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# **XVFI: eXtreme Video Frame Interpolation**

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Figure 1. Some examples of our X4K1000FPS dataset, which contain diverse motions in 4K-resolution of 1000-fps. The numbers below the examples are the magnitude means of optical flows between two input frames in 30 fps. Please refer to the arXiv version to watch this figure as a video clip.

# Abstract

In this paper, we firstly present a dataset (X4K1000FPS) of 4K videos of 1000 fps with the extreme motion to the research community for video frame interpolation (VFI), and propose an extreme VFI network, called XVFI-Net, that first handles the VFI for 4K videos with large motion. The XVFI-Net is based on a recursive multi-scale shared structure that consists of two cascaded modules for bidirectional optical flow learning between two input frames (BiOF-I) and for bidirectional optical flow learning from target to input frames (BiOF-T). The optical flows are stably approximated by a complementary flow reversal (CFR) proposed in BiOF-T module. During inference, the BiOF-I module can start at any scale of input while the BiOF-T module only operates at the original input scale so that the inference can be accelerated while maintaining highly accurate VFI performance. Extensive experimental results show that our XVFI-Net can successfully capture the essential information of objects with extremely large motions and complex textures while the state-of-the-art methods exhibit poor performance. Furthermore, our XVFI-Net framework also performs comparably on the previous lower resolution benchmark dataset, which shows a robustness of our algorithm as well. All source codes, pre-trained models, and proposed X4K1000FPS datasets are publicly available at https://github.com/JihyongOh/XVFI.

# 1. Introduction

Video frame interpolation (VFI) converts low frame rate (LFR) contents to high frame rate (HFR) videos by synthesizing one or more intermediate frames between given two consecutive frames, and then the videos of fast motion can be smoothly rendered in an increased frame rate, thus yielding reduced motion judder [28, 24, 23, 10]. Therefore, it is widely used for various practical applications, such as adaptive streaming [45], novel view interpolation synthesis [11], frame rate up conversion [29, 5, 49], slow motion generation [18, 4, 30, 32, 27, 34] and video restoration [21, 42, 14, 41]. However, VFI is significantly challenging, which is attributed to diverse factors such as occlusions, large motions and change of light. Recent deeplearning-based VFI has been actively studied, showing remarkable performances [47, 4, 7, 37, 25, 13, 31, 50, 6, 33]. However, they are often optimized for existing LFR benchmark datasets of low resolution (LR), which may lead to poor VFI performance, especially for videos of 4K resolution  $(4096 \times 2160)$  or higher with very large motion [1, 21]. Such 4K videos often contain frames of fast motion with extremely large pixel displacements for which conventional convolutional neural networks (CNNs) do not effectively work with receptive fields of limited sizes.

To solve the above issues for deep learning-based VFI methods, we directly photographed 4K videos to construct a high-quality HFR dataset of high resolution, called X4K1000FPS. Fig. 1 shows some examples of our X4K1000FPS dataset. As shown, our videos of 4K resolution have extremely large motions and occlusions.

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Figure 2. VFI results for extreme motions. Our XVFI-Net can generate a more stable intermediate frame with very large motions than two recent SOTA methods, FeFlow [13] and DAIN [4], which are newly trained on our dataset for fair comparisons.

We also first propose an extreme VFI model, called XVFI-Net, that is effectively designed to handle such a challenging dataset of 4K@1000fps. Instead of directly capturing extreme motions through consecutive feature spaces with deformable convolution as recent trends in video restoration [13, 46, 42, 41, 20], or using very largesized pretrained networks with extra information such as contexts, depths, flows and edges [4, 50, 30, 13], our XVFI-Net is simple but effective, which is based on a recursive multi-scale shared structure. The XVFI-Net has two cascaded modules: one for the bidirectional optical flow learning between two input frames (BiOF-I) and the other for the bidirectional optical flow estimating from target to the inputs (BiOF-T). The BiOF-I and BiOF-T modules are trained in combination with multi-scale losses. However, once trained, the BiOF-I module can start from any downscaled input upward while the BiOF-T module only operates at the original input scale at inference, which is computationally efficient and helps to generate an intermediate frame at any target time instance. Structurally, the XVFI-Net is adjustable in terms of the number of scales for inference according to the input resolutions or the motion magnitudes, even if training is once over. We also propose a novel optical flow estimation from time t to those of the inputs, called a complementary flow reversal (CFR) that effectively fills the holes by taking complementary flows. Extensive experiments are conducted for fair comparison and our XVFI-Net that has a relatively smaller complexity outperforms previous VFI SOTA methods on our X4K1000FPS, especially for extreme motions as shown in Fig. 2. A further experiment on the previous LR-LFR benchmark dataset also demonstrates the robustness of our XVFI-Net. Our contributions are summarized as:

• We first propose a high-quality of HFR video dataset of 4K resolution, called X4K1000FPS (4K@1000fps) which contains a wide variety of textures, extremely large motions, zoomings and occlusions.

