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Towards Discovery and Attribution of Open-world GAN Generated Images

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Abstract

With the recent progress in Generative Adversarial Networks (GANs), it is imperative for media and visual forensics to develop detectors which can identify and attribute images to the model generating them. Existing works have shown to attribute images to their corresponding GAN sources with high accuracy. However, these works are limited to a closed set scenario, failing to generalize to GANs unseen during train time and are therefore, not scalable with a steady influx of new GANs. We present an iterative algorithm for discovering images generated from previously unseen GANs by exploiting the fact that all GANs leave distinct fingerprints on their generated images. Our algorithm consists of multiple components including network training, out-of-distribution detection, clustering, merge and refine steps. Through extensive experiments, we show that our algorithm discovers unseen GANs with high accuracy and also generalizes to GANs trained on unseen real datasets. We additionally apply our algorithm to attribution and discovery of GANs in an online fashion as well as to the more standard task of real/fake detection. Our experiments demonstrate the effectiveness of our approach to discover new GANs and can be used in an open-world setup.

1. Introduction

With an ever increasing number of GANs introduced each year, concerns about the malicious use of this technology, especially in the case of social media content [1, 2, 3] are increasing at an alarming rate which can have adverse impacts on public security and privacy. Therefore, a plethora of works have been proposed which focus on the real/fake detection task [4, 5, 6]. However, it is also important to focus on the problem of attribution, i.e. identifying the source of these images. Attributing images to their sources can potentially deter malicious organizations and hold them accountable by leading legal proceedings. Additionally, as GANs are becoming part of commercial services



Figure 1. A plethora of GANs are released every year, and there could be a set of images that come from several unknown sources. Our approach is capable of discovering and attributing unknown GAN sources while requiring label supervision for only an initial small set of GANs. We attribute with high accuracies, seen GANs from a set of images as well as identify and cluster unknown GAN sources with high purities.

such as face animation applications, their popularity draws piracy and plagiarism [7] which is an attack on intellectual property. Therefore, it is pertinent to develop effective techniques to attribute images to specific sources.

To address this problem, [7, 8, 9] perform attribution for multiple GAN architectures and obtain high classification accuracies. However, they are limited to the closed-world setup as they attribute only to the GANs seen during training and are incapable of identifying unseen GANs. Such a setup is infeasible in practical scenarios where there are a large number of images belonging to sources not seen during training. This raises the question of whether we can discover these new sources and group together the set of images which are generated by them. We term this problem as "GAN discovery and attribution" as it involves attributing images to known sources as well as discovering unknown sources. This is a much more challenging and real world setup as the number of sources are unknown and keep increasing. Additionally, there can be a significant domain shift based on the dataset type of GAN generated images.

Many works such as [5, 7, 8] show that GANs leave unique artificial signatures in the images they generate. We exploit this information to implicitly identify signatures and cluster images belonging to unseen sources together while

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also attributing images to seen sources. We propose a novel iterative pipeline which utilizes a fixed set of images, labeled according to their corresponding sources, and perform GAN attribution and discovery on an unlabeled set of images. Our approach generalizes to an open-world setup where images in the unlabeled/discovery set are not restricted to be from the labeled class sources. Additionally, due to the iterative nature of our pipeline, we can continuously discover images from new GANs added to our discovery set in an online manner. Our approach only requires labels for an initial set of images from real datasets and a few GANs trained on these real datasets with each real/GAN source representing a separate class. While we can discover unseen GANs trained on these real datasets, we additionally show through experiments that we can discover new real datasets and GANs trained on these new datasets as well without them being present in the initial labeled set.

Attribution and discovery in an open-world setup requires us to separate images belonging to seen sources during training from the unseen sources. We therefore introduce an explicit out-of-distribution (OOD) step using the deep network features to separate the images belonging to the two types of sources. We propose to incorporate the Winner Take All (WTA) hash [10] which, to the best of our knowledge, has previously never been used for OOD detection. Additionally, we obtain clusters for the OOD images and perform merge and refine steps to improve the grouping of the unknown GANs using 1-Nearest Neighbour (NN) graphs and kernel SVMs, respectively. We combine these components into a single unified pipeline which is executed iteratively for improving the features and clusters while attributing seen sources and discovering new GAN sources.

Through extensive experiments, we demonstrate the capability of our approach in an open-world setup. We show the efficacy of our approach to generalize to a wide range of dataset setups. We also analyze the importance of the various stages. Additionally, we provide an approach to apply our algorithm for the problem of real/fake image detection and show competitive results on a variety of dataset setups.

We summarize our contributions as follows: 1) We introduce a new problem for discovering and attributing images from real and GAN sources in an open-world setup; 2) We propose a novel iterative pipeline consisting of several components such as OOD detection, clustering and merge and refine stages providing a strong benchmark for this task, and; 3) We analyze the capability of our approach to discover GANs on a variety of dataset setups and also present several insights into the various stages of our pipeline.

2. Related Work

OOD Detection and Open Set Recognition: Several works [11, 12] have tackled OOD detection but require an OOD dataset for tuning hyperparameters, which is not

possible as open-world knowledge is not known apriori. [13] removes this constraint but requires modification of the training setup to decompose confidence scores into two probabilities.

On similar lines is the task of open set recognition [14]. [15, 16, 17] use the Extreme Value Theory to discard unknown samples but require setting thresholds for reconstruction errors and/or probability values to detect OOD samples which requires careful tuning for each dataset. [18] provides a detailed survey of more works in this area.

Open World learning: While Open Set Recognition only rejects the unseen classes, Open World learning [19] also focuses on reasoning about the unseen classes. [20] tackles this problem using meta classifiers but are limited to the product classification problem. [21, 22, 23, 24] also focus on a similar problem but require the unlabeled set to only contain unseen classes and knowledge about number of unseen classes in some cases.

Rank correlation: [10] compute the WTA hash which are ordinal embeddings providing a highly non-linear sparse transformation of the feature vector. [25] use this hashing algorithm for performing fast large scale object detection. To the best of our knowledge, no work utilizes ranking based measures for OOD detection.

