)\nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x})\right)dt + \sigma_t d\boldsymbol{w}$, and the corresponding backward process is $d\boldsymbol{x} = \left(\boldsymbol{f}_t(\boldsymbol{x}) - \frac{1}{2}\left(g_t^2 + \sigma_t^2\right)\nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x})\right)dt + \sigma_t d\bar{\boldsymbol{w}}$, where $\boldsymbol{w}$ is the forward time Brownian motion and $\bar{\boldsymbol{w}}$ is the forward time Brownian motion. Compared to GANs, diffusion models have longer sampling time consummations. Several methods have been proposed to accelerate the generation process, including [9, 39, 50], DDIM [42], Consistency models [45], etc.

Consistency type models A function is called a consistency function if its output is the same at every point on

a trajectory. Formally, given a trajectory, $\boldsymbol{x}_t, t \in [0,T]$, the function satisfies $f(\boldsymbol{x}_{t_1}) = \mathbb{E}[f(\boldsymbol{x}_{t_2})]$, if $t_1, t_2 \in [0,T]$. If this trajectory is not a probability trajectory, then the expected symbol $\mathbb{E}$ in the above formula can be removed. [6] proposed Consistency Diffusion Models (CDM), which proves that when the forward diffusion process satisfies $d\boldsymbol{x}_t = g(t)d\boldsymbol{w}_t$, $\boldsymbol{h}(\boldsymbol{x},t) = \nabla \log q_t(\boldsymbol{x}) g^2(t) + \boldsymbol{x}$ is a consistency function. They add consistency regularity above during training to improve the sampling effectiveness of the model. [45] proposed consistency models. Unlike consistency diffusion models, Consistency Models (CM) utilize deterministic sampling to obtain a one-step sampling model by learning the mapping from each point $\boldsymbol{x}_t$ on the trajectory to $\boldsymbol{x}_0$. When training a diffusion model to obtain the trajectory $\boldsymbol{x}_t$, it is called consistency distillation. When using conditional-trajectories to approximate non-conditional trajectories, it is called consistency training. Compared to consistency distillation, consistency training has a lower sampling effectiveness. Concurrently, [22] induces a new temporal variable, while calculating the previous step's x through multi-step iteration, and incorporates a discriminator after a period of training and achieved SOTA results in distillation. Our work concentrates on energy-efficient training from scratch also with different objective functions.

3. Method

3.1. Preliminary

3.1.1 Score-Based Generative Models

Score-Based Generative Models [44], as an extension of diffusion models, extends the diffusion to continuous time, and the forward and backward processes are no longer limited to the diffusion process. Given a distribution p_t, where $t \in [0,T]$, p_0 is the data distribution and p_T is normal distribution. From p_0 to p_T, this distribution increasingly approximates a normal distribution. We sample $\boldsymbol{x}_t$ from p_t distribution. If we can obtain $\boldsymbol{x}_{t'}$ from the formula $d\boldsymbol{x} = \left(\boldsymbol{f}_t(\boldsymbol{x}) - \frac{1}{2}\left(g_t^2 - \sigma_t^2\right)\nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x})\right) dt + \sigma_t d\boldsymbol{w}$, where $\boldsymbol{w}$ is the forward time Brownian motion and $t' > t$, then we can obtain $\boldsymbol{x}_{t'}$ from the formula $d\boldsymbol{x} = \left(\boldsymbol{f}_t(\boldsymbol{x}) - \frac{1}{2}\left(g_t^2 + \sigma_t^2\right)\nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x})\right) dt + \sigma_t d\boldsymbol{w}$, where $\boldsymbol{w}$ is the backward time Brownian motion and $t' < t$. If $\sigma_t = 0$, this formula turns into a ordinary differential equation $d\boldsymbol{x} = \left(\boldsymbol{f}_t(\boldsymbol{x}) - \frac{1}{2} g_t^2 \nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x})\right) dt$. We can generate a new sample by numerically solving this Ordinary Differential Equation (ODE). For each $\boldsymbol{x}_T \sim p_T$, this ODE describes a trajectory from $\boldsymbol{x}_T$ to $\boldsymbol{x}_0$.

3.1.2 Consistency Training

Denote $\{\boldsymbol{x}_t\}$ as a ODE trajectory, a function is called consistency function, if $\boldsymbol{g}(\boldsymbol{x}_{t_1}, t_1) = \boldsymbol{g}(\boldsymbol{x}_{t_2}, t_2)$, for any $\boldsymbol{x}_{t_1}, \boldsymbol{x}_{t_2} \in \{\boldsymbol{x}_t\}$. To reduce the time consumption for sampling from diffusion models, consistency training utilizes a model to fit the consistency function $\boldsymbol{g}(\boldsymbol{x}_{t_1}, t_1) = \boldsymbol{g}(\boldsymbol{x}_{t_2}, t_2) = \boldsymbol{x}_0$. The ODE trajectory selected by consistency training is

$$d\boldsymbol{x} = t\nabla_{\boldsymbol{x}} \log p_t(\boldsymbol{x}) dt, t \in [0,T]. \tag{1}$$

In this setting, the distribution of

$$p_t(\boldsymbol{x}) = p_0(\boldsymbol{x}) * \mathcal{N}(0, t^2 \boldsymbol{I}),$$

where $*$ is convolution operator. The consistency models are denoted as $\boldsymbol{f}(\boldsymbol{x}_t, t, \boldsymbol{\theta})$. Consistency model is defined as

$$\boldsymbol{f}(\boldsymbol{x}_t, t, \boldsymbol{\theta}) = \frac{0.5^2}{r_t^2 + 0.5^2}\boldsymbol{x}_t + \frac{0.5 r_t}{\sqrt{0.5^2 + r_t^2}} \boldsymbol{F}_{\boldsymbol{\theta}}\left(\left(\frac{1}{\sqrt{r_t^2 + 0.5^2}}\right)\boldsymbol{x}_t, t\right), \tag{2}$$

where $\boldsymbol{\theta}$ represents the parameters of the model, $\boldsymbol{F}_{\boldsymbol{\theta}}$ is the output of network, $r_t = t - \epsilon$, and ϵ is a small number for numeric stability.