- We propose the CFR that can generate stable optical flow estimation from time *t* to the input frames, boosting both qualitative and quantitative performances.
- Our proposed XVFI-Net can start from any downscaled input upward, which is adjustable in terms of the number of scales for inference according to the input resolutions or the motion magnitudes.
- Our XVFI-Net achieves state-of-the-art performance on the testset of X4K1000FPS with a significant margin compared to the previous VFI SOTA methods while having computational efficiency with a small number of filter parameters. All source codes and proposed X4K1000FPS dataset are publicly available at https://github.com/JihyongOh/XVFI.

## 2. Related Work

## 2.1. Video Frame Interpolation

Most VFI methods can be categorized into optical flowor kernel-based [27, 32, 18, 30, 34, 47, 4, 1, 2, 25, 33, 31] and pixel hallucination-based [13, 46, 7, 37, 21] methods. Flow-based VFI. Super-SloMo [18] first linearly combines predicted optical flows between two input frames to approximate flows from the target intermediate frame to the input frames. Quadratic video frame interpolation [47] utilizes four input frames to cope with nonlinear motion modeling by quadratic approximation, which limits the VFI generalization when two input frames are given. It also proposes flow reversal (projection) for more accurate image warping. On the other hand, DAIN [4] gives different weights of overlapped flow vectors depending on the object depth of the scene via a flow projection layer. However, DAIN employs and fine-tunes both PWC-Net [40] and MegaDepth [26], which is computationally burdened for inferring intermediate HR frames. AdaCoF proposes a generalized warping module to deal with complex motion [25]. However, it is not adaptive to handle the frames of higher resolutions due to a fixed dilation degree, after once trained.

**Pixel Hallucination-based VFI**. FeFlow [13] has benefited from deformable convolution [9] to the center frame generator by replacing optical flows with offset vectors. Zooming Slow-Mo [46] also interpolates middle frames with the help of deformable convolution in the feature domain. However, since these methods directly hallucinate pixels unlike the flow-based VFI methods, the predicted frames tend to be blurry when fast-moving objects are present.

Most importantly, the aforementioned VFI methods are difficult to operate on the entire HR frames *at once*, due to their heavy computational complexity. On the other hand, our XVFI-Net is designed to efficiently operate on the entire 4K frame input at once with a smaller number of parameters and is capable of effectively capturing large motions.

### 2.2. Networks for Large Pixel Displacements

PWC-Net [40] is a state-of-the-art optical flow estimator that has been adopted in several VFI methods for pretrained flow estimators [47, 4, 31]. Since PWC-Net has a 6-level feature pyramid structure to have larger sizes of receptive fields, it enables to effectively predict large motions. IM-Net [34] also adopts a multi-scale structure to cover large displacements of objects in adjacent frames while the coverage is limited in the size of the adaptive filters. Despite of the multi-scale pyramid structures, the above methods lack adaptivity because the coarsest level of each network is fixed after once trained, i.e. each scale level consists of its own (not shared) parameters. The RRPN [50] shares weight parameters across different scale levels in a flexible recurrent pyramid structure. However, it only infers the centered frame, not at arbitrary time instances. So it can only synthesize recursively the intermediate frames of time at a power of 2. As a result, the prediction errors are accumulated as intermediate frames are generated iteratively between the two input frames. Therefore, RRPN has limited temporal flexibility for VFI at arbitrary target time instance t.

Distinguished from the above methods, our proposed XVFI-Net has a scalable structure with shared parameters for various input resolutions. Different from RRPN [50], the XVFI-Net is structurally divided into the BiOF-I and BiOF-T modules, which allows predicting an intermediate frame at arbitrary time t with the help of the complementary flow reversal in an efficient way. That is, the BiOF-T module can be skipped at the down-scaled levels in inference so that our model can infer the intermediate frame of 4K at once, without any patch-wise iteration unlike all other previous methods, which can be applied in real-world applications.

