

001 A. Training Details

002 The training process consists of two main stages: geometric
003 prompt learning and adapter fine-tuning.

004 A.1 Geometry Prompt Learning

005 For geometry prompt learning (Stage I), we first construct
006 multi-geometric graph structures using k-nearest neighbors
007 (k=10) in three complementary spaces: Euclidean, Hyper-
008 bolic (k=-1), and Spherical (k=1). The input features of
009 dimension 1024 are processed through geometric encoders
010 with a hidden dimension of 512, eventually producing 256-
011 dimensional geometric embeddings for each space. During
012 training, we employ the AdamW optimizer with an initial
013 learning rate of 1e-3 and weight decay of 1e-5. A step-wise
014 learning rate scheduler is applied with step size 100 and de-
015 cay factor 0.5. To ensure efficient training, we use a batch
016 size of 1024 and train for 100 epochs.

017 A.2 Adapter Fine-tuning

018 For adapter fine-tuning (Stage II), we build upon Qwen2-
019 VL-2B as our base model. The geometry adapter is inte-
020 grated every four transformer layers, consisting of three
021 types of feed-forward networks: a standard Euclidean FFN
022 inherited from the pre-trained weights, a Hyperbolic FFN
023 based on the Lorentz model with learnable scale, and a
024 Spherical FFN utilizing von Mises-Fisher distribution with
025 learnable concentration. These experts are orchestrated
026 through a gating mechanism with temperature $\tau = 0.1$. We
027 utilize LoRA for efficient fine-tuning, with rank 16, alpha
028 32, and dropout 0.1. The training process employs mixed-
029 precision (bf16) and runs with a batch size of 16 per GPU
030 for 3 epochs. We use the AdamW optimizer with a learning
031 rate of 2e-5 and weight decay of 0.01, incorporating 500
032 warmup steps. The maximum sequence length is set to 512
033 tokens.

034 A.3 Data Pre-processing

035 For data processing, images are resized to 144×144 pix-
036 els and normalized to [0,1] range. Spectral data is en-
037 coded into 1024-dimensional features and L2 normalized.
038 These features are then projected into different geomet-
039 ric spaces through manifold-specific mappings, resulting in
040 256-dimensional representations in each space.

041 B. Riemannina Geometry

042 A smooth manifold M is referred to as a Riemannian man-
043 ifold when it possesses a Riemannian metric g . Curva-
044 ture c is an important measure of the degree of geodesic
045 bending. For each point $x \in M$, there exists a tangent
046 space $T_x M \subseteq \mathbb{R}^d$ that surrounds x , where the metric g
047 is applied to determine the manifold’s shape. The rela-
048 tionship between the tangent space and the manifold is es-

049 tablished through the use of exponential and logarithmic
050 maps. In particular, the exponential map at point x , rep-
051 resented as $\exp_x^c(\cdot) : T_x M \rightarrow M$, transforms points from
052 the tangent space into the manifold, while the logarithmic
053 map function is the inverse function of exponential map
054 $\log_x^c(\cdot) = (\exp_x^c(\cdot))^{-1}$.

055 In this paper, we use three geometric spaces of different
056 curvature to form a Riemannian expert: Euclidean space
057 ($c = 0$), hyperbolic space ($c < 0$), and spherical space
058 ($c > 0$).

059 B.1 Euclidean space

060 Euclidean space is based on Euclidean coordinates. Since
061 the curvature is zero, the geodesic remains parallel. Eu-
062 clidean space can be used to describe a flat universe very
063 well. Each galaxy is influenced by its neighbors, capturing
064 the local structure of galaxies in the universe. The exponen-
065 tial mapping of Euclidean Spaces is defined as:

$$066 \exp_{x_p}^c(x) = \mathbf{x}_p + \mathbf{x}. \quad (1)$$

067 B.2 Hyperbolic space

068 A hyperbolic space is defined as
069 $\mathbb{H}_c^d = \{\mathbf{x}_p \in \mathbb{R}^{d+1} : \langle \mathbf{x}_p, \mathbf{x}_p \rangle_{\mathcal{L}} = 1/c\}$, where d repre-
070 sents the dimension and the inner product is defined as
071 $\langle \mathbf{x}, \mathbf{y} \rangle_{\mathcal{L}} = -x_1 y_1 + \sum_{j=2}^d x_j y_j$. In a hyperbolic space,
072 The geodesic distance between the two points is:

$$073 d(x, y) = \frac{1}{\sqrt{-c}} \operatorname{arccosh}(c * \langle \mathbf{x}, \mathbf{y} \rangle_{\mathcal{L}}). \quad (2)$$

074 Since the curvature is negative, the geodesic will diverge.
075 This helps to describe the evolution of galaxies in a uni-
076 verse, and thus reflects the internal hierarchy of galaxies.
077 Its exponential map is defined as:

$$078 \exp_{x_p}^c(x) = \cosh(\sqrt{-c} \|\mathbf{x}\|) \mathbf{x}_p + \sinh(\sqrt{-c} \|\mathbf{x}\|) \frac{\mathbf{x}}{\sqrt{-c} \|\mathbf{x}\|}. \quad (3)$$

079 B.3 Sphere space

080 Spherical space is defined as $\mathbb{S}_c^d = \{\mathbf{x}_p \in \mathbb{R}^{d+1} : \langle \mathbf{x}_p, \mathbf{x}_p \rangle_{\mathbb{S}} = 1/c\}$, where the inner product is the stan-
081 dard Euclidean inner product $\langle \mathbf{x}, \mathbf{y} \rangle_{\mathbb{S}} = \sum_{j=1}^{d+1} x_j y_j$. The
082 geodesic distance between the two points is:
083

$$084 d(x, y) = \frac{1}{\sqrt{c}} \arccos(c \langle \mathbf{x}, \mathbf{y} \rangle_{\mathbb{S}}). \quad (4)$$

085 Geodesics in spherical space are convergent. Therefore,
086 it can reflect the global information of the galaxy. Capture
087 the overall star map content. Its exponential map is defined
088 as

$$089 \exp_{x_p}^c(x) = \cosh(\sqrt{c} \|\mathbf{x}\|) \mathbf{x}_p + \sinh(\sqrt{c} \|\mathbf{x}\|) \frac{\mathbf{x}}{\sqrt{c} \|\mathbf{x}\|}. \quad (5)$$

