

SeNM-VAE: Semi-Supervised Noise Modeling with Hierarchical Variational Autoencoder

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Abstract

The data bottleneck has emerged as a fundamental challenge in learning based image restoration methods. Researchers have attempted to generate synthesized training data using paired or unpaired samples to address this challenge. This study proposes SeNM-VAE, a semi-supervised noise modeling method that leverages both paired and unpaired datasets to generate realistic degraded data. Our approach is based on modeling the conditional distribution of degraded and clean images with a specially designed graphical model. Under the variational inference framework, we develop an objective function for handling both paired and unpaired data. We employ our method to generate paired training samples for real-world image denoising and super-resolution tasks. Our approach excels in the quality of synthetic degraded images compared to other unpaired and paired noise modeling methods. Furthermore, our approach demonstrates remarkable performance in downstream image restoration tasks, even with limited paired data. With more paired data, our method achieves the best performance on the SIDD dataset.

1. Introduction

Image restoration is a fundamental and essential problem in image processing and computer vision, aiming to restore the underlying signal from its corrupted observation. Traditional methods employ the Maximum a Posteriori (MAP) framework, transforming the image restoration problem into an optimization problem. In these approaches, the objective function comprises a data fidelity term and a regularization term corresponding to the degradation and prior models, respectively. Over the years, the prior model has been extensively studied. Before the advent of deep learning, researchers utilized hand-crafted priors,

such as sparsity [45, 48], non-local similarity [6, 12], and low-rankness [15, 19]. Recently, harnessing the power of deep neural networks has enabled achieving more accurate prior models through pre-trained generative models derived from a plethora of unlabeled clean signals [28, 51].

Deep learning based methods have achieved remarkable success in image restoration tasks, such as image denoising [20, 65, 66] and super-resolution (SR) [13, 14, 40, 54]. These methods aim to learn an end-to-end mapping for restoration using paired training data. Owing to the powerful representational capabilities of deep neural networks, these methods typically outperform traditional approaches. However, their effectiveness is contingent upon the availability of high-quality paired training data.

Collecting training data poses its challenges. First, real-world degradation is highly complex due to the intricate camera image signal processing (ISP) pipeline [2, 18, 21], rendering the simulation process challenging. Another approach entails manual collection, where clean and degraded pairs are obtained through long and short exposure [5] or using statistical methods [1, 46]. Nevertheless, these approaches inevitably suffer from the misalignment problem between clean and degraded images [57], making the process expensive and time-consuming.

We conclude that a key problem in real-world image restoration is obtaining an accurate degradation model. With the degradation model, one can tackle the restoration problem either via a classical optimization based method with a pre-defined prior model [9, 70] or a supervised learning based method with synthesized training data [61, 71]. Accordingly, we investigate a scenario where a limited amount of paired data and a large amount of unpaired data are available, referred to as a semi-supervised dataset. Our approach involves learning the unknown degradation model from this semi-supervised training dataset and synthesizing more paired data using this degradation model. We then use

existing image restoration networks to learn a supervised image restoration model from the synthesized data. To obtain the degradation model, we design a graphical model that characterizes the relationship between the noisy image y and the clean image x . We introduce two latent variables, z , and z_n , representing the image content and degradation information, respectively. Furthermore, we assume that x is generated by z , and y is generated by z and z_n . Using the idea from VAE [30], we approximate the conditional distribution $p(y|x)$ with encoding and decoding processes. To effectively utilize the semi-supervised dataset, we employ a mixed inference model for $q(z|x, y)$ to further decompose the objective function for paired and unpaired datasets. We apply our SeNM-VAE model to learn real-world image degradation. Experimental results demonstrate that the proposed SeNM-VAE model exhibits promising performance in noise modeling, achieving comparable results to supervised learning methods trained with fully paired data. Moreover, we achieve the best performance by finetuning an existing denoising network on the SIDD benchmark. Our main contributions are summarized as follows.

- Leveraging limited paired data and abundant unpaired data, we propose SeNM-VAE to obtain an effective model for simulating the degradation process. This is important for generating high-quality training samples for real-world image restoration tasks when obtaining training samples is difficult. Using the variational inference method, SeNM-VAE is based on a specially designed graphical model and a hierarchical structure with multi-layer latent variables.
- Experimental results on the real-world noise modeling and downstream applications, such as image denoising and SR, validate the advantages of the proposed SeNM-VAE, and we achieve the best performance on the SIDD benchmark.

2. Related work

Semi-supervised image restoration. To alleviate the challenges of acquiring paired data for image restoration tasks, researchers have been investigating semi-supervised techniques, including image dehazing [35], deraining [11, 27, 58, 60], and low-light image enhancement [41]. These approaches typically rely on image priors, such as Total Variation (TV) [48] and the dark channel prior [22], to formulate a loss function for unlabeled datasets. Some recent works, such as [60], have employed CycleGAN [72] loss for unpaired datasets. However, these methods are often designed heuristically and lack theoretical rigor. In contrast, our approach is based on a specially designed graphical model, and the loss function is derived through variational inference, enhancing our method’s interpretability.

Deep degradation modeling. Due to the limitations of

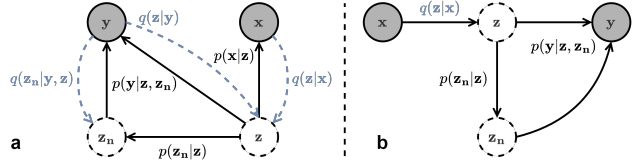


Figure 1. **a**: generation process for (x, y) and the corresponding inference model. **b**: degradation generation procedure.