### 3. Proposed X4K1000FPS Dataset

Although numerous methods for VFI have been both trained and evaluated over the diverse benchmark datasets, such as Adobe240fps [39], DAVIS [35], UCF101 [38], Middlebury [3] and Vimeo90K [48], none of the datasets contains rich amounts of 4K videos with HFR. These limits the study of elaborate VFI methods required for VFI applications for targeting very high resolution videos.

To tackle the challenging extreme VFI task, we provide a rich set of 4K@1000 fps video that we photographed using a Phantom Flex $4K^{TM}$  camera with the 4K spatial resolution of  $4096 \times 2160$  at 1,000 fps, producing 175 video scenes, each with 5,000 frames by shooting for 5 seconds.

In order to select valuable data samples for VFI, we estimated bidirectional occlusion maps and optical flows of every 32 frames of the scenes using IRR-PWC [16]. The occlusion map indicates part of the objects to be occluded

Detect	Occlusion [16]			Flow magnitude [16]		
Dataset	$25_{th}$	50 <sub>th</sub>	75 <sub>th</sub>	25 <sub>th</sub>	50 <sub>th</sub>	75 <sub>th</sub>
Vimeo90K [48]	<u>6.8</u>	11.9	18.1	3.1	4.9	7.1
Adobe240fps [39]	0.8	1.7	3.2	3.8	8.9	16.3
X-TEST (ours)	2.1	5.6	17.7	23.9	81.9	138.5
X-TRAIN (ours)	6.9	<u>10.1</u>	15.7	5.5	<u>18.0</u>	<u>59.5</u>
$25_{4b}$ 50 <sub>4b</sub> and $75_{4b}$ represent percentiles of each datset						

Table 1. The occlusion and optical flow magnitude statistics of VFI datasets: 3,782 test triplets of Vimeo90K [48], randomly selected 200 clips of Adobe240fps [39], 15 clips of X-TEST and 4,408 clips of X-TRAIN.

in the next frames. The occlusion makes optical flow estimation and frame interpolation challenging [43, 4, 16]. Thus, we manually selected 15 scenes as our testset, called X-TEST, by considering the degrees of occlusion, optical flow magnitudes and scene diversity. Each scene for X-TEST simply contains one test sample that consists of two input frames in a temporal distance of 32 frames and approximately corresponds to 30 fps. The test evaluation is set to interpolate 7 intermediate frames, which results in the consecutive frames of 240 fps. For the training dataset, called X-TRAIN, we cropped and selected 4,408 clips of  $768 \times 768$ -sized and the lengths of 65 consecutive frames by considering the amounts of occlusion. More details are described in *Supplementary Material*.

Table 1 compares the statistics of datasets: Vimeo90K [48], Adobe240fps [39], our X-TEST and X-TRAIN. We estimated the occlusion range in [0,255] and optical flow magnitudes [16] between input pairs and calculated their percentiles for each dataset. As shown in Table 1, our datasets contain comparable occlusion but significantly larger motion, compared to the previous VFI datasets.

# 4. Proposed Method : XVFI-Net Framework

#### 4.1. Design Considerations

Our XVFI-Net aims at interpolating an intermediate frame  $I_t$  at an arbitrary time t between two consecutive input frames,  $I_0$  and  $I_1$ , of HR with extreme motion.

Scale Adaptivity. An architecture with a fixed number of scale levels like PWC-Net [40] is difficult to adapt to various spatial resolutions of the input video, because the structure in each scale level is *not shared* across different scale levels, so the new architecture with an increased scale depth needs to be retrained. In order to have a scale adaptivity to various spatial resolutions of input frames, our XVFI-Net is designed to have optical flow estimation starting at any desired coarse scale level, adapting to the degree of motion magnitudes in the input frames. To do so, our XVFI-Net shares its parameters across different scale levels.

**Capturing Large Motion**. In order to effectively capture a large motion between two input frames, the Feature Extrac-

tion Block of XVFI-Net first reduces the spatial resolution of two input frames by a module scale factor M via a strided convolution, thus yielding the spatially reduced feature that is then converted to two contextual feature maps  $C_0^0$  and  $C_1^0$ . The Feature Extraction Block in Fig. 3 is composed of the strided convolution and two residual blocks [15]. Then, XVFI-Net at each scale level estimates optical flows from target frame  $I_t$  to two input frames in the reduced spatial size by M. The predicted flows are upscaled ( $\times M$ ) to warp the input frames at each scale level to time t.