090	C. Special Tokens and Templates	
091	C.1 Special Modality Tokens	
092	To effectively integrate multi-modal features into the input	
093	sequence, we carefully selected special tokens with rela-	
094	tively low frequency in the pre-trained vocabulary to repre-	
095	sent different modalities. Specifically, we use token “ \tilde{A} ” for	
096	spectral features, “ φ ” for Euclidean geometric structure, “ \emptyset ”	
097	for spherical geometric structure, and “ α ” for hyperbolic	
098	geometric structure. During forward propagation, these to-	
099	kens’ embeddings are dynamically replaced with their cor-	
100	responding modal embeddings after geometry-specific pro-	
101	jection and normalization. This design allows the model to	
102	seamlessly incorporate multi-geometric and spectral infor-	
103	mation while maintaining the pre-trained model’s linguistic	
104	capabilities.	
105	C.2 Task-specific Templates	
106	In this section, we present the task-specific templates for	
107	two main categories of tasks: galaxy property estimation	
108	and galaxy morphology classification. For each task, we	
109	utilize special modality tokens introduced in Section to	
110	incorporate different modalities. The key modalities in-	
111	clude Image, Spectral (where available), and Geometry in-	
112	formation. To better leverage knowledge from pre-trained	
113	models, we customize the descriptions of special modal-	
114	ity tokens according to each task’s characteristics, enabling	
115	Galaxy Walker to align multi-modal representations better.	
116	C.2.1 Galaxy Property Estimation	
117	Galaxy property estimation encompasses four regression	
118	tasks:	
119	• Stellar Mass (M^*) Prediction: For numerical regression	
120	of the total mass of stars in a galaxy.	
121	• Mass-Weighted Stellar Metallicity (Z_{MW}) Prediction:	
122	For estimating the abundance of heavy elements in stars.	
123	• Mass-Weighted Galaxy Age (t_{age}) Prediction: For de-	
124	terminating the mass-weighted average age of stars (in	
125	Gyr).	
126	• Specific Star-Formation Rate (sSFR) Prediction: For	
127	calculating the rate of star formation per unit stellar mass.	
128	For these prediction tasks, we employ a numerical head	
129	for regression. In the templates, we use the “num” token	
130	to represent all numerical values as the model’s target re-	
131	sponse.	
132	C.2.2 Galaxy Morphology Classification	
133	Galaxy morphology classification includes ten distinct clas-	
134	sification tasks:	
135	1. Smooth (SMH)	
136	2. Disk-Edge-On (DEO)	
137	3. Spiral-Arms (SPR)	
	4. Bar (BAR)	138
	5. Bulge-Size (BLG)	139
	6. How-Rounded (RND)	140
	7. Edge-On-Bulge (EOB)	141
	8. Spiral-Winding (SWP)	142
	9. Spiral-Arm-Count (SAC)	143
	10. Merging (MRG)	144
	For classification tasks, we structure the templates as	145
	multiple-choice questions, with the model required to select	146
	from options labeled (a), (b), (c), etc. The specific options	147
	for each classification task are presented in Table 1.	148
	D. Additional Experiments	149
	D.1 The Impact of Prompt	150
	To investigate whether our designed prompts can effectively	151
	leverage knowledge from pre-trained models to improve	152
	performance, we conduct experiments comparing three dif-	153
	ferent prompt settings:	154
	• Concat: Directly concatenating modality tokens (Image	155
	Token, Spectral Token, Geometry Token) with the ques-	156
	tion text without any connecting words or explanations.	157
	• Simple Prompt: Adding basic connecting words to de-	158
	scribe what each modality token represents, building	159
	upon the Concat setting.	160
	• Prompt with Knowledge Background: Using our care-	161
	fully designed templates from Section , which incorporate	162
	detailed explanations of how each modality token con-	163
	tributes to the specific task, combined with relevant do-	164
	main knowledge.	165
	As shown in Figure 15, the Prompt with Knowledge	166
	Background setting consistently outperforms the other two	167
	approaches. In property estimation tasks, this setting	168
	achieves notably better results across all metrics, with par-	169
	ticular improvements in sSFR prediction. For morphology	170
	classification tasks, while all three settings perform com-	171
	petitively, the Knowledge Background prompts still demon-	172
	strate advantages, especially in complex features such as	173
	Bar and Spiral Arm Count classification. These results	174
	suggest that carefully designed prompts incorporating do-	175
	main knowledge can effectively help the model leverage	176
	pre-trained knowledge for better task performance.	177
	D.2 Parameter-Efficient Training Strategy Analysis	178
	We evaluate three different training strategies to investigate	179
	the effectiveness of our parameter-efficient approach:	180
	• Geometry Adapter Only: Training only the newly added	181
	components including projection π_θ , Geometry Adapter,	182
	and Num Head weights.	183

Table 1. Options for Galaxy Morphology Classification Tasks

Task	Options
Smooth	(a) Smooth (b) Featured or Disk (c) Artifact
Disk-Edge-On	(a) Yes (b) No
Spiral-Arms	(a) Yes (b) No
Bar	(a) Strong Bar (b) Weak Bar (c) No Bar
Bulge-Size	(a) Dominant (b) Large (c) Moderate (d) Small (e) None
How-Rounded	(a) Round (b) In-Between (c) Cigar-Shaped
Edge-On-Bulge	(a) Boxy (b) None (c) Rounded
Spiral-Winding	(a) Tight (b) Medium (c) Loose
Spiral-Arm-Count	(a) 1 (b) 2 (c) 3 (d) 4 (e) More than 4 (f) Can't Tell
Merging	(a) None (b) Minor Disturbance (c) Major Disturbance (d) Merger

Galaxy Walker: Stellar Mass Estimation

User: Stellar mass refers to the total mass of all the stars in a galaxy. It is a critical parameter for understanding galaxy formation and evolution and can be analyzed through multiple perspectives. Specifically, the **[Image token]** utilizes celestial image data to assess morphology and luminosity, which helps in the initial estimation of stellar mass. The **[Spectral token]** analyzes stellar spectral characteristics, such as absorption line width and radiation intensity, to directly infer mass parameters. The **[Euclidean token]** provides the object's position in flat space, aiding in the mass calculation by considering distance measurements. The **[Hyperbolic token]** describes the geometrical properties in negatively curved space, modeling more complex cosmic structures and helping to understand the distribution of massive stars in a negatively curved universe. The **[Sphere token]** uses spherical geometry in positively curved space to evaluate an object's position in the spherical coordinate system, leading to a more accurate mass estimation.

Assistant: NUM

Figure 1. Prompt template for stellar mass estimation.

- 184 • **Geometry Adapter + LoRA:** Training the Geometry
185 Adapter components plus LoRA modules in attention and
186 linear layers.
- 187 • **Full-Parameter Training:** Fine-tuning all model param-
188 eters.

189 As shown in Table 3, our Geometry Adapter + LoRA
190 strategy achieves comparable or even superior performance
191 to full-parameter training across most metrics. Notably,
192 it outperforms full-parameter training in property estima-
193 tion tasks, achieving better R^2 scores for all four prop-
194 erties (M_* , Z_{MW} , t_{age} , $sSFR$). For morphology clas-
195 sification, the performance difference is minimal, with
196 our parameter-efficient approach showing slight advantages
197 in several categories (DEO, SPR, BAR). The Geometry
198 Adapter Only setting, while using the fewest trainable pa-
199 rameters, still maintains strong performance, suggesting
200 that the geometric adaptation components effectively cap-
201 ture domain-specific features. These results demonstrate
202 that our parameter-efficient strategy can match or exceed
203 the performance of full-parameter training while signifi-
204 cantly reducing the number of trainable parameters and
205 computational cost.

Hardware	Inference Time (s)
NVIDIA H100	0.38
NVIDIA A100	1.14
Ascend 910B	1.52

Table 2. **Inference time comparison across different hardware platforms.** Times are averaged over 100 runs with batch size 1. Ascend 910B results are measured using FP16 precision, while NVIDIA results use BF16 precision.

D.3 Inference Time Analysis

To evaluate the practical deployment potential of Galaxy-
Walker, we conduct inference time benchmarks across dif-
ferent hardware platforms. We measure the average infer-
ence time per sample using batch size 1, with BF16 pre-
cision on NVIDIA GPUs and FP16 precision on Ascend
hardware.

The results demonstrate that GalaxyWalker achieves
practical inference speeds across all tested platforms. The
NVIDIA H100 shows superior performance with an average
inference time of 0.38 seconds per sample, while the A100
and Ascend 910B maintain reasonable inference speeds at

Galaxy Walker: Mass-Weighted Stellar Metallicity Estimation

User: Mass-weighted stellar metallicity measures the abundance of elements heavier than hydrogen and helium in a galaxy's stars, weighted by their mass. This aids in understanding the galaxy's chemical evolution and can be analyzed through multiple perspectives. Specifically, the **[Image token]** helps observe the color and brightness variations of celestial objects, providing initial metallicity estimates. The **[Spectral token]** offers a detailed analysis of spectral lines, such as the strength and shift of metal lines, to directly infer the mass-weighted metallicity. The **[Euclidean token]** provides precise coordinates in flat space, aiding in the calculation of metallicity distribution within stars by using distance information. The **[Hyperbolic token]** describes the geometrical properties in negatively curved space, modeling complex star cluster structures and giving geometrical background support for metallicity distribution. The **[Sphere token]** employs spherical geometry in positively curved space to understand the distribution of celestial objects within the spherical coordinate system, leading to comprehensive metallicity estimation.

Assistant: NUM

Figure 2. Prompt template for mass-weighted stellar metallicity estimation.

Galaxy Walker: Mass-Weighted Galaxy Age Estimation

User: Mass-weighted galaxy age refers to the average age of stars within a galaxy, weighted by their mass, providing insights into the galaxy's formation history. This can be analyzed through multiple perspectives. Specifically, the **[Image token]** assesses morphology and color via celestial images to estimate the age distribution of stellar populations in the galaxy. The **[Spectral token]** primarily uses spectral analysis, such as examining the spectral energy distribution and absorption line changes, to determine the overall age of the galaxy. The **[Euclidean token]** provides the galaxy's coordinates in flat space, assisting in refining age estimation based on distance and position. The **[Hyperbolic token]** describes complex geometrical backgrounds in negatively curved space, aiding in the detailed understanding of mass-weighted age composition. The **[Sphere token]** utilizes positively curved space in spherical geometry to assist in distribution analysis and age estimation of different regions within the galaxy.

Assistant: NUM

Figure 3. Prompt template for mass-weighted galaxy age estimation.

218 1.14 and 1.52 seconds respectively. These results suggest
219 that GalaxyWalker is suitable for real-world applications
220 across various hardware configurations.

