# GS-SLAM: Dense Visual SLAM with 3D Gaussian Splatting <br> Supplementary Material 

## Overview

This supplementary material complements our primary study, offering extended details and data to enhance the reproducibility of our GS-SLAM. It also includes supplementary evaluations and a range of qualitative findings that further support the conclusions presented in the main paper:
$\triangleright$ Sec. 1: Proofs of gradient computation, including the details of pose gradient derivation and depth gradient derivation.
$\triangleright$ Sec. 2: Coarse-to-fine pose optimization algorithm, including pseudocode and visualization of how our algorithm worked.
$\triangleright$ Sec. 3: Additional performance comparison, including the additional visualization on the Replica and TUM-RGBD dataset.
$\triangleright$ Sec. 4: Additional ablation result, including the addition qualitative result on render, tracking and mapping performance.
$\triangleright$ Sec. 5: Additional implementation details, including more details for reproducibility of our GS-SLAM.

## 1. Proofs of Gradient Computation

To derive gradients for pose $\mathbf{P}=\{\mathbf{R}, \mathbf{t}\}$, recall that we store the pose in separate quaternion $\mathbf{q} \in \mathbb{R}^{4}$ and translation $\mathbf{t} \in \mathbb{R}^{3}$ vectors. To derive gradients for rotation, we recall the conversion from a unit quaternion $\mathbf{q}=\left[q_{r}, q_{i}, q_{j}, q_{k}\right]^{T}$ to rotation matrix $\mathbf{R}$ :

$$
\mathbf{R}=2\left[\begin{array}{ccc}
\frac{1}{2}-\left(q_{j}^{2}+q_{k}^{2}\right) & \left(q_{i} q_{j}-q_{r} q_{k}\right) & \left(q_{i} q_{k}+q_{r} q_{j}\right)  \tag{14}\\
\left(q_{i} q_{j}+q_{r} q_{k}\right) & \frac{1}{2}-\left(q_{i}^{2}+q_{k}^{2}\right) & \left(q_{j} q_{k}-q_{r} q_{i}\right) \\
\left(q_{i} q_{k}-q_{r} q_{j}\right) & \left(q_{j} q_{k}+q_{r} q_{i}\right) & \frac{1}{2}-\left(q_{i}^{2}+q_{j}^{2}\right)
\end{array}\right]
$$

Also, we recall that the pose $\mathbf{P}$ is consisits of two part $\frac{\partial \mathbf{m}_{i}}{\partial \mathbf{P}}$ and $\frac{\partial \boldsymbol{\Sigma}^{\prime}}{\partial \mathbf{P}}$ when ignore view-dependent color. For simplicity of the formula, we denote $\mathbf{X}_{i}=[x, y, z]^{T}$ in the camera coordinate as $\mathbf{X}_{i}^{c}=\mathbf{P} \mathbf{X}_{i}=\left[x^{c}, y^{c}, z^{c}\right]^{T}$.
Pose gradients back-propagation by $\frac{\partial \mathbf{m}_{i}}{\partial \mathbf{P}}$. We find the following gradients for translation $\mathbf{t}$ and $\frac{\partial \mathbf{X}_{i}^{c}}{\partial t}$ :

$$
\frac{\partial \mathbf{m}_{i}}{\partial \mathbf{t}}=\frac{\partial \mathbf{m}_{i}}{\partial \mathbf{X}_{i}^{c}}=\left[\begin{array}{ccc}
\frac{f_{x}}{z^{c}} & 0 & -\frac{f_{x} x^{c}}{z^{c}}  \tag{15}\\
0 & \frac{f_{y}}{z^{c}} & -\frac{f_{y y^{c}}}{\left(z^{c}\right)^{2}}
\end{array}\right]
$$