# 4.2. XVFI-Net Architecture

**BiOF-I module.** Fig. 4 shows our XVFI-Net architecture in scale *s*, where  $I^s$  denotes bicubicly down-scaled by  $1/2^s$ . First, contextual pyramid  $\mathbf{C} = \{C^s\}$  is recurrently extracted from  $C_0^0$  and  $C_1^0$  via a stride 2 convolution, and then utilized as an input for XVFI-Net at each scale level s (s = 0, 1, 2, ...), where s = 0 denotes the scale of the original input frames. Let  $F_{t_a t_b}^s$  denotes optical flow from time  $t_a$  to  $t_b$  at scale s.  $F_{01}^s$  and  $F_{10}^s$  are the bidirectional flows between input frames at scale s.  $F_{t_0}^s$  and  $F_{t_1}^s$  respectively.

The estimated flows  $F_{01}^{s+1}$ ,  $F_{10}^{s+1}$  from the previous scale (s + 1) are  $\times 2$  bilinearly up-scaled to be set as the initial flows for the current scale s, i.e.,  $\tilde{F}_{01}^s = F_{01}^{s+1} \uparrow_2$ ,  $\tilde{F}_{10}^s = F_{10}^{s+1} \uparrow_2$ . To update the initial flows in the current scale,  $C_0^s$  and  $C_1^s$  are first warped by the initial flows, that is,  $\tilde{C}_{01}^s = W(\tilde{F}_{01}^s, C_1^s)$  and  $\tilde{C}_{10}^s = W(\tilde{F}_{10}^s, C_0^s)$ , respectively, where W is a backward warping operation [17]. Then  $\tilde{C}_{01}^s, \tilde{C}_{10}^s, C_0^s, C_1^s$  together with  $\tilde{F}_{01}^s, \tilde{F}_{10}^s$  are fed to an auto-encoder-based BiFlownet as in Fig. 4 to output residual flows over the initial flows and a trainable importance mask z [31]. Then  $F_{01}^s, F_{10}^s$  are obtained. They are then fed as input to the BiOF-T module and are also used as the initial flows to the next scale s - 1.

**BiOF-T module**. Hereafter, we omit superscript s for the notion of feature tensors at each scale, unless mentioned. Although the linear approximation with optical flows  $F_{01}$ ,  $F_{10}$  [18] or the flow reversal of  $F_{0t}$ ,  $F_{1t}$  [47] allows to estimate the flows  $F_{t0}, F_{t1}$  at arbitrary time t, there are few shortcomings. The linear approximation is inaccurate to predict  $F_{t0}$  and  $F_{t1}$  for fast-moving objects because the anchor points of  $F_{01}$  and  $F_{10}$  are severely misaligned. On the other hand, the flow reversal can align the anchor points but *holes* may appear in estimated  $F_{t0}$  and  $F_{t1}$ . To stabilize the performance of the flow reversal, we take complementary advantages of both the linear approximation and flow reversal. So, a stable optical flow estimate from time tto 0 or 1 can be computed by a normalized linear combination of a negative anchor flow and a complementary flow, which we call a complementary flow reversal (CFR). The resulting complementary reversed optical flow maps,  $F_{t0}$ and  $F_{t1}$ , from time t to 0 and 1 are given by,



Figure 3. Adjustable and efficient scalability of our XVFI-Net framework. Even if the lowest scale depth  $S_{trn}$  during training is set to 1 in this example, inference can start from any scale level.

$$\tilde{F}_{t0}^{\mathbf{x}} = \frac{(1-t)\sum_{\mathcal{N}_0} w_0 \cdot (-F_{0t}^{\mathbf{y}}) + t \sum_{\mathcal{N}_1} w_1 \cdot F_{1\cdot(1-t)}^{\mathbf{y}}}{(1-t)\sum_{\mathcal{N}_0} w_0 + t \sum_{\mathcal{N}_1} w_1}$$
(1)

$$\tilde{F}_{t1}^{\mathbf{x}} = \frac{(1-t)\sum_{\mathcal{N}_0} w_0 \cdot F_{0\cdot(1-t)}^{\mathbf{y}} + t\sum_{\mathcal{N}_1} w_1 \cdot (-F_{1t}^{\mathbf{y}})}{(1-t)\sum_{\mathcal{N}_0} w_0 + t\sum_{\mathcal{N}_1} w_1}$$
(2)