To train the consistency model $\boldsymbol{f}(\boldsymbol{x}_t, t, \theta)$, we need to divide the time interval $[0,T]$ into several discrete time steps, denoted as $t_0 = \epsilon < t_1 < t_2 < \cdots < t_N = T$. N gradually increases as the training progresses, satisfying

$$N(k) = \lceil \sqrt{\frac{k}{K}((s_1+1)^2 - s_0^2) + s_0^2} - 1 \rceil + 1,$$

where K denotes the total number of training steps, s_1 is the end of time steps, s_0 is the beginning of time steps and k refers to the current training step. Denote

$$\mathcal{L}_{CD}^n = \sum_{k=1}^{n} \mathbb{E}[d(\boldsymbol{f}(\boldsymbol{x}_{t_k}, t_k, \boldsymbol{\theta}), \boldsymbol{f}(\boldsymbol{x}_{t_{k-1}}^{\Phi}, t_{k-1}, \boldsymbol{\theta}^-))],$$

where $d(\cdot)$ is a distance function, $\boldsymbol{\theta}^-$ is the exponentially moving average of each batch of $\boldsymbol{\theta}$, and $\boldsymbol{x}_{t_{n+1}} \sim p_{t_{n+1}}$. $\boldsymbol{x}_{t_n}^{\Phi}$ is obtained from $\boldsymbol{x}_{t_{n+1}}$ through the ODE solver Φ using Eq. (1). About $\boldsymbol{\theta}$ and $\boldsymbol{\theta}^-$, the equation is given as $\boldsymbol{\theta}_{k+1}^- = \mu(k)\boldsymbol{\theta}_k^- + (1-\mu(k))\boldsymbol{\theta}_k$, where $\mu(k) = \exp(\frac{s_0 \log \mu_0}{N(k)})$ and μ_0 is the coefficient at the beginning.

However, calculating $\mathcal{L}_{CD}^{\Phi}$ requires training another score-based generative model. They also propose using conditional trajectories to approximate $x_{t_n}^{\Phi}$. This loss is denoted as

$$\mathcal{L}_{CT}^n = \sum_{k=1}^{n} \mathbb{E}[d(f(\boldsymbol{x}_0 + t_k \boldsymbol{z}, t_k, \boldsymbol{\theta}), f(\boldsymbol{x}_0 + t_{k-1}\boldsymbol{z}, t_{k-1}, \boldsymbol{\theta}^-))],$$

where $\boldsymbol{x}_0 \sim p_0$ and $\boldsymbol{z} \sim \mathcal{N}(0, I)$. $\mathcal{L}_{CT} = \mathcal{L}_{CT}^N$ is called consistency training loss. Using this loss to train the consistency model is called consistency training. This loss is proven [45] to satisfy

$$\mathcal{L}_{CT}^n = \mathcal{L}_{CD}^n + o(\Delta t), \tag{3}$$

when the ODE solver Φ is Euler solver.

3.1.3 Generative Adversarial Networks

Generative Adversarial Networks (GANs), as generative models, are divided into two parts during training. One part is the generator, denoted as $G(\cdot)$, which is used to generate samples from the approximated target distribution. The other part is the discriminator, denoted as $D(\cdot)$. The training of GANs is alternatively optimizing $G(\cdot)$ and $D(\cdot)$: 1) train to distinguish whether the sample is a generated sample; 2) train $G(\cdot)$ to deceive the discriminator. These two steps are alternated in training. One type of GANs can be described as the following minimax problem: $\min_G \max_D V(G,D) = \mathbb{E}_{\boldsymbol{x}\sim p_{\text{data}}(\boldsymbol{x})}[\log D(\boldsymbol{x})] + \mathbb{E}_{\boldsymbol{z}\sim p_{\boldsymbol{z}}(\boldsymbol{z})}[\log(1-D(G(\boldsymbol{z})))]$. It can be proven that this minimax problem is equivalent to minimizing the JS-divergence between p_{data} and $G(\boldsymbol{z})$, where $\boldsymbol{z}\sim p_{\boldsymbol{z}}$.

To improve the training stability of GANs, many methods have been proposed. A practical approach is the zero-centered gradient penalty. This is achieved by using the following regularization:

$$\mathcal{L}_{gp} = \|\nabla_{\boldsymbol{x}} D(\boldsymbol{x})\|^2, \boldsymbol{x}\sim p_{\text{data}}. \tag{4}$$

To reduce computational overhead, this regularization can be applied intermittently every few training steps, rather than at every step.

3.2. Analysis the Loss Function

Theorem 3.1. *If the consistency model satisfies the Lipschitz condition: there exists $L>0$ such that for all $\boldsymbol{x}$, $\boldsymbol{y}$ and t, we have $\|\boldsymbol{f}(\boldsymbol{x},t,\boldsymbol{\theta}) - \boldsymbol{f}(\boldsymbol{y},t,\boldsymbol{\theta})\|_2 \le L\|\boldsymbol{x}-\boldsymbol{y}\|_2$, then minimizing the consistency loss will reduce the upper boundary of the W-distance between the two distributions. This can be formally articulated as the following theorem:*

$$\begin{aligned}\mathcal{W}[f_{t_k}, g_{t_k}] &= \mathcal{W}[f_{t_k}, p_0] \\ &\le L\mathcal{W}[q_{t_k}, p_{t_k}] + \mathcal{L}_{CT}^{t_k} + t_k O(\Delta t) + o(\Delta t),\end{aligned} \tag{5}$$

where the definition of $p_t, \boldsymbol{f}$, $\mathcal{L}_{CT}^{t_k}$ and $\boldsymbol{g}$ is consistent with that in Sec. 3.1.2. $\Delta t = \max(t_k - t_{k-1})$. The distribution f_t is defined as $\boldsymbol{f}(\boldsymbol{x}_t, t, \boldsymbol{\theta})$, where $\boldsymbol{x}_t \sim q_t$, and the distribution g_t is defined as $\boldsymbol{g}(\boldsymbol{y}_t, t)$, where $\boldsymbol{y}_t \sim p_t$. The distribution q_t represents the noise distribution when generating samples.

Proof. The W-distance (Wasserstein-distance) is defined as follows:

$$\mathcal{W}_\rho[p,q] = \inf_{\gamma\in\prod[p,q]} \iint \gamma(\boldsymbol{x},\boldsymbol{y})\|\boldsymbol{x}-\boldsymbol{y}\|_\rho d\boldsymbol{x} d\boldsymbol{y},$$

where γ is any joint distribution of p and q. For convenience, we take the case of $\rho=2$ and simply denote $\|\cdot\|$ as $\|\cdot\|_2$, and denote $\mathcal{W}[p,q]$ as $\mathcal{W}_2[p,q]$. Let $\{\boldsymbol{x}_{t_k}\}$ or $\{\boldsymbol{y}_{t_k}\}$ be the points on the same trajectory defined by the ODE in Eq. (1) on the ODE trajectory. For $\mathcal{W}[f_{t_k}, g_{t_k}]$, we have the following inequality:

$$\begin{aligned}&\mathcal{W}[f_{t_k}, g_{t_k}] \\ =&\inf_{\gamma^*\in\prod[f_{t_k},g_{t_k}]} \iint \gamma^*(\hat{\boldsymbol{x}}_{t_k},\hat{\boldsymbol{y}}_{t_k})\|\hat{\boldsymbol{x}}_{t_k}-\hat{\boldsymbol{y}}_{t_k}\|_\rho d\hat{\boldsymbol{x}}_{t_k} d\hat{\boldsymbol{y}}_{t_k} \\ \overset{(i)}{\le}&\iint \gamma(\hat{\boldsymbol{x}}_{t_k},\hat{\boldsymbol{y}}_{t_k})\|\hat{\boldsymbol{x}}_{t_k}-\hat{\boldsymbol{y}}_{t_k}\| d\hat{\boldsymbol{x}}_{t_k} d\hat{\boldsymbol{y}}_{t_k}, \gamma\in\prod[f_{t_k},g_{t_k}] \\ =&\mathbb{E}_{\hat{\boldsymbol{x}}_{t_k},\hat{\boldsymbol{y}}_{t_k}\sim\gamma\in\prod[f_{t_k},g_{t_k}]}[\|\hat{\boldsymbol{x}}_{t_k}-\hat{\boldsymbol{y}}_{t_k}\|] \\ \overset{(ii)}{=}&\mathbb{E}_{\boldsymbol{x}_{t_k},\boldsymbol{y}_{t_k}\sim\gamma\in\prod[q_{t_k},p_{t_k}]}[\|\boldsymbol{f}(\boldsymbol{x}_{t_k},t_k,\phi)-\boldsymbol{g}(\boldsymbol{y}_{t_k},t_k)\|].\end{aligned}$$

Here, (i) holds because γ is the joint distribution of any p_t and q_t. (ii) is obtained through the law of the unconscious statistician. Since the joint distribution $\gamma\in\prod[q_{t_k},p_{t_k}]$ in the above formula is arbitrary, so we choose the distribution satisfying $\mathbb{E}_{\boldsymbol{x}_{t_k},\boldsymbol{y}_{t_k}\sim\gamma^*}[\|\boldsymbol{y}_{t_k}-\boldsymbol{x}_{t_k}\|] = \mathcal{W}[q_{t_k},p_{t_k}]$. We denote it as γ^*. The expectation $\mathbb{E}_{\boldsymbol{x}_{t_k},\boldsymbol{y}_{t_k}\sim\boldsymbol{\gamma}^*}[\|\boldsymbol{f}(\boldsymbol{x}_{t_k},t_k,\theta) - g(\boldsymbol{y}_{t_k},t_k)\|]$ satisfies the following inequality:

$$\begin{aligned}&\mathbb{E}_{\boldsymbol{x}_{t_k},\boldsymbol{y}_{t_k}\sim\gamma^*}[\|\boldsymbol{f}(\boldsymbol{x}_{t_k},t_k,\boldsymbol{\theta}) - \boldsymbol{g}(\boldsymbol{y}_{t_k},t_k)\|] \\ \le&\mathbb{E}_{\boldsymbol{y}_{t_k}\sim p_{t_k}}[\|\boldsymbol{g}(\boldsymbol{y}_{t_k},t_k) - \boldsymbol{f}(\boldsymbol{y}_{t_k},t_k,\boldsymbol{\theta})\|] + L\mathcal{W}[q_{t_k},p_{t_k}].\end{aligned} \tag{6}$$

If the ODE solver is Euler ODE solver, we have:

$$\begin{aligned}&\mathbb{E}_{\boldsymbol{y}_{t_k}\sim p_{t_k}}[\|\boldsymbol{g}(\boldsymbol{y}_{t_k},t_k) - \boldsymbol{f}(\boldsymbol{y}_{t_k},t_k,\boldsymbol{\theta})\|] \\ \le&\mathbb{E}_{\boldsymbol{y}_{t_{k-1}}\sim p_{t_{k-1}}}[\|\boldsymbol{g}(\boldsymbol{y}_{t_{k-1}},t_{k-1}) - \boldsymbol{f}(\boldsymbol{y}_{t_{k-1}},t_{k-1},\boldsymbol{\theta})\|] \\ &+ L(t_k - t_{k-1})O(t_k - t_{k-1}) \\ &+ \mathbb{E}_{\boldsymbol{y}_{t_k}\sim p_{t_k}}[\|\boldsymbol{f}(\boldsymbol{y}^{\phi}_{t_{k-1}},t_{k-1},\boldsymbol{\theta}) - \boldsymbol{f}(\boldsymbol{y}_{t_k},t_k,\boldsymbol{\theta})\|]\end{aligned} \tag{7}$$

The detailed proofs for the aforementioned inequalities can be found in Appendix B. We iterate multiple times until t_0. At this point, from Eq. (2), we have $\|g(y_{t_0},t_0) - f(y_{t_0},t_0,\theta)\| = 0$. So, we can obtain the inequality below:

$$\begin{aligned}&\mathbb{E}_{\boldsymbol{y}_{t_k}\sim p_{t_k}}[\|\boldsymbol{g}(\boldsymbol{y}_{t_k},t_k) - \boldsymbol{f}(\boldsymbol{y}_{t_k},t_k,\boldsymbol{\theta})\|] \\ \le&\mathcal{L}_{CD}^k + \sum_{i=1}^k L(t_i - t_{i-1})O((t_i - t_{i-1})) \\ \overset{(i)}{=}&\mathcal{L}_{CT}^k + \sum_{i=1}^k t_k O((\Delta t)) + o(\Delta t).\end{aligned}$$

Here, (i) holds because $\Delta t = \max(t_k - t_{k-1})$, and the relationship between $\mathcal{L}_{CD}^k$ and $\mathcal{L}_{CT}^k$ in Eq. (3). Since consistency function $\boldsymbol{g}(\boldsymbol{x}_t,t) = \boldsymbol{x}_0$, it follows that $\mathcal{W}[f_{t_k},g_{t_k}] = \mathcal{W}[f_{t_k},p_0]$. Putting these together, the proof is complete. □

Analyzing Eq. (5), $\mathcal{W}[q_{t_k},p_{t_k}]$ is the W-distance between the two sampling distributions, which is independent of the model. We set $q_t = p_t$ to eliminate $\mathcal{W}[q_{t_k},p_{t_k}]$. The term $o(\Delta t)$ and $t_k O(\Delta t)$ originate from approximation errors, where $t_k O(\Delta t)$ increases with the increase of t_k. The remaining term is $\mathcal{L}_{CT}^k = \sum_{i=1}^k \mathbb{E}[d(f(\boldsymbol{x}_0 +$

$t_i\boldsymbol{z}, t_i, \boldsymbol{\theta}), f(\boldsymbol{x}_0+t_{i-1}\boldsymbol{z}, t_{i-1}, \boldsymbol{\theta}^-))]$. It can be seen that this term also accumulates errors. The quality of the model's generation depends not only on the current loss at t_k, $\mathbb{E}[d(f(\boldsymbol{x}_0+t_k\boldsymbol{z}, t_k, \boldsymbol{\theta}), f(\boldsymbol{x}_0+t_{k-1}\boldsymbol{z}, t_{k-1}, \boldsymbol{\theta}^-))]$, but also on the sum of all losses for values less than k. These two accumulated errors may be one of the reasons why consistency training requires as large a batch size and large model size as possible. During training, it is not only necessary to ensure a smaller loss at the current t_k, but also to use a larger batch size and larger model size to ensure a smaller loss at previous t values. Besides, reducing Δt can help to lower this upper bound. However, as described in the original text [45], reducing Δt in practical applications does not always lead to performance improvements.

3.3. Enhancing Consistency Training with Discriminator

Following the analysis in Sec. 3.2, it can be observed that the W-distance at time t_k depends not only on the loss at t_k, but also on the loss at previous times. This could be one of the reasons why consistency training requires as large a batch size and model size as possible. However, it can be noted that at each moment t_k, the ultimate goal is to reduce the distance between the generated distribution and the target distribution. In order to reduce the gap between two distributions, we propose not only using the W-distance, but also other distances, such as JS-divergence. Inspired by GANs, we suggest incorporating a discriminator into the training process.

It can be proven that when the generator training loss is given by

$$\mathcal{L}_G = \log(1 - D(\boldsymbol{f}(\boldsymbol{x} + t_{n+1}\boldsymbol{z}, t_{n+1}, \boldsymbol{\theta}_g), t_{n+1}, \boldsymbol{\theta}_d)), \quad (8)$$

and the discriminator training loss is given by

$$\begin{aligned}\mathcal{L}_D = &-\log(1 - D(\boldsymbol{f}(\boldsymbol{x}_g + t_{n+1}\boldsymbol{z}, t_{n+1}), \boldsymbol{\theta}_d) \\ &- \log(D(\boldsymbol{x}_r, t_{n+1}, \boldsymbol{\theta}_d)),\end{aligned} \quad (9)$$

minimizing the loss leads to $\min_{\boldsymbol{f}}(-2\log 2 + 2JSD\left(f_{t_k} \| p_0\right))$, which is equivalent to minimizing the JS-divergence. D is the discriminator. It can be observed that this loss does not depend on the previous t_k loss, and can directly optimize the distance between the current t_k distributions. Therefore, the required batch size and model size can be smaller compared to consistency training.

However, although the ultimate goals of the two distances are the same, e.g., when the JS-divergence is 0, the W-distance is also 0, at which point the gradient of the discriminator is also 0. However, at this point, the gradient of $\mathcal{L}_{CT}$ may not be 0 due to the aforementioned error. Moreover, when $\mathcal{L}_{CT}$ is relatively large, the optimization direction of $\mathcal{L}_{CT}$ may conflict with $\mathcal{L}_G$. Consider the extreme case where the output of f_{t_n} is completely random, it is clear that $\mathcal{L}_{CT}$ and $\mathcal{L}_G$ are in conflict, when training $\boldsymbol{f}$ at time t_{n+1}. On the other hand, when $\mathcal{L}_{CT}$ is relatively small, the model f is easier to fit at t_n than at t_{n+1}, thus generating better quality. Also, since x_t and $x_{t_{n+1}}$ are close enough, their discriminators are also close enough, thus jointly improving the generation quality. Therefore, we employ the coefficient λ to balance the proportion between $\mathcal{L}_{CT}$ and $\mathcal{L}_G$. Furthermore, as $\mathcal{L}_{CT}^k$ increases with k, the W-distance also increases. In order to improve the performance of consistency training, the weight of $\mathcal{L}_G$ should also increase. We utilize the formula Eq. (10) to give $\mathcal{L}_G$ more weight, where w is the weight at $n = N-1$, and w_{mid} is the weight at $n = (N-1)/2$.

$$\lambda_N(n) = w\left(\frac{n}{N-1}\right)^{\log_{\frac{1}{2}}(\frac{w_{mid}}{w})}. \quad (10)$$

Please note, even though the fitting targets of all f_{t_k} are q_0, we choose for the form $D(\boldsymbol{x}_t, t, \boldsymbol{\theta}_d)$ rather than $D(\boldsymbol{x}_t, \boldsymbol{\theta}_d)$ when constructing the discriminator. Although theoretically, the optimal distribution of the generator trained by these two discriminators is p_0, and for two similar samples, the discriminator in the form of $D(\boldsymbol{x}_t, \boldsymbol{\theta}_d)$ will generate similar gradients at different t, we find in our experiments Sec. 4.3.3 that this form of discriminator is not as effective as $D(\boldsymbol{x}_t, t, \boldsymbol{\theta}_d)$. The training algorithm is described in Algorithm 1.

3.4. Gradient Penalty Based Adaptive Data Augmentation

For smaller datasets, in the field of GANs, there are many data augmentation works to improve generation effects. Inspired by StyleGAN2-ADA[46], we also utilize adaptive differentiable data augmentation. However, unlike StyleGAN2-ADA, which adjusts the probability of data augmentation based on the accuracy of the discriminator over time, it is difficult to adjust the augmentation probability through the accuracy of a single discriminator in our model due to the varying training difficulties at different t. As described in Sec. 4.3.2, we find that the stability of the discriminator's gradient has a significant impact on training. This may be due to the interaction between $\mathcal{L}_{CT}$ and $\mathcal{L}_G$. We propose to adjust the probability of data augmentation based on the value of the gradient penalty over time. Given a differential data augmentation function $A(\boldsymbol{x}, p_{aug})$, where p_{aug} is the probability of applying the data augmentation, the augmented discriminator is defined by:

$$D_{aug}(\boldsymbol{x}_t, t, p_{aug}, \boldsymbol{\theta}_d) = D(A(\boldsymbol{x}_t, p_{aug}), t, \boldsymbol{\theta}_d).$$

The probability p_{aug} is updated by

$$p_{aug} \leftarrow \text{Clip}_{[0,1]}(p_{aug} + 2([\mathcal{L}_{gp}^- \geq \tau] - 0.5)p_r),$$

where $[\cdot]$ denotes the indicator function, which takes a value of 1 when the condition is true and 0 otherwise. $\text{Clip}_{[0,1]}(\cdot)$

Table 1. Training steps and model parameter size are reported. BS stands for Batch Size. For ACT, Params represent parameters of the consistency model + discriminator.

Dataset	Method	BS	Steps	Params	Fid
CIFAR10	CT	512	800K	73.9M	8.7
	CT	256	800K	73.9M	10.4
	CT	128	800K	73.9M	14.4
	ACT-Aug	**80**	**300K**	**27.5M+14.1M**	**6.0**
ImageNet	CT	2048	800K	282M	13.0
	ACT	**320**	**400K**	**107M+54M**	**10.6**
LSUN Cat	CT	2048	1000K	458M	20.7
	ACT	**320**	**165K**	**113M+57M**	**13.0**

Table 2. Sample quality of ACT on the ImageNet dataset with the resolution of 64×64. Our ACT significantly outperforms CT.

Method	NFE (↓)	FID (↓)	Prec. (↑)	Rec. (↑)
BigGAN-deep [3]	1	4.06	**0.79**	0.48
ADM [8]	250	**2.07**	0.74	0.63
EDM [21]	79	2.44	0.71	**0.67**
DDPM [19]	250	11.0	0.67	0.58
DDIM [42]	50	13.7	0.65	0.56
DDIM [42]	10	18.3	0.60	0.49
CT	1	13.0	**0.71**	0.47
ACT	1	**10.6**	0.67	**0.56**

represents the operation of clipping the value to the interval $[0, 1]$. p_r denotes the update rate at each iteration, and $\mathcal{L}_{gp}^{-}$ is the exponential moving average of $\mathcal{L}_{gp}$, defined as $\mathcal{L}_{gp}^{-} = \mu_p \mathcal{L}_{gp}^{-} + (1-\mu_p)\mathcal{L}_{gp}$. p_r and μ_p are constants within the range $[0, 1]$. This algorithm is described in Algorithm 2 shown in Appendix D. Our motivation for proposing the use of data augmentation is to mitigate the overfitting phenomenon in the discriminator. We conduct experiments on CIFAR10 to verify the method. However, the performance of data augmentation on large datasets, such as ImageNet 64×64, remains to be explored.

Algorithm 1 Adversarial Consistency Training

Input: dataset $\mathcal{D}$, initial consistency model parameter θ_g, discriminator θ_d, step schedule $N(\cdot)$, EMA decay rate schedule $\mu(\cdot)$, optimizer $\text{opt}(\cdot,\cdot)$, discriminator $D(\cdot,\cdot,\theta_d)$, adversarial rate schedule $\lambda(\cdot)$, gradient penalty weight w_{gp}, gradient penalty interval I_{gp}.
$\boldsymbol{\theta}_g^{-} \leftarrow \boldsymbol{\theta}$ and $k \leftarrow 0$
repeat
  Sample $\boldsymbol{x} \sim \mathcal{D}$, and $n \sim \mathcal{U}[\![1, N(k)]\!]$
  Sample $\boldsymbol{z} \sim \mathcal{N}(0, \boldsymbol{I})$ ▷ Train Consistency Model
  $\mathcal{L}_{CT} \leftarrow d(\boldsymbol{f}(\boldsymbol{x} + t_{n+1}\boldsymbol{z}, t_{n+1}, \boldsymbol{\theta}_g), \boldsymbol{f}(\boldsymbol{x} + t_n \boldsymbol{z}, t_n, \boldsymbol{\theta}_g^{-}))$
  $\mathcal{L}_G \leftarrow \log(1 - D(\boldsymbol{f}(\boldsymbol{x} + t_{n+1}\boldsymbol{z}, t_{n+1}, \boldsymbol{\theta}_g), t_{n+1}, \boldsymbol{\theta}_d))$
  $\mathcal{L}_f \leftarrow (1 - \lambda_{N(k)}(n+1))\mathcal{L}_{CT} + \lambda_{N(k)}(n+1)\mathcal{L}_G$
  $\boldsymbol{\theta}_g \leftarrow \text{opt}(\boldsymbol{\theta}_g, \nabla_{\boldsymbol{\theta}_g}(\mathcal{L}_f))$
  $\boldsymbol{\theta}_g^{-} \leftarrow \text{stopgrad}(\mu(k)\boldsymbol{\theta}_g^{-} + (1 - \mu(k))\boldsymbol{\theta}_g)$
  Sample $\boldsymbol{x}_g \sim \mathcal{D}$, $\boldsymbol{x}_r \sim \mathcal{D}$, and $n \sim \mathcal{U}[\![1, N(k)]\!]$
  Sample $\boldsymbol{z} \sim \mathcal{N}(0, \boldsymbol{I})$ ▷ Train Discriminator
  $\mathcal{L}_D \leftarrow -\log(D(\boldsymbol{x}_r, t_{n+1}, \boldsymbol{\theta}_d)) - \log(1 - D(\boldsymbol{f}(\boldsymbol{x}_g + t_{n+1}\boldsymbol{z}, t_{n+1}, \boldsymbol{\theta}_d))$
  $\mathcal{L}_{gp} \leftarrow w_{gp}\|\nabla_{\boldsymbol{x}_r} D(\boldsymbol{x}_r, t_{n+1}, \boldsymbol{\theta}_d)\|^2 [k \mod I_{gp} = 0]$
  $\mathcal{L}_d \leftarrow \lambda_{N(k)}(n+1)\mathcal{L}_D + \lambda_{N(k)}(n+1)\mathcal{L}_{gp}$
  $\boldsymbol{\theta}_d \leftarrow \text{opt}(\boldsymbol{\theta}_d, \nabla_{\boldsymbol{\theta}_d}(\mathcal{L}_d))$
  $k \leftarrow k + 1$
until convergence

4. Experiments

In this section, we report experimental settings and results on CIFAR-10, ImageNet64 and LSUN Cat 256 datasets.

4.1. Generation Performance

In this section, we report the performance of our model on the CIFAR10, ImageNet 64×64 datasets and LSUN Cat 256×256 datasets. The results demonstrate a significant improvement of our method over the original approach. We exhibit the results on CIFAR10 in Tab. 3, on ImageNet 64×64 in Tab. 2 and on LSUN Cat 256×256 in Tab. 4, respectively. The FID on CIFAR10 improves from 8.7 to 6.0. It improves from 13 to 10.6 on ImageNet 64×64, and it improves from 20.7 to 13.0 on LSUN Cat 256×256.

Furthermore, we demonstrate the performance of the consistency training on different batch sizes, and the sizes of the models used by the proposed method and consistency training, in Tab. 1. As can be discerned from the data in the table, the batch size has a significant impact on consistency training. When the batch size is set to 256, the FID score escalates to 10.4 from 8.7. Besides, with a batch size of 128, the FID rises to 14.4. On the CIFAR10 dataset, the proposed method outperforms consistency training, achieving an FID of 6.0 with a batch size of 80, versus 8.7 with a batch size of 512. On ImageNet 64x64, it achieves an FID of 10.6 with a batch size of 320, compared to consistency training's 13.0 with a batch size of 2048. Besides, on LSUN Cat 256 × 256, the proposed method attains an FID of 13.0 with a batch size of 320, better than consistency training's 20.7 with a batch size of 2048. Fig. 1 shows the generated samples from model training on ImageNet 64×64 and LSUN Cat 256×256. Figs. E7 and E8 shows more generated samples from model training on LSUN Cat 256×256. Appendix A provides explanations for all metrics. Appendix E shows zero-shot image inpainting.

4.2. Resource Consumption

We utilize the DDPM model architecture as our backbone. While DDPM's performance isn't as high as [8] and [44], it has fewer parameters and attention layers, enabling faster execution. Our model is significantly smaller than the 63.8M model used by consistency training on CIFAR10, with only 27.5M (41.6M with discriminator during training) parameters. On the ImageNet 64×64 dataset, our model,

Table 3. Sample quality of ACT on the CIFAR10 dataset. We compare ACT with state-of-the-art GANs and (efficient) diffusion models. We show that ACT achieves the best FID and IS among all the one-step diffusion models.

Method	NFE (↓)	FID (↓)	IS (↑)
BigGAN [3]	1	14.7	9.22
AutoGAN [14]	1	12.4	8.40
ViTGAN [28]	1	6.66	9.30
TransGAN [20]	1	9.26	9.05
StyleGAN2-ADA [46]	1	2.92	**9.83**
StyleGAN2-XL [41]	1	**1.85**	-
Score SDE [44]	2000	2.20	**9.89**
DDPM [19]	1000	3.17	9.46
EDM [21]	36	**2.04**	9.84
DDIM [42]	50	4.67	-
DDIM [42]	20	6.84	-
DDIM [42]	10	8.23	-
1-Rectified Flow [30]	1	378	1.13
Glow [23]	1	48.9	3.92
Residual FLow [4]	1	46.4	-
DenseFlow [16]	1	34.9	-
DC-VAE [35]	1	17.9	8.20
CT [45]	1	8.70	8.49
ACT	1	6.4	8.93
ACT-Aug	1	**6.0**	**9.15**

with only 107M parameters (161M with discriminator during training), is smaller than the 282M model used by consistency training. The smaller model and batch size reduce resource consumption. In our experiments on CIFAR10, we utilize 1 NVIDIA GeForce RTX 3090, as opposed to the 8 NVIDIA A100 GPUs used for consistency training. For the ImageNet 64×64 experiments, we employ 4 NVIDIA A100 GPUs, in contrast to the 64 A100 GPUs used for training in the consistency training setup. For the LSUN Cat 256×256 experiments, we employ 8 NVIDIA A100 GPUs, in contrast to the 64 A100 GPUs used for training in the consistency training setup [45].

4.3. Ablation Study

4.3.1 Impacts of λ_N

When $\lambda_N \equiv 0$, this reduces to consistency training. Conversely, when $\lambda_N \equiv 1$, it becomes Generative Adversarial Networks (GANs). According to the analysis in Sec. 3.2, as λ_N increases, adversarial consistency training gains the capacity to enhance model performance with smaller batch sizes, leveraging the discriminator. However, as discussed in Sec. 3.3, an overly large λ_N can lead to an excessive consistency training loss, thereby causing a conflict between $\mathcal{L}_{CT}$ and $\mathcal{L}_G$. Furthermore, it has been noted in the literature that for GANs, high-dimensional inputs may detrimentally affect model performance [34]. Therefore, as λ_N increases, the model performance exhibits a pattern of initial improvement followed by a decline. Firstly, we demonstrate the phenomenon of mode collapse when $\lambda_N \approx 1$ on CIFAR10. As illustrated in Fig. E6, the phenomenon of mode collapse is observed. It can be noted that, apart from the initial t_k where the residual structure from Eq. (2) results in outputs with substantial input components, preventing mode collapse, the other t_k values all exhibit mode collapse.

Table 4. Sample quality of ACT on the LSUN Cat dataset with the resolution of 256×256. Our ACT significantly outperforms CT. †Distillation techniques.

Method	NFE (↓)	FID (↓)	Prec. (↑)	Rec. (↑)
DDPM [19]	1000	17.1	0.53	0.48
ADM [8]	1000	**5.57**	0.63	**0.52**
EDM [21]	79	6.69	**0.70**	0.43
PD† [39]	1	18.3	0.60	0.49
CD† [45]	1	11.0	0.65	0.36
CT [45]	1	20.7	0.56	0.23
ACT	1	**13.0**	**0.69**	**0.30**

For a score-based model as defined in Sec. 3.1.1, the learned sampling process is the reverse of the diffusion process $p_t(\boldsymbol{x}_0|\boldsymbol{x}_t)$. However, the distribution $q_t(\boldsymbol{x}_0|\boldsymbol{x}_t)$ learned via Eqs. (8) and (9) does not consider the forward process of the diffusion. We conduct further experiments where the form of the discriminator is changed to $D(\boldsymbol{x}_0, \boldsymbol{x}_t, t, \boldsymbol{\theta}_d)$, and it can be proven Appendix C that the distribution learned by the generator is $p_t(\boldsymbol{x}_0|\boldsymbol{x}_t)$. However, we also observe the phenomenon of mode collapse in our experiments. Fig. 2 illustrates the training collapse on ImageNet 64×64 when $\lambda_N \equiv 0.3$. It can be observed that at around 150k training steps, the $\mathcal{L}_{CT}$ becomes unstable and completely collapses around 170k. We have included the training curves for the proper λ_N in the Appendix E. It can be observed that at this point, $\mathcal{L}_{CT}$ and several other training losses remain stable. Essentially, a smaller w_{mid} and a larger w are preferable choices.

4.3.2 Connection between gradient penalty and training stability

In Sec. 3.3, we analyze the relationship between $\mathcal{L}_{CT}$ and $\mathcal{L}_G$, highlighting the importance of gradient stability. In this section, we conduct experiments to validate our previous analysis and demonstrate the rationality of the ACT-Aug method proposed in Sec. 3.4.

Fig. 2 illustrates the relationship among the values of the gradient penalty ($\mathcal{L}_{gp}$), consistency training loss ($\mathcal{L}_{CT}$), and FID. It can be observed that almost every instance of instability in $\mathcal{L}_{CT}$ is accompanied by a relatively large $\mathcal{L}_{gp}$. Fig. 3 illustrates the relationship among these three on the CIFAR10 dataset. It can be seen that in the mid-stage of training, $\mathcal{L}_{gp}$ begins to slowly increase, a process that is accompanied by a gradual increase in $\mathcal{L}_{CT}$ and FID. Therefore, we believe that gradient stability is crucial for adversarial consistency training. Based on this, we propose ACT-Aug (Sec. 3.4) on small datasets, using $\mathcal{L}_{gp}$ as an indicator to adjust the probability of data augmentation, thereby stabilizing $\mathcal{L}_{gp}$ around a certain value.

Figure 1. Generated samples on ImageNet 64×64 (top two rows) and LSUN Cat 256×256 (the third row).

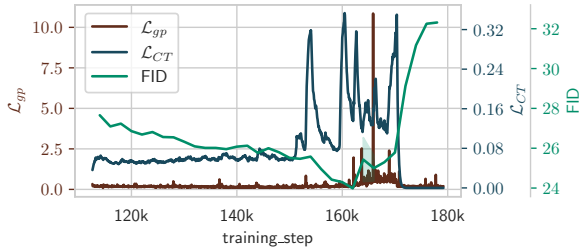

Figure 2. $\mathcal{L}_{gp}$, $\mathcal{L}_{CT}$, and FID of ACT on ImageNet 64x64 ($\lambda_N \equiv 0.3$, an overly large λ_N leads to training collapse. Additionally, drastic changes in $\mathcal{L}_{gp}$ closely follow changes in $\mathcal{L}_{CT}$).

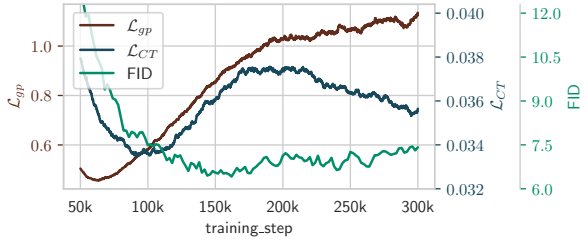

Figure 3. $\mathcal{L}_{gp}$, $\mathcal{L}_{CT}$, and FID of ACT on CIFAR10 ($\lambda_N \equiv 0.3$, an appropriate λ_N. In the later stages of training, without data augmentation, $\mathcal{L}_{CT}$, $\mathcal{L}_{gp}$, and FID all show relatively large increases).

4.3.3 Discriminator

Activation Function Generally, GANs employ LeakyReLU as the activation function for the discriminator. This function is typically considered to provide better gradients for the generator. On the other hand, SiLU is the activation function chosen for DDPM, and it is generally regarded as a stronger activation function compared to LeakyReLU. Tab. 5 displays the FID scores of different activation functions on CIFAR10 at 50k and 150k training steps. Contrary to previous findings, we discovery that utilizing the SiLU function for the discriminator leads to faster convergence rates and improved final performance. A possible reason is that $\mathcal{L}_{CT}$ provides an additional gradient direction, which mitigates the overfitting of the discriminator.

Different Backbone Tab. 5 also displays the FID scores of different architecture on CIFAR10 at 50k and 150k training steps. In our investigation, we have evaluated the discriminators of StyleGAN2, ProjectedGAN and the down-

Table 5. Ablation study of the discriminator.

Discriminator	Activation	t-emb	Fid (50k)	Fid (150k)
DDPM-res	LeakyReLU	False	18.7	10.6
DDPM-res	LeakyReLU	True	11.5	7.4
DDPM-res	SiLU	True	**9.9**	7.0
DDPM	SiLU	True	12.5	**6.5**
StyleGAN2	LeakyReLU	True	16.7	9.5
ProjectedGAN	LeakyReLU	True	19.4	16.6

sampling part of DDPM (simply denoted as DDPM) as described in Appendix A. Due to the significant role of residual structures in designing GANs' discriminators, we incorporate residual connections between different downsampling blocks in DDPM, denoted as DDPM-res. It can be observed that DDPM performs the best. Although DDPM-res exhibits a faster convergence rate during the early stages of training, its performance in the later stages is not as satisfactory as that of DDPM. Furthermore, we find that DDPM demonstrates superior training stability compared to DDPM-res. We also experiment with whether or not to feed t into the discriminator, denoted as t-emb. We find that feeding t yields better results. This might be due to the fact that the optimal value of the discriminator varies with different t_k, hence the necessity of t-emb for better fitting.

5. Conclusion

We proposed Adversarial Consistency Training (ACT), an improvement over consistency training. Through analyzing the consistency training loss, which is proven to be the upper bound of the W-distance between the sampling and target distributions, we introduced a method that directly employs Jensen-Shannon Divergence to minimize the distance between the generated and target distributions. This approach enables superior generation quality with less than $1/6$ of the original batch size and approximately $1/2$ of the original model parameters and training steps, thereby having smaller resource consumption. Our method retains the beneficial capabilities of consistency models, such as inpainting. Additionally, we proposed to use gradient penalty-based adaptive data augmentation to improve the performance on small datasets. The effectiveness has been validated on CIFAR10, ImageNet 64×64 and LSUN Cat 256×256 datasets, highlighting its potential for broader application in the field of image generation.

However, the interaction between $\mathcal{L}_{CT}$ and $\mathcal{L}_G$ can be further explored to improve our method. In addition to using JS-Divergence, other distances can also be used to reduce the distance between the generated and target distributions. In the future, we will focus on these two aspects to further boost the performance.

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