The gradients for rotation quaternion $\mathbf{q}$ is as follow:

$$
\left.\begin{array}{ll}
\frac{\partial \mathbf{X}_{i}^{c}}{\partial q_{r}}=2\left[\begin{array}{ccc}
0 & -q_{k} y & q_{j} z \\
q_{k} x & 0 & -q_{i} z \\
-q_{j} x & q_{i} y & 0
\end{array}\right], & \frac{\partial \mathbf{X}_{i}^{c}}{\partial q_{i}}=2\left[\begin{array}{cc}
0 & q_{j} y
\end{array} q_{k} z\right. \\
q_{j} x & -2 q_{i} y  \tag{16}\\
-q_{k} x & q_{r} y \\
-2 q_{i} z
\end{array}\right], ~ \begin{array}{ccc}
-2 q_{j} x & q_{i} y & q_{r} z \\
\frac{\partial \mathbf{X}_{i}^{c}}{\partial q_{j}}=2\left[\begin{array}{ccc}
q_{i} x & 0 & q_{k} z \\
-q_{r} x & q_{k} y & -2 q_{j} z
\end{array}\right], & \frac{\partial \mathbf{X}_{i}^{c}}{\partial q_{k}}=2\left[\begin{array}{ccc}
-2 q_{k} x & -q_{r} y & q_{i} z \\
q_{r} x & -2 q_{k} y & q_{j} z \\
q_{i} x & q_{j} y & 0
\end{array}\right]
\end{array}
$$

Pose gradients back-propagation by $\frac{\partial \boldsymbol{\Sigma}^{\prime}}{\partial \mathbf{P}}$. We first derive the gradients for $\mathbf{E}=\mathbf{J} \mathbf{P}^{-1}=\left[e_{00}, e_{01}, e_{02} ; e_{10}, e_{11}, e_{12}\right]$, where $\mathbf{J}=\frac{\partial \mathbf{m}_{i}}{\partial \mathbf{X}^{c}}$ is the Jacobian of $\mathbf{m}_{i}$ w.r.t. $\mathbf{X}^{c}$ :

$$
\begin{equation*}
\frac{\partial \boldsymbol{\Sigma}^{\prime}}{\partial \mathbf{P}}=\frac{\partial\left(\mathbf{J P}^{-1} \boldsymbol{\Sigma} \mathbf{P}^{-T} \mathbf{J}^{T}\right)}{\partial \mathbf{P}} \tag{17}
\end{equation*}
$$

Then, we back-propagate the gradient to $\mathbf{E}$ :

$$
\begin{align*}
& \frac{\partial \operatorname{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{00}}=\left[\begin{array}{c}
2 e_{00} \Sigma_{00}+e_{01} \Sigma_{01}+e_{01} \Sigma_{10}+e_{02} \Sigma_{02}+e_{02} \Sigma_{20} \\
e_{10} \Sigma_{00}+e_{11} \Sigma_{01}+e_{12} \Sigma_{02} \\
e_{10} \Sigma_{00}+e_{11} \Sigma_{10}+e_{12} \Sigma_{20} \\
0
\end{array}\right] \\
& \frac{\partial \operatorname{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{01}}=\left[\begin{array}{c}
e_{00} \Sigma_{01}+e_{00} \Sigma_{10}+2 e_{01} \Sigma_{11}+e_{02} \Sigma_{12}+e_{02} \Sigma_{21} \\
e_{10} \Sigma_{10}+e_{11} \Sigma_{11}+e_{12} \Sigma_{12} \\
e_{10} \Sigma_{01}+e_{11} \Sigma_{11}+e_{12} \Sigma_{21} \\
0
\end{array}\right] \\
& \frac{\partial \mathrm{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{02}}=\left[\begin{array}{c}
e_{00} \Sigma_{02}+e_{00} \Sigma_{20}+e_{01} \Sigma_{12}+e_{01} \Sigma_{21}+2 e_{02} \Sigma_{22} \\
e_{10} \Sigma_{20}+e_{11} \Sigma_{21}+e_{12} \Sigma_{22} \\
e_{10} \Sigma_{02}+e_{11} \Sigma_{12}+e_{12} \Sigma_{22} \\
0
\end{array}\right] \\
& \frac{\partial \mathrm{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{10}}=\left[\begin{array}{c}
0 \\
e_{00} \Sigma_{00}+e_{01} \Sigma_{10}+e_{02} \Sigma_{20} \\
e_{00} \Sigma_{00}+e_{01} \Sigma_{01}+e_{02} \Sigma_{02} \\
2 e_{10} \Sigma_{00}+e_{11} \Sigma_{01}+e_{11} \Sigma_{10}+e_{12} \Sigma_{02}+e_{12} \Sigma_{20}
\end{array}\right]  \tag{18}\\
& \frac{\partial \mathrm{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{11}}=\left[\begin{array}{c}
0 \\
e_{00} \Sigma_{01}+e_{01} \Sigma_{11}+e_{02} \Sigma_{21} \\
e_{00} \Sigma_{10}+e_{01} \Sigma_{11}+e_{02} \Sigma_{12} \\
e_{10} \Sigma_{01}+e_{10} \Sigma_{10}+2 e_{11} \Sigma_{11}+e_{12} \Sigma_{12}+e_{12} \Sigma_{21}
\end{array}\right] \\
& \frac{\partial \operatorname{vec}\left(\boldsymbol{\Sigma}^{\prime}\right)}{\partial e_{12}}=\left[\begin{array}{c}
0 \\
e_{00} \Sigma_{02}+e_{01} \Sigma_{12}+e_{02} \Sigma_{22} \\
e_{00} \Sigma_{20}+e_{01} \Sigma_{21}+e_{02} \Sigma_{22} \\
e_{10} \Sigma_{02}+e_{10} \Sigma_{20}+e_{11} \Sigma_{12}+e_{11} \Sigma_{21}+2 e_{12} \Sigma_{22}
\end{array}\right]
\end{align*}
$$

In the mapping process, oversized 3D Gaussians are controlled through the delete, split, and clone process, so the magnitude of the covariance $\boldsymbol{\Sigma}$ is small enough. When back-propagate the gradients to pose $\mathbf{P}$, the intermediate term in Eq. (18) can be ignored.
Pose gradients back-propagation by depth supervision. Point-based depth alpha blending and color alpha blending share similarities; therefore, we implement the backpropagation of gradients for depth in the same manner for color:

$$
\begin{align*}
& \frac{\partial D}{\partial \alpha_{i}}=d_{i} \prod_{j=1}^{i-1}\left(1-\alpha_{j}\right)-\sum_{k=i+1}^{n} d_{k} \alpha_{k} \prod_{j=1, j \neq i}^{k-1}\left(1-\alpha_{j}\right), \\
& \frac{\partial D}{\partial d_{i}}=\alpha_{i} \prod_{j=1}^{i-1}\left(1-\alpha_{j}\right), \tag{19}
\end{align*}
$$

where $n$ is the number of the 3D Gaussian splats that affect the pixel in the rasterization.

## 2. Coarse-to-fine Pose Optimization Algorithm

Our coarse-to-fine pose optimization algorithms are summarized in Algorithm 1.

Our algorithm is designed for splatting-based pose estimation, which uses $\alpha$-blending on 3D Gaussians in strict


Figure 8. Visualization of the rasterized result before and after selecting reliable Gaussians. GS-SLAM coarse-to-fine strategy can effectively remove the unreliable 3D Gaussians to obtain more precise tracking results. In the enlarged figure, it can be seen that the abnormal optimized 3D Gaussians are removed. Note that the pixel without any 3D Gaussian will not affect the gradients of the pose. The background color in \#office 0 and \#office 3 is set to black, while in \#room 0 is white.
front-to-back order rather than the volume rendering technique used by current NeRF-Based SLAM [11, 27, 35, 41, 48, 53, 55].

Visualization of the unreliable area removed in the fine stage is shown in Fig. 8. In the \#Use all 3DGS column, we can see artifacts within the red bounding boxes resulting from improperly optimized positions in the past mapping process. These artifacts significantly impact the accuracy of pose estimation, as they introduce excessive optimization errors in the loss function. Our proposed reliable 3D Gaussians selection in coarse-to-fine strategy, as shown in the second column, filters the unreliable 3D Gaussians. The remaining background(black in \#Office 0, \#Office 3 and white in \#Room 0) on the image plane would be ignored while back-propagating gradients to pose. Details about tracking and mapping settings can be seen in Sec. 5 .

## 3. Additional Performance Comparison

Render performance on TUM-RGBD dataset. As shown in Fig. 11, we compare our method to current state-of-the-art NeRF-Based SLAM method CoSLAM [41], ESLAM [11], Point-SLAM [27] and ground truth image. We

```
Algorithm 1 Coarse-to-fine pose optimization
\(W, H\) : width and height of the input images
    \(\mathbf{P}^{(0)} \leftarrow \mathbf{P}_{t-1}, \mathbf{P}_{t-2} \quad \triangleright\) Init Pose
    \(i_{c}, i_{f} \leftarrow 0 \quad \triangleright\) Coarse and Fine Iteration Count
    for \(i_{c}<T_{c}\) do
        \(\hat{I}_{c} \leftarrow \operatorname{Rasterize}\left(\mathbf{G}, \mathbf{P}^{\left(i_{c}\right)}, \frac{1}{2} H, \frac{1}{2} W\right)\)
                        \(\triangleright\) Coarse Render
        \(\begin{array}{lr}L \leftarrow \operatorname{Loss}\left(I_{c}, \hat{I}_{c}\right) & \triangleright \operatorname{Loss} \\ \mathbf{P}^{\left(i_{c}+1\right)} \leftarrow \operatorname{Adam}(\nabla L) & \triangleright \text { Backprop \& Step }\end{array}\)
        \(i_{c} \leftarrow i_{c}+1\)
    end for
    \(\mathbf{G}_{\text {selected }} \leftarrow \operatorname{ReliableGS}\left(\mathbf{G}, \mathbf{P}^{\left(i_{c}+1\right)}, D, \varepsilon\right)\)
                                    \(\triangleright\) Select Reliable G
    for \(i_{f}<T_{f}\) do
    \(\hat{I}_{f} \leftarrow \operatorname{Rasterize}\left(\mathbf{G}_{\text {selected }}, \mathbf{P}^{\left(i_{c}+i_{f}\right)}, H, W\right)\)
                                \(\triangleright\) Fine Render
    \(L \leftarrow \operatorname{Loss}\left(I_{f}, \hat{I}_{f}\right) \quad \triangleright \operatorname{Loss}\)
    \(\mathbf{P}^{\left(i_{c}+i_{f}+1\right)} \leftarrow \operatorname{Adam}(\nabla L) \quad \triangleright\) Backprop \& Step
    \(i_{f} \leftarrow i_{f}+1\)
    end for
```

Table 9. Ablation study of tracking, mapping, and rendering performance on whole Replica dataset [31]. We present detailed ablation results on the entire Replica dataset to demonstrate the significant advantages of our proposed modules. Our method introduces a novel approach that combines coarse-to-fine pose estimation with an adaptive 3D Gaussian expansion strategy. This comprehensive methodology successfully increases the render, tracking, and mapping quality.

| Method | Metric | Room 0 | Room 1 | Room 2 | Office | 0 | Office | 1 | Office | 2 | Office | 3 | Office | Avg. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| w/o delete in mapping | ATE [cm] $\downarrow$ | 0.58 | 0.63 | 0.57 | 0.76 |  | 0.38 |  | 0.61 |  | 0.62 |  | 0.87 | 0.63 |
|  | Depth L1 [cm] $\downarrow$ | 1.68 | 1.17 | 1.92 | 1.30 |  | 1.46 |  | 1.82 |  | 1.79 |  | 1.83 | 1.62 |
|  | Precision [\%] $\uparrow$ | 53.55 | 68.76 | 50.58 | 67.03 |  | 77.52 |  | 59.45 |  | 53.37 |  | 49.03 | 59.91 |
|  | Recall [\%] $\uparrow$ | 49.32 | 61.88 | 45.57 | 61.60 |  | 65.67 |  | 50.15 |  | 46.09 |  | 42.80 | 52.89 |
|  | F1 [\%] $\uparrow$ | 51.35 | 65.14 | 47.94 | 64.20 |  | 71.10 |  | 54.41 |  | 49.46 |  | 45.70 | 56.16 |
|  | PSNR [dB] $\uparrow$ | 31.22 | 33.33 | 33.58 | 38.17 |  | 39.97 |  | 30.77 |  | 32.04 |  | 34.86 | 34.24 |
|  | SSIM $\uparrow$ | 0.967 | 0.975 | 0.977 | 0.984 |  | 0.990 |  | 0.974 |  | 0.969 |  | 0.980 | 0.977 |
|  | LPIPS $\downarrow$ | 0.094 | 0.075 | 0.086 | 0.053 |  | 0.046 |  | 0.096 |  | 0.100 |  | 0.080 | 0.079 |
| Coarse in tracking | ATE [cm] $\downarrow$ | 0.91 | 0.87 | 0.52 | 0.71 |  | 0.65 |  | 0.56 |  | 0.50 |  | 0.71 | 0.68 |
|  | Depth L1 [cm] $\downarrow$ | 1.48 | 0.94 | 1.47 | 0.84 |  | 0.97 |  | 1.52 |  | 1.58 |  | 1.28 | 1.26 |
|  | Precision [\%] $\uparrow$ | 59.68 | 70.51 | 62.66 | 83.11 |  | 87.79 |  | 66.85 |  | 61.34 |  | 66.55 | 69.81 |
|  | Recall [\%] $\uparrow$ | 57.54 | 64.98 | 57.58 | 76.36 |  | 74.58 |  | 58.25 |  | 54.07 |  | 59.01 | 62.80 |
|  | F1 \%] $\uparrow$ | 56.50 | 67.63 | 60.01 | 79.59 |  | 80.22 |  | 62.25 |  | 57.48 |  | 62.55 | 65.78 |
|  | PSNR [dB] $\uparrow$ | 29.13 | 32.08 | 33.12 | 38.62 |  | 40.69 |  | 32.02 |  | 32.02 |  | 35.05 | 34.09 |
|  | SSIM $\uparrow$ | 0.954 | 0.970 | 0.971 | 0.986 |  | 0.993 |  | 0.978 |  | 0.967 |  | 0.980 | 0.975 |
|  | LPIPS $\downarrow$ | 0.120 | 0.085 | 0.093 | 0.051 |  | 0.037 |  | 0.097 |  | 0.117 |  | 0.089 | 0.086 |
| Fine in tracking | ATE [cm] $\downarrow$ | 0.49 | 0.82 | 5.59 | 0.69 |  | 0.57 |  | 0.55 |  | 0.40 |  | 0.74 | 1.23 |
|  | Depth L1 [cm] $\downarrow$ | 1.39 | 0.91 | 5.84 | 0.87 |  | 1.26 |  | 1.49 |  | 1.55 |  | 1.27 | 1.82 |
|  | Precision [\%] $\uparrow$ | 62.61 | 73.71 | 16.45 | 81.63 |  | 72.86 |  | 69.08 |  | 61.88 |  | 67.05 | 63.16 |
|  | Recall [\%] $\uparrow$ | 59.18 | 67.68 | 15.53 | 75.53 |  | 64.77 |  | 59.73 |  | 54.40 |  | 59.45 | 57.03 |
|  | F1 [\%] $\uparrow$ | 61.29 | 70.57 | 15.98 | 78.46 |  | 68.57 |  | 64.06 |  | 57.90 |  | 63.02 | 59.98 |
|  | PSNR [dB] $\uparrow$ | 30.84 | 33.247 | 27.25 | 38.41 |  | 40.46 |  | 32.13 |  | 32.03 |  | 35.18 | 33.69 |
|  | SSIM $\uparrow$ | 0.964 | 0.975 | 0.901 | 0.985 |  | 0.992 |  | 0.978 |  | 0.966 |  | 0.980 | 0.968 |
|  | LPIPS $\downarrow$ | 0.096 | 0.076 | 0.188 | 0.052 |  | 0.037 |  | 0.095 |  | 0.119 |  | 0.089 | 0.094 |
| Our full | ATE [cm] $\downarrow$ | 0.48 | 0.53 | 0.33 | 0.52 |  | 0.41 |  | 0.59 |  | 0.46 |  | 0.70 | 0.50 |
|  | Depth L1 [cm] $\downarrow$ | 1.31 | 0.82 | 1.26 | 0.81 |  | 0.96 |  | 1.41 |  | 1.53 |  | 1.08 | 1.15 |
|  | Precision [\%] $\uparrow$ | 64.58 | 83.11 | 70.13 | 83.43 |  | 87.77 |  | 70.91 |  | 63.18 |  | 68.88 | 74.09 |
|  | Recall [\%] $\uparrow$ | 61.29 | 76.83 | 63.84 | 76.90 |  | 76.15 |  | 61.63 |  | 62.91 |  | 61.50 | 67.63 |
|  | F1 [\%] $\uparrow$ | 62.89 | 79.85 | 66.84 | 80.03 |  | 81.55 |  | 65.95 |  | 59.17 |  | 64.98 | 70.16 |
|  | PSNR [dB] $\uparrow$ | 31.56 | 32.86 | 32.59 | 38.70 |  | 41.17 |  | 32.36 |  | 32.03 |  | 35.23 | 34.56 |
|  | SSIM $\uparrow$ | 0.968 | 0.973 | 0.971 | 0.986 |  | 0.993 |  | 0.978 |  | 0.970 |  | 0.981 | 0.978 |
|  | LPIPS $\downarrow$ | 0.094 | 0.075 | 0.093 | 0.050 |  | 0.033 |  | 0.009 |  | 0.110 |  | 0.088 | 0.069 |

showcase the render quality of different methods using the final reconstructed environment model, presented in descending order from top to bottom. Our GS-SLAM provides the clearest results, particularly evident in the complex \#fr3_office scene, displaying a higher richness in detail information, indicating its superiority in handling details and edges.
Render performance on Replica dataset. As shown in Fig. 9, our GS-SLAM method performs superior in all tested scenarios. It delivers renderings with clear, welldefined edges and richly textured surfaces that closely align with the ground truth. This suggests that GS-SLAM not only captures the geometric detail with high precision but also accurately reconstructs the textural information of the scenes. The method's ability to render sharp images even in regions with complex textures and lighting conditions underscores its potential for accurate 3D environment mapping.

## 4. Additional Ablation Results

More detailed ablation experiments. In Tab. 9, we present our ablation study that demonstrates the effectiveness of our

Table 10. Ablation of the depth supervision on Replica \#Room0.

| Setting | \#Room0 |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ATE $\downarrow$ | Depth L1 $\downarrow$ | Precision $\uparrow$ | Recall $\uparrow$ | F1 $\uparrow$ | PSNR $\uparrow$ | SSIM $\uparrow$ | LPIPS $\downarrow$ |  |
| w/o Depth | 0.80 | 3.21 | 14.28 | 15.01 | 14.63 | 29.76 | 0.956 | 0.107 |  |
| w/ Depth | $\mathbf{0 . 4 8}$ | $\mathbf{1 . 3 1}$ | $\mathbf{6 4 . 5 8}$ | $\mathbf{6 1 . 2 9}$ | $\mathbf{6 2 . 8 9}$ | $\mathbf{3 1 . 5 6}$ | $\mathbf{0 . 9 6 8}$ | $\mathbf{0 . 0 9 4}$ |  |

proposed approach on the comprehensive Replica dataset. The experiment contrasts different module arrangements, including disabling our Gaussian delete method in mapping, using only coarse images in tracking, using fine images in tracking, and using our fully integrated method. The results distinctly highlight the superiority of our complete methodology, particularly evident in improved metrics across the board, from ATE to LPIPS. This confirms the benefits of our coarse-to-fine pose estimation and adaptive 3D Gaussian expansion strategy.
Effect of adaptive 3D Gaussian expansion strategy. Fig. 6 demonstrates the reconstructed mesh with and without our adaptive 3D Gaussian expansion strategy. The comparison is based on the Replica dataset Room0 subsequence. The left side displays a more coherent surface mesh due to our expansion strategy, while the right side lacks this delete strategy and results in less accuracy in reconstruction.


Figure 9. Additional render result comparison on Replica [31]. Our GS-SLAM can achieve more clear edges and better results in regions with rich texture than the previous SOTA methods.

Effect of depth supervision. Tab. 10 illustrates quantitative evaluation using depth supervision in mapping. In contrast to the original color-only supervision in [13], the depth supervision can significantly improve the tracking and mapping performance by providing accurate geometry constraints for the optimization. Our implementation with depth achieves better tracking ATE of 0.48, mapping precision of 64.58 , and rendering PSNR of 31.56 compared with the implementation without depth supervision.

## 5. Additional Implementation Details

Mapping hyper-parameters. The 3D Gaussian representation and pose are trained using Adam optimizer with initialized position learning rate $l r_{\mathbf{X}_{\text {init }}}=1.6 e^{-5}$, final position learning rate $l r_{\mathbf{X}_{\text {final }}}=1.7 e^{-7}$, max attenuation steps 100. Other Spherical Harmonics coefficients learning rate $l r_{\boldsymbol{Y}}$, opacity learning rate $l r_{\Lambda}$, scaling learning rate $l r_{\mathbf{S}}$ and rotation learning rate $l r_{\mathbf{R}}$ set to $5 e^{-4}, 1 e^{-2}, 2 e^{-4}, 4 e^{-5}$ respectively. In all experiments, we set the photometric loss weighting 0.8 , geometric loss weighting 0.3 , and keyframe window size $K=10$. In the mapping process, we densify the 3D Gaussians every 10 iterations before the first

70 iterations in a total of 100 iterations. And the scale and grad threshold for clone or split is set to 0.02 m and 0.002 . For the stability of the optimization, first-order coefficients of spherical harmonics coefficients are only optimized in bundle adjustment. Note that we only optimize the camera pose in the latter half of the iterations due to the adverse impact of improper 3D Gaussians on optimization. Despite this, there are still negative optimizations for camera poses at some point. In addition, in all TUM-RGBD sequences and Replica Office subsequence, we set the background color to black, while in other Room subsequence, we set the background to white. In the Replica dataset, we use 10 iterations for tracking and 100 iterations for mapping with max keyframe interval $\mu_{k}=30$, while in the challenging TUM RGB-D dataset, we use 30 iterations for tracking, with max keyframe interval $\mu_{k}=5$.

Mapping mesh comparison method. We follow PointSLAM and use TSDF-Fusion [4] to generate mesh from predicted pose and depth. We also evaluate map rendering quality in Sec. 4.3. That's because there is no direct way to get surface or mesh in 3DGS-based SLAM, as they do not represent scenes with density fields and can not directly
generate mesh via marching cube. GS-SLAM achieves comparable map reconstruction results, better tracking accuracy, and higher FPS than Point-SLAM. Despite this, we explored generating mesh from 3DGS centers and Gaussian marching cube [36] in Fig. 10, but the results are not satisfactory.


Figure 10. Generate mesh from 3DGS with different methods.
Tracking hyper-parameters. The pose is trained using FusedAdam optimizer with learning rate $l r_{\mathbf{t}}=2 e^{-4}, l r_{\mathbf{q}}=$ $5 e^{-4}$, and photometric loss weighting 0.8 , in the first five iterations we do the coarse pose estimation, while in the later iterations use the reliable 3D Gaussians to do the fine pose estimation. In addition, to exclude the pixel without proper color optimization. If the loss on the pixel is more than ten times the median loss, the pixel will be ignored.


Figure 11. Additional render result comparison on TUM-RGBD [8]. Thanks to fast back-propagation of splatting in optimized 3D Gaussians, our GS-SLAM can reconstruct dense environment maps with richness and intricate details.

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