where **x** denotes a pixel location at time t and **y** is at time 0 or 1.  $w_i = z_i^{\mathbf{y}} \cdot G(|\mathbf{x} - (\mathbf{y} + F_{it}^{\mathbf{y}})|)$  is a Gaussian weight depending on the distance between **x** at time t and  $\mathbf{y} + F_{it}^{\mathbf{y}}$  at time i (= 0 or 1) while also considering the learnable importance mask of each flow by  $z_i^{\mathbf{y}}$  [31]. Also,  $-F_{0t}^{\mathbf{y}}$  (or  $-F_{1t}^{\mathbf{y}}$ ) and  $F_{1\cdot(1-t)}^{\mathbf{y}}$  (or  $F_{0\cdot(1-t)}^{\mathbf{y}}$ ) in Eq. 1 (or Eq. 2) are defined as a negative anchor flow and a complementary flow, respectively. Furthermore, the anchor flows are normalized flows that can be calculated as  $F_{0t} = tF_{01}$  and  $F_{1t} = (1 - t)F_{10}$ to intermediate time t. It should be noted in Eq. 1 and Eq. 2 that the complementary flows are also normalized as  $F_{1\cdot(1-t)} = tF_{10}$  and  $F_{0\cdot(1-t)} = (1 - t)F_{01}$  which complementally fill the holes occurred in the reversed flows. By doing so, we can fully exploit the temporal-densely captured X4K1000FPS dataset to train our XVFI-Net for VFI at arbitrary time t. The neighborhoods of **x** are defined as,

$$\mathcal{N}_0 = \{ \mathbf{y} \mid \text{round}(\mathbf{y} + F_{0t}^{\mathbf{y}}) = \mathbf{x} \}$$
(3)

$$\mathcal{N}_1 = \{ \mathbf{y} \mid \operatorname{round}(\mathbf{y} + F_{1t}^{\mathbf{y}}) = \mathbf{x} \}.$$
(4)

To refine the bidirectional flow approximates  $\tilde{F}_{t0}$ ,  $\tilde{F}_{t1}$ , we rewarp the feature maps  $(C_0, C_1)$  to  $\tilde{C}_{t0}$  and  $\tilde{C}_{t1}$ by  $\tilde{F}_{t0}$  and  $\tilde{F}_{t1}$ , respectively. We concatenate and feed  $C_0, C_1, \tilde{C}_{t0}, \tilde{C}_{t1}$ , and  $\tilde{F}_{t0}, \tilde{F}_{t1}$  to the auto-encoder-based TFlownet as in Fig. 4 (similarly to refine  $\tilde{F}_{01}, \tilde{F}_{10}$ ). The outputs of TFlownet are used to compose refined flows  $F_{t0}, F_{t1}$ which are then bilinearly up-scaled  $(\times M)$  back to the size



Figure 4. The architecture of our proposed XVFI-Net in scale s.

of  $I_t^s$ . The flow estimation in the spatially reduced size by M has three advantages: (i) enlarged receptive fields, (ii) lowered computational costs and (iii) smooth optical flows. This strategy maximizes the benefit of flow-based VFI that can fully utilize the texture information of the original input frames by warping them with the estimated flows, compared to the hallucination-based methods that suffer from a lack of sharpness in restoration from down-scaled feature maps. The above up-scaled flows are used to warp the input frames  $I_0^s$  and  $I_1^s$  to be  $\tilde{I}_{t0}^s$  and  $\tilde{I}_{t1}^s$ , respectively. The  $C_0^s, C_1^s, \tilde{C}_{t0}^s, \tilde{C}_{t1}^s, F_{t0}^s, F_{t1}^s, I_0^s, I_1^s, \tilde{I}_{t0}^s$  and  $\tilde{I}_{t1}^s$  are all aggregated to be fed into the U-Net [36]-based Refinement Block. Then, both the generated occlusion mask  $m^s$  and residual image  $\tilde{I}_r^s$  are finally used to blend the warped frames  $\tilde{I}_{t0}^s$  and  $\tilde{I}_{t1}^s$ , which is given by,

$$\hat{I}_{t}^{s} = \frac{(1-t) \cdot m^{s} \cdot \tilde{I}_{t0}^{s} + t \cdot (1-m^{s}) \cdot \tilde{I}_{t1}^{s}}{(1-t) \cdot m^{s} + t \cdot (1-m^{s})} + \tilde{I}_{r}^{s}$$
(5)

where  $\hat{I}_t^s$  is the final result of each scale level s.

