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SfmCAD: Unsupervised CAD Reconstruction by Learning Sketch-based Feature Modeling Operations

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Figure 1. *SfmCAD* parses voxel shapes and reconstructs them into a parameterized set of sketch-based feature modeling operations: the input voxels, neural typed sketch+path representation, and the final CAD model (each part is randomly colored).

Abstract

This paper introduces SfmCAD, a novel unsupervised network that reconstructs 3D shapes by learning the Sketchbased Feature Modeling operations commonly used in modern CAD workflows. Given a 3D shape represented as voxels, SfmCAD learns a neural-typed sketch+path parameterized representation, including 2D sketches of feature primitives and their 3D sweeping paths without supervision, for inferring feature-based CAD programs. SfmCAD employs 2D sketches for local detail representation and 3D paths to capture the overall structure, achieving a clear separation between shape details and structure. This conversion into parametric forms enables users to seamlessly adjust the shape's geometric and structural features, thus enhancing interpretability and user control. We demonstrate the effectiveness of our method by applying Sfm-CAD to many different types of objects, such as CAD parts, ShapeNet objects, and tree shapes. Extensive comparisons show that SfmCAD produces compact and faithful 3D reconstructions with superior quality compared to alternatives. The code is released at https://github.com/ BunnySoCrazy/SfmCAD.

1. Introduction

Reconstructing shapes into CAD representations is a fundamental problem in computer vision and graphics with numerous commercial applications in industrial design and manufacturing [39]. Recent years have seen an increased interest in leveraging deep learning techniques to learn geometric representations of 3D shapes, including implicit fields [2, 25, 28], geometric primitives [19, 22, 24, 37], boundary representation (B-Rep) [9, 17], or Constructive Solid Geometry (CSG) [3, 36, 49], each with its unique characteristics and applications, contributing to the rich tapestry of research and development in this field.

However, current CAD reconstruction methods are still lacking *detail reconstruction accuracy, compactness*, and *interpretability* of the obtained models. For example, a typical line of research is dedicated to reconstruction-oriented tasks, *i.e.*, representing 3D shapes as parametric primitives, implicit fields, or B-rep. These methods deliver a high level of detail and accuracy by capturing intricate details and complex geometries with remarkable precision. However, constructing CAD models by assembling instances of primitives or by identifying faces, edges, and vertices is a tedious process [35]. Besides, the results often include complex and unintuitive operations that make the model difficult to inter-

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pret and edit. This lack of control poses significant challenges in scenarios where user interaction and shape manipulation are required.

A straightforward approach to CAD reconstruction is to learn CSG representation [14, 30, 36, 49] that implicitly recovers the CAD design history. A CSG 3D shape is expressed as a tree with leaves consisting of volumetric primitives (*e.g.*, cubes, spheres, and cylinders) that are combined using Boolean operations in the CSG inner nodes. Despite the sought-after attribute of compact shape representation, these methods often fall short regarding reconstruction accuracy by using only a set of simple typed primitives.

We introduce SfmCAD, a novel neural model for reconstructing 3D shapes into their CAD representation. Compared to related work, SfmCAD improves the reconstruction accuracy and the level of model editability by decoupling 3D structures and local geometric details of the shape. SfmCAD is inspired by feature-based modeling, a predominant method for creating 3D models in modern CAD systems, which sequentially add features (e.g., holes, slots, bosses) that represent common manufacturing operations [6, 41, 42]. Specifically, we employ unsupervised learning to retrieve a neural typed sketch+path representation of 3D shapes. Taking 3D voxel data as input, SfmCAD learns implicit fields that embody the sketch profile and generates control points for a Bézier curve, constituting the sweeping path for the component's geometry. The basic extrusion operation has been learned in a supervised [18, 38] or unsupervised [23, 31] manner. However, our sketch+path representation supports not only extrude but also sweep, *loft*, and *revolve* operations, thus enhancing the shape representation capabilities, as demonstrated in Fig. 1.

At the core of the SfmCAD is a two-stage learning strategy that operates in a coarse-to-fine manner to tackle the inherent complexity and time-intensiveness of simultaneous sketch profile and sweeping path learning. Initially, the network is trained to learn a coarse Box+Path representation of the shape, enabling a quick grasp of the shape's path and broad structure using box-like geometric proxies. Then, an implicit network delves deeper into the geometric details of the shape, enhancing the reconstruction accuracy. We demonstrate the capability and versatility of our method by applying SfmCAD to many different types of objects, including CAD parts [16], ShapeNet objects [1], tree branches [20], and by comparing to previous works. We claim the following contributions:

- We propose SfmCAD, a novel neural approach that parses 3D shapes as a set of industry-standard sketchbased CAD modeling operations. To the best of our knowledge, SfmCAD is the first unsupervised and universal neural network for learning the common CAD commands, including extrude, sweep, loft, and revolve.
- 2. We introduce novel decoupling of 3D structures and

local geometric details, which are represented by 3D Bézier curves and implicit 2D sketches. This representation ensures accurate reconstruction and ease of editing.

3. We propose a two-stage learning strategy, namely 3D Box+Path learning and 2D implicit sketch learning, which significantly accelerates the training speed in shape parser learning.

2. Related work

Geometric primitive extraction. Geometric primitive is a commonly used representation for approximating and abstracting 3D shapes [13]. Traditional methods based on RANSAC [32], Hough transform [10], or variational optimization [4, 46] have been used to detect and fit primitives on point clouds or polygonal meshes, but they often require careful parameter tuning for each shape.

To overcome the overwhelming complexity of traditional methods, deep neural networks addressed the primitive segmentation/detection from point clouds [19, 47], they fit parametric surfaces [22, 29, 37], or detect parametric curves and sharp corners [9, 24, 40] to achieve compact CAD reconstructions. Although achieving remarkable accuracy on reconstruction tasks, these methods only output individual primitives with limited types, which restricts their capability for reconstructing complex and more general 3D shapes. Learning CSG-based reconstruction. CSG reconstruction embodies a 3D shape of high complexity and nonconvexity with CSG boolean operations to represent the 3D shape construction process [5]. CSGNet [36] first develops a neural model that parses a shape into a sequence of CSG operations. More recent works follow the line of CSG parsing by advancing the inference without any supervision [14] or improving representation capability with a three-layer reformulation of the classic CSG-tree [30], or handling richer geometric and topological variations by introducing quadric surface primitives [49, 50]. However, CSG reconstruction tends to combine a large number of shape primitives that limit the user editing capabilities. Moreover, using only basic primitives (e.g., boxes, spheres) is insufficient for approximating complicated shapes, thus usually limiting the reconstruction accuracy of small details [50].

Learning feature-based reconstruction. Modern CAD workflows use feature-based modeling that decomposes a target shape into a sequence of CAD commands [34], such as drawing a sketch followed by CAD operations such as extrusion, loft, etc. This paradigm makes modeling more efficient and in tune with how designers and engineers work. Recent work has explored the potential of deep learning to generate 2D engineering sketches [7, 27, 33], or directly learn B-Rep CAD models [6, 11, 12, 17]. Several approaches propose generative models for CAD design, predicting a sequence of CAD modeling operations to produce editable CAD models, such as DeepCAD [42], Fu-



Figure 2. Sketch-based feature modeling operators supported in SfmCAD. The resulting 3D shape of each operation is called a feature primitive.

sion360 [41], Zone graph [43], and SkexGen [44]. These works focus on parametric CAD generation and do not address the reconstruction task of CAD models with suitable geometric loss functions.

Most closely related to our work are the approaches that learn sketch+extrude operation (*e.g.*, Point2Cyl [38], ExtrudeNet [31], SECAD-Net [23]), in which a collection of extrusions are predicted to build CAD models. While expressive within their scopes, these methods are limited to only one type of CAD operation (*i.e.*, extrude) to simplify the search space. SfmCAD includes loft, revolve, and sweep reconstructions, broadening the shape representation capabilities. This approach enables us to test on a broader range of shapes beyond CAD.

3. Problem Statement and Overview

Sketch-based feature modeling creates 2D engineering sketches and then lifts them to 3D along a path using CAD operations [8, 21]. Here, we first introduce this *typed sketch+path* representation for sketch-based modeling and then give an overview of its generation from a voxel model.

3.1. Typed Sketch+Path Modeling

We define a profile as a closed curve, and its enclosed region is composed of one or multiple inner/outer loops. We define a sketch as the collection of one profile and its loops in a 2D plane. Let Z denote the sketch and C be a 3D path to extend the sketches to create a 3D solid shape. We define four principal operations that are commonly used in modern CAD workflow (see Fig. 2): *Extrude* extends Z along a linear path, *Revolve* produces a model by rotating Z around an axis, *Sweep* moves Z along a specified path to generate generalized cylinder shapes, and *Loft* allows for variations in the sketch, interpolating between multiple distinct sketches $\{Z_1, Z_2, \ldots, Z_n\}$ along the shortest distances between them to create complex shapes.

Considering the similarity between the above operations, *i.e.*, lifting 2D sketches to a 3D shape along a 3D path, we use a general *typed sketch+path* to represent all of these operations, where the term 'typed' indicates the specific type of operation. Without loss of generality, we call the 3D

path a *sweeping path* and call the lofted or swept 3D shape a *feature primitive*. We further use a Bézier curve $\Upsilon(t)$ to represent the sweeping path:

$$\mathcal{C} = \Upsilon(t) = \sum_{i=0}^{n} \binom{n}{i} (1-t)^{n-i} t^{i} \mathbf{P}_{i}, \quad t \in [0,1] \quad (1)$$

where \mathbf{P}_i is a control point. The Bézier cubic is expressive enough to approximate the shapes shown in the paper, but higher-order curves can be obtained by simply changing the number of control points output by the network.

Moreover, it is noteworthy that the *Extrude* and *Revolve* operations can be regarded as general variants of the sweep operation because a Bézier curve becomes a linear path (for *Extrude*) if all the control points are collinear and an *n*-piece (usually n = 4) cubic Bézier curve can approximate a circular path (for *Revolve*) [45]. In the following, we focus on reconstructing Sweep and Loft operations, where Sweep contains Extrude and Revolve, and the Loft is restricted to contain only two sketches with a linear path between them.

3.2. Overview

Given a 3D voxel shape, we aim to reconstruct the CAD model by neurally decomposing the target shape into a sequence of typed sketch+path representation, which can be executed by the corresponding CAD commands to assemble a compact CAD model. Learning the path and sketch of a shape simultaneously is challenging and time-consuming. Thus, we propose a two-stage learning approach to improve the efficiency of network training. First, the network learns a *Box+Path* representation to enclose the input shape, capturing the sweeping path, basic geometry, and rotation angles. Then, we learn implicit sketches that refine the coarse box+path into a detailed shape representation.

Fig. 3 details the two-stage learning network. We begin with a 3D convolutional encoder that transforms the voxel input into a feature vector \mathbf{z} , which is then processed through a multilayer perceptron (MLP), yielding matrices **P** and **B**. Here, **P** are the control points of the Bézier curves representing the sweeping paths (Fig. 3 (b)), and \mathbf{B} encapsulates the box+path parameters (Fig. 3 (c)), including length, width, and sweep's twist angles. Once the sweeping paths are derived from Stage 1, we focus on learning the geometric details surrounding each path. The feature z is then mapped to N_p local features via another MLP. These vectors are subsequently concatenated with test points and fed into an implicit sketch network. The output from this network includes two occupancy values that represent the top and bottom sketches (Fig. 3 (d)), respectively. We then obtain the final CAD reconstruction by sweeping or lofting the detected sketches along the paths (Fig. 3 (e)).



Figure 3. Network architecture for SfmCAD: Stage 1 encodes the input voxels into feature z via a 3D convolutional encoder. An MLP then processes z to generate the control point coordinates P_1, \ldots, P_4 for each Bézier curve, as well as the dimensions l, w and twist angles δ^u, δ^b for each Box proxy \mathcal{B} . In Stage 2, another MLP transforms feature z into local features z', which are then concatenated with the testing point coordinate and fed into the implicit sketch network to predict the sketch SDF value. After extending the sketches along the paths, we combine all parts for the final reconstruction.



Figure 4. 2D illustration of our Box+Path representation (right) to approximate the input shape (left), which can be decomposed into a set of feature primitives (middle, the green arrows indicate the sweeping paths).

4. Methodology

Here, we first present the box+path representation, which can be efficiently learned to approximate the input shape by stacking a set of box-like proxies along the sweeping path. Then, we define the neural sketch+path to refine the coarse reconstruction. Finally, we introduce the two-stage learning network for inferring this coarse-to-fine reconstruction.

4.1. Box+Path Representation

Previous unsupervised methods [23, 30, 31] for computing the Signed Distance Function (SDF) for geometric primitives (*e.g.*, cubes, spheres, cylinders) rely on linear transformations that convert global testing point coordinates into local ones. However, the inherent non-linearity of curved paths limits the direct application of linear methods. We introduce a linear approximation method for the curved SDF computation, which we term Box+Path representation. We will first discuss the Box-Path in a 2D context to provide a more intuitive understanding before expanding it to 3D.

Box+Path in 2D. Specifically, we approximate one feature primitive \mathcal{P} using a discrete set of N_s rigid box proxies,

i.e., $\mathcal{P} = \{\mathcal{B}_i\}_{i=1}^{N_s}$. The center position \mathbf{c}_i of each box \mathcal{B}_i is obtained by uniformly sampling the Bézier curve $\Upsilon(t)$:

$$c_i = \Upsilon\left(i/N_s\right), \quad i = 1, \dots, N_s \tag{2}$$

The height h_i and the normal vector (or heading direction) \mathbf{n}_i of each box are calculated as

$$h_i = |\mathbf{c}_{i+1} - \mathbf{c}_i|, \mathbf{n}_i = \frac{\mathbf{c}_{i+1} - \mathbf{c}_i}{|\mathbf{c}_{i+1} - \mathbf{c}_i|}$$
(3)

By incorporating a learnable width parameter w, the 2D Box+Path can be fully characterized.

Box+Path in 3D. When extended to 3D space, we introduce the tangent vector \mathbf{t}_i and the binormal vector \mathbf{b}_i to parameterize the orientation of the *i*-th box proxy. To allow the sketch to rotate by a prescribed angle along the sweeping path, we should learn rotation angles δ^u and δ^b at the start and end points of the sweeping path. Then, the intermediate rotation angles δ_i are obtained by linear interpolation along the sweeping path. Next, we compute the tangent vector \mathbf{t}_i as the cross product of the normal \mathbf{n}_i and the positive z-axis unit vector \mathbf{e}_z . We then rotate \mathbf{t}_i around \mathbf{n}_i :

$$\mathbf{t}_i = R_{\mathbf{n}_i} (\mathbf{n}_i \times \mathbf{e}_z, \delta_i), \tag{4}$$

where $R_{\mathbf{n}_i}(\mathbf{v}, \delta_i)$ represents a counter-clockwise rotation of vector \mathbf{v} with angle δ_i around \mathbf{n}_i . The binormal vector \mathbf{b}_i is obtained as a cross product of $\mathbf{n}_i \times \mathbf{t}_i$. Altogether, the triplet $\{\mathbf{n}_i, \mathbf{t}_i, \mathbf{b}_i\}$ defines the orientation for each box along the curve path. The 3D Box+Path is fully characterized by incorporating learnable dimension parameters l, w.

4.2. Neural Sketch+Path

We present differentiable methods for lofting or sweeping 2D sketches into 3D solid shapes to accurately reconstruct

the feature primitives. The shape of each 2D sketch is defined by an implicit representation, where we use \hat{S}_{sk} to represent the SDF of sketches. We now describe the differentiable operators that calculate the SDF of the 3D feature primitives corresponding to the sketches.

Differentiable Sketch-Extrude. In the context of generating the geometry of feature primitives from sketch and extrude operations, $\hat{S}_{extrude}^i$ denotes the *i*-th sketch-extrude operation, \mathbf{x}_{iz} represents the *z*-component of the *i*-th position vector, and h_i is the height of the *i*-th feature primitive. We introduce a set of intermediate functions \mathcal{M}_1 , \mathcal{M}_2 , and \mathcal{M}_3 to facilitate a clearer formulation:

$$\mathcal{M}_1(\hat{\mathcal{S}}_{\mathsf{sk}}^i) = \max(\hat{\mathcal{S}}_{\mathsf{sk}}^i, |\mathbf{x}_{i_z}| - h_i),$$

$$\mathcal{M}_2(\hat{\mathcal{S}}_{\mathsf{sk}}^i) = \max(\hat{\mathcal{S}}_{\mathsf{sk}}^i, 0),$$

$$\mathcal{M}_3 = \max(|\mathbf{x}_{i_z}| - h_i, 0).$$

The SDF of the *i*-th extrusion primitive is then given by:

$$\hat{\mathcal{S}}_{\mathsf{extrude}}^{i} = \min(\mathcal{M}_{1}(\hat{\mathcal{S}}_{\mathsf{sk}}^{i}), 0) + \sqrt{\mathcal{M}_{2}(\hat{\mathcal{S}}_{\mathsf{sk}}^{i})^{2} + \mathcal{M}_{3}^{2}} \quad (5)$$

Differentiable Sketch-Loft. For the loft operation, we interpolate between two distinct sketches, $\hat{S}_{sk}^{u_i}$ and $\hat{S}_{sk}^{l_i}$, at the upper and lower faces of the *i*-th feature primitive. Given the interpolation factor α as $|\mathbf{x}_{i_z}|/h_i$, the linearly interpolated sketch, $\hat{S}_{sk}^{i_{\alpha}}$, is computed as:

$$\hat{\mathcal{S}}_{\mathsf{sk}}^{i_{\alpha}} = (1-\alpha) \cdot \hat{\mathcal{S}}_{\mathsf{sk}}^{l_{i}} + \alpha \cdot \hat{\mathcal{S}}_{\mathsf{sk}}^{u_{i}}.$$
(6)

We use the same intermediate variables as in the extrusion case, but with \hat{S}^{i}_{sk} replaced by $\hat{S}^{i_{\alpha}}_{sk}$. The SDF of the *i*-th loft primitive can be expressed similarly to Eq. 5:

$$\hat{\mathcal{S}}_{\mathsf{loft}}^{i} = \min(\mathcal{M}_{1}(\hat{\mathcal{S}}_{\mathsf{sk}}^{i_{\alpha}}), 0) + \sqrt{\mathcal{M}_{2}(\hat{\mathcal{S}}_{\mathsf{sk}}^{i_{\alpha}})^{2} + \mathcal{M}_{3}^{2}}.$$
 (7)

Differentiable Sketch-Sweep. For sweep operation, we decompose it into a series of N_s extrusions. We denote the predicted SDF for the *j*-th extrude segment as $\hat{S}_{\text{extrude}}^i$. The SDF of the *i*-th sweep primitive is then obtained by taking the minimum of the SDFs of all extrusion segments:

$$\hat{\mathcal{S}}^{i}_{\mathsf{sweep}} = \min_{j \in 1, \dots, N_s} \hat{\mathcal{S}}^{j}_{\mathsf{extrude}}.$$
(8)

Transformation to Parametric CAD. Following [23], we transform implicit sketches into parametric ones. With the control points of Bézier curves outputted by the network, we can achieve the sketch+path parametric reconstruction.

4.3. Two-stage Network Training

Stage 1: Box+Path learning. In this stage, the network predicts the control point coordinates $\{\mathbf{P}_1, ..., \mathbf{P}_4\}$ of the cubic Bézier curve and the parameters $\{l_i, w_i, \delta^u, \delta^b\}$ describing the *i*-th Box+Path \mathcal{B}_i . These parameters subsequently inform the computation of the remaining parameters $\{h_i, \mathbf{n}_i, \mathbf{t}_i, \mathbf{b}_i\}$, as detailed in Sect. 4.1. To align the

path of \mathcal{B} with the target shape path, we first compute the SDF, $\hat{\mathcal{S}}_{box}^{ij}$, for each box at the *i*-th primitive and *j*-th segment, where $i \in [1, N_p]$ and $j \in [1, N_s]$, with N_p and N_s representing the total number of primitives and segments. Taking the union over the $\hat{\mathcal{S}}_{box}^{ij}$ yields the SDF for the overall box+path $\hat{\mathcal{S}}_{\mathcal{B}}$:

$$\hat{\mathcal{S}}_{\mathcal{B}} = \bigcup_{i=1}^{N_p} \bigcup_{j=1}^{N_s} \hat{\mathcal{S}}_{\text{box}}^{ij}, \tag{9}$$

where $\bigcup(x) = \text{softmin}(\mu \cdot x) \cdot x$ and μ is a hyperparameter. We then apply a differentiable converter Ψ similar to prior works [23, 31] to transform the $\hat{S}_{\mathcal{B}}$ into occupancy, yielding $\hat{\mathcal{O}}_{\mathcal{B}} = \Psi(\hat{S}_{\mathcal{B}})$, where $\Psi(x) = (\tanh(-\beta \cdot x) + 1)/2$, and β is a hyperparameter. We then compute the Mean Squared Error (MSE) loss between $\hat{\mathcal{O}}_{\mathcal{B}}$ and the ground truth occupancy $\tilde{\mathcal{O}}$:

$$\mathcal{L}_{\mathcal{B}} = \mathbb{E}_{x \in \mathcal{X}} \left[|| \hat{\mathcal{O}}_{\mathcal{B}} - \tilde{\mathcal{O}} ||_2^2 \right], \tag{10}$$

where \mathcal{X} is the set of all testing points. The exclusive use of $\mathcal{L}_{\mathcal{B}}$ may lead to potential challenges: (1) the emergence of the curve with acute angles, and (2) the dimensions of \mathcal{B} vastly outstrip the path length. Both increase the risk of shape self-intersections, which are considered invalid in CAD. To address these issues, we introduce two additional regularization terms,

$$\mathcal{L}_{\rm sm} = \frac{1}{N_p} \sum_{i=1}^{N_p} (1 - \min_{j=1,\dots,N_s} (\mathbf{n}_{i,j} \cdot \mathbf{n}_{i,j+1}))$$
(11)

$$\mathcal{L}_{\text{lw}} = \frac{1}{2N_p} \sum_{i=1}^{N_p} \text{ReLU}(h_i + w_i - 2 \cdot \Theta), \quad (12)$$

where \mathcal{L}_{sm} penalizes the sharpest curvature in the curve by maximizing the inner product between adjacent n, and \mathcal{L}_{lw} penalizes any length or width greater than a threshold Θ . Combine with balance factors λ_1, λ_2 , the overall loss of Stage 1 is:

$$\mathcal{L}_{\text{box}} = \mathcal{L}_{\mathcal{B}} + \lambda_1 \mathcal{L}_{\text{sm}} + \lambda_2 \mathcal{L}_{\text{lw}}$$
(13)

Stage 2: Implicit sketch learning. Using the path learned in Stage 1, we progress towards fine reconstruction in Stage 2 by learning sketches. We initially utilize a Multi-Layer Perceptron (MLP) to convert the feature z into N_p local features z'. These local features are then concatenated with the local $\{x, y\}$ coordinates of each point and fed into an implicit sketch network, which is essentially an MLP predicting the SDF value \hat{S}_{sk}^i . For the sketch-loft operation, two implicit sketch networks are used to learn $\hat{S}_{sk}^{u_i}$ and $\hat{S}_{sk}^{l_i}$. Following the computation methods outlined in Sect. 4.2, we can derive the predicted overall occupancy value $\hat{\mathcal{O}}_F$ by:

$$\hat{\mathcal{O}}_{\mathrm{F}} = \begin{cases} \Psi(\bigcup_{i=1}^{N_p} \hat{\mathcal{S}}_{\mathsf{sweep}}^i), & \text{for sweep operation} \\ \Psi(\bigcup_{i=1}^{N_p} \hat{\mathcal{S}}_{\mathsf{loft}}^i), & \text{for loft operation.} \end{cases}$$

Finally, an MSE loss \mathcal{L}_{rec} is computed against the ground truth $\tilde{\mathcal{O}}$:

$$\mathcal{L}_{\text{rec}} = \mathbb{E}_{x \in \mathcal{X}} \left[|| \hat{\mathcal{O}}_{\text{F}} - \tilde{\mathcal{O}} ||_2^2 \right].$$
(14)

The direct computation of \mathcal{L}_{rec} over the entire point set \mathcal{X} requires the repetition of \mathcal{X} corresponding to $\mathcal{S}_{\mathsf{extrude}}$ for $N_p \times N_s$ times, which is time-consuming. To accelerate the training of the implicit sketch network, we propose a realtime sampling strategy, exploiting the sketch consistency trait inherent in the sweep operation. Specifically, we sample grid-like testing points y_i in the base sketch plane of the *i*-th path Υ_i obtained in the first stage. The occupancy value of y_i is determined by inputting it into the implicit sketch network and applying the converter Ψ . Subsequently, y_i is moved along the curve for $N_s - 1$ times, with its occupancy value directly replicated, yielding $\hat{\mathcal{O}}_{F_i}^*$. The ground truth occupancy value $\tilde{\mathcal{O}}_i^*$ is provided by the input voxel. After performing this procedure for all paths and conducting a union operation, the loss function corresponding to realtime sampling is given by:

$$\mathcal{L}_{\rm rec}^* = \mathbb{E}_{y \in \mathcal{Y}} \left[|| \hat{\mathcal{O}}_{\rm F}^* - \tilde{\mathcal{O}}^* ||_2^2 \right], \tag{15}$$

where \mathcal{Y} represents the set of testing points obtained through real-time sampling, and * denotes computation using real-time sampling data.

Note that the SfmCAD is designed to choose between learning either loft or sweep operations, which is determined by its hyperparameters. However, enabling the network to concurrently learn both operations is also viable, with details provided in the supplementary materials.

5. Results and Evaluation

We evaluate the performance of SfmCAD on two reconstruction tasks: (1) holistic shapes of different categories and (2) semantically segmented shapes. We show the output editability of SfmCAD in the supplemental materials.

5.1. Setup

Implementation details. We implemented SfmCAD in Py-Torch by using an NVIDIA[®] TITAN RTX GPU. The Adam optimizer [15] is utilized with a learning rate 1e-4 and beta values of (0.5, 0.99). The hyperparameters in Sect. 4.3 are set to: $\mu = 20, \beta = 50, \Theta = 0.1, \lambda_1 = 0.05, \lambda_2 = 0.05$. In our evaluations, we employ the best-performing operation (Loft/Sweep) for each category of holistic shapes and every part of segmented shapes. SfmCAD trains for 500 epochs per stage with a batch size of 24, followed by fine-tuning each test shape for 200 iterations per stage. All baseline methods are trained for 1,000 epochs and fine-tuned for 400 iterations for a fair comparison.

Evaluation metrics. We utilize three common metrics for 3D shape reconstruction: Chamfer Distance (CD), Normal



Figure 5. Visual comparison on ABC dataset.

Table 1. Quantitative comparison on ABC dataset.

Methods	CD↓	ECD↓	NC↑
UCSG-Net [14]	1.233	21.786	0.866
CSG-Stump [30]	0.671	7.751	0.892
ExtrudeNet [31]	0.519	7.111	0.885
SECAD-Net [23]	0.506	7.286	0.884
Ours	0.395	5.038	0.919

Consistency (NC), and Edge Chamfer Distance (ECD). All experiments generate the reconstructed shapes via Marching Cubes at a resolution of 256^3 . To calculate CD, we sample 8,192 points from the ground truth and predicted shape surfaces. For ECD, we employ a threshold of 0.1 for normal cross-products to identify points close to the edges on the ground truth surface and 0.5 for the predicted surface, considering the lack of sharpness in shapes generated by Marching Cubes. For better visual clarity, we magnify the CD and ECD by factors of 10^3 and 10^2 .

5.2. Reconstruction from Holistic Shape

We compare SfmCAD with UCSG-Net [14], CSG-Stump [30], ExtrudeNet [31] and SECAD-Net [23]. We test these methods on holistic shapes from different sources, including CAD parts in ABC [16], ShapeNet objects [1], and a synthetic tree dataset. The comparison against CAPRI-Net [49] is provided in the supplementary materials.

Evaluation on ABC dataset. We employ the voxel grids and sampling point data provided by [49]. The dataset included 5,000 groups of data for training and 1,000 for testing. We select 100 shape subsets from the test set for eval-



Figure 6. Visual comparison on ShapeNet dataset.

Table 2. Quantitative comparison on ShapeNet dataset.

Methods	CD↓	ECD↓	NC↑
UCSG-Net [14]	2.111	23.616	0.815
CSG-Stump [30]	2.168	17.592	0.818
ExtrudeNet [31]	0.910	14.110	0.849
SECAD-Net [23]	0.836	14.818	0.837
Ours	0.626	14.096	0.867

Table 3. Quantitative comparison on Tree dataset.

Methods	ExtrudeNet [31]	SECAD-Net [23]	Ours
CD↓	7.242	2.197	0.686
NC↑	0.608	0.622	0.722

uation. The visual results are shown in Fig. 5, while the quantitative results are presented in Tab. 1.

Evaluation on ShapeNet dataset. We utilize three categories from ShapeNet: chair, table, and display. The voxel grids and sampling points are provided by [3]. We selected 120 shapes for evaluation, with 40 from each category. Visual and quantitative results are in Fig. 6 and Tab. 2.

Evaluation on tree branches. We use a procedural modeling approach of Palubicki et al. [26] to generate tree meshes voxelized into a resolution of 64^3 . We adopt the method from [2] to obtain sampling points and occupancy values. This process results in 5,000 data groups, of which 4,500 are used for training and 500 for testing. We train all methods using increasingly denser voxel resolutions $(16^3, 32^3, 64^3)$ and select 50 trees for numerical evalua-



Figure 7. Visual comparison on Tree dataset.

tion. Note given the cylindrical nature of tree branches, we adapt our Box+Path representation by substituting boxes with cylinders for the final reconstruction (see Fig. 7 and Tab. 3 for visual and quantitative results).

Summary of comparative analysis. As demonstrated in Tables 1, 2, and 3, SfmCAD consistently outperforms other methods in terms of CD, ECD, and NC, suggesting that the sketch+path representation of SfmCAD offers more flexible shape expression capabilities than the geometric primitives used by UCSG-Net and CSG-Stump, as well as the simple sketch+extrusion operations employed by ExtrudeNet and SECAD. Figures 5, 6, and 7 further show SfmCAD's ability to generate detailed reconstructions (such as thin structures) across diverse shape categories.

5.3. Reconstruction from Segmented Shape

Semantic segmentation provides information for reconstructing complex shapes. Previous CAD reconstruction methods [23, 31] could not utilize this information because their single-type primitives lack the flexibility to represent each part independently. In contrast, SfmCAD successfully reconstructs multiple primitives with its sketch+path representation capability.

We show the task of unsupervised CAD reconstruction utilizing semantic segmentation. The evaluation is conducted on PartNet dataset [48], which provides instancelevel 3D part information. We utilize three categories: chair, table, and trashcan. We voxelize the segmented parts and sampled occupancy values at resolutions 16^3 , 32^3 , 64^3 following the scheme by [2]. This process yields a total of 12,000 chair parts (1,229 complete), 12,000 table parts (1,491 complete), and 3,000 trashcan parts (234 complete). The train-test split for all categories was set as 5:1. We selected 90 complete shapes, including 40 tables, 40 chairs, and 10 trashcans, for evaluation.

All methods were trained on part shapes using increas-



Figure 8. Visual comparison on PartNet dataset.

Table 4. Quantitative comparison on PartNet dataset.

Methods	CD↓	ECD↓	NC↑
ExtrudeNet [31]	3.251	0.549	0.783
SECAD-Net [23]	1.888	0.472	0.818
Ours	1.410	0.446	0.814

Table 5. Ablation study on sweep twist angles and loss terms.

Settings	$-(\delta^u, \delta^l)$	$-\delta^l$	$-\mathcal{L}_{lw}$	$-\mathcal{L}_{sm}$	Ours
CD↓	4.092	3.367	4.804	3.268	3.142
ECD↓	0.173	0.139	0.164	0.154	0.133
NC↑	0.655	0.714	0.685	0.732	0.776

ingly denser voxel resolutions $(16^3, 32^3, 64^3)$. For each part, we set ExtrudeNet [31] and SECAD-Net [23] to output an extruded cylinder and SfmCAD to output a sketch+path shape. After reconstructing all parts, they were reassembled to obtain the final CAD models.

The quantitative results in Tab. 4 indicate that our method outperforms others. Compared to the closest competitor, SECAD-Net, SfmCAD improves the CD by 25.3% and the ECD by 5.5%. Fig. 8 illustrates that the sketch+extrusion reconstruction of ExtrudeNet and SECAD can only characterize the nonlinear shapes through sketches. In contrast, SfmCAD can model these complex shapes using sketches and free-form paths, enabling a more refined reconstruction.

5.4. Ablation Study

We conducted an ablation study by using 40 box+path reconstructions on chair class from PartNet to evaluate the efficiency of our network design and loss terms. Initially, we disable the two sweep twist angles δ^u , δ^l or δ^l . Then we separately discarded \mathcal{L}_{sm} and \mathcal{L}_{lw} . The visual results in Fig. 9 and the quantitative results in Tab. 5 suggest that



Figure 9. Visual comparison between reconstruction results for ablation study. From top to bottom, each column shows the predicted 3D path, vector $\{n, t, b\}$, and the box+path representation.

removing any of these settings negatively affects the reconstruction performance of SfmCAD.

6. Conclusion and Future Work

We have presented an unsupervised neural network for CAD reconstruction that infers high-level CAD modeling operations. We have also introduced a unique sketch+path representation that encapsulates the local geometric details and overall structural information of the 3D shape. A novel two-stage learning strategy, operating in a coarse-to-fine manner, was proposed to address the complexity of simultaneous sketch and path learning, thus improving the efficiency of network training. We evaluated SfmCAD using several different categories of objects and demonstrated its advantages by comparing it to state-of-the-art methods.

In future work, we plan to explore using 2D sketches and 3D part templates to enhance the efficiency of unsupervised CAD reconstruction. Besides, given the manipulable property of SfmCAD's outputs, extending this work for generative CAD design or modeling would be meaningful.

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