Clustering: Clustering is a highly explored field yet there is no one-size fits all solution. [26] use a first Nearest Neighbours (1-NN) graph to perform parameter free clustering. Inspired from their work, we use a similar 1-NN graph for our merge step. [27] perform K-means clustering on a network's features and retrain the network using the cluster labels as pseudo-labels. Our approach partly involves this setup but contains several other components such as OOD detection and merge and refine steps. Spectral clustering [28, 29, 30] is another common approach but requires eigenvalues for a large Laplacian which is not tractable for large datasets, as is our case. Another common direction is training a deep network [31, 32, 33, 34, 35] which learns embeddings/clusters based on minimizing an objective function. However, these require careful training so as to not diverge while learning the features in an unsupervised manner.

Real/fake detection and GAN attribution: A plethora of works [2, 3, 4, 5] exist for the problem of real/fake detection but are only limited to this binary classification problem and are not directly applicable to GAN attribution and discovery. [5, 7, 8] tackle this problem but are, however, limited to the GANs that they train on and fail to generalize in an open world setup. [36] propose a more dynamic approach to incrementally include GANs for attribution but require clean datasets with images coming from only a single GAN source which does not hold in practice, as images could be generated from multiple sources. To the best of our knowledge, there exists no work dealing with open-world GAN discovery and attribution which is a much harder task than

just real/fake detection or closed set GAN attribution.

3. Proposed Approach

3.1. Overview

In this section, we briefly describe our approach as shown in Fig. 2. Our initial labeled set consists of n_s images corresponding to the seen classes and is denoted by $\mathcal{I}_s = \{I_{s_1}, I_{s_2}, ..., I_{s_{n_s}}\},$ and their ground truth class labels, denoted by $\mathcal{Y}_s = \{y_{s_1}, y_{s_2}, ..., y_{s_{n_s}}\}$. The discovery set consists of n_t unlabeled images, from both seen and unseen classes, and is denoted by $\mathcal{I}_t = \{I_{t_1}, I_{t_2}, ..., I_{t_{n_t}}\}$. Our pipeline proceeds iteratively, and at any point in the pipeline, our discovery set is partitioned into \mathcal{I}_c and \mathcal{I}_n . \mathcal{I}_c is a set of n_c clustered images with predicted labels \mathcal{Y}_c while \mathcal{I}_n is a set of images which could be potentially clustered in future iterations. In each iteration, we improve the predicted labels in the clustered set (\mathcal{I}_c) and add new samples from the non-clustered set (\mathcal{I}_n) into the clustered set. We do this via several stages using algorithms or tools which have previously not been applied for the specific tasks. We also combine the various stages in a unified manner for iteratively improving the features and clusters.

Network training: Our network consists of a feature extractor $f(\cdot)$ and classifier $g(\cdot)$. We train the network in a supervised manner using the two sets of images and labels, labeled set $(\mathcal{I}_s, \mathcal{Y}_s)$ and clustered set $(\mathcal{I}_c, \hat{\mathcal{Y}}_c)$.

Out-of-distribution detection: We use $f(\cdot)$ to extract features for \mathcal{I}_c and \mathcal{I}_n and perform OOD detection. This stage predicts samples from \mathcal{I}_n to be in-distribution or OOD with respect to the clusters in \mathcal{I}_c . The in-distribution samples are classified using the classifier and attributed to \mathcal{I}_c with the corresponding predicted labels.

Clustering: We use the K-means algorithm to overcluster the remaining samples in \mathcal{I}_n . These clusters are then added to the clustered set \mathcal{I}_c with a new set of labels based on the cluster labels. At the end of this stage all samples have a predicted label and the non-clustered set, \mathcal{I}_n , is empty.

Merge and refine: To deal with overclustering we perform merge and refine operations. Specifically, coherent clusters are merged to reduce the number of clusters. This reduces the purity of the clusters and hence a refine operation is performed which throws away impure clusters, or samples likely to not have belonged to their existing clusters. The rejected samples are added to the non-clustered set \mathcal{I}_n . At the end of this stage, we have a new clustered set, \mathcal{I}_c along with its predicted labels $\hat{\mathcal{Y}}_c$, and non-clustered set, \mathcal{I}_n . The four steps described above are then repeated. We now describe each of the steps enumerated above in detail.

3.2. Network Training

This stage involves training the network using the cluster labels $\hat{\mathcal{Y}}_c$ corresponding to \mathcal{I}_c and \mathcal{Y}_s corresponding to \mathcal{I}_s in a supervised manner. The network consists of a feature generation network $f(\cdot)$ parameterized by θ_f , constructed using an off-the-shelf CNN followed by a few fully connected layers to reduce the dimensionality. The classification part of the network $g(\cdot)$ parameterized by θ_g involves a fully connected layer followed by the softmax function.

The parameters of the network θ_f , θ_g are optimized as per the following expression:

$$\min_{\theta_f, \theta_g} \left[\frac{1}{n_c} \sum_{i=1}^{n_c} \mathcal{L} \left(g_{\theta_g}(f_{\theta_f}(I_{c_i})), \hat{y}_{c_i} \right) + \frac{1}{n_s} \sum_{j=1}^{n_s} \mathcal{L} \left(g_{\theta_g}(f_{\theta_f}(I_{s_j})), y_{s_j} \right) \right], \quad (1)$$

where \mathcal{L} is the cross-entropy loss, I_{c_i} and \hat{y}_{c_i} are the *i*th images and labels from \mathcal{I}_c and \mathcal{Y}_c respectively while I_{s_j} and y_{s_j} are the *j*th images and labels from \mathcal{I}_s and \mathcal{Y}_s respectively. Subsequent to network training, we use the feature generation network to extract the features \mathcal{X}_c and \mathcal{X}_n corresponding to the clustered set of images \mathcal{I}_c , and non-clustered set of images \mathcal{I}_n , respectively.

3.3. Out-of-distribution detection

We utilize the WTA hashing algorithm proposed by Yagnik *et al.* [10] who show that ordinal representations of feature vectors provide strong nonlinear transformations and demonstrate their algorithm's capability on downstream tasks, such as similarity search and classification. They show that such rank correlation measures are robust to noise unlike cosine or Euclidean based distances. Additionally, Euclidean/cosine based distances are highly sensitive to thresholds used for OOD detection which would require careful hyperparameter tuning for different dataset setups. We refer readers to their work or our supplementary material for a detailed explanation of the WTA hash.

The WTA hash maps a d dimensional feature vector \boldsymbol{x} to a H dimensional vector \boldsymbol{x}_H with elements lying in [K]. Using this hash for each feature vector, we then represent the distance between any two feature vectors \boldsymbol{x} and \boldsymbol{y} , as $d(\boldsymbol{x}, \boldsymbol{y})$, which is the Hamming distance between their corresponding hashes. For each class in set $\hat{\mathcal{Y}}_c = \{\hat{y}_i \in [N], i \in [n_c]\}$ (n_c is the number of samples in the clustered set, N is number of clusters), we obtain OOD detectors in the following manner: For a cluster with cluster label $j \in [N]$ and for a feature sample $i \in [n_c]$ in the nonclustered set represented by $\boldsymbol{x}_{n_i} \in \mathcal{X}_n$, we compute the distance of \boldsymbol{x}_{n_i} from each sample in the cluster j. We then average these sample distances to get the distance of sample \boldsymbol{x}_{n_i} from cluster j, *i.e.*,

$$d_j(x_{n_i}) = \frac{1}{N_j} \sum_{k=1, y_{c_k}=j}^{n_c} d(\boldsymbol{x}_{n_i}, \boldsymbol{x}_{c_k}),$$
(2)



Figure 2. Illustration of our algorithm, where we iteratively discover new classes and retrain our network using them as pseudo-labels.

where N_j represents the number of samples in cluster j. The detector then classifies x_{n_i} as an in-distribution sample of class j if $d_j(x_{n_i}) < t_j$ for a threshold t_j for class j. The threshold t_j is computed using the intra cluster distances for each cluster j and setting a high percentile of these distances as the threshold. By doing so, the algorithm learns different thresholds for different clusters and is controlled only by a single percentile scalar which generalizes across different dataset setups. A test sample, x_{n_i} is classified as an OOD sample to \mathcal{X}_c , if all of the detectors for the clusters classify it as OOD. All in-distribution samples are classified using our classifier and their corresponding labels lie in $\hat{\mathcal{Y}}_c$. The samples are subsequently added to \mathcal{I}_c .

3.4. Clustering

We now overcluster samples remaining in \mathcal{I}_n by running K-Means on the feature set \mathcal{X}_n . We form a high number of clusters in order to get clusters with high purity. Once the clusters are obtained, they are added to the clustered set \mathcal{I}_c . Their new labels, corresponding to the cluster labels, are added to $\hat{\mathcal{Y}}_c$. At the end of this stage, no samples remain in the non-clustered set. More importantly, as we generate a large number of clusters, it makes the clustered set highly fragmented. In order to reduce the number of clusters and improve the purity of the clusters we perform a merge and refine step as explained in the following section.

3.5. Merge and refine

Overclustering results in a highly fragmented cluster set which could belong to the same class. To deal with this, a merge step is performed. Anything less than an ideal merge step results in impure clusters. To improve the purity a refine step is also performed. We discuss these in detail below.

3.5.1 Merge

We merge clusters in \mathcal{I}_c using a 1-Nearest Neighbour graph. We obtain centroids, u_j , for each cluster $j \in [N]$ (N is the number of clusters) by averaging the features of all samples in the cluster. Using the hashing described in Section 3.3 for each centroid, we define the distance between two centroid feature vectors u_i and u_j , $d(u_i, u_j)$, as the Hamming distance between their corresponding hashes u_{iH} and u_{jH} .

We use the centroid distances between every pair of clusters to create a directed 1-Nearest Neighbour graph with each node representing a cluster centroid. A directed edge is present from one node to another if the latter node is the nearest neighbour centroid of the former node. Strongly connected components are computed for this graph and each connected component in the graph is considered to be a merged cluster. This stage generates a new set of labels, $\hat{\mathcal{Y}}_c$, for the clustered set \mathcal{I}_c .

3.5.2 Refine

As the merge step is not ideal, it reduces the average purity of the clusters. In order to increase it, a refine step is performed to remove impure samples from each cluster. As the ground truth labels are unknown, SVM classifiers are leveraged to obtain a proxy measure for purity. [37, 38] show that weak SVM classifiers can be fit to a single positive instance with the remaining samples as negatives. Therefore, we use this formulation of weak classifiers that can fit to the majority class distribution of a cluster and mark the samples which do not belong to the majority class as negatives. For each cluster $j \in [N]$, an SVM classifier, Q_j , is trained in a one-vs-all manner, where the positive samples belong to cluster j while the rest of the samples in the clustered set are negative samples. After training Q_i , we use the SVM to predict the labels for samples in cluster j as positive and negative. The samples which are predicted negative are then rejected and added back into the non-clustered set \mathcal{I}_n . If the percentage of predicted positive samples by Q_j in cluster j

the samples are added to \mathcal{I}_n . Additionally, some refined clusters might have very few samples and the class distribution for training the network in the next iteration could become long tailed. In order to avoid this issue, we threshold clusters based on their sizes and discard those below a size threshold τ into \mathcal{I}_n .

is below a threshold ϵ , the entire cluster is discarded and all

After the refine step we have a new set of clustered images with their corresponding pseudolabels. These are used along with the seen class train data \mathcal{I}_s in order to train the network for the next iteration.

3.6. Cluster set initialization

The start of every iteration of our pipeline requires a clustered set \mathcal{I}_c along with the seen labeled set \mathcal{I}_s . For the first iteration, as we do not have any pseudolabels for the discovery set \mathcal{I}_t , we train our network using only the set \mathcal{I}_s and their corresponding ground truth labels \mathcal{Y}_s . Our OOD detection step then determines whether images in \mathcal{I}_t belong to the seen classes \mathcal{Y}_s or not. In-distribution samples are classified and are added to the clustered set \mathcal{I}_c while OOD samples are added to \mathcal{I}_n . At the end of this stage, we now have a clustered and non-clustered set for the discovery set images. The rest of the stages of our pipeline, *i.e.*, K-Means Clustering, Merging and Refinement proceed as explained in the previous sections using the initialized \mathcal{I}_c and \mathcal{I}_n . The refine step then produces a set of images in the clustered set with their corresponding cluster labels as pseudo-labels which are used to train the network for the next iteration. Additionally, at every iteration t, the feature extractor is initialized with the weights of the previous iteration t-1. The classifier is replaced with a new linear layer with weights randomly initialized as number of classes, which is dependent on number of clusters N, change across iterations. The algorithm then proceeds for a few iterations until fraction of undiscovered samples fall below a small threshold.