### 4.3. Adjustable and Efficient Scalability

Adjustable Scalability. Fig. 3 shows a VFI framework of our XVFI-Net that can begin from any scale level by  $\times 1/2^s$ recurrent down-scaling the contextual feature map  $C_0^0$  and  $C_1^0$ , and predicts the coarsest optical flow to capture extreme motion effectively. Then the estimated flows  $F_{01}^s$ ,  $F_{10}^s$ are transmitted to the next scale s - 1, and the flow is updated gradually to the original scale s = 0. We aim that the number of scales can be decided for inference, adaptive to the spatial resolution and degree of motion magnitudes for the input frames, even after once trained. To generalize the XVFI-Net learning for the input of any scale level, a multiscale reconstruction loss in Eq. 7 is applied for every output  $\hat{I}_t^s$  for the selected scale depth  $S_{trn}$  during training.

Efficient Scalability. As shown in Fig. 3, the computation through the BiOF-T module is always taken place at the

original scale (s = 0) during inference no matter which scale level the BiOF-I starts from, which are denoted as the arrows in the light orange color. Since  $F_{01}^s$  and  $F_{10}^s$  are the only information that passes across different scale levels through the BiOF-I module (from the previous scale to the next scale level) as shown in Fig. 3, we only pass the two optical flows recursively until reaching the original scale level. Then, the BiOF-T module processes  $F_{10}^{s=0}$  and  $F_{01}^{s=0}$ to estimate  $F_{t1}^{s=0}$  and  $F_{t0}^{s=0}$  only at the original scale level. This is architecturally very beneficial because (i) the BiOF-I module is responsible to stably capture extreme motion by recursively learning the bidirectional flows between input time instances 0 and 1 across multiple scale levels, and (ii) the BiOF-T module finely predicts the bidirectional flows in the original scale only from any target time t to times 0 and 1 based on the stably estimated flows  $F_{10}^{s=0}$  and  $F_{01}^{s=0}$ , unlike the RRPN [50].

**Loss Functions.** We adopt a multi-scale reconstruction loss to train the shared parameters of our XVFI-Net. To further encourage the smoothness of the obtained optical flow, the first-order edge-aware smoothness loss is used for  $F_{t0}^0$  and  $F_{t1}^0$  at the original scale [19]. The total loss function is a weighted sum of the two loss functions as follows:

$$\mathcal{L}_{total} = \mathcal{L}_r + \lambda_s \cdot \mathcal{L}_s \tag{6}$$

$$\mathcal{L}_{r} = \sum_{s=0}^{S_{trn}} \|\hat{I}_{t}^{s} - I_{t}^{s}\|_{1}$$
(7)

$$\mathcal{L}_s = \sum_{i=0,1} \exp(-e^2 \sum_c \left| \nabla_{\mathbf{x}} I^0_{t_c} \right|)^{\intercal} \cdot \left| \nabla_{\mathbf{x}} F^0_{ti} \right| \qquad (8)$$

where  $c, e^2$  and x denote color channel index, an edge weighting factor and a spatial coordinate, respectively.

#### **5. Experiment Results**

The proposed X-TRAIN dataset contains 4,408 clips of the sizes of  $768 \times 768$  and the lengths of 65 consecutive frames. Each training sample is randomly fetched on the fly from each clip. A training sample is defined as a

triplet with two input frames  $(I_0, I_1)$  and one target frame  $(I_t, 0 < t < 1)$ . The temporal distance between  $I_0$  and  $I_1$  is randomly selected in the range [2, 32] where  $I_t$  is also randomly determined between the selected  $I_0$  and  $I_1$ . By doing so, our training samples are stochastically well obtained by fully exploiting our X-TRAIN dataset of temporally dense video clips to learn various t accordingly.

The weights of the XVFI-Net are initialized with Xavier initialization [12] and the mini-batch size is set to 8. XVFI-Net is trained via total of 110,200 iterations (200 epochs) by using the Adam optimizer [22] with the initial learning rate of  $10^{-4}$ , reduced by a factor of 4 at [100, 150, 180]-th epoch. The hyperparameter M,  $\lambda_s$  and e are set to 4, 0.5 and 150, respectively. We also randomly crop  $384 \times 384$ -sized patches from the original size of X-TRAIN and randomly flip both spatial and temporal directions for data augmentation. Training takes about a half-day with an NVIDIA TI-TAN RTX<sup>TM</sup> GPU with PyTorch.

#### 5.1. Comparison to the Previous Methods

We compare our XVFI-Net with three previous VFI methods, DAIN [4], