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Learning Transferable Negative Prompts for Out-of-Distribution Detection

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Abstract

Existing prompt learning methods have shown certain capabilities in Out-of-Distribution (OOD) detection, but the lack of OOD images in the target dataset in their training can lead to mismatches between OOD images and In-Distribution (ID) categories, resulting in a high false positive rate. To address this issue, we introduce a novel OOD detection method, named 'NegPrompt', to learn a set of negative prompts, each representing a negative connotation of a given class label, for delineating the boundaries between ID and OOD images. It learns such negative prompts with ID data only, without any reliance on external outlier data. Further, current methods assume the availability of samples of all ID classes, rendering them ineffective in open-vocabulary learning scenarios where the inference stage can contain novel ID classes not present during training. In contrast, our learned negative prompts are transferable to novel class labels. Experiments on various ImageNet benchmarks show that NegPrompt surpasses stateof-the-art prompt-learning-based OOD detection methods and maintains a consistent lead in hard OOD detection in closed- and open-vocabulary classification scenarios. Code is available at https://github.com/mala-lab/negprompt.

1. Introduction

Since the advent of deep learning, numerous image recognition models [5, 9, 29] have relied solely on image features for classification. However, in recent years large pre-trained vision-language models (VLMs), such as CLIP [37], integrated natural language processing into computer vision, enhancing the semantic understanding capabilities of computer vision models. It has been observed that these VLMs excel in image classification, particularly in zero-shot scenarios. This is attributed to their extensive self-supervised pre-training on web-scale image-text data, which has endowed them with robust semantic transfer abilities.



Figure 1. Illustration of the key intuition of NegPrompt. For each ID class, NegPrompt trains a small set of learnable prompts that have negative semantics to the learned positive prompt of the given class. As a result, OOD samples exhibit higher similarity to the negative prompts than the positive prompts.

Despite the strong zero-shot classification capabilities of VLMs, numerous research efforts are put to unleash their potential, e.g., by investigating whether models like CLIP can achieve enhanced performance with training on downstream target datasets. This has led to the development of various techniques to fine-tune CLIP [8, 18], among which prompt learning has sparked widespread interest. Prompt learning (or prompt tuning) [19, 39, 50], a methodology originating from natural language processing, focuses on learning the prompt inputs into a large-scale pre-trained network, rather than learning or fine-tuning the parameters of the network. In CLIP, a common prompt is 'a photo of a [class name]'. The aim of prompt learning, e.g., in approaches like CoOp [54], is to learn a soft/differentiable context vector to replace the fixed text prompt like 'a photo of a', thereby leveraging CLIP's powerful generalization in semantic understanding while also fine-tuning for specific target datasets [53, 54].

However, even though prompt learning enhances the target dataset perception capabilities of VLMs, it struggles with Out-Of-Distribution (OOD) detection [10, 26]. Under the OOD detection task, the test set comprises images from both the training classes – in-distribution (ID) data –

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and images from other unknown categories (OOD images). VLM-based classification is typically performed by first replacing the '[class name]' with the class label of each category in a prompt, which is then processed by the text encoder of CLIP to obtain the class embedding and assign the class label that has the highest cosine similarity with the embedding of a test image from the image encoder of CLIP. However in OOD detection tasks, the models do not have access to the class names of OOD images, thereby lacking the knowledge about OOD data.

This issue, exacerbated by the models' tendency towards overconfidence that often predicts OOD data as ID images with high confidence [34], undermines their ability to effectively detect OOD images.

There have been a number of CLIP-based methods designed specifically for VLM-driven OOD detection methods, but most of them [6, 32, 46] focused on a zero-shot setting where no training data of the target dataset is available. Due to the lack of adaptation to the target dataset, they tend to detect unusual ID images as OOD data. Among them, CLIPN [46], which trains an additional 'no' text encoder to provide prompt embeddings of not having specific classes, is the best detector, but it relies on a large-scale auxiliary dataset to train such a text encoder and it is computationally expensive.

The most related work is a very recent approach Lo-CoOp [33] that utilizes the training ID data to tune CLIP to capture local features of the ID classes in the prompt. It shows substantially improved performance compared to zero-shot methods [32], but it may compromise the ID classification accuracy due to an overemphasis on modeling local features. LoCoOp also lacks knowledge about OOD samples, making it difficult to differentiate boundary ID/OOD images.

In this work, we propose a novel CLIP-based OOD detection method, named **NegPrompt**. Inspired by [25], Negprompt is designed to learn a set of *negative prompts*, each representing a negative connotation of a given ID class label, to delineate the boundaries between ID and OOD images, as shown in Fig. 1. The negative prompts represent specialized ID-class-dependent concepts, guiding the models to pay attention to the characteristics that are contrary to or disjoint from the ID classes. NegPrompt aims to utilize ID training data and *positive prompts* (*i.e.*, the text prompt embeddings of ID classes) to learn such negative prompts in a way to which OOD images exhibits higher similarity than ID images.

Essentially, the learned negative prompts have similar semantics to the text prompts generated from the 'no' text encoder in CLIPN, but NegPrompt presents a fundamentally different approach: it capitalizes on the generalization ability of the CLIP model and learns the negative prompts with training ID data only, eliminating the reliance on external data and the extensive computation overhead as in CLIPN.

Furthermore, benefiting from the superior generalization ability of CLIP, our method does not require the exposure to all ID classes during training. In other words, the model learns *transferable negative prompts* by using only a small subset of the ID classes, after which we can obtain the negative prompts for the other ID classes by simply replacing the '[class name]' in the prompts with the name of those unexposed classes. This allows our model to work in openvocabulary [7, 31] learning settings, where the models are required to classify images of novel classes that are not seen during training, in addition to a set of training base classes.

Our main contributions can be summarized as follows:

- We propose a prompt learning-based OOD detection approach NegPrompt, which is able to learn negative semantics relative to specific ID classes, thereby enhancing the VLMs' sensitivity to unknown samples. It is a lightweight method that does not require training extra encoders on external data as in related methods [46].
- NegPrompt possesses an open-vocabulary capability due to the transferability of its negative prompts. This means that with training images from just a small subset of ID classes and the class names of all IDs, we can achieve OOD detection on test data with all these ID classes. To the best of our knowledge, there have been no previous fine-tuning methods exploring such a capability.
- Extensive experiments on multiple ImageNet-based benchmarks show that NegPrompt consistently outperforms current state-of-the-art methods in both conventional and hard OOD Detection settings.

2. Related Work

2.1. Pre-trained Vision-Language Models

Understanding the semantic information of images remains a significant challenge in the field of computer vision. With the advent of Transformer [44] in computer vision tasks [5], CLIP [37] has been introduced as one of the most advanced pre-trained VLMs. Utilizing contrastive learning [21], large-scale models and datasets [38], CLIP employs imagetext pairs as the training data for self-supervised learning. This approach has successfully trained the model to align visual and text signals in a latent space. Concurrently, other researchers [1, 24, 49] have also shown the remarkable generalization capabilities of CLIP and similar vision-language models [17] in various downstream tasks [7, 20, 56].

2.2. Prompt Learning

The concept of prompt learning was initially focused on automating the creation of templates/prompts for extracting knowledge from Bert [4] or GPT [36]. To bypass manual creation, prompt learning advocates the use of supervised learning to automate the prompt development. [39] proposed a gradient-based approach for identifying the

best prompt, establishing the foundation of prompt learning. Later, CoOp [54] integrated prompt learning into computer vision. CoOp learns a segment of the context before it is fed into the text encoder of CLIP, thus tailoring the learned prompt to the specific target dataset. Many other prompt learning methods for different vision tasks [13, 18, 20, 40, 47, 53, 55] are subsequently introduced. However, they are not designed for OOD detection, so they struggle with dealing with the unknown OOD samples during inference.

2.3. Out-of-Distribution Detection

OOD detection is committed to identifying images in image classification tasks that belong to categories not present in the training dataset, typically originating from a different distribution. While traditional OOD detection methods often tackle the problem by either exploiting the prediction logits to define OOD scores [10, 12, 15, 26, 27] or focusing on the class-agnostic information in feature space that is not recoverable from logits [41, 45], recent methods [11, 14, 22, 28, 30, 42, 52] introduce extra or synthetic OOD data, employing fine-tuning to elevate their model's sensitivity towards unknown classes.

With the introduction of large pre-trained VLMs, OOD detection has embarked on a new trajectory driven by VLMs. MCM [32] aims to integrate the idea of maximum softmax probability [10] into the inference process of CLIP, while ZOC [6] enhances OOD detection in a zero-shot setting by learning an additional image interpreter and guessing the category of images. CLIPN [46] and LoCoOp [33], the most related methods to ours, are based on text prompts. However, CLIPN, during its pretraining phase, trains an additional negative text encoder using a large external dataset to improve its negative semantic prompt, which increases network parameters and deviates from prompt learning that is focused on tuning the target data. LoCoOp, on the other hand, uses prompt learning for matching text and image local features, which can compromise the global perception capability of CLIP and reduce classification accuracy for in-distribution (ID) samples. Also, its model lacks knowledge about OOD samples, which can often lead to high detection errors.

3. Method

In this paper, we propose an approach named NegPropmt that leverages pre-trained VLMs, specifically CLIP, to learn negative prompts relative to ID classes for the purpose of OOD detection. The negative prompts are learned in the CLIP's text-image-aligned embedding space with the support of training ID data and their positive prompts (*i.e.*, prompt embeddings of ID classes); no external outlier data is required. Due to its general effectiveness, the popular prompt learning method CoOp [54] is used by default to provide the positive prompts for training NegPrompt.

3.1. Preliminaries

Problem Statement. Formally, we assume that we have two datasets, namely ID dataset denoted as D^{in} and OOD dataset denoted as D^{out}. The ID dataset consists of imagelabel pairs (x^{in}, y^{in}) , where $y^{in} \in Y^{in} = \{0, 1, 2, 3...k\}$ belong to the ID class set. Similarly, the OOD dataset contains image-label pairs (x^{out}, y^{out}) , but all $y^{out} \in Y^{out} =$ $\{k+1, k+2, ...\}$ belong to the OOD class set. It is important to note that these two sets do not intersect, meaning that $Y^{in} \cap Y^{out} = \emptyset$. As we have a test set X^{test} consists of images from ID and OOD, the goal of OOD detection is to train a classifier $\phi(x)$ that takes an image x as input and returns whether the image belongs to OOD. Unlike existing studies using full-/zero-shot ID training samples, we only use a few samples (16 samples per class) for D_{train}^{in} like [33] does. In the open-vocabulary detection setting, we only use a small part (10%) but not all the classes of D_{train}^{in} . CLIP and CoOp. CLIP [37] is currently one of the most popular image-text models. During the pre-training phase, it uses large-scale image-text pairs for self-supervised contrastive learning, aligning images and texts into the same latent space. The main components of CLIP are an image encoder $Encoder^{image}(I)$ and a text encoder $Encoder^{text}(T)$, which respectively accept image and text inputs. In zero-shot image classification tasks, assume we have k class labels for classification, such as "cat", "dog", etc., CLIP first incorporates the class labels into pre-designed hard/unlearnable text prompts, such as "a photo of a [class name]", forming a prompt input set of "a photo of a cat", "a photo of a dog" and so on. These prompts are then individually fed into the text encoder $Encoder^{text}(T)$ to obtain k text features T^{f} . The testing image is then input into the image encoder to obtain an image feature I^{f} . The cosine similarity is calculated between the normalized image feature and all text features, formally, $Sim(T^f, I^f) = T^{\tilde{f}} \cdot I^f$, and the text feature T^{f} with the highest similarity to I^{f} is considered to be the category to which the image belongs.

Besides zero-shot classification, many have explored ways to improve CLIP's performance when the target data is accessible. CoOp [54] introduces prompt learning with CLIP by freezing its encoders and using backpropagation to learn dataset-specific soft/learnable prompts. The text prompts are represented as $t_i = \{\omega_1^{pos}, \omega_2^{pos}, ..., \omega_n^{pos}, c_i\}$, where c_i is the word embedding of the class name and ω^{pos} s are learnable vectors that have positive semantics w.r.t. the class *i*. The goal is to optimize these $\omega^{positive}$ s. Specifically, t_i is processed by $Encoder^{text}$ to yield $T_i^{f,pos}$ as a positive prompt embedding of the class *i*, and then the prediction probability is computed as:

$$p(y=i|x) = \frac{\exp(sim(T_i^{f,pos}, I^f)/\tau)}{\sum_{j=1}^k \exp(sim(T_j^{f,pos}, I^f)/\tau)},$$
 (1)



Figure 2. Overview of NegPropmt. Given the CLIP model and positive prompts learned by existing prompt learning methods such as CoOp [54], NegPrompt learns a set of negative prompts relative to different ID class labels via three loss functions that enforce the separation between negative prompts and ID images, and between negative and positive prompts, as well as the diversity of the negative prompts.

where $I^f = Encoder^{image}(x)$ and τ is a temperature parameter. Next, cross-entropy loss is used to maximize similarity between ID class text embeddings and images.

$$\mathcal{L}_{positive} = \mathbb{E}_{\mathbf{x}_{in} \sim D_{\text{train}}^{\text{in}}} \left[-\log(p(y=i|x)) \right].$$
(2)

This method largely improves CLIP's classification performance by adapting the learnable prompts to the target data. The resulting prompt embeddings of ID classes are used as positive prompts to support the accurate learning of negative prompts in our method below.

3.2. Proposed Approach

NegPrompt aims to learn a set of negative prompts, each representing a negative connotation of an ID class. As shown in Fig. 2, it involves generating a series of prompts that resemble the positive prompts obtained through CoOp, but with a negative class semantic, such as "A photo of not a [class label]". These negative prompts, combined with class labels, can generate a range of negative text features around the positive prompts, so that OOD images exhibit higher similarity to the negative prompts than ID images.

3.2.1 Learning Negative Prompts

To acquire accurate negative prompts representing negative class semantics, we first utilize CoOp to learn positive prompts ω^{pos} s, after which we consider positive prompts to accurately capture the class semantics of samples in the ID dataset. Thereafter, we freeze the positive prompts and focus solely on learning the negative prompts. A negative prompt is denoted as $\{\omega_1^{neg}, \omega_2^{neg}, ..., \omega_n^{neg}\}$, where *n* represents the number of context vectors we aim to learn. By utilizing the frozen CLIP text encoder, we can obtain negative prompt embeddings $T_{l,i}^{f,neg} = Encoder^{text}(t_{l,i}^{neg})$, where $t_{l,i}^{neg} = \{\omega_{l,1}^{neg}, \omega_{l,2}^{neg}, ..., \omega_{l,n}^{neg}, c_i\}$ is the *l*-th negative prompt relative the ID class *i*. Thus, due to the presence of the negative prompts, we turn the prediction probability into the following form:

$$p(y=i|x) = \frac{\exp(S_i^{f,pos})}{\sum_{j=1}^k \exp(S_j^{f,pos}) + \sum_{l=1}^p \sum_{j=1}^k \exp(S_{l,j}^{f,neg})}$$
(3)

where $S_j^{f,pos} = sim(T_j^{f,pos}, I^f)/\tau$, $S_{l,j}^{f,neg} = sim(T_{l,j}^{f,neg}, I^f)/\tau$ and p is the number of negative prompts we aim to learn for each ID class. The objective is to learn negative text prompt embeddings that can effectively separate ID and OOD samples around the positive text features. To achieve this, we introduce the following three loss functions:

Negative-Image Separation Loss. One of our objectives is to have the negative text prompt embeddings serve as the closest text features to OOD images. However, we only have images from the ID dataset; no OOD images are available. To remedy this problem, we take an alternative approach that aims to push the negative text features away from the ID images. In this regard, we draw inspiration from OE [11]. Contrary to the approach in OE, where the probability distribution of outlier images is evenly distributed among all ID labels, we distribute the probability distribution obtained from ID images evenly among all negative prompts. Since the network parameters are frozen, this drives the negative text features to move away from the ID

images, resulting in the learning of prompts with a negative connotation. The formulation is as follows:

$$\mathcal{L}_{NIS} = \mathbb{E}_{x_{\text{in}} \sim D_{\text{train}}^{\text{in}}} [H(\mathbf{u}; F(x))], \qquad (4)$$

where F(x) is the probability vector computed as $Softmax(S^{f,neg})$, and **u** is a uniform distribution and H is the cross entropy loss.

Negative-Positive Distance Loss. To avoid learning trivial negative prompts that are distant from both ID and OOD images, we need to control the negative text feature within a certain range between the ID and OOD images. To this end, we devise a constraint, enforcing that the negative text feature does not deviate too far from the positive text feature. Therefore, we introduce the following loss function to guarantee a certain level of similarity between the negative and positive text feature in the latent space:

$$\mathcal{L}_{NPD} = -\frac{1}{k*p} \sum_{j=1}^{k} \sum_{i=1}^{p} sim(T_{i,j}^{f,neg}, T_j^{f,pos}).$$
 (5)

Negative-Negative Distance Loss. Furthermore, to ensure that we are effectively learning diverse, non-overlapping negative prompts, we extend the distances between different negative text features within the same label via the following loss function:

$$\mathcal{L}_{NND} = \frac{1}{k * p * (p-1)} \sum_{j=1}^{k} \sum_{i=1}^{p} \sum_{l \neq i} sim(T_{i,j}^{f,neg}, T_{l,j}^{f,neg}).$$
(6)

Overall, our NegPrompt objective consists of the above three losses. During training, we are able to obtain a diverse set of non-trivial prompts that effectively convey negative meanings relative to the ID class labels by minimizing the following overall loss:

$$\mathcal{L}_{NegativePrompts} = \mathcal{L}_{NIS} + \beta * \mathcal{L}_{NPD} + \gamma * \mathcal{L}_{NND},$$
(7)

where β and γ are hyper-parameters to balance the losses.

3.2.2 Open-Vocabulary Capability

Since the negative prompts we learn do not depend on specific class labels but are instead generic templates representing negative semantics of any given class labels, it is possible to utilize the generalization ability of CLIP to learn a set of transferable negative prompts. Specifically, instead of utilizing all of the ID classes D_{train}^{in} , NegPrompt may only employ its small subset $D_{train}^{in,sub}$ for training the negative prompts ω^{neg} , where $D_{train}^{in,sub} = \{(x, y_{sub}^{in}) \mid y_{sub}^{in} \subset y^{in}\}$. After obtaining the trained negative prompts, we combine them with the remaining ID class names, *i.e.*, replace c_i in $t_{l,i}^{neg}$ with the unseen ID class names, to obtain the corresponding negative prompts for the novel ID classes that are

	ID	OOD
Split-1	All dog classes	Non-animal classes
Split-2	Half of hunting dog classes	Other 4-legged animal classes
Split-3	Mix of common classes	Mix of common classes

Table 1. Three ImageNet-1K splits for hard OOD detection.

unseen during training. This approach, which achieves outof-distribution detection by only exposing with a small portion of ID images, is unprecedented in prior research. We refer this as to be open-vocabulary OOD detection.

3.2.3 Inference

During inference, we employ the MCM [32] scoring approach for OOD detection, but with the addition of our negative prompts into the softmax function. Particularly, MCM uses the inverse of the maximum softmax score in Eq. 1 as the OOD score. Our OOD scoring extends MCM and defines it as: $s(x) = \max(p(y = i|x))$, where p(y = i|x) is defined in Eq. 3 that also includes the similarities of the test image to the negative prompts, in addition to the similarities to the positive prompts. The rationale behind this is that for ID images, they will be matched to one of the positive text features, leading to a higher $S^{f,pos}$ but lower $S^{f,neg}$, and thereby a higher maximum softmax score (*i.e.*, a lower OOD score). Conversely, for OOD data, it will be matched to one of the negative text features, resulting in a lower maximum softmax score (*i.e.*, a higher OOD score).

4. Experiment

4.1. Experimental Details

Datasets. For conventional OOD detection, we use a popular benchmark in which ImageNet-1K [3] with 1,000 classes is used as the ID dataset, and the same OOD datasets as in [32] are used, including subsets of Texture [2], iNaturalist [43], Places [51] and SUN [48]. In addressing the more challenging OOD scenarios, we partitioned the ImageNet1k dataset into two segments: one segment of the data serves as the ID, while the other serves as OOD. As shown in Table 1, three different splits are derived, following from [35]. We further create another ImageNet split, Split-4, in which the first 100 classes are used as ID data and the subsequent 900 classes are used as OOD samples. Following CoOp and LoCoOp [33, 54], during our training process, we utilized only few-shot training data for each category. Particularly, we only train the model with 16 images per ID class and without any exposure to OOD images. During testing, we employ the entire ID and OOD test set for evaluation.

Implementation Details. Following existing studies [46], we use CLIP based on CLIP-B/16 which is pre-trained from OpenCLIP [16]. NegPrompt is trained using 16-shot images of all ID classes under the normal OOD detection setting. For open-vocabulary OOD detection, we train our model using only the images of the first 10% classes from the ID dataset, withholding 90% ID classes that only appear