4. Experiments

We now evaluate our approach on real world dataset setups while providing detailed analysis of the several components of our pipeline. In Section 4.1, we describe the implementation details. Our labeled dataset consists of images from 4 real datasets as well as from certain GANs trained on these real datasets as shown in Table 1. Together, they make up 12 classes in the labeled set. Our discovery set consists of additional images from these 12 classes as well as from 8 unseen GANs as shown in Table 1 making up a total of 20 classes. We use, by default, this dataset for all our experiments unless mentioned otherwise. Note that the same GAN trained on different datasets corresponds to different classes. Section 4.2 shows extensive comparisons with other related works on GAN attribution and real/fake image detection. Section 4.3 provides several insights into our algorithm and also analyzes several components of our pipeline. Subsequently, we examine the results of our pipeline on varying dataset setups. Section 4.4.1 shows an analysis of number of GANs needed in our labeled set to reliably discover new GANs in the discovery set. Section 4.4.2 changes number of unseen real datasets as well as corresponding GANs in the discovery set and shows the effectiveness of our approach to discover these new classes.

4.1. Experimental details

For our feature extractor, we use the standard ResNet-50 [53] backbone. We add 3 fully-connected layers to reduce

Table 1. List of GANs trained on the corresponding 4 real datasets used in our labeled and discovery set. Note that the same GAN can be trained on multiple datasets.

Dataset	Labeled GANs	Discovery GANs
CelebA[39]	StarGAN[40],	StarGAN, BEGAN[42],
	AttGAN[41]	ProGAN[43], SNGAN [44],
		AttGAN, MMDGAN[45],
		CramerGAN[46]
CelebA-HQ	ProGAN,	ProGAN, StyleGAN,
[43]	StyleGAN[47]	ResNet19[48]
ImageNet [49]	BigGAN[50],	BigGAN, S3GAN, SNGAN
	S3GAN[51]	
LSUN	ProGAN,	ProGAN, MMDGAN,
Bedroom [52]	MMDGAN	SNGAN

the dimensionality of the feature vector to 128. Another fully connected layer is used as the classification head on top of the feature extractor. The full network is trained in a supervised manner and using cross entropy loss. Every image is resized and center cropped to 256×256 except when specified otherwise. We use a batch size of 256 for our training for each iteration of the pipeline. The weights are optimized using the Adam optimizer with $\beta_1 = 0.9$, $\beta_2 = 0.999$ and a fixed learning rate of 0.0001 throughout our training. For the first iteration, we train our network for 50 epochs, while for subsequent iterations we train for 100 epochs, as the network takes longer to converge with additionally discovered samples with noisy pseudo labels. For our OOD detection step using WTA hash described in Section 3.3, we use H = 2048 hashes and a window size of K = 2. Our clustering stage uses the K-Means algorithm for 500 clusters initialized using K-Means++ [54]. For the refine stage, we train SVMs with the RBF-kernel. We set the threshold, $\epsilon = 0.5$, for dropping a cluster, as described in Section 3.5.2. To avoid training on clusters with very few samples, we discard clusters with less than 100 members.

Metrics and analysis: We evaluate our pipeline on 2 clustering metrics. We use Average Purity as a metric for evaluating the overall purity of our clusters with respect to the true labels of the discovery set. We also use Normalized Mutual Information (NMI), which is another commonly used clustering metric. At various stages or iterations of our pipeline, a small fraction of the discovery set samples remain non-clustered and in order to provide a fair evaluation across different experiments/baselines we attribute all the non-clustered samples to their nearest clusters and evaluate on the full discovery set, unless mentioned otherwise.

4.2. Benchmark Evaluation

As there exists no prior work dealing with open-world GAN discovery, we provide baselines by modifying recent works involving GAN attribution [7] and real/fake image detection [5]. We additionally include the recent approach of [24] which deals with novel category discovery.

Yu et al. [7] deals with GAN attribution in a closedworld setup and hence cannot be directly incorporated to

Table 2. Comparison of our method with baselines derived from [5, 7, 24]. We try two fixed setups for number of clusters k = 20,500 and finally let our approach discover the suitable number of clusters k = 209. Compared to the 2 baselines, we obtain the highest Average Purity and NMI when number of clusters k = 209. Ours [only §3.2] corresponds to a single iteration of network training and clustering. The fully supervised setup is the upper bound when all classes are seen.

Method	k = 20		k = 500		k = 209	
	Avg. Purity	NMI	Avg. Purity	NMI	Avg. Purity	NMI
Yu et al. [7]	0.656	0.706	0.759	0.518	0.734	0.554
Han et al. [24]	0.680	0.709	-	-	-	-
Wang et al. [5]	0.710	0.759	0.857	0.575	0.840	0.624
Ours [only §3.2]	0.661	0.743	0.814	0.561	0.795	0.609
Ours	-	-	-	-	0.861	0.724
Fully supervised	0.928	0.929	0.996	0.658	0.997	0.728

our problem setup. Therefore, we train their network on our labeled set and obtain features for our discovery set. We cluster the features using K-Means for 3 different values of k. k = 20 corresponds to the true number of classes in our test set while k = 500 corresponds to an overclustered regime. k = 209 represents the number of clusters our algorithm returns at the end of 4 iterations. We compare across multiple values of k as Average Purity and NMI are known to be sensitive to number of clusters.

Wang *et al.* [5] tackles real/fake detection and again cannot be directly used in our problem setup. Therefore, we modify their classification head to be multiclass and train their network on our labeled set using their training and preprocessing strategies and extract the features for our discovery set. We provide three similar baselines by performing clustering similar to the baselines generated from [7].

Han *et al.* [24] discover novel visual categories but require the discovery set to only contain unseen classes. We therefore use our anomaly detection approach on their features to separate out the seen and unseen classes whose cluster assignments are then predicted separately using their approach. As they require knowledge of number of unseen classes for their predictions, we compare with the k = 20setup which corresponds to the true number of classes.

Finally, we provide a baseline for our approach by performing network training and clustering the feature space into k = 20,500,209 clusters. We also provide an upperbound for our approach using a fully supervised case where the labeled set consists of images from all classes in the discovery set and perform clustering on the generated features.

The results for these comparisons are provided in Table 2. Our algorithm achieves the highest Average Purity and NMI compared to all other baselines for the case of k = 209. For k = 20,500, [5] outperforms a single iteration of network training and clustering because it does not involve OOD detection, merge or refine for this comparison. However, at the end of 4 iterations, for the case of

Table 3. We analyze the effect of the various stages of our pipeline. The number of clusters in the merge step decreases with negligible drop in Avg. Purity and increased NMI. The Refine step further increases the NMI and Avg. Purity by a big margin for the discovered samples. Note that the numbers corresponding to all samples in the refine step are included for the sake of fair comparison but are not actually computed by our approach.

Stage	No. of clusters	Avg. Purity	NMI
Clustering	512	0.793	0.682
Merge	391	0.792	0.689
Refine (Discovered)	111	0.849	0.838
Refine (All)	111	0.772	0.720

Table 4. We evaluate our algorithm over multiple iterations. Avg. Purity, NMI and % of discovered samples progressively increases.

Iteration	Avg. Purity	NMI	% Samples Clustered	Sources Discovered
1	0.772	0.720	72.5	16/20
2	0.853	0.724	88.8	20/20
3	0.861	0.724	92.3	20/20
4	0.861	0.724	93.7	20/20

k = 209, we significantly outperform all baselines in terms of both Average Purity and NMI. The fully supervised approach provides an upper bound for all 3 cases. Note that we do not compare across number of clusters as Average Purity increases in general with more clusters while NMI decreases.

4.3. Ablation Study

Our algorithm is fairly robust to the various hyperparameter values used in our stages. Experiments for varying hyperparameter values are shown in the supplementary material. In this section, we analyze the importance of each stage and the progress of our pipeline over multiple iterations.

We evaluate the effect of Clustering, Merge, and Refine stages in the first iteration of our pipeline. The results are summarized in Table 3. Note that the Average Purity drops only slightly in the merge step while the number of clusters drop significantly demonstrating the effectiveness of the 1-NN merge step explained in Section 3.5. From the merge to the refine step, Average Purity drops for the full discovery set as many samples remain undiscovered and we evaluate the metric over the full discovery set by naïvely attributing them to the nearest cluster. However, the metrics evaluated on only the discovered samples increase significantly which shows that SVMs can identify the pure clusters and samples while rejecting the impure ones.

Next, we evaluate our pipeline over multiple iterations. We show the results in Table 4. The pipeline discovers only a small fraction of images and GANs in the first iteration while in subsequent iterations, more samples are added to the clustered set and more GANs are discovered. Average Purity and NMI both increase or remain constant over the four iterations which shows the effectiveness of

Table 5. Varying number of GANs per dataset. We obtain the best metrics with the maximum number of GANs per dataset although discovering fewer samples compared to the first setup.

# of GANs	Avg. Purity	NMI	% Samples Clustered	Sources Discovered
0	0.497	0.559	99.78	8/12
1	0.897	0.772	94.48	11/12
2	0.954	0.789	95.98	11/12

our approach to discover as well as improve clusters. Our OOD stage obtains an accuracy of 86.97% for seen classes, 99.87% for unseen classes and 92.87% overall. The high unseen class accuracy is because of setting a lower threshold to reduce false negative errors which do not get corrected in subsequent stages.

4.4. Varying dataset setups

In this section, we provide an analysis by varying the dataset setups based on number of GANs per real dataset in the labeled set or on adding new real datasets and GANs trained on them in the unlabeled set.

4.4.1 Effect of number of GANs per dataset

We answer the question of how many GANs per dataset are needed in our labeled set to reliably discover new ones in our discovery set. We have 3 labeled dataset setups: 1) Our first setup consists of 4 real datasets: CelebA, CelebA-HQ, ImageNet and LSUN-Bedroom with no GANs; 2) In addition to the 4 datasets in the first setup, our second setup has 4 GANs: StarGAN, ProGAN, BigGAN and MMDGAN trained on the respective datasets; 3) In addition to the previous setup, we have 4 more GANs per dataset: AttGAN, StyleGAN, S3GAN and ProGAN.

In order to fairly evaluate the 3 setups, we use a common discovery set consisting of all the classes in the second setup. Additionally, we have a set of GANs not present in all 3 labeled sets, namely, BEGAN, ResNet19 (from CompareGAN [48]), SNGAN and CramerGAN corresponding to the 4 real datasets. The results are summarized in Table 5. Due to most information being present in the labeled set, the third setup performs best on both Average Purity and NMI. Despite the second setup having only a single GAN per dataset, it performs fairly well on the two metrics. On the other hand, the first setup, which does not have any GANs in the labeled set, fails to discover new ones as it cannot see any GAN-related artifacts in the labeled set and thus fails to discriminate based on this during discovery.

4.4.2 Discovering new dataset images

In an open-world setting, the discovery set may contain images from new real datasets not seen in the labeled set along with GAN generated images corresponding to these datasets. To see whether the proposed approach can handle these situations we perform experiments covering 3

Table 6. Effect of adding new datasets and GANs trained on new datasets at test time. (*) provides the corresponding comparison when the real datasets are present in the labeled set (Sec. 4.4.2)

Test Set	Purity	NMI	Sources Discovered	# of Clusters
New Real	0.942	0.813	14/16	103
New Real*	0.989	0.989	15/16	56
New GANs	0.976	0.828	16/16	105
New GANs*	0.95	0.835		87
New Real + New GANs	0.850	0.730	20/20	141
New Real + New GANs*	0.977	0.856	19/20	128

setups. Each setup uses the default labeled set in Table 1 but additional classes in the discovery set as follows: 1) New real datasets: New real datasets namely DTD [55], FashionGen [56], and Night and Shoes datasets (from Pix2Pix [57]); 2) GANs on new real classes: New GANs trained on the four new real world datasets, namely, Pro-GAN on DTD, DCGAN [58] on FashionGen, and a separate Pix2Pix on Night and Shoes datasets; 3) New Real + New GANs: A combination of GANs and real datasets from the previous two setups.

In order to provide a benchmark for comparison, we show the performance when the four real datasets are in the labeled set (marked with a *). The results are shown in Table 6. In the first setup the goal is to discover new dataset sources. Our approach discovers most of the sources with high Purity and NMI, although it's performance is lower than the benchmark as expected because the labeled set for the benchmark contains all the classes present in the discovery set. In the second setup, our method discovers all unseen GANs even though they are trained on unseen datasets unlike the benchmark which does slightly worse in terms of Avg. Purity and number of GANs discovered likely because of the reduced number of final clusters. The third setup is more challenging due to the addition of both unseen datasets and GANs trained on them to the discovery set. However our approach discovers all unseen sources with reliable Average Purity and NMI while its corresponding benchmark does not discover all sources possibly because it restricts itself to lesser but purer clusters with higher NMI.

4.4.3 Online discovery

Here we extend our approach to an online setup where new GANs are added to the discovery set in an online fashion based on the chronological order they were published. Our setup consists of 9 GANs from 4 real sources in our labeled set and 4 new GANs in the discovery set. We additionally introduce 2 sets of 3 GANs each in an online fashion. Details of the datasets are provided in supplementary material. We show our results in Table 7. We train our setup for 2 iterations with the initial discovery set of 17 sources. It can be



Figure 3. Samples from clusters discovered by our approach for unseen GANs with the majority class in parenthesis. It can be noticed that they are not just focusing on the object structure and semantics rather the underlying source.

Table 7. Evaluation of our algorithm in an online setup. We have 17 sources in our initial discovery set and add 3 sources each at iteration 3 and 5 causing an initial drop in results. The pipeline eventually performs better after training on the new samples.

Iteration	Avg. Purity	NMI	% Samples Clustered	Sources Discovered
1	0.846	0.826	89.39	15/17
2	0.916	0.798	92.42	16/17
3	0.805	0.771	95.74	18/20
4	0.805	0.744	96.87	19/20
5	0.731	0.716	95.68	22/23
6	0.802	0.705	95.36	22/23

seen that Average Purity increases in the second step and it also discovers an additional GAN source. When new GANs are introduced in iterations 3 and 5, the performance drops as the network is not trained on the new classes. However, after a single iteration the Average Purity increases significantly and NMI drops only slightly even though number of clusters increase. At the end of 6 iterations, we discover all the GAN sources added on the fly, except one. This shows that our approach works in an online setting, continuously discovering new GANs iteratively.

4.5. Real/Fake detection

We now apply our method to the common problem of real/fake detection. We use the binary classification model from [5], but trained on our labeled set and use majority voting to mark a cluster and all its constituent images as real or fake. We compare this with using the model directly on all samples and compare the performance in Table 8 for our original setup and for the three setups defined in Sec. 4.4.2. We observe that in most settings, we outperform the standard predictions which are evaluated samplewise. We attribute it to the fact that the clustering is able to correct model's mistakes as it groups samples according to the source. As cluster assignments are less accurate due to increased difficulty of the final setup, our performance is lower but nevertheless, competitive with [5].

4.6. Qualitative analysis of clusters

We visually inspect a few clusters generated by our method to see whether they focus on the semantic information or the GAN source. To this end we visualize random images from some of the highly pure clusters correspond-

Table 8. We evaluate the real/fake detection accuracy (%) using the clustering obtained from our network.

Approach	Original	New Real	New GANs	New Real + New GANs
Wang <i>et al</i> . [5]	92.56%	87.35%	98.42%	89.09%
Ours	98.62%	89.84%	99.10%	83.33%

ing to unseen GANs trained on ImageNet, LSUN-Bedroom, CelebA and CelebA-HQ. As evident from Fig. 3 the cluster in the case of SNGAN-ImageNet does not seem to be object-specific, while the cluster for SNGAN-LSUN does not focus on specific room decor, lighting conditions, layout etc. Similarly, clusters corresponding to the face datasets seem to be focusing on the GAN source rather than specific facial attributes like expression, orientation, age etc. In addition to visualizing these clusters, we also add a qualitative analysis of the merge step in the supplementary material showing sub-clusters that are merged by our pipeline.

5. Conclusion

We proposed a new problem of open-world GAN discovery and attribution. We presented an iterative approach to discover and attribute images from multiple GAN sources in a discovery set. Our framework discovers and groups GANs not seen during training by implicitly focusing on GAN-based fingerprints. We show ablation studies for the different components of our pipeline. We also show the generalization of our approach to various dataset setups and its extension to an online setting. As there have been no works addressing this problem, we compare with several baselines based on state-of-the-art related works and provide a strong benchmark for this task. Even though our approach works in an online setup, network training is an expensive step for each iteration. One potential direction for future work is to utilize approaches from continual learning literature [59] for faster training, to learn in a never-ending setup discovering new GANs on-the-fly. We hope, given the general formulation of the stages, our framework is utilized for other similar tasks as well. To facilitate such exploration of different scenarios we plan to release the toolset we have developed for our work to bolster future research in this area.

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References

- Kai Shu, Amy Sliva, Suhang Wang, Jiliang Tang, and Huan Liu. Fake news detection on social media: A data mining perspective. ACM SIGKDD explorations newsletter, 19(1):22–36, 2017.
- [2] Andreas Rössler, Davide Cozzolino, Luisa Verdoliva, Christian Riess, Justus Thies, and Matthias Nießner. Faceforensics: A large-scale video dataset for forgery detection in human faces. arXiv preprint arXiv:1803.09179, 2018. 1, 2
- [3] Andreas Rossler, Davide Cozzolino, Luisa Verdoliva, Christian Riess, Justus Thies, and Matthias Nießner. Faceforensics++: Learning to detect manipulated facial images. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 1–11, 2019. 1, 2
- [4] Francesco Marra, Diego Gragnaniello, Davide Cozzolino, and Luisa Verdoliva. Detection of gan-generated fake images over social networks. In 2018 IEEE Conference on Multimedia Information Processing and Retrieval (MIPR), pages 384–389. IEEE, 2018. 1, 2
- [5] Sheng-Yu Wang, Oliver Wang, Richard Zhang, Andrew Owens, and Alexei A Efros. Cnn-generated images are surprisingly easy to spot... for now. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, volume 7, 2020. 1, 2, 5, 6, 8
- [6] Xu Zhang, Svebor Karaman, and Shih-Fu Chang. Detecting and simulating artifacts in gan fake images. In 2019 IEEE International Workshop on Information Forensics and Security (WIFS), pages 1–6. IEEE, 2019. 1
- [7] Ning Yu, Larry S Davis, and Mario Fritz. Attributing fake images to gans: Learning and analyzing gan fingerprints. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 7556–7566, 2019. 1, 2, 5, 6
- [8] F. Marra, D. Gragnaniello, L. Verdoliva, and G. Poggi. Do gans leave artificial fingerprints? In 2019 IEEE Conference on Multimedia Information Processing and Retrieval (MIPR), pages 506–511, 2019. 1, 2
- [9] Michael Albright and Scott McCloskey. Source generator attribution via inversion. 1
- [10] Jay Yagnik, Dennis Strelow, David A Ross, and Ruei-sung Lin. The power of comparative reasoning. In 2011 International Conference on Computer Vision, pages 2431–2438. IEEE, 2011. 2, 3
- [11] Shiyu Liang, Yixuan Li, and Rayadurgam Srikant. Enhancing the reliability of out-of-distribution image detection in neural networks. arXiv preprint arXiv:1706.02690, 2017. 2
- [12] Kimin Lee, Kibok Lee, Honglak Lee, and Jinwoo Shin. A simple unified framework for detecting out-of-distribution samples and adversarial attacks. In Advances in Neural Information Processing Systems, pages 7167–7177, 2018. 2
- [13] Yen-Chang Hsu, Yilin Shen, Hongxia Jin, and Zsolt Kira. Generalized odin: Detecting out-of-distribution image without learning from out-of-distribution data. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 10951–10960, 2020. 2
- [14] Walter J Scheirer, Anderson de Rezende Rocha, Archana Sapkota, and Terrance E Boult. Toward open set recognition. *IEEE transactions on pattern analysis and machine intelligence*, 35(7):1757–1772, 2012. 2
- [15] Lalit P Jain, Walter J Scheirer, and Terrance E Boult. Multi-

class open set recognition using probability of inclusion. In *European Conference on Computer Vision*, pages 393–409. Springer, 2014. 2

- [16] Poojan Oza and Vishal M Patel. C2ae: Class conditioned auto-encoder for open-set recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 2307–2316, 2019. 2
- [17] Ethan M Rudd, Lalit P Jain, Walter J Scheirer, and Terrance E Boult. The extreme value machine. *IEEE* transactions on pattern analysis and machine intelligence, 40(3):762–768, 2017. 2
- [18] Terrance E Boult, Steve Cruz, Akshay Raj Dhamija, M Gunther, James Henrydoss, and Walter J Scheirer. Learning and the unknown: Surveying steps toward open world recognition. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 33, pages 9801–9807, 2019. 2
- [19] Abhijit Bendale and Terrance Boult. Towards open world recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 1893–1902, 2015. 2
- [20] Hu Xu, Bing Liu, Lei Shu, and P Yu. Open-world learning and application to product classification. In *The World Wide Web Conference*, pages 3413–3419, 2019. 2
- [21] Yen-Chang Hsu, Zhaoyang Lv, and Zsolt Kira. Learning to cluster in order to transfer across domains and tasks. arXiv preprint arXiv:1711.10125, 2017. 2
- [22] Kai Han, Andrea Vedaldi, and Andrew Zisserman. Learning to discover novel visual categories via deep transfer clustering. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 8401–8409, 2019. 2
- [23] Zifeng Wang, Batool Salehi, Andrey Gritsenko, Kaushik Chowdhury, Stratis Ioannidis, and Jennifer Dy. Openworld class discovery with kernel networks. arXiv preprint arXiv:2012.06957, 2020. 2
- [24] Kai Han, Sylvestre-Alvise Rebuffi, Sebastien Ehrhardt, Andrea Vedaldi, and Andrew Zisserman. Automatically discovering and learning new visual categories with ranking statistics. arXiv preprint arXiv:2002.05714, 2020. 2, 5, 6
- [25] Thomas Dean, Mark A Ruzon, Mark Segal, Jonathon Shlens, Sudheendra Vijayanarasimhan, and Jay Yagnik. Fast, accurate detection of 100,000 object classes on a single machine. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, pages 1814–1821, 2013. 2
- [26] Saquib Sarfraz, Vivek Sharma, and Rainer Stiefelhagen. Efficient parameter-free clustering using first neighbor relations. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, pages 8934–8943, 2019. 2
- [27] Xueting Yan, Ishan Misra, Abhinav Gupta, Deepti Ghadiyaram, and Dhruv Mahajan. Clusterfit: Improving generalization of visual representations. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 6509–6518, 2020. 2
- [28] Xu Yang, Cheng Deng, Feng Zheng, Junchi Yan, and Wei Liu. Deep spectral clustering using dual autoencoder network. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 4066–4075, 2019. 2
- [29] Andrew Y Ng, Michael I Jordan, and Yair Weiss. On spectral clustering: Analysis and an algorithm. In Advances in neural information processing systems, pages 849–856, 2002. 2

- [30] Ulrike Von Luxburg. A tutorial on spectral clustering. *Statis*tics and computing, 17(4):395–416, 2007. 2
- [31] Jianwei Yang, Devi Parikh, and Dhruv Batra. Joint unsupervised learning of deep representations and image clusters. In Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, pages 5147–5156, 2016. 2
- [32] Junyuan Xie, Ross Girshick, and Ali Farhadi. Unsupervised deep embedding for clustering analysis. In *International conference on machine learning*, pages 478–487, 2016. 2
- [33] Xifeng Guo, Long Gao, Xinwang Liu, and Jianping Yin. Improved deep embedded clustering with local structure preservation. In *Proceedings of the Twenty-Sixth International Joint Conference on Artificial Intelligence, IJCAI-17*, pages 1753–1759, 2017. 2
- [34] Yazhou Ren, Kangrong Hu, Xinyi Dai, Lili Pan, Steven CH Hoi, and Zenglin Xu. Semi-supervised deep embedded clustering. *Neurocomputing*, 325:121–130, 2019. 2
- [35] Lei Yang, Xiaohang Zhan, Dapeng Chen, Junjie Yan, Chen Change Loy, and Dahua Lin. Learning to cluster faces on an affinity graph. In *Proceedings of the IEEE Conference* on Computer Vision and Pattern Recognition, pages 2298– 2306, 2019. 2
- [36] Francesco Marra, Cristiano Saltori, Giulia Boato, and Luisa Verdoliva. Incremental learning for the detection and classification of gan-generated images. In 2019 IEEE International Workshop on Information Forensics and Security (WIFS), pages 1–6. IEEE, 2019. 2
- [37] Tomasz Malisiewicz, Abhinav Gupta, and Alexei A. Efros. Ensemble of exemplar-svms for object detection and beyond. In *ICCV*, 2011. 4
- [38] Abhinav Shrivastava, Tomasz Malisiewicz, Abhinav Gupta, and Alexei A. Efros. "data-driven visual similarity for crossdomain image matching". "ACM Transaction of Graphics (TOG) (Proceedings of ACM SIGGRAPH ASIA)", 30(6), 2011. 4
- [39] Ziwei Liu, Ping Luo, Xiaogang Wang, and Xiaoou Tang. Deep learning face attributes in the wild. In *Proceedings of International Conference on Computer Vision (ICCV)*, December 2015. 5
- [40] Yunjey Choi, Minje Choi, Munyoung Kim, Jung-Woo Ha, Sunghun Kim, and Jaegul Choo. Stargan: Unified generative adversarial networks for multi-domain image-to-image translation. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 8789–8797, 2018. 5
- [41] Zhenliang He, Wangmeng Zuo, Meina Kan, Shiguang Shan, and Xilin Chen. Attgan: Facial attribute editing by only changing what you want. *IEEE Transactions on Image Processing*, 28(11):5464–5478, 2019. 5
- [42] David Berthelot, Thomas Schumm, and Luke Metz. Began: Boundary equilibrium generative adversarial networks. *arXiv preprint arXiv:1703.10717*, 2017. 5
- [43] Tero Karras, Timo Aila, Samuli Laine, and Jaakko Lehtinen. Progressive growing of gans for improved quality, stability, and variation. *arXiv preprint arXiv:1710.10196*, 2017. 5
- [44] Takeru Miyato, Toshiki Kataoka, Masanori Koyama, and Yuichi Yoshida. Spectral normalization for generative adversarial networks. *arXiv preprint arXiv:1802.05957*, 2018.
 5

- [45] Chun-Liang Li, Wei-Cheng Chang, Yu Cheng, Yiming Yang, and Barnabás Póczos. Mmd gan: Towards deeper understanding of moment matching network. In Advances in Neural Information Processing Systems, pages 2203–2213, 2017. 5
- [46] Marc G Bellemare, Ivo Danihelka, Will Dabney, Shakir Mohamed, Balaji Lakshminarayanan, Stephan Hoyer, and Rémi Munos. The cramer distance as a solution to biased wasserstein gradients. arXiv preprint arXiv:1705.10743, 2017. 5
- [47] Tero Karras, Samuli Laine, and Timo Aila. A style-based generator architecture for generative adversarial networks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 4401–4410, 2019. 5
- [48] Karol Kurach, Mario Lučić, Xiaohua Zhai, Marcin Michalski, and Sylvain Gelly. A large-scale study on regularization and normalization in gans. In *International Conference on Machine Learning*, pages 3581–3590. PMLR, 2019. 5, 7
- [49] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In 2009 IEEE conference on computer vision and pattern recognition, pages 248–255. Ieee, 2009. 5
- [50] Andrew Brock, Jeff Donahue, and Karen Simonyan. Large scale gan training for high fidelity natural image synthesis. *arXiv preprint arXiv:1809.11096*, 2018. 5
- [51] Mario Lucic, Michael Tschannen, Marvin Ritter, Xiaohua Zhai, Olivier Bachem, and Sylvain Gelly. Highfidelity image generation with fewer labels. *arXiv preprint arXiv:1903.02271*, 2019. 5
- [52] Fisher Yu, Ari Seff, Yinda Zhang, Shuran Song, Thomas Funkhouser, and Jianxiong Xiao. Lsun: Construction of a large-scale image dataset using deep learning with humans in the loop. arXiv preprint arXiv:1506.03365, 2015. 5
- [53] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In Proceedings of the IEEE conference on computer vision and pattern recognition, pages 770–778, 2016. 5
- [54] David Arthur and Sergei Vassilvitskii. k-means++: The advantages of careful seeding. Technical report, Stanford, 2006. 5
- [55] M. Cimpoi, S. Maji, I. Kokkinos, S. Mohamed, and A. Vedaldi. Describing textures in the wild. In *Proceedings of the IEEE Conf. on Computer Vision and Pattern Recognition (CVPR)*, 2014. 7
- [56] Negar Rostamzadeh, Seyedarian Hosseini, Thomas Boquet, Wojciech Stokowiec, Ying Zhang, Christian Jauvin, and Chris Pal. Fashion-gen: The generative fashion dataset and challenge. arXiv preprint arXiv:1806.08317, 2018. 7
- [57] Phillip Isola, Jun-Yan Zhu, Tinghui Zhou, and Alexei A Efros. Image-to-image translation with conditional adversarial networks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 1125–1134, 2017. 7
- [58] Alec Radford, Luke Metz, and Soumith Chintala. Unsupervised representation learning with deep convolutional generative adversarial networks. arXiv preprint arXiv:1511.06434, 2015. 7
- [59] Zhizhong Li and Derek Hoiem. Learning without forgetting. *IEEE transactions on pattern analysis and machine intelli*gence, 40(12):2935–2947, 2017. 8