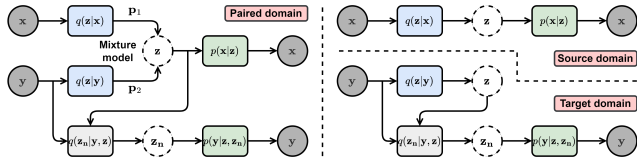


Figure 2. Data flow of the proposed semi-supervised noise modeling method that models three kinds of data: paired domain (degraded-clean image pairs), source domain (only clean images), and target domain (only degraded images).

Gaussian noise in capturing the signal-dependence of real-world noise [46, 70], researchers are exploring data-driven approaches that utilize either normalizing flow [2, 31] or GAN [63] to generate realistic noisy images with paired training data. Furthermore, some studies have employed unpaired data to learn the unknown degradation process, which mostly utilizes the GAN model and techniques such as cycle-consistency [7, 37] proposed in [72] and domain adversarial [16, 59]. Other unpaired degradation modeling methods include those based on Flow and VAE [61, 71]. In contrast, we propose a semi-supervised degradation modeling approach for real-world image restoration that leverages both paired and unpaired datasets.

3. Our methodology

In this section, we present our semi-supervised noise modeling method. Formally, our goal is to estimate the conditional distribution $p(y|x)$ with one paired dataset $\{(x_i, y_i)\}_{i=1}^{N_p}$ and two unpaired datasets $\{x_i\}_{i=1}^{N_s}$, $\{y_i\}_{i=1}^{N_t}$, where N_p , N_s , and N_t denote the number of paired, source, and target training samples, respectively. Subsequently, we can generate paired training samples using the data from the source domain. In general, we can learn a conditional generative model to sample from $p(y|x)$ with paired samples $\{(x_i, y_i)\}$, whereas those conventional generative models are incapable of utilizing unpaired samples. Furthermore, if N_p is small, achieving an accurate generative model becomes challenging. In this work, we propose a model that exploits the information of unpaired data with the assistance of the provided paired samples.

3.1. Proposed model

To estimate the conditional density function $p(y|x)$, the traditional Maximal Likelihood (ML) estimation is

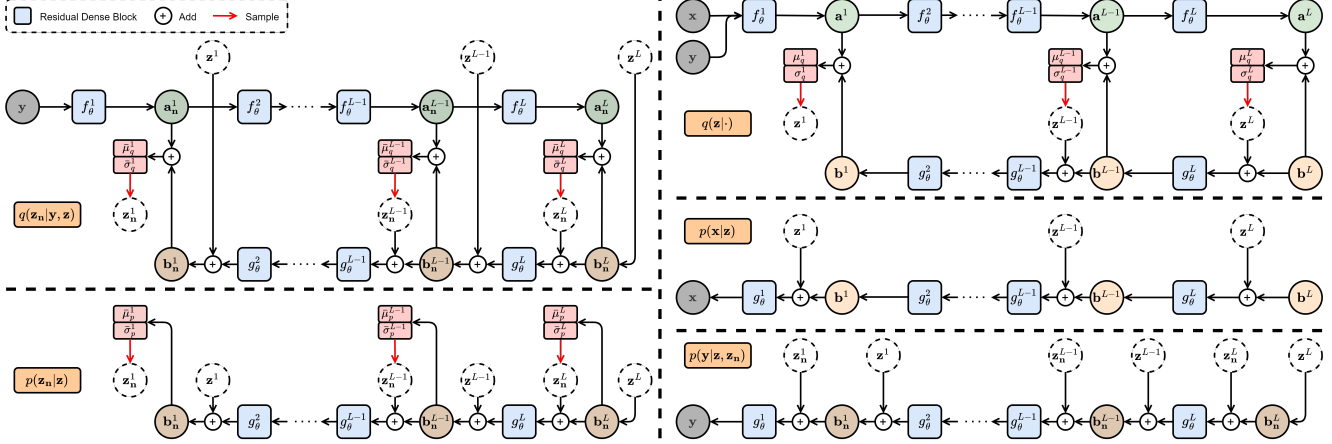


Figure 3. The hierarchical structure and network architecture.

to maximize the conditional log-likelihood function: $\max_{\theta} \mathbb{E}_{p(\mathbf{x}, \mathbf{y})} \log p_{\theta}(\mathbf{y}|\mathbf{x})$, where θ denotes the model parameter. Parameterizing $p(\mathbf{y}|\mathbf{x})$ in high-dimensional spaces directly is usually difficult. Thus, we consider the latent variable model. In particular, we assume there are two latent variables, \mathbf{z} and \mathbf{z}_n , which encode the image content and degradation information, respectively. Since practical degradation is signal-dependent, \mathbf{z} and \mathbf{z}_n may be entangled with each other in the latent space. To account for this entanglement, we employ the factorization $p(\mathbf{z}, \mathbf{z}_n) = p(\mathbf{z})p(\mathbf{z}_n|\mathbf{z})$, where we assume that \mathbf{z}_n is generated from \mathbf{z} . Moreover, we assume \mathbf{x} is generated by \mathbf{z} , and \mathbf{y} is generated by \mathbf{z} and \mathbf{z}_n , see Figure 1a for the generative process of (\mathbf{x}, \mathbf{y}) . By introducing an inference model $q(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y})$, we can decompose the conditional log-likelihood as

$$\begin{aligned} \log p(\mathbf{y}|\mathbf{x}) &= \mathbb{E}_{q(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y})} \log \frac{p(\mathbf{y}, \mathbf{z}, \mathbf{z}_n|\mathbf{x})}{q(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y})} \\ &\quad + D_{\text{KL}}(q(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y}) \| p(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y})), \end{aligned} \quad (1)$$

where D_{KL} denotes the Kullback–Leibler (KL) divergence, and the expectation term in (1) is called the conditional Evidence Lower Bound (cELBO) [50]. Due to the intractability of the original log-likelihood function, we choose to maximize the cELBO for density estimation. From the graphical model in Figure 1a, we have

$$\begin{aligned} p(\mathbf{y}, \mathbf{z}, \mathbf{z}_n|\mathbf{x}) &= p(\mathbf{z}|\mathbf{x})p(\mathbf{z}_n|\mathbf{z})p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n), \\ p(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y}) &= p(\mathbf{z}|\mathbf{x}, \mathbf{y})p(\mathbf{z}_n|\mathbf{y}, \mathbf{z}). \end{aligned} \quad (2)$$

To match the factorization of $p(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y})$, we choose

$$q(\mathbf{z}, \mathbf{z}_n|\mathbf{x}, \mathbf{y}) = q(\mathbf{z}|\mathbf{x}, \mathbf{y})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}), \quad (3)$$

then the cELBO becomes

$$\begin{aligned} \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})} \log p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n) - D_{\text{KL}}(q(\mathbf{z}|\mathbf{x}, \mathbf{y}) \| p(\mathbf{z}|\mathbf{x})) \\ - \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})). \end{aligned} \quad (4)$$

Please refer to the Appendix for the detailed derivation process. However, the inference model $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$ requires paired training data, which hinders the decomposition of the above cELBO to utilize unpaired data. One approach to overcome this limitation and further decouple $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$ is to use a mixture model [49]. Specifically, we define $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$ as a linear combination of two mixture components $q(\mathbf{z}|\mathbf{x})$ and $q(\mathbf{z}|\mathbf{y})$, i.e.,

$$q(\mathbf{z}|\mathbf{x}, \mathbf{y}) = p_1 q(\mathbf{z}|\mathbf{x}) + p_2 q(\mathbf{z}|\mathbf{y}). \quad (5)$$

where p_1 and p_2 are the mixture weights, and we choose $p_1 = p_2 = 0.5$ in our method. However, this formulation leads to the absence of a closed-form solution for the KL divergence between $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$ and the conditional prior distribution $p(\mathbf{z}|\mathbf{x})$ in the cELBO. Fortunately, we have the following proposition:

Proposition 1. *Let $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$ be a mixture model of $q(\mathbf{z}|\mathbf{x})$ and $q(\mathbf{z}|\mathbf{y})$, as described in (5), then:*

$$\begin{aligned} D_{\text{KL}}(q(\mathbf{z}|\mathbf{x}, \mathbf{y}) \| p(\mathbf{z}|\mathbf{x})) &\leq p_1 D_{\text{KL}}(q(\mathbf{z}|\mathbf{x}) \| p(\mathbf{z}|\mathbf{x})) \\ &\quad + p_2 D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| p(\mathbf{z}|\mathbf{x})). \end{aligned} \quad (6)$$

Moreover, suppose that $q(\mathbf{z}|\mathbf{x}) = p(\mathbf{z}|\mathbf{x})$ by sharing the same neural network. Then:

$$D_{\text{KL}}(q(\mathbf{z}|\mathbf{x}, \mathbf{y}) \| p(\mathbf{z}|\mathbf{x})) \leq p_2 D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x})). \quad (7)$$

See the supplemental material file for the proof. Utilizing proposition 1, we obtain a lower bound for (4):

$$\begin{aligned} \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})} \log p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n) - p_2 D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x})) \\ - \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})). \end{aligned} \quad (8)$$

Furthermore, we introduce a reconstruction term, $\mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})} \log p(\mathbf{x}|\mathbf{z})$, for the source domain data. This reconstruction term serves two purposes. Firstly, it facilitates the utilization of the source domain data. Secondly,

it aids in regularizing the inference model, $q(\mathbf{z}|\mathbf{x}, \mathbf{y})$, ensuring that the image content variable, \mathbf{z} , encapsulates all essential information from the clean image, \mathbf{x} , such that it can be faithfully reconstructed through $p(\mathbf{x}|\mathbf{z})$. The objective function for our method is defined as:

$$\begin{aligned} \text{Loss} &= \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})) \\ &+ \lambda D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x})) - \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})} \log p(\mathbf{x}|\mathbf{z}) \quad (9) \\ &- \mathbb{E}_{q(\mathbf{z}|\mathbf{x}, \mathbf{y})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})} \log p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n). \end{aligned}$$

In this formulation, we draw inspiration from the β -VAE framework [24], where we introduce a weight parameter λ in front of the term $D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x}))$ to effectively balance the two KL divergence terms in (9). Consequently, we can decompose (9) as

$$\text{Loss} = \text{Loss}_p + \text{Loss}_s + \text{Loss}_t, \quad (10)$$

where

$$\begin{aligned} \text{Loss}_p &:= -p_1 \mathbb{E}_{q(\mathbf{z}|\mathbf{x})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})} \log p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n) \\ &+ p_1 \mathbb{E}_{q(\mathbf{z}|\mathbf{x})} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})) \\ &- p_2 \mathbb{E}_{q(\mathbf{z}|\mathbf{y})} \log p(\mathbf{x}|\mathbf{z}) + \lambda D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x})), \\ \text{Loss}_s &:= -p_1 \mathbb{E}_{q(\mathbf{z}|\mathbf{x})} \log p(\mathbf{x}|\mathbf{z}), \\ \text{Loss}_t &:= -p_2 \mathbb{E}_{q(\mathbf{z}|\mathbf{y})q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})} \log p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n) \\ &+ p_2 \mathbb{E}_{q(\mathbf{z}|\mathbf{y})} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})). \end{aligned} \quad (11)$$

It is clear that Loss_p , Loss_s , and Loss_t correspond to data from the paired, source, and target domains, respectively. Therefore, the loss function described in (9) can be computed with both paired and unpaired datasets. The data flow for each domain within our approach is depicted in Figure 2.

3.2. Model settings

Degradation generation. Upon completion of the training process, it becomes feasible to synthesize degraded data from a clean input. Given a clean image \mathbf{x} , we can generate the corresponding degraded image from $p(\mathbf{y}|\mathbf{x})$ using ancestral sampling. This process involves first deriving the image content latent variable \mathbf{z} from $q(\mathbf{z}|\mathbf{x})$, followed by sampling the degradation latent variable \mathbf{z}_n from $p(\mathbf{z}_n|\mathbf{z})$. Subsequently, the corresponding degraded image \mathbf{y} is generated from $p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n)$, as depicted in Figure 1b.

Hierarchical structure. To enhance the quality of our generative performance, we employ a hierarchical VAE architecture, as proposed in previous studies [10, 53]. Specifically, we assume that our latent variable \mathbf{z} and \mathbf{z}_n is composed of L layers:

$$\mathbf{z} = (\mathbf{z}^1, \dots, \mathbf{z}^L), \quad \mathbf{z}_n = (\mathbf{z}_n^1, \dots, \mathbf{z}_n^L). \quad (12)$$

Using the chain rule, the probabilistic distribution in (9) can

be decomposed as

$$\begin{aligned} q(\mathbf{z}|\mathbf{x}) &= \prod_{l=1}^L q(\mathbf{z}^l|\mathbf{x}, \mathbf{z}^{>l}), \quad q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) = \prod_{l=1}^L q(\mathbf{z}_n^l|\mathbf{y}, \mathbf{z}, \mathbf{z}_n^{>l}), \\ q(\mathbf{z}|\mathbf{y}) &= \prod_{l=1}^L q(\mathbf{z}^l|\mathbf{y}, \mathbf{z}^{>l}), \quad p(\mathbf{z}_n|\mathbf{z}) = \prod_{l=1}^L p(\mathbf{z}_n^l|\mathbf{z}, \mathbf{z}_n^{>l}). \end{aligned} \quad (13)$$

where $\mathbf{z}_n^{>l} = (\mathbf{z}_n^{l+1}, \dots, \mathbf{z}_n^L)$. Then, the KL divergences in (9) can be factorized as:

$$\begin{aligned} D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n|\mathbf{z})) &= D_{\text{KL}}(q(\mathbf{z}_n^L|\mathbf{y}, \mathbf{z}) \| p(\mathbf{z}_n^L|\mathbf{z})) \\ &+ \sum_{l=1}^{L-1} \mathbb{E}_{q(\mathbf{z}_n^{>l}|\mathbf{y}, \mathbf{z})} [D_{\text{KL}}(q(\mathbf{z}_n^l|\mathbf{y}, \mathbf{z}, \mathbf{z}_n^{>l}) \| p(\mathbf{z}_n^l|\mathbf{z}, \mathbf{z}_n^{>l}))], \\ D_{\text{KL}}(q(\mathbf{z}|\mathbf{y}) \| q(\mathbf{z}|\mathbf{x})) &= D_{\text{KL}}(q(\mathbf{z}^L|\mathbf{y}) \| q(\mathbf{z}^L|\mathbf{x})) \\ &+ \sum_{l=1}^{L-1} \mathbb{E}_{q(\mathbf{z}^{>l}|\mathbf{y})} [D_{\text{KL}}(q(\mathbf{z}^l|\mathbf{y}, \mathbf{z}^{>l}) \| q(\mathbf{z}^l|\mathbf{x}, \mathbf{z}^{>l}))], \end{aligned}$$

where the conditional distributions $q(\mathbf{z}_n^l|\mathbf{z}_n^{>l}, \mathbf{y}, \mathbf{z})$, $p(\mathbf{z}_n^l|\mathbf{z}, \mathbf{z}_n^{>l})$, $q(\mathbf{z}^l|\mathbf{y}, \mathbf{z}^{>l})$, and $q(\mathbf{z}^l|\mathbf{x}, \mathbf{z}^{>l})$ are chosen to be Gaussian distributions, allowing us to calculate the KL divergence in a closed-form expression.

Model architecture. For the inference model $q(\mathbf{z}|\mathbf{x})$, we choose

$$q(\mathbf{z}^l|\mathbf{x}, \mathbf{z}^{>l}) = \mathcal{N}(\mu_q^l(\mathbf{a}^l, \mathbf{b}^l), \sigma_q^l(\mathbf{a}^l, \mathbf{b}^l)), \quad l = 1, \dots, L, \quad (14)$$

where \mathbf{a}^l and \mathbf{b}^l are encoding and decoding features in l -th layer, respectively, and μ_q^l and σ_q^l are networks that convert $(\mathbf{a}^l, \mathbf{b}^l)$ to the parameters of a Gaussian distribution. The encoding features $\{\mathbf{a}^l\}_{l=1}^L$ are recursively obtained through

$$\mathbf{a}^1 = f_\theta^1(\mathbf{x}), \quad \mathbf{a}^l = f_\theta^l(\mathbf{a}^{l-1}), \quad l = 2, \dots, L, \quad (15)$$

where f_θ^l represents the basic block in l -th layer. The decoding feature \mathbf{b}^l can be obtained through:

$$\mathbf{b}^L = \mathbf{0}, \quad \mathbf{b}^{l-1} = g_\theta^l(\mathbf{z}^l, \mathbf{b}^l), \quad l = 2, \dots, L, \quad (16)$$

where \mathbf{z}^l is sampled from $\mathcal{N}(\mu_q^l(\mathbf{a}^l, \mathbf{b}^l), \sigma_q^l(\mathbf{a}^l, \mathbf{b}^l))$, and g_θ^l is the basic block in l -th decoding layer. We choose the structure of $q(\mathbf{z}|\mathbf{y})$ to be the same as $q(\mathbf{z}|\mathbf{x})$.

For the inference model $q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})$, we assume that the degradation latent variable \mathbf{z}_n is distributed as follows:

$$q(\mathbf{z}_n^l|\mathbf{y}, \mathbf{z}, \mathbf{z}_n^{>l}) = \mathcal{N}(\bar{\mu}_q^l(\mathbf{a}_n^l, \mathbf{b}_n^l), \bar{\sigma}_q^l(\mathbf{a}_n^l, \mathbf{b}_n^l)), \quad l = 1, \dots, L, \quad (17)$$

where \mathbf{a}_n^l and \mathbf{b}_n^l are encoding and decoding features, respectively, and $\bar{\mu}_q^l$ and $\bar{\sigma}_q^l$ are Gaussian parameterization networks in the l -th layer. The encoding feature \mathbf{a}_n^l is computed recursively as follows:

$$\mathbf{a}_n^1 = f_\theta^1(\mathbf{y}), \quad \mathbf{a}_n^l = f_\theta^l(\mathbf{a}_n^{l-1}), \quad l = 2, \dots, L, \quad (18)$$

and the decoding feature is obtained through

$$\mathbf{b}_n^L = \mathbf{z}^L, \quad \mathbf{b}_n^{l-1} = \mathbf{z}^{l-1} + g_\theta^l(\mathbf{z}_n^l, \mathbf{b}_n^l), \quad l = 2, \dots, L, \quad (19)$$

where \mathbf{z}_n^l is sampled from (17).

For the conditional prior distribution $p(\mathbf{z}_n|\mathbf{z})$, we employ the same architecture as in $q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})$, and assume

$$p(\mathbf{z}_n^l|\mathbf{z}, \mathbf{z}_n^{>l}) = \mathcal{N}(\bar{\mu}_p^l(\mathbf{b}_n^l), \bar{\sigma}_p^l(\mathbf{b}_n^l)), \quad l = 1, \dots, L, \quad (20)$$

where the decoding feature \mathbf{b}_n^l is derived from (19), $\bar{\mu}_p^l$ and $\bar{\sigma}_p^l$ are Gaussian parameterization networks.

In the case of the generative models, we choose

$$p(\mathbf{x}|\mathbf{z}) = \mathcal{N}(g_\theta^1(\mathbf{z}^1, \mathbf{b}^1), \mathbf{I}), p(\mathbf{y}|\mathbf{z}, \mathbf{z}_n) = \mathcal{N}(g_\theta^1(\mathbf{z}_n^1, \mathbf{b}_n^1), \mathbf{I}). \quad (21)$$

We adopt the Residual Dense Block [69] (RDB) as our basic block for f_θ^l and g_θ^l , see Figure 3.

Degradation level controllable generation. The degradation generation model should be capable of producing images with varying degradation levels, enabling the generation of images with different degradation levels using a single clean input. Therefore, we leverage training data from the paired domain to train a degradation level prediction network and then utilize this network to estimate the degradation level of images within the target domain. During training, we concatenate the latent variable \mathbf{z}_n sampled from $q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})$ with its corresponding degradation level. In the generation stage, we concatenate the specified degradation level to \mathbf{z}_n sampled from $p(\mathbf{z}_n|\mathbf{z})$ to enable conditional image generation.

4. Experiment and results

We first evaluate the performance of our model in real-world noise modeling tasks and then validate the downstream performance on image denoising and SR tasks. In particular, we utilize our model to learn the unknown degradation process, and then we generate synthetic degraded images from the source domain to augment the original paired training samples. Finally, we apply an off-the-shelf supervised learning network to derive a restoration model from both the synthetic dataset and the original paired data.

4.1. Datasets

SIDD: The smartphone image denoising dataset (SIDD) [1] offers a collection of 30,000 noisy images captured by five representative smartphone cameras across ten diverse scenes under varying lighting conditions, alongside their corresponding ground truth images. Here, we utilize the SIDD-Medium dataset, which includes 320 paired clean and noisy images. For each image in the dataset, we randomly crop 300 patches of size 256×256 , yielding a total of 96,000 paired data. To establish a semi-supervised

dataset, we randomly select 0.01% (10), 0.1% (96), and 1% (960) paired samples from the cropped SIDD-Medium dataset, serving as the paired domain. These 96,000 paired images are then divided into two subsets, each containing 48,000 paired images. We utilize the clean images from the first subset as the source domain and the noisy images from the second subset as the target domain, resulting in 48,000 unpaired clean and noisy images in each domain. The SIDD dataset also includes validation and benchmark datasets, each containing 1,280 image blocks of size 256×256 .

DND: The Darmstadt Noise Dataset (DND) [46] comprises a benchmark dataset containing 1,000 image blocks of size 512×512 extracted from 50 real-world noisy images obtained from four commercial cameras. We directly assess models trained with the SIDD dataset on this benchmark.

AIM19: Track 2 of the AIM 2019 real-world SR challenge [38] provides a dataset of unpaired degraded and clean images. The degraded images are synthesized with an unknown combination of noise and compression. The challenge also provides a validation set of 100 paired images. To construct a semi-supervised dataset, we select the first 10 paired images from the validation dataset to serve as the paired domain and leverage the originally provided unpaired dataset as source and target domains. Performance evaluation is then conducted on the remaining 90 images within the validation set.

NTIRE20: Track 1 of NTIRE 2020 SR challenge [39] follows the same setting as the AIM19 dataset, inclusive of an unpaired training set and 100 validation images. Following the methodology of AIM19, we establish the semi-supervised dataset by amalgamating the original unpaired training set with the initial 10 paired images from the validation set. The performance is evaluated on the remaining 90 images within the validation set.

4.2. Implementation details

We train all SeNM-VAE models for 300k iterations using the Adam optimizer [29]. The initial learning rate is set to 10^{-4} and halved at 150k, 225k, 270k, and 285k iterations. The batch size is set to 8, consisting of randomly cropped patches of size 64×64 . Batches are sampled randomly from the paired, source, and target domains with equal probability. We apply random flips and rotations to augment the data. The KL regularization parameter λ is set to 10^{-7} . The number of hierarchical layers L is 7. Furthermore, we utilize the KL annealing method [4] for $D_{\text{KL}}(q(\mathbf{z}_n|\mathbf{y}, \mathbf{z})||p(\mathbf{z}_n|\mathbf{z}))$. Specifically, we employ a linear annealing scheme in the first 10k iterations to prevent posterior collapse. To enhance the generation capacity of the VAE model, we incorporate the LPIPS [42, 68] loss and GAN loss [33] to supplement the original L2 loss for noisy image reconstruction. For the SIDD dataset, SeNM-VAE is trained with 0.01% (10), 0.1% (96), and 1% (960) of paired

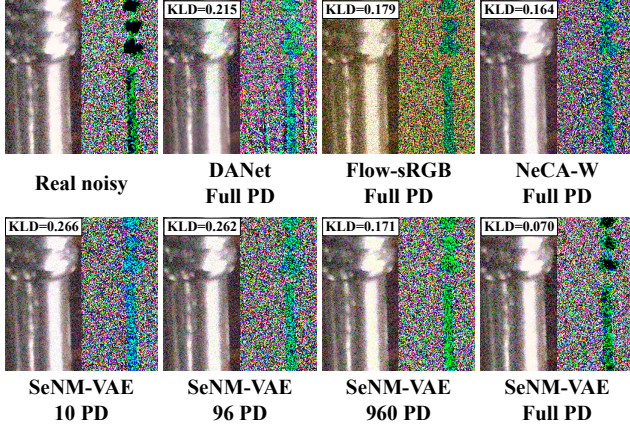


Figure 4. Visual comparison of generated noisy images, "PD" denotes paired data.

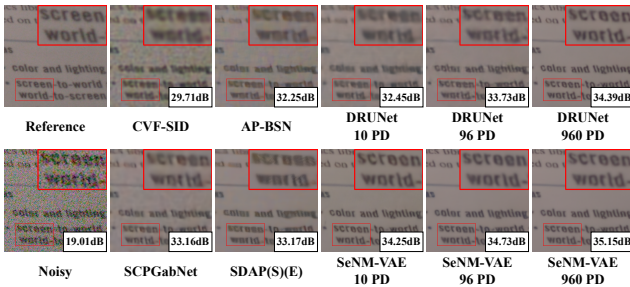


Figure 5. Visual comparison of denoising performance.

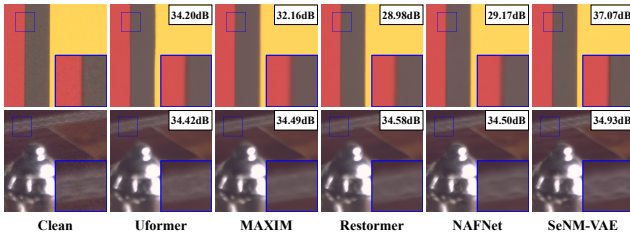


Figure 6. Visual comparison of denoising performance.

data. In addition, we include all paired data from the SIDD dataset to train our model, using only Loss_p in (11) as our objective function.

4.3. Noise synthesis

We first validate the performance of our method through real-world noise modeling tasks on the SIDD dataset.

Compared methods. We compare our SeNM-VAE with three unpaired noise modeling methods, namely C2N [25], DeFlow [61], and LUD-VAE [71], as well as three fully paired noise modeling methods, namely DANet [63], Flow-sRGB [31], and NeCA-W [17].

Experiment settings and evaluation metrics. All methods are trained on the SIDD dataset. After training, we apply the trained models to synthesize noisy images using

Method	# Paired Data	FID ↓	KLD ↓	PSNR ↑
C2N [25]		33.97	0.169	34.23
DeFlow [61]	0	39.45	0.205	33.82
LUD-VAE [71]		35.31	0.108	34.91
SeNM-VAE	0.01% (10)	17.25	0.036	36.73
	0.1% (96)	16.76	0.027	36.92
	1% (960)	15.10	0.020	37.28
DANet [63]		26.22	0.081	36.25
Flow-sRGB [31]	100%	28.60	0.047	33.24
NeCA-W [17]		19.96	0.030	37.04
SeNM-VAE		13.79	0.011	38.29
Real noise	100%	0	0	38.34

Table 1. Comparison of noise quality on SIDD validation dataset. DnCNN [65] is used as a downstream denoising model.

clean images from the SIDD validation set. This allows us to compute the FID [23] score and the KL divergence between synthetic and real noisy images within the validation set. Furthermore, using clean images from the SIDD training dataset, we generate noisy images to create synthesized training sets. DnCNN [65] models are then trained on these synthesized paired datasets. The performance of DnCNN models is evaluated on the SIDD validation dataset. We employ PSNR to evaluate denoising performance. Higher PSNR values indicate that the noise models are closer to the real noise model, signifying better noise quality.

Results. The results are shown in Table 1. Compared with the unpaired noise modeling approaches, our SeNM-VAE shows remarkable success across all three metrics, even when trained with just 10 paired samples. In contrast to fully paired noise modeling approaches, SeNM-VAE outperforms the SOTA methodology, NeCA-W [17], utilizing only 1% of the original SIDD dataset’s paired data. Furthermore, when fully paired data is employed, our method significantly surpasses other noise modeling methods on all three metrics. The results demonstrate the effectiveness of our approach in generating high-quality synthetic noisy images. The visual results are illustrated in Figure 4, demonstrating that our method successfully captures the variance change of real-world noise across different regions within the image, particularly when using fully paired data.

4.4. Downstream denoising

One significant application of our method is to benefit downstream denoising tasks. After training, we generate synthetic paired data using clean images from the source domain. Then, we employ DRUNet [67] as the downstream denoising model and train it on both the generated synthetic dataset and the data from the paired domain.

Compared methods. We compare our semi-supervised denoising method with direct training on the paired domain, and several self-supervised denoising methods, namely N2V [32], N2S [3], CVF-SID [43], AP-BSN + R³ [34], SCPGabNet [36], SDAP(S)(E) [44], and a fully supervised

Method	# Paired Data	SIDD Validation		SIDD Benchmark		DND Benchmark	
		PSNR \uparrow	SSIM \uparrow	PSNR \uparrow	SSIM \uparrow	PSNR \uparrow	SSIM \uparrow
N2V [32]	0	29.35	0.6510	27.68	0.668	-	-
N2S [3]		30.72	0.787	29.56	0.808	-	-
CVF-SID [43]		34.17	0.872	34.71	0.917	36.50	0.924
AP-BSN + R ³ [34]		35.91	0.8815	35.97	0.925	38.09	0.937
SCPGabNet [36]		36.53	0.8860	36.53	0.925	38.11	0.939
SDAP(S)(E) [44]		37.55	0.8943	37.53	0.936	38.56	0.940
DRUNet	0.01% (10)	34.48	0.8658	34.45	0.909	34.37	0.904
SeNM-VAE		37.96	0.9107	37.93	0.949	38.47	0.946
DRUNet	0.1% (96)	37.68	0.9053	37.63	0.944	38.16	0.942
SeNM-VAE		38.91	0.9134	38.85	0.953	39.32	0.951
DRUNet	1% (960)	38.93	0.9150	38.89	0.954	38.95	0.949
SeNM-VAE		39.39	0.9176	39.34	0.956	39.47	0.953
DRUNet	100%	39.55	0.9187	39.51	0.957	39.52	0.952
VDN [62]		39.29	0.9109	39.26	0.955	39.38	0.952
DeamNet [47]		39.40	0.9169	39.35	0.955	39.63	0.953

Table 2. Comparison of denoising performance on SIDD and DND datasets.

Method	SIDD Validation		SIDD Benchmark	
	PSNR \uparrow	SSIM \uparrow	PSNR \uparrow	SSIM \uparrow
Uformer [56]	39.89	0.960	39.74	0.958
MAXIM [52]	39.96	0.960	39.84	0.959
Restormer [64]	40.02	0.960	39.86	0.959
NAFNet [8]	40.30	0.961	40.15	0.960
SeNM-VAE	40.49	0.962	40.38	0.961

Table 3. Comparison of denoising performance on SIDD dataset. SeNM-VAE is trained using the full SIDD dataset and utilized to generate synthetic data for finetuning NAFNet.

Method	PSNR \uparrow	SSIM \uparrow	LPIPS \downarrow
FSSR [16]	20.97	0.5383	0.374
Impressionism [26]	21.93	0.6128	0.426
DASR [59]	21.05	0.5674	0.376
DeFlow [61]	21.43	0.6003	0.349
LUD-VAE [71]	22.25	0.6194	0.341
ESRGAN [54]	21.47	0.5748	0.353
SeNM-VAE	22.48	0.6343	0.333

Table 4. Comparison of SR performance on AIM19. ESRGAN and SeNM-VAE are trained with 10 paired data.

Method	PSNR \uparrow	SSIM \uparrow	LPIPS \downarrow
FSSR [16]	21.01	0.4229	0.435
Impressionism [26]	25.24	0.6740	0.230
DASR [59]	22.98	0.5093	0.379
DeFlow [61]	24.95	0.6746	0.217
LUD-VAE [71]	25.78	0.7196	0.220
ESRGAN [54]	25.05	0.6707	0.246
SeNM-VAE	25.91	0.7222	0.216

Table 5. Comparison of SR performance on NTIRE20. ESRGAN and SeNM-VAE are trained with 10 paired data.

trained DRUNet [67], VDN [62], and DeamNet [47].

Experiment settings and evaluation metrics. The denoising models are trained for 300k iterations with Adam optimizer. The initial learning rate is 10^{-4} and halved every 100k iterations. We evaluate the denoising performance of

all the denoising methods on the SIDD validation dataset, the SIDD benchmark dataset, and the DND benchmark dataset, and report PSNR and SSIM [55] for each dataset.

Results. The results are presented in Table 2. The table indicates that our SeNM-VAE approach enhances performance compared to the baseline models on the SIDD and DND datasets. Additionally, our method improves upon the results of self-supervised denoising methods on the SIDD dataset, even with access to only 10 paired data samples. When utilizing 1% paired data, our method yields results comparable to the fully supervised trained DRUNet model. As such, SeNM-VAE offers an effective strategy to narrow the performance gap between self-supervised and supervised denoising methods. Figure 5 showcases visual results, where our approach achieves sharper edges and more thorough noise removal compared to other methods.

4.5. Finetune denoising network

Another application of our method involves generating additional training samples to finetune the denoising network. We utilize our SeNM-VAE, trained with all paired data from the SIDD dataset, to produce extra training data from clean images in the SIDD dataset. We then finetune a pre-trained denoising network, NAFNet [8]. These results are presented in Table 3. The table illustrates that our method can significantly enhance the denoising performance of NAFNet, leading to superior performance on the SIDD dataset. Visual results are shown in Figure 6, where our method notably yields sharper edges and preserves more image information.

4.6. Downstream SR

We apply our method to simulate the degradation process in real-world SR tasks. Assume the degradation process is $y = \mathcal{D}(x) + n$, where both the downsample operator \mathcal{D} and noise n remain unknown. We substitute \mathcal{D} with the Bicubic

Total Loss	FID ↓	KLD ↓	PSNR ↑
w/o recon. \mathbf{x}	24.26	0.070	35.60
w/ recon. \mathbf{x}	17.25	0.036	36.73

Table 6. Ablation on the reconstruction loss for the clean image \mathbf{x} on SIDD validation dataset with 10 paired data.

downsample operator \mathcal{B} and incorporate the disparity between \mathcal{D} and \mathcal{B} into the noise term, yielding $\mathbf{y} = \mathcal{B}(\mathbf{x}) + \mathbf{n}'$, where $\mathbf{n}' = \mathbf{n} + \mathcal{D}(\mathbf{x}) - \mathcal{B}(\mathbf{x})$. After training, we generate synthetic low-resolution data and employ ESRGAN [54] to train a restoration model.

Compared methods. We compare our semi-supervised SR method with five unpaired degradation modeling methods, namely FSSR [16], Impressionism [26], DASR [59], DeFlow [61], LUD-VAE [71], and a supervised trained ESRGAN [54].

Experiment settings and evaluation metrics. All the SR models are trained for 60k iterations with Adam optimizer. We evaluate each SR method on the final 90 images from the AIM19 and NTIRE20 validation datasets. Performance metrics, including PSNR, SSIM, and LPIPS [68], are reported for both datasets.

Results. The results are detailed in Table 4 and Table 5. Our method surpasses both the supervised ESRGAN model and the unpaired degradation modeling methods, which highlights the effectiveness of our model in leveraging a limited amount of paired data alongside unpaired data to enhance the generation of high-quality training samples.

4.7. Ablation study and discussions

Ablation on reconstruction loss for clean image \mathbf{x} . We perform an ablation experiment to the additional loss $-\mathbb{E}_{q(\mathbf{z}|\mathbf{x},\mathbf{y})} \log p(\mathbf{x}|\mathbf{z})$ in (9) on the SIDD dataset with 10 paired samples, and the results are shown in Table 6. The table demonstrates an improvement in noise modeling performance with the inclusion of this reconstruction loss. One reason is that the reconstruction loss acts as Loss_s for source domain data in (11), allowing effective utilization of source domain data. Moreover, the reconstruction loss enables the transformation from noisy image \mathbf{y} to the clean image \mathbf{x} , aiding in the disentanglement of image information \mathbf{z} from noisy information \mathbf{z}_n , which further enhances the model’s ability to learn the noise distribution.

Analysis on the training domains. To demonstrate the efficacy of our model in utilizing information from unpaired data domains, we conduct experiments using different numbers of unpaired data on the SIDD dataset with 10 paired data. Specifically, we randomly select 0, 96, and 960 images for the source and target domains to illustrate our model’s capacity to exploit information from unpaired data domains. Then, we conduct ablation studies using only two domains to understand the roles of the source and target do-

Paired	# Data Source	Target	FID ↓	KLD ↓	PSNR ↑
10	0	0	19.79	0.073	35.97
10	96	96	17.52	0.054	36.67
10	960	960	17.54	0.036	36.78
10	100%	0	22.98	0.043	36.23
10	0	100%	19.11	0.050	36.24
10	100%	100%	17.25	0.036	36.73

Table 7. Comparison of noise quality on SIDD validation dataset with different numbers of unpaired samples.

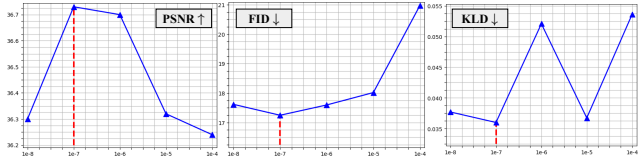


Figure 7. Parameter analysis of KL weight λ on SIDD validation dataset with 10 paired data.

ains in the training process. The results are summarized in Table 7. From the table, we find that the noise modeling performance improves with increasing unpaired data, and incorporating all three domains yields the best noise modeling results. The findings indicate our model’s effectiveness in leveraging information from unpaired datasets.

Analysis on KL weight λ . We perform a parameter analysis for the KL weight coefficient λ . The results are presented in Figure 7. The figure shows that setting λ in the range of 10^{-6} to 10^{-7} leads to better noise modeling results than other cases.

5. Conclusion

This paper presents SeNM-VAE, a semi-supervised noise modeling approach based on deep variational inference. The proposed method employs a latent variable model to capture the conditional distribution between corrupted and clean images, allowing for the transformation from a clean image to its corrupted counterpart. Our approach decomposes the objective function, enabling training with both paired and unpaired datasets. We apply SeNM-VAE to real-world noise modeling and downstream denoising and super-resolution tasks. Our method further improves upon other degradation modeling methods and achieves the best performance on the SIDD dataset.

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