Galaxy Walker: Specific Star-Formation Rate Estimation

User: The specific star-formation rate (sSFR) is the rate of star formation per unit stellar mass in a galaxy, indicating how actively the galaxy is forming stars relative to its existing stellar mass. It can be analyzed through multiple perspectives. Specifically, the **[Image token]** helps analyze star-forming regions, morphology, and density variations via celestial images for initial estimation of the star-formation rate. The **[Spectral token]** provides detailed spectral analysis, especially the intensity and distribution of emission lines, to measure the current star-formation rate. The **[Euclidean token]** offers precise positioning in flat space, aiding in inferring the star-formation rate based on distance and velocity information. The **[Hyperbolic token]** describes geometrical properties in negatively curved space, modeling complex cosmic environments and star cluster structures for supporting star-formation rate estimation. The **[Sphere token]** utilizes positively curved space in spherical geometry to understand the distribution of star formation within the spherical coordinate system, assisting in specific rate determination.

Assistant: NUM

Figure 4. Prompt template for specific star-formation rate estimation.

Galaxy Walker: Galaxy Smoothness Classification

User: The morphological class of a galaxy can be analyzed using multiple tokens: the morphological classification of galaxies, such as spiral, elliptical, or irregular, can be directly observed by analyzing their images. Specifically, the **[Image token]** utilizes celestial images to assess the galaxy's overall shape and structural features, helping to classify it as smooth, featured, or an artifact. The **[Euclidean token]** offers the galaxy's precise coordinates in flat space, allowing for spatial analysis and comparison with known morphological classes. The **[Hyperbolic token]** provides insights into negative curvature space, aiding in the understanding of complex structures that might influence the galaxy's morphology. The **[Sphere token]** uses spherical geometry to interpret the galaxy's appearance in positively curved space, helping to refine its classification. **Please choose from these options: (a) Smooth (b) Featured or Disk (c) Artifact.**

Assistant:

[The choice of true label]

Figure 5. Prompt template for galaxy smoothness classification.

Galaxy Walker: Disk-Edge-On Classification

Prompt: Determining if a galaxy is disk-edge-on can be analyzed using multiple tokens: edge-on disk galaxies are characterized by their flat, edge-like appearance when observed. This can be directly identified from images. Specifically, the **[Image token]** offers visual information on the galaxy's edge-on appearance, which is indicative of a disk-edge-on orientation. The **[Euclidean token]** gives the galaxy's precise coordinates in flat space, assisting in spatial orientation analysis. The **[Hyperbolic token]** models the galaxy's structure in a negatively curved space, helping to understand any distortions that confirm its disk-edge-on nature. The **[Sphere token]** uses spherical geometry to analyze the galaxy's orientation in positively curved space. **Please choose from these options: (a) Yes, it is a disk-edge-on galaxy (b) No, it is not a disk-edge-on galaxy.**

Assistant: [The choice of true label]

Figure 6. Prompt template for disk-edge-on classification.

Galaxy Walker: Spiral Arms Classification

Prompt: Determining if a galaxy has spiral arms can be analyzed using multiple tokens: spiral-arm galaxies typically exhibit distinct spiral patterns in images. Specifically, the **[Image token]** provides visual information to identify the presence and patterns of spiral arms. The **[Euclidean token]** provides the galaxy's coordinates in flat space, aiding in spatial relationship analysis of spiral structures. The **[Hyperbolic token]** models the galaxy in a negatively curved space, providing geometric context for the spiral arms' formation. The **[Sphere token]** uses spherical geometry to interpret the distribution and winding of spiral arms in positively curved space. **Please choose from these options: (a) Yes, it is a spiral-arms galaxy (b) No, it is not a spiral-arms galaxy.**

Assistant: [The choice of true label]

Figure 7. Prompt template for spiral arms classification.

Galaxy Walker: Bar Type Classification

Prompt: Determining the type of bar in a galaxy can be analyzed using multiple tokens: bar structures in galaxies can be directly observed through images, revealing their length and strength. Specifically, the **[Image token]** offers visual information to observe and classify the bar's strength in the galaxy. The **[Euclidean token]** gives the galaxy's position in flat space, assisting in the spatial analysis of the bar. The **[Hyperbolic token]** helps model the galaxy's structure in negatively curved space, which aids in understanding the bar type. The **[Sphere token]** uses spherical geometry to analyze the distribution of stellar masses in the bar, refining its classification. **Please choose from these options: (a) Strong Bar (b) Weak Bar (c) No Bar.**

Assistant: [The choice of true label]

Figure 8. Prompt template for bar type classification.

Galaxy Walker: Bulge Size Classification

Prompt: Determining the bulge size of a galaxy can be analyzed using multiple tokens: the size of a galaxy's bulge can be observed in images by its prominence. Specifically, the **[Image token]** provides visual information to assess the bulge's prominence in the galaxy. The **[Euclidean token]** offers the galaxy's coordinates in flat space, assisting in spatial analysis of the bulge's physical size. The **[Hyperbolic token]** models the galaxy in negatively curved space, which helps in understanding the bulge size in a broader context. The **[Sphere token]** uses spherical geometry to analyze the distribution and density of stars within the bulge. **Please choose from these options:(a) Dominant Bulge (b) Large Bulge (c) Moderate Bulge (d) Small Bulge (e) No Bulge.**

Assistant: [The choice of true label]

Figure 9. Prompt template for bulge size classification.

Galaxy Walker: Galaxy Roundness Classification

Prompt: Determining the shape of a galaxy can be analyzed using multiple tokens: the shape of a galaxy can be directly observed by analyzing its images. Specifically, the **[Image token]** provides visual information to classify the galaxy as round, in-between, or cigar-shaped. The **[Euclidean token]** gives the galaxy's precise coordinates in flat space, aiding in the geometric analysis of its shape. The **[Hyperbolic token]** models the galaxy's structure in negatively curved space, providing a complex geometric context for its shape classification. The **[Sphere token]** uses spherical geometry to analyze the galaxy's three-dimensional shape in positively curved space. **Please choose from these options: (a) Round (b) In-Between (c) Cigar-Shaped.**

Assistant: [The choice of true label]

Figure 10. Prompt template for galaxy roundness classification.

Galaxy Walker: Edge-On Bulge Classification

Prompt: Determining the type of bulge in an edge-on galaxy can be analyzed using multiple tokens: the type of bulge in an edge-on galaxy can be identified by observing its images, which show whether it is boxy or rounded. Specifically, the **[Image token]** gives visual information to identify and classify the bulge as boxy, rounded, or absent in an edge-on galaxy. The **[Euclidean token]** offers the galaxy's coordinates in flat space, assisting in the spatial analysis of the bulge. The **[Hyperbolic token]** models the galaxy in negatively curved space, helping to understand the bulge type in a broader geometrical context. The **[Sphere token]** uses spherical geometry to analyze the three-dimensional distribution of stars within the bulge. **Please choose from these options:(a) Boxy Bulge (b) No Bulge (c) Rounded Bulge.**

Assistant: [The choice of true label]

Figure 11. Prompt template for edge-on bulge classification.

Galaxy Walker: Spiral Winding Classification

Prompt: Analyzing how tightly wound the spiral arms of a galaxy are can be done using multiple tokens: the tightness of spiral arms can be directly observed in images, showing the winding patterns clearly. Specifically, the **[Image token]** provides visual information to determine the tightness of the spiral arms. The **[Euclidean token]** gives the galaxy’s precise coordinates in flat space, aiding in the spatial analysis of spiral arm winding. The **[Hyperbolic token]** models the galaxy’s structure in negatively curved space, helping to understand the geometric properties affecting spiral arm tightness. The **[Sphere token]** uses spherical geometry to analyze the three-dimensional winding of the spiral arms. **Please choose from these options:(a) Tight Winding (b) Medium Winding (c) Loose Winding.**

Assistant: [The choice of true label]

Figure 12. Prompt template for spiral winding classification.

Galaxy Walker: Spiral Arm Count Classification

Prompt: Determining the number of spiral arms in a galaxy can be analyzed using multiple tokens: the number of spiral arms in a galaxy can be directly counted from images. Specifically, the **[Image token]** provides visual information to count and identify the number of spiral arms. The **[Euclidean token]** gives the galaxy’s precise coordinates in flat space, aiding in the spatial analysis of the spiral arms. The **[Hyperbolic token]** models the galaxy’s structure in negatively curved space, providing a geometric context for the number of spiral arms. The **[Sphere token]** uses spherical geometry to analyze the three-dimensional distribution of spiral arms.

Please choose from these options:(a) 1 Spiral Arm (b) 2 Spiral Arms (c) 3 Spiral Arms (d) 4 Spiral Arms (e) More than 4 Spiral Arms (f) Can’t Tell.

Assistant: [The choice of true label]

Figure 13. Prompt template for spiral arm count classification.

Galaxy Walker: Galaxy Merging State Classification

Prompt: Determining the merging state of a galaxy can be analyzed using multiple tokens: the merging state of a galaxy can be observed through signs of disturbance or merging in images. Specifically, the **[Image token]** provides visual information to observe signs of merging or disturbances. The **[Euclidean token]** offers the galaxy’s coordinates in flat space, aiding in assessing merging stages from spatial data. The **[Hyperbolic token]** models the galaxy in negatively curved space, helping to understand the geometric properties affecting the merging state. The **[Sphere token]** uses spherical geometry to analyze the three-dimensional interactions of merging galaxies. **Please choose from these options: (a) No Merging (b) Minor Disturbance (c) Major Disturbance (d) Merger.**

Assistant: [The choice of true label]

Figure 14. Prompt template for galaxy merging state classification.

Training Strategy	Property Estimation (R^2 Score)				Morphology Classification (F1 Score)									
	M_*	Z_{MW}	t_{age}	sSFR	SMH	DEO	SPR	BAR	BLG	RND	EOB	SWP	SAC	MRG
Geometry Adapter Only	0.89	0.67	0.50	0.81	0.74	0.95	0.94	0.68	0.81	0.80	0.85	0.77	0.62	0.75
Geometry Adapter + LoRA	0.91	0.69	0.52	0.84	0.76	0.97	0.96	0.71	0.83	0.82	0.87	0.79	0.64	0.77
Full-Parameter Training	0.90	0.68	0.51	0.82	0.77	0.96	0.95	0.69	0.82	0.81	0.86	0.78	0.63	0.76

Table 3. **Comparison of different training strategies.** Results show that our parameter-efficient approach (Geometry Adapter + LoRA) achieves comparable or even superior performance to full-parameter training while requiring significantly fewer trainable parameters. The best results for each metric are shown in **bold**.

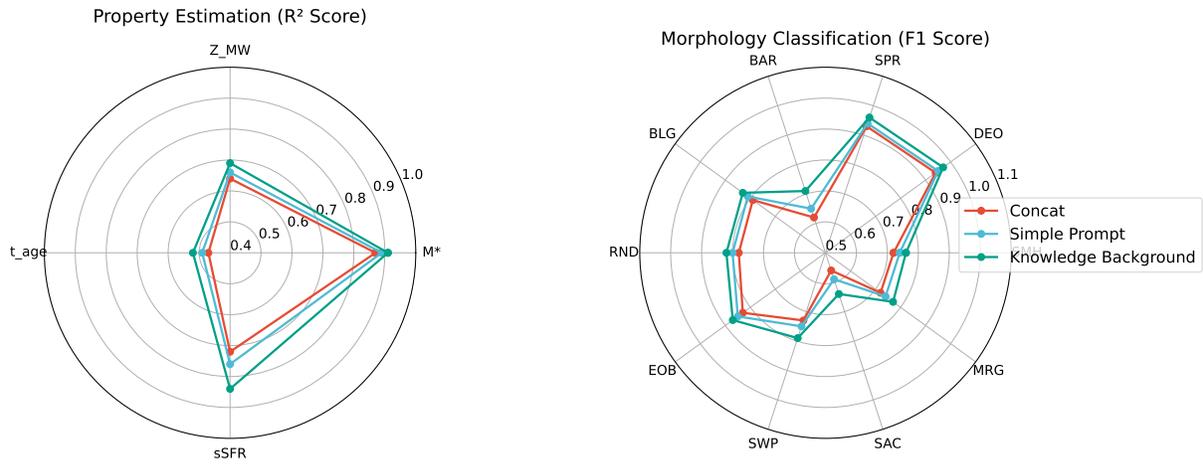


Figure 15. **Performance comparison of different prompt settings.** The radar plots show the performance of three prompt settings across property estimation tasks (left) and morphology classification tasks (right). The Knowledge Background prompts consistently outperform simpler approaches, demonstrating the effectiveness of incorporating domain knowledge into prompts. The improvement is particularly notable in property estimation tasks, where the Knowledge Background setting achieves superior performance in all metrics, with the most significant gains in sSFR estimation. For morphology classification, while the margins are smaller, the Knowledge Background setting still shows consistent advantages, especially in complex features like Bar and Spiral Arm Count classification.