# FRAME: Floor-aligned Representation for Avatar Motion from Egocentric Video

Supplementary Material

#### **A. Model Details**

#### A.1. Camera Model

In this project we use the camera model introduced by Kannala et Al. [3]. In the following paragraph, we summarize its main characteristics and describe how we employed it in this project.

For a normalized undistorted pixel (u, v), let  $\theta$  represent the angle between the incoming ray and the optical axis, and r the radial distance in the image plane. By definition, in the pinhole model the following relation holds  $r = \tan(\theta)$ .

The distorted radial coordinate is given by:

$$r_d = \theta \cdot (1 + k_1 \theta^2 + k_2 \theta^4 + k_3 \theta^6 + k_4 \theta^8), \quad (1)$$

where  $k_1, k_2, k_3, k_4$  are specific to each the lens.

The relationship between distorted and undistorted coordinates is given by

$$u = \left(\frac{r}{r_d}\right) u_d, \quad v = \left(\frac{r}{r_d}\right) v_d$$
 (2)

where the d suffix stands for the distorted quantity.

#### A.1.1. Unprojection

We call unprojection the process of obtaining the 3D coordinates given a 2D pixel and its distance from the camera. To unproject a point, it is necessary to undistort it and subsequently obtain its 3D coordinates via the standard pinhole model. To undistort pixels we need to solve Equation 1 for  $\theta$ . Since it contains higher-order terms in  $\theta$ , direct inversion is intractable. Therefore, we follow OpenCV [1] in using a fixed point algorithm, starting with  $\theta_0 = r_d$  and iterating  $\theta_{n+1} = f(\theta_n)$ . In practice, we empirically observe that 5 steps are enough to find an accurate solution.

Once  $\theta$  converges, it's possible to compute  $r = \tan(\theta)$ and obtain the undistorted pixel coordinates. Given the undistorted pixels and their associated depth, we can obtain their 3D coordinates directly by inverting the pinhole model equation.

$$x' = \frac{u - c_x}{f_x}, \quad y' = \frac{v - c_y}{f_y}$$
 (3)

Where f is the focal length and c the coordinates of the optical axis intersection with the image plane The 3D coordinates (X, Y, Z) are then obtained by scaling the normalized coordinates by the corresponding depth value d at each pixel:

$$X = d \cdot x', \quad Y = d \cdot y', \quad Z = d \tag{4}$$

#### A.2. SoftArgmax

In order to obtain the  $u_k, v_k$  pixel coordinates of each joint k and their depth  $d_k$  we define the weight matrices  $\mathbf{Q}^x, \mathbf{Q}^y$  as

$$Q_{ij}^x = \frac{j}{W-1} \quad Q_{ij}^y = \frac{i}{H-1}$$
 (5)

This allows us to perform a *soft-argmax* operation [4] to obtain the normalized 2D coordinates in a differentiable way.

$$u_{k} = \sum_{i,j} (\mathbf{Q}^{x} \otimes \hat{\mathbf{H}}_{k})_{ij},$$
  
$$v_{k} = \sum_{i,j} (\mathbf{Q}^{y} \otimes \hat{\mathbf{H}}_{k})_{ij},$$
  
(6)

Where  $\otimes$  denotes the Hadamard product

#### **B.** Metrics

**PA-MPJPE** We adopt the definition established in prior work [2]. PA-MPJPE quantifies the similarity between predicted and ground-truth 3D poses by computing the mean per-joint Euclidean distance after Procrustes alignment. This alignment removes pelvis translation and applies a similarity transform (rotation, translation, and scale) to minimize the discrepancy between poses.

**3D-PCK** 3D-PCK quantifies the percentage of predicted 3D keypoints within 10 cm of the ground-truth. For each joint, the Euclidean distance is calculated, and predictions below the threshold are deemed correct.

**Jitter** Jitter quantifies temporal smoothness by comparing frame-to-frame changes in predicted and ground-truth 3D joint positions. Although there are multiple ways to quantify it, we follow Physcap [6] and compute:

$$\frac{1}{N \cdot J} \sum_{n=1}^{N} \sum_{j=1}^{J} \left| \| \mathbf{v}_{n, \text{pred}}^{j} \| - \| \mathbf{v}_{n, \text{gt}}^{j} \| \right|$$

where N is the number of sequences, J is the number of joints,  $\mathbf{v}_{n,\text{pred}}$  and  $\mathbf{v}_{n,\text{gt}}$  are the predicted and ground-truth joint velocity at frame n for joint j, respectively.

**Non-penetration Percentage** This metric measures the fraction of all poses where all predicted 3D joints remain above the ground plane (y > 0)

**Mean Penetration Error** (MPE) MPE measures the average penetration depth of joints below the ground plane  $(y \le 0)$ .

**Foot Sliding Velocity** This metric evaluates foot velocity discrepancies between prediction and ground truth when feet are in contact with the ground. The sliding velocity error is computed as:

$$\frac{1}{N_c} \sum_{n=1}^{N_c} \sum_{j=1}^{4} \|(\mathbf{v}_{n,\text{pred}}^j - \mathbf{v}_{n,\text{gt}}^j) \cdot \mathbf{1}_{\text{xz}}\| \quad \text{if joint } j \text{ is in contact}$$

where  $N_c$  is the number of contact frames, 4 is the number of feet joints, and  $\mathbf{1}_{xz}$  is a vector that projects the velocity onto the xz-plane.

# **C. Data Collection**

## C.1. Recording Rig

The recording rig is built on the Meta Quest 3 [5], chosen for its lightweight design and comfort, allowing for prolonged use. The Quest 3 includes an RGB outward-facing camera with high-quality passthrough capabilities, enabling users to interact naturally with their surroundings. The headset computes on-device 6D head pose data, streamed continuously via HTTP from the Quest 3 to a Raspberry Pi worn by the user, with a custom-built Unity [7] application handling data transmission.

**Egocentric Video Synchronization** The fisheye cameras mounted on the VR headset record at 30Hz as the studio camera array, but their clocks are not hardware synchronized. To address this, we use a simple visual cue: toggling the studio lights on and off at the beginning and end of each session. This provides a temporal reference, allowing us to align the fisheye camera frames with the studio's frame of reference. Manual intra-frame adjustments are applied to account for any residual offsets or rolling shutter artifacts, ensuring tight alignment across all frames.

### References

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