Supplementary Materials of SOK-Bench: A Situated Video Reasoning Benchmark with Aligned Open-World Knowledge

1. Graph Generation Algorithms

The generation processes are shown in Algorithm 1 for Situated Knowledge Graph (SKG), Algorithm 2 for General Knowledge Graph (GKG), and Algorithm 3 for Situated Commonsense Knowledge Graph (SCKG). Please find the algorithms in the last page in details.

2. Question Templates for Bottom-up Generation

Table 1 provides an overview of the question template types. There are six primary types: Object counterfactual, Object contribution, Object reasoning, Action counterfactual, Action purpose, and Action possibility. Within each main type, we further develop subtypes by incorporating spatiotemporal reasoning, such as considering object attributes and object-object relationships (*e.g.*, "+ obj attribute + obj-obj relationship"). Our benchmark is primarily constructed through the generation of question-answer pairs using template-based bottom-up approaches.

3. Case Studies for Top-down Generation

By utilizing a prompt template of the form $\langle video \ content, integrated \ graph, QA \ examples, \ generation \ goal, \ output \ format \rangle$, we effectively guide the LLM in generating multi-hop questions based on multiple edges extracted from the *integrated graph*. This prompt design, as depicted in Table 2, offers several advantages. Firstly, it enables the generation of diverse and high-quality questions and corresponding answers. Secondly, it facilitates the alignment between the generated QA pairs and the underlying knowledge graphs by instructing the LLM to demonstrate the alignment of edges in the graph (*e.g.*, <1>, <23>) with the QA pairs, thereby enhancing the interpretability and reasoning steps. Please see Figre 1 for QA examples.

In the absence of this prompt template, when LLM is directly prompted to generate questions based solely on the video content, there is a risk of obtaining simplistic questions that lack situated common-sense reasoning (e.g., "What ingredients did the person use to cook mapo Table 1. Question template types for Bottom-up QA generation

Object counterfactual (<i>e.g.</i> , What would happen if the person did not use)	vanilla (obj) + obj attributes + obj-obj relationships + obj attribute + obj-obj relationship + obj general knowledge
Object contribution (e.g., Why the person use)	vanilla (obj) + obj attributes + obj-obj relationships + obj attribute + obj-obj relationship + obj general knowledge
Object inference (<i>e.g.</i> , What are the two objects	s which <interaction>)</interaction>
Action counterfactual (<i>e.g.</i> , What would happen if the person did not)	vanilla (act) + before / after action + before / after action + obj attr / rela
Action purpose (<i>e.g.</i> , Why the person)	vanilla (act) + before/after action + before / after action + obj attr / rela
Action possibility (<i>e.g.</i> , What mistake might the	person make if <possibility>)</possibility>

tofu?") or questions that cannot be answered based on the video (*e.g.*, "Who will eat the mapo tofu?"). While our approach does not entirely eliminate such situations, our prompt design significantly mitigates this issue. Although there may still be instances where the LLM generates relatively straightforward questions (*e.g.*, "What is the color of tofu?"), our method ensures that the generated questions are correct, as we constrain the LLM's output within the boundaries defined by the knowledge graphs.

4. Object and Action Overview

Our benchmark includes 1005 objects and 505 actions. The word clouds of objects and actions are presented in Figure 2 and Figure 3 respectively.

5. Data Quality Evaluation and Validation

We enlisted the assistance of human evaluators to assess the quality of our benchmark through visual inspection. Example QAs by top-down generation



Question: Why is transparent substance important in the recipe for mapo tofu?

A. It is made up of two hydrogen atoms and one oxygen atom. **B. It helps to create the sauce, hydrate and soften tofu, and enhance flavor absorption.**

C. It is important only because it dissolves and distributes seasonings. D. It is important in the recipe for mapo tofu because it is essential for human survival. Question: How would the taste of the dish change if you skip adding ground pork and salt?

A. The dish would lack the meatiness and seasoning, resulting in a less flavorful mapo tofu.√ B. The dish would taste even spicier

C. The dish would become more authentic mapo tofu.

D. The dish would become more authentic maps told.

Question: How would the dish change if the ingredient fried with mapo tofu paste was replaced with chicken?

- A. The dish would taste exactly the same.
- B. The dish would be no more mapo tofu.

C. The dish would be more flavorful.

D. Chicken would alter the traditional taste of maps to fu. \checkmark

Figure 1. Example of top-down generated question-answer pairs.

Table 2. Exemplary prompts for top-down QA generation

video content	#System#: You are a helpful, pattern-following assistant. You are very good at deciphering a video, such as summarizing video content, figuring out related commonsense knowledge, and identifying the inner logic. As a commonsense-driven assistant, your task is to analyze a video (length: 119 seconds) that showcases a person introducing 6 cooking steps of mapo tofu. The steps are described in a specific format of '[Step N (from <timestamp>to <timestamp>): detailed description of cooking actions]' as follows:</timestamp></timestamp>
integrated graph	<pre>#System#: From the <video>, use your commonsense reasoning ability, you can get a <knowledge graph="">shown in JSON format: {<0>: {'head': 'tofu', 'edge': 'counterfactual', 'tail': 'The dish would no longer be mapo tofu.'}, <1>: {'head': 'tofu', 'edge': 'contribution', 'tail': ' adds texture and absorbs the flavors of the sauce in mapo .'}, <6>: {'head': 'cut tofu into square pieces', 'edge': 'things related to', 'tail': 'tofu'}</knowledge></video></pre>
	}
QA examples	 #User#: Based on video content and <knowledge graph="">, use your creativity, generate a HARD question which involves reasoning involving multiple indexes from <knowledge graph="">. The description of the question should be natural. Then, answer the question with correct answer, provide 3 wrong answers. Output in JSON format with key 'question', 'correct answer', '3 wrong answers'. Others cannot answer the question unless they have known <video content="">.</video></knowledge></knowledge> #Assistant#: {question: <ingredient a="">is mixed with <ingredient b="">to create a slurry, which is added to the to thicken the sauce. What are <ingredient a="">and <ingredient b="">?, correct answer: constarch and water, 3 wrong answers:}</ingredient></ingredient></ingredient></ingredient>
generation goal	#User#: Based on video content and <knowledge graph="">, use your creativity, generate a HARD question which involves reasoning involving multiple indexes from <knowledge graph="">.</knowledge></knowledge>
output format	#User#: The description of the question should be natural. Then, answer the question with correct answer, provide 3 wrong answers. Output in JSON format with key 'question', 'correct answer', '3 wrong answers'. Others cannot answer the question unless they have known <video content="">.</video>

From each of the 12 question types, we validated all 44K question-answer pairs with the effort from 8 non-CS PhD students with STEM skills, degrees and responsible attitudes, ensuring no conflict of interest. The quality validation process consisted of two stages. In the first stage, the evaluators examined whether the questions and answers were correct based on its comprehension, semantics, and logic. This entailed verifying the accuracy of the answer, determining if the question was answerable, and assessing its relevance to the accompanying video (refer to the "Correctness" column in Table 3). The 3-voter validation was carried out. Overall, human evaluation indicated

<u>92.05%±0.2%</u> of the generated pairs as correct with a 99% confidence level. In the second stage, for all the "correct" question-answer pairs, the evaluators further assessed whether the question could be answered without watching the video. For instance, consider the following example: "Question: What is the color of tofu? Answer: White." Although this question-answer pair is correct and related to the video on cooking mapo tofu, the question can be answered solely through commonsense and does not require watching the video. The evaluators calculated the proportion of questions that could only be answered by watching the video (refer to the "Need video to answer" column in Table 3).

chilli powder atte garlic sauce garlic water salt seeds green salt provide the powder yogurt paste garlic save for vegetable stock baking powder of the stoc uce Sauce fectuce sauce bok cho fish spring onion cheese variation of the second etable oil Recarrot white Corn starch ā coriander ξ M_{cha} powder Igreen Onion cinnamon garami masala ∩ Ve Ο salt egg 60 powders butter powder oil se powder oil stick teabags teabags red powder oil pepper bay Leat alt pepper ck whole wheat sarlic saltmilk olive sarlic pepper olive tomato sauce onions baking toth worcestershire sauce salt teabags red powder lemon, white wine dry mango red bellowered mines oil reper carrots red riour backing white wine dry mango red bellowered mines oil reper carrots red red chilis oil reper to a salt ground cumin powder base red red chilis yogurt turmeric masala potatoes soaked daletates tart paste pepper flakes segame seeds paste onion butter oil ans cabage minored so a salt ground cumin butter oil onion bay green chili ground pepper 80 nicken garlic sardina arrdana V Sauceuter star ing yo turmeric chickens cope vest uclass salta spicy mayonalise CUTTY base Soly dried_oregano ~ ē cabbage minced garlic Chili enugreek leaves Water tomato saltchicken stock **DOMO** lime juice **Oil** flour black tomato ferugreek leaves water tomato tomato puree butter milk cheese pepper salt cumine potatoes curry 'n green baking sodamasala black pepper م mozzarella cheesepepper oll <u>onio</u>n onions oil elter butter parley sit . Kidney heave powder water ackie a chili b1<u>الم</u> emon afoetida bay CUMIN SEEdSchicken breast sauce milk salt Figure 2. Word could of objects presented in our benchmark.

garlic add bowl add ingredient add milk flour salt lime juice baking powder tomato purce boiling water worcestershire sauce pan put processor coat powder salt leaves add top add black pepper lidpita bread white pepper flakes whisk onion add seeds add mozzarella cheese oil onor rigs witter and salt pepper powder salt add sugar add salt whisk office add vegetable mozzarella cheese oil onion rings white wine paste add salt pepper badd flour tomato sauce stir add bean sprout add oil butfinely chop bicces addpowder baking COOK add soy stir fry chicken piece Depaper towelsesame oil olicit add pass add flour tomato sauce stir add bean s paid put finely chop pieces addpower bay 1 pieces addpower bay minced garlicsmall pieces red ch mix 5 deep fryadd onion chicken breast pieces out of the pieces addpower baker season , add red chill powder vegetab chicken wing ⊂add green cumin seeds baking soda C ad tomato paste Leaf add diced wadd ginger clam e chopped on add itter red pepper add meat of ym add chopped onion pan mi mix 5 c deep fry add onion chicken breat oil pot season add red chilli powder vegetable oil mixture add powder add breat of top P add tsp pan cook or dd butter minced ginger chicken stock place 0D10 bowder add red ittill powder vegetable oil mixture add oll add fish sauce meat powder add tsp pan cook green onion egg cabbage leaves plastic wrapDOWI top tadd tsp pan cook green onion add yogur pot add prastic wrapDOWI both boil mix will chopped green garlic work add yogur pot add prastic add Olive oil broth boil melt butter ind stirbread crumb add powder water mix golden brown add cumin rollgreen chili prasm coriander bowder add bowder add tomato 5 r 1ng rollgreen chili pram coriander powder add tomato Water add bell pepper chili powder Eng en Hot oil lemon a seed red chili Figure 3. Word cloud of actions presented in our benchmark.

The results indicate that our benchmark exhibits a high level of correctness and a high ratio of questions that necessitate watching the video for answering. A high correctness ratio signifies the validity of our automated questionanswer generation approach. A high ratio of questions requiring video comprehension demonstrates that the majority of generated questions demand both spatiotemporal reasoning based on the video content and situated commonsense reasoning. This accomplishment aligns with our objective in designing the benchmark.

6. Experiment Settings

For deployable models (Video-LLaMa, Video-ChatGPT, PandaGPT and AskAnything), we use their pre-trained 7B versions, respectively. For GPT4-Vision, we provide 5 frames chosen equidistantly in each video.

When evaluating these models in multiple choice setting, we observe that sometimes they do not give explicit choices, but instead answers the question directly (see examples). Therefore, we map an answer to a choice by:

• If the answer can be parsed into an integer choice successfully, use it as the model's choice.

Table 3. QA quality validation

QA type	Correctness ¹	Need video to answer ²
object counterfactual + spatiotemporal	0.91	0.98
object contribution + spatiotemporal	0.92	0.98
object counterfactual + general knowledge	0.95	0.88
object contribution + general knowledge	0.94	0.89
action purpose + spatiotemporal	0.92	0.98
action counterfactual + spatiotemporal	0.88	0.99
object inference	0.95	0.95
object counterfactual	0.92	0.94
action counterfactual	0.91	0.95
action purpose	0.95	0.96
action possibility	0.98	0.96
object contribution	0.94	0.92

¹ Correctness = num of correct QA pairs / total num of QA pairs

² Need video to answer = num of QA pairs which can only be correctly answered by watching the video / total num of QA pairs

- Otherwise, we compute the BLEU score between each choice and the model's output, and choose the maximum as its choice.
- We notice that API models generally do not need this fix, as they show better instruction following abilities.

Please refer to Figure 4 for an illustration of example

results obtained by the baseline models on our benchmark.

7. Ablation Studies

7.1. Effectiveness of Prompting Generation.

By referring to Table 3, it becomes evident that when incorporating spatiotemporal information (*i.e.*, "+spatiotemporal"), nearly all the questions can only be answered by watching the accompanying videos. This finding effectively validates the significance of MLLMs in generating top-notch situated commonsense questions.

As indicated in Table 4, when prompts include a specified knowledge *aspect*, a broader range of knowledge is generated. By incorporating *general knowledge examples* (π) and *output format* (ϕ) , we are able to generate the same number of knowledge pieces using significantly fewer tokens, while ensuring that all the generated content can be parsed in JSON format (see Table 5).

 $\{\pi_i^{obj}\}, \{\pi_i^{act}\}, \text{ generation goal instructions } \{\omega\}, \text{ output format instructions } \{\phi\}$

Table 4. Number of pieces of generated knowledge per object with or without knowledge aspect.

	Num of knowledge / obj
w/o aspect	8
w/ aspect	26

Table 5. Number of tokens used and ratio of JSON parsable content by different prompt strategies

	Num of tokens / vid	JSON parse ¹
Gen Goal	7090	0%
+ Format	4559	11.1%
+ Examples + Format	3512	100%

¹ The ratio represents the number of outputs that can be parsed as JSON format divided by the total number of outputs

7.2. Effectiveness of Few-Shot Self-Prompting.

We present a comparison between two scenarios: one involving Few-Shot Self-Prompting and the other without, as depicted in Table 6. The table clearly demonstrates that the utilization of Few-Shot Self-Prompting techniques enables LLM to generate significantly more specific and concrete situated commonsense knowledge. Table 6. Comparison between between two scenarios: one with Few-Shot Self-Prompting and one without. A case about cooking buffalo wings is shown here. Column of "object contribution to cooking" shows the generated contents by LLM.

w/

w/

	objects	object contribution to cooking
o FSSP ¹	wings	are rinsed, seasoned, cooked, and mixed with buffalo sauce in the cooking process
	garlic powder	adds flavor to the buffalo wings
	chili powder	adds flavor to the buffalo wings
	paprika	adds flavor and a hint of smokiness to the buffalo wings
	salt	enhances the flavor of the buffalo wings
	cayenne pepper	adds spiciness to the buffalo wings
	buffalo wing sauce	adds flavor to the wings
FSSP ²	wings	are the main ingredient and are cooked until crispy before being coated in buffalo sauce
	garlic powder	is used as a seasoning for the wings, adding a savory and aromatic flavor to the dish
	chili powder	adds a spicy kick to the wings, en- hancing the overall flavor and heat of the dish
	paprika	adds a smoky and slightly sweet fla- vor to the wings, enhancing their overall taste and appearance
	salt	enhances the flavor of the wings, bringing out the natural taste of the meat and other seasonings
	cayenne pepper	adds a spicy and fiery flavor to the wings, giving them a delicious and bold taste
	buffalo wing sauce	adds a tangy and zesty flavor to the wings, giving them their signature taste and texture

¹ w/o FSSP: without Few-Shot Self-Prompting

 $^2\,$ w/ FSSP: with Few-Shot Self-Prompting

A video showing the cooking process of Buffalo Wings



(a) Model: GPT-4 Vision

Question: Look What would happen if the person did not use the thing which also can be used to widely used in hungarian, spanish, and indian cuisines in culinary traditions and central and south america in origin during the cooking process?

GT answer: The buffalo wings would lack the smoky and slightly sweet flavor that paprika adds.

Model output: If the person did not use salt, which is commonly used in Hungarian, Spanish, Indian cuisines, and originates from Central and South America, the dish would likely have less flavor and taste bland, as salt is a basic seasoning that enhances the taste of food.

(b) Model: Valley

Question: What would happen if the person did not use the thing which also can be used to varies (odorless to distinct) in odor and varies (depending on the type of oil) in boiling point during the cooking process? Please choose from the following choices (0 or 1 or 2 or 3). 0: The Thai fried rice would lack the necessary lubrication and frying element, resulting in a dry and less flavorful dish; 1: The Thai fried rice would lack the distinctive and aromatic flavors that spices provide, resulting in a less flavorful dish; 2: The Thai fried rice would lack a significant source of protein and the overall flavor profile would be affected; 3: The Thai fried rice would lack texture, color, and essential nutrients, resulting in a less balanced and flavorful dish. Please give only a number chosen from 0, 1, 2, or 3.

GT answer: 0: The Thai fried rice would lack the necessary lubrication and frying element, resulting in a dry and less flavorful dish.

Model output: Based on the video, if the person did not use the spoon to mix the ingredients in the frying pan, the dish would not be well-combined and the flavors might not be evenly distributed. The spoon is an essential tool in the cooking process, as it helps to ensure that the ingredients are mixed properly and cooked evenly. Without the spoon, the dish would likely be less appetizing and less enjoyable to eat.

(c) Lateral comparison

Question: What would happen if the person did not use the thing which also can be used to widely used in hungarian, spanish, and indian cuisines in culinary traditions and central and south america in origin during the cooking process? Please choose from the following choices (0 or 1 or 2 or 3). 0: The buffalo wings would be less spicy and have a milder flavor without black pepper; 1: The flavor of the buffalo wings would be slightly different without the garlic powder; 2: The buffalo wings would lack the smoky and slightly sweet flavor that paprika adds; 3: The buffalo wings would not have the same crispy texture without the oil. Please give only a number chosen from 0, 1, 2, or 3.

GT answer: 2: The buffalo wings would lack the smoky and slightly sweet flavor that paprika adds

#GPT4-V#: 2.

#Ask Anything#: 2

#PandaGPT#: If the person did not use the sauce that can be widely used in Hungarian, Spanish, and Indian cuisines in culinary traditions and Central and South America in origin, the buffalo wings would have a less spicy and milder flavor without black pepper (0). The flavor of the buffalo wings would be slightly different without garlic powder (1), but still have the smoky and slightly sweet flavor that paprika adds (2). The buffalo wings would lack the crispy texture without the oil (3).

#Valley#: 1: The person is using a spoon to stir the food in the pot.

#VideoLLaMa#: (corrupted output)

Figure 4. (a): An example showcasing the GPT-4 Vision results in a direct-answer setting. (b): A typical instance where the model's output lacks a specific choice but provides an explanation in a multichoice setting. To determine the correctness of the model's output, we compute the similarity between the model's output and each available option. (c): A comparative analysis conducted among the baseline models..

Algorithm 1: Situated Knowledge Graph

```
Input: video v, manual annotations of events \{y_t\}, Large
            Language Model LLM, Vision-Language Model
            VL, generation goal instructions \{\omega\}, output
            format instructions \{\phi\}
1 Function GetSKG(v, \{y_t\}):
        Init: Situated Knowledge Graph G_v = []
        /* 1 parse objs and acts from
             annotations and output in JSON
              format */
        objs \{o_i\} \leftarrow \text{LLM}\left(\langle \{y_t\} \mid \omega_{obj}, \phi_{obj} \rangle\right);
2
        acts \{a_t\} \leftarrow \text{LLM}\left(\langle \{y_t\} \mid \omega_{act}, \phi_{act} \rangle\right);
3
        /* 2 obtain obj attributes and
             obj-obj relationships */
        sample frames with timestamps \{f_{t^*}\} \leftarrow v;
4
        for each f_{t^*} \in \{f_{t^*}\} do
5
             extract obj strings from frames
6
             o^* \leftarrow \text{VL}\left(\left\langle f_{t^*} \mid \omega_{obj}^* \right\rangle\right);
7
             parse objs in JSON format
8
             \{o_i^*\} \leftarrow \text{LLM}\left(\left\langle o^* \mid \phi_{obj}^* \right\rangle\right);
0
             // check missing objs (VL may
                   fail to recognize objs in
                   frames)
             for each o_i \in \{o_i\} do
10
                  if o_i in t^* & o_i \notin \{o_i^*\} then
11
                    | \{o_i^*\} := \{o_i^*\} + o_i
12
             // obj attributes
             for each o_i^* \in \{o_i^*\} do
13
                  get obj attributes
14
                  attr_i \leftarrow VL\left(\left\langle f_{t^*} \mid \omega_{attr}^i \right\rangle\right);
15
                  // add edges of <time, obj>
                        and <obj, attribute> to SKG
                  add edge (t^*, o_i^*) to G_v;
16
                  add edge (o_i^*, attr_i) to G_v;
17
             // obj-obj spatial relations
             for each pair (o_i^*, o_i^*) do
18
                  get obj-obj spatial relations
19
                  re_{i,j} \leftarrow \text{VL}\left(\langle f_{t^*}, \omega_{re}^{i,j} \rangle\right);
20
                  // add edge of <obj i,</pre>
                        relationship, obj j> to SKG
                  add edge (o_i^*, re_{i,j}, o_j^*) to G_v;
21
        /* 3 align acts with objs */
22
        for each f_{t^*} \in \{f_{t^*}\}, each a_t \in \{a_t\} do
             for each o_i^* \in \{o_i^*\} do
23
                  if t^* in t & o_i^* in a_t then
24
                       // add edges of <act, obj>
                             to SKG
                       add edge (a_t, o_i^*) to G_v;
25
             // add edges of <time, act> to
                   SKG
             add edge (t, a_t) to G_v;
26
        return G_v;
27
```

Algorithm 2: General Knowledge Graph **Input:** Situated Knowledge Graph G_v , Large Language Model LLM, general knowledge aspects $\{\eta_i^{obj}\},\$ $\{\eta_i^{act}\}\$ with corresponding knowledge examples $\{\pi_i^{obj}\}, \{\pi_i^{act}\}, \text{ generation goal instructions } \{\omega\},\$ output format instructions $\{\phi\}$ 1 Function GetGKG(G_v): **Init:** General Knowledge Graph $G_{gk} = []$ extract objs $\{o_i\}$, acts $\{a_t\}$ from G_v ; 2 /* 1 general knowledge of objs */ for $o_i \in \{o_i\}$ do 3 // e.g., knowledge aspects of physical, chemical, usage, ... for $\eta_j^{obj} \in \{\eta_j^{obj}\}, \pi_j^{obj} \in \{\pi_j^{obj}\}$ do construct generation goal based on one aspect 4 5 $\omega_{obj}^* \leftarrow \langle o_i \mid \omega_{obj}, \eta_j^{obj} \rangle;$ 6 generate knowledge in desired JSON format 7 $\begin{array}{l} \overset{j}{\kappa_{i}^{j}} \leftarrow \texttt{LLM}\left(\langle \pi_{j}^{obj}, \omega_{obj}^{*}, \phi_{obj} \rangle\right); \\ \text{add edge}\left(o_{i}, \eta_{j}^{obj}, \kappa_{i}^{i}\right) \text{to } \boldsymbol{G}_{gk}; \end{array}$ 8 9 /* 2 general knowledge of acts */ for $a_t \in \{a_t\}$ do 10 for $\eta_j^{act} \in \{\eta_j^{act}\}, \pi_j^{act} \in \{\pi_j^{act}\}$ do 11 construct generation goal based on one aspect 12 $\omega_{act}^* \leftarrow \langle a_t \mid \omega_{act}, \eta_j^{act} \rangle ;$ 13 generate knowledge in desired JSON format 14 $\kappa_{i}^{j} \leftarrow \text{LLM}\left(\left\langle \pi_{j}^{act}, \omega_{act}^{*}, \phi_{act} \right\rangle \right)$; 15 add edge $(a_t, \eta_i^{act}, \kappa_i^j)$ to G_{gk} ; 16 return G_{qk} ; 17

Algorithm 3: Situated Commonsense Knowledge Graph

```
Input: Situated Knowledge Graph G_v, General
              Knowledge Graph G_{qk}, Large Language Model
              LLM, situated commonsen knowledge aspects
              \{\eta_i^{obj}\}, \{\eta_i^{act}\}, \text{generation goal instructions } \{\omega\},\
             output format instructions \{\phi\}
1 Function GetSCKG (m{G}_v, m{G}_{gk}):
         Init: Situated Commonsense Knowledge Graph
                 G_{sk} = [], J = 2
         extract objs \{o_i\}, acts \{a_t\} from G_v;
 2
         g_v \leftarrow \text{texturalized } \boldsymbol{G}_v;
 3
         /* 1 sc knowledge of objs */
         for each \eta_j^{obj} \in {\{\eta_j^{obj}\}} do
 4
               // e.g., knowledge aspects of
                     counterfactual and obj
                     contribution
               situated commonsense examples \pi_i = [];
 5
               repeat
 6
                    for o_i \in \{o_i\} do
 7
                          k_g \leftarrow knowledge related to o_i in G_{gk};
 8
                          \omega_{obj}^* \leftarrow \langle o_i \mid \omega_{obj}, \eta_j^{obj} \rangle ;
 9
                          \kappa_i^j \leftarrow \text{LLM}\left(\langle g_v, k_g, \pi_j, \omega_{obj}^*, \phi_{obj} \rangle\right);
10
                          add or update \kappa_i^j in \pi_j;
add or update (o_i, \eta_j^{obj}, \kappa_i^j) in G_{sk};
11
12
               until Finishing J iterations;
13
         /* 2 sc knowledge of acts */
         for \eta_j^{act} \in \{\eta_j^{act}\} do
14
               // e.g., knowledge aspects of
                     counterfactual and act purpose
               situated commonsense examples \pi_i = [];
15
               repeat
16
                     for a_t \in \{a_t\} do
17
                          k_g \leftarrow knowledge related to a_t in G_{gk};
18
                          \tilde{\omega_{act}^*} \leftarrow \langle a_t \mid \tilde{\omega_{act}}, \eta_j^{act} \rangle;
19
                          \kappa_i^j \leftarrow \text{LLM}\left(\langle g_v, k_g, \pi_j, \omega_{act}^*, \phi_{act} \rangle\right);
20
                          add or update \kappa_i^j in \pi_j;
21
                          add or update (a_t, \eta_j^{act}, \kappa_i^j) in \boldsymbol{G}_{sk} ;
22
               until Finishing J iterations;
23
         return G_{sk};
24
```