Mathad	Texture		iNaturalist		Places		SUN		Avg	
Wiethou	AUC \uparrow	FPR95 \downarrow								
Zero-shot methods										
MCM [32] [†]	86.11	57.77	94.61	30.91	89.77	44.69	92.57	34.59	90.76	42.74
CLIPN [46] [†]	90.93	40.83	95.27	23.94	92.28	33.45	93.92	26.17	93.10	31.10
CLIP-based posthoc methods										
MSP [10] [†]	74.84	73.66	77.74	74.57	72.18	79.12	73.97	76.95	74.98	76.22
MaxLogit [12] [†]	88.63	48.72	88.03	60.88	87.45	55.54	91.16	44.83	88.82	52.49
Energy [27] [†]	88.22	50.39	87.18	64.98	87.33	57.40	91.17	46.42	88.48	54.80
ReAct [41] [†]	88.13	49.88	86.87	65.57	87.42	56.85	91.04	46.17	88.37	54.62
ODIN [26] [†]	87.85	51.67	94.65	30.22	85.54	55.06	87.17	54.04	88.80	47.75
Prompt learning methods										
CoOp [54]	89.47	45.00	93.77	29.81	90.58	40.11	93.29	40.83	91.78	51.68
LoCoOp [33] [†]	90.19	42.28	96.86	16.05	91.98	32.87	95.07	23.44	93.52	28.66
NegPrompt (Ours)	91.60	35.21	98.73	6.32	93.34	27.60	95.55	22.89	94.81	23.01
Open-vocabulary OOD detection										
CoOp (10%)	87.58	50.55	91.08	42.53	89.56	46.12	91.52	41.92	89.94	45.28
LoCoOp (10%)	88.21	47.32	94.47	34.90	91.64	39.85	92.54	26.30	90.15	37.09
NegPrompt (Ours) (10%)	90.30	39.31	98.39	7.48	92.68	29.75	93.70	26.92	93.76	25.86

Table 2. Conventional OOD detection results. We trained using ImageNet1k as the ID and CLIP-B/16 as the CLIP backbone. The boldfaced results indicate the best performance. Results marked with † are taken from [46] and [33]. 'METHOD' (10%) in open-vocabulary OOD detection is to evaluate the performance of the 'METHOD' when only images from 10% ID classes are accessible during training.

together with OOD data during inference. We train a shared positive prompt and two shared negative prompts w.r.t. each training ID class. The hyperparameters β and γ are set to 0.1 and 0.05, respectively (see Appendix A for detail). In the first stage, CoOp is trained for 100 epochs to obtain the positive prompts. In the second stage, the positive prompts are frozen, and our model is trained for 10 epochs to learn the negative prompts. For all experiments, we report the averaged results over three runs with different random seeds.

Comparison Methods. To substantiate the effectiveness of NegPrompts, we conduct an empirical analysis of three distinct categories of methodologies employed for OOD detection utilizing Vision-language models. These categories encompass zero-shot pretraining approaches, the methods that combine the CLIP image encoder with classical approaches, and the methods grounded in prompt learning. In the context of zero-shot methods, we opted for the two recent methods, MCM [32] and CLIPN [46]. MCM employs the original CLIP, utilizing the maximum softmax probability operation on the similarities for detection, and CLIPN involves an additional training phase during pretraining, specifically training a negative text encoder using large external data. For the second group of methods, we adapt previous logits-based methodologies to the use of the CLIP image encoder, including MSP [10], Energy [27], MaxLogit [12], ReAct [41] and ODIN [26], to serve as the CLIP-adapted methods. For the prompt learning methods, NegPrompt is compared with CoOp [54] and LoCoOp [33].

Evaluation Metrics. Two OOD detection metrics are used. The first metric is the False Positive Rate at a 95% True Negative Rate (FPR95), which denotes the rate of falsely identified OOD instances when the true negative rate is maintained at 95%. The second metric is the Area Under the Receiver Operating Characteristic curve (AUROC), representing the measure of OOD ranking across various classification thresholds. We also check the classification accuracy of the ID data to evaluate how the OOD detectors affect the ID classification.

4.2. Comparison to State-of-the-art Models

Conventional OOD Detection. The results of conventional OOD detection are reported in Table 2. It is clear that our proposed NegPrompt achieves consistently superior performance in both individual OOD datasets and the averaged results. When compared with the zero-shot methods, on average, our approach surpasses the best competing method CLIPN by more than 1.5% in AUC and around 8% in FPR95, despite the fact that CLIPN requires the use of an additional large external dataset to train an additional negative text encoder. In other words, although NegPrompt is significantly more lightweight than CLIPN in model size, it can substantially and consistently outperform CLIPN in both metrics across all OOD datasets. The adapted post-hoc methods generally do not leverage the CLIP's capabilities well and thus perform less effectively.

NegPrompt also substantially surpasses both prompt learning-based methods, reducing the FPR95 by about 28% (CoOp) and 5% (LoCoOp). This indicates that the learned negative prompts provide informed knowledge about OOD data, which is lacking in the competing methods, helping largely reduce detection errors.

Hard OOD Detection. Hard OOD detection presents unique challenges as the OOD samples often exhibit some similar features as the ID samples. The results on the four hard OOD datasets derived from ImageNet-1K are shown in Table 3. Similar empirical observations can be derived. Our method NegPropmt is consistently the best performer in the average performance, showcasing its general effec-

Mathad	Split-1		Split-2		Split-3		Split-4		Avg	
Method	AUC ↑	FPR95 \downarrow	AUC ↑	FPR95 \downarrow	AUC ↑	$FPR95\downarrow$	AUC ↑	FPR95 \downarrow	AUC \uparrow	$\overline{FPR95}\downarrow$
Zero-shot methods										
MCM	97.93	9.17	88.10	56.40	90.34	33.05	98.72	4.73	93.77	25.83
CLIPN	99.38	2.07	97.77	10.55	90.03	36.85	98.83	4.68	96.50	13.53
CLIP-based posthoc methods										
MSP	77.85	63.60	68.73	83.63	79.10	70.55	82.40	65.52	77.02	70.83
MaxLogit	99.87	0.49	98.06	8.69	90.96	34.34	99.35	2.66	97.06	11.55
Energy	99.88	0.46	98.18	8.40	90.65	35.02	99.36	2.83	97.02	11.68
ReAct	99.34	0.72	97.91	9.33	90.72	35.65	99.12	2.94	96.77	12.16
ODIN	98.78	1.12	98.23	8.18	89.92	37.20	98.76	13.20	96.42	14.92
Prompt learning methods										
СоОр	98.53	6.78	88.25	50.76	90.64	33.89	98.54	5.11	93.99	24.14
LoCoOp	98.64	6.29	84.63	61.09	91.30	27.79	98.83	41.44	93.35	34.15
NegPrompt (Ours)	99.85	0.62	98.54	7.60	93.89	22.89	99.57	1.60	97.96	8.18
Open-vocabulary OOD detection										
CoOp (10%)	97.97	12.217	80.11	74.62	87.92	46.00	96.59	16.60	90.65	37.36
LoCoOp (10%)	98.00	9.23	87.02	52.18	80.51	59.93	82.41	48.72	86.99	42.52
NegPrompt (Ours) (10%)	99.66	1.36	96.30	19.89	91.75	26.92	98.14	5.24	96.46	13.36

Table 3. Hard OOD detection results. We use the same notations here as those used in Table 2.

tiveness across different dataset splits. The superiority of NegPrompt over the zero-shot and prompt learning-based methods is similar to that in Table 2. Although it is slightly less effective than Energy under the Split-1 setting, it outperforms Energy in all other metrics, achieving maximally over 3% AUC and 12% FPR95 improvement among the performance on the other OOD datasets.

Note that the results in Table 3 are generally more promising than that in Table 2. This is mainly because the OOD detection difficulty in all four ImageNet-1K splits is largely reduced since the number of their ID classes is significantly less than that in the full ImageNet-1K data.

Open-Vocabulary OOD Detection. The open-vocabulary OOD detection results are reported in both Tables 2 and 3. Impressively, even when training on only 10% ID classes, our approach can still perform better than the competing methods using the full ID classes, *e.g.*, the average AUC and FPR95 in Table 2. In this open-vocabulary setting, in general, both LoCoOp and CoOp exhibit a much larger performance decline than NegPrompt, especially on the results in Table 3, in which CoOp has over 3% AUC drop and LoCoOp has over 6% AUC drop while our method has only about 1.5% AUC drop. These results demonstrate that the negative prompts in NegPrompt have much better transferability than those in the two competing methods.

4.2.1 Classification Accuracy on ID Data

We also evaluate the classification accuracy on the ID data when using NegPrompt for OOD detection, with CoOp, Lo-CoOp, MCM and CLIPN as the baselines. The classification accuracy results on the full ImageNet-1K test data are shown in Table 4. When using the full ImageNet-1K training ID class data, our method NegPrompt can maintain the same classification accuracy as CoOp.

Our accuracy is slightly compromised when using only 10% ID classes in our training. On the other hand, the OOD

72.1
71.7
67.0
71.9
72.1

Table 4. Top-1 Accuracy. Results with † are taken from [33].



Figure 3. Similarity of ID/OOD and Positive/Negative Prompts.

detection in LoCoOp compromises the ID classification accuracy, dropped from 72.1% in CoOp to 71.7%. This may be attributed to its focus on the localized regions within the background rather than the primary object of interest, resulting in the missing of some discriminative features for ID data classification. CLIPN and MCM, being zero-shot methods, have not been exposed to the target ID data, leading to a much lower accuracy than the other methods.

Ablation Study	Texture		iNaturalist		Places		SUN		Avg		
Ablation Study	AUC \uparrow	FPR95 \downarrow	AUC ↑	$\text{FPR95} \downarrow$	ACC \uparrow						
Backbones											
ResNet-50	79.44	72.73	90.97	44.10	84.35	61.37	88.04	50.55	85.70	57.19	68.2
ResNet-101	82.97	70.83	93.96	31.3	86.41	51.66	88.81	47.61	88.04	50.35	70.3
ViT-B-32	90.43	38.79	97.40	12.64	92.83	32.79	92.82	26.03	93.37	27.56	72.6
# Negative Prompts											
1	90.04	40.67	98.24	9.23	90.37	32.62	92.26	27.33	92.73	27.46	72.1
Training Process											
One-stage	80.25	72.87	77.02	95.74	82.53	95.94	81.13	95.72	80.23	90.07	62.8
ViT-B-16 & 2 & Two-stage	90.30	39.31	98.39	7.48	92.68	29.75	93.70	26.92	93.76	25.86	72.1

Table 5. Results of our ablation experiments.



Figure 4. T-SNE visualization of NegPrompt, utilizing a subset of ImageNet - TinyImageNet as the dataset.

4.3. Analysis of NegPrompt

4.3.1 Why Does NegPrompt Work?

To better understand the effectiveness of NegPrompt, we summarize the average maximum similarity between ID/OOD images and positive/negative prompts, as shown in Fig. 3. Across all four OOD datasets, ID images have the highest similarity with positive prompts, and OOD images with negative prompts. This suggests positive prompts are closer to ID images and negative prompts to OOD images in latent space, ensuring OOD images receive lower softmax scores (*i.e.*, higher OOD scores) than ID images in Eq. 3.

Using TinyImageNet [23], a subset of ImageNet, we further visualized the learned negative text features with its test data [6]. Learning three negative prompts per ID class, the results in Fig. 4 demonstrate that positive text features from positive prompts align closely with ID images in latent space. Conversely, the negative text features encoded from negative prompts lie outside of the ID data, with OOD images interspersed among them. This suggests negative text features effectively act as a fence aligning much better to the OOD images than the ID images, well supporting the OOD detection while preserving the ID classification accuracy.

4.3.2 Ablation Study

Table 5 shows our ablation study results on the backbone, the number of negative prompts, and the training process. **Backbones.** We experiment with diverse CLIP backbones. The results reveal that for CNN-based backbones

like ResNet50 and ResNet101, the OOF detection performance is not as proficient as the ViT-based backbones. Regarding ViT-B-32 and ViT-B-16, their performance is found to be uneven. Overall, the performance of OOD detection tends to increase with more advanced backbones.

The Number of Negative Prompts. The number of negative prompts also influences the results. It is observed that the OOD detection performance improves when increasing the number of negative prompts from one to two. Therefore, it is suggested to further increase the number of negative prompts for better detection accuracy. However, note that with an increase in the number of negative prompts, the computational cost also rises rapidly. A good balance between computational cost and detection accuracy is needed when determining the number of negative prompts.

Training Process. The training process is also important. As discussed before, due to the necessity of anchoring the positive prompts, a two-stage training process is used in our model. This process involves training the positive prompts in the first stage and freezing them before proceeding to train the negative prompts in the second stage. When simultaneously training both positive and negative prompts in a unified step, the model's ability to effectively learn positive prompts is significantly undermined, and consequently we obtain unstable negative prompts, leading to the largely decreased OOD detection performance.

5. Conclusion

We present NegPrompt, a novel approach for prompt learning-based OOD detection. It utilizes VLMs to learn a small set of negative prompts for conveying negative semantics relative to ID classes. Our empirical results reveal that NegPrompt 1) achieves superior OOD detection performance compared to the SOTA models across various OOD datasets in both conventional and hard OOD detection scenarios, and 2) learns transfer negative prompts that enable excellent open-vocabulary OOD detection performance.

6. Acknowledgement

This work was supported by the National Natural Science Foundation of China 62276016, 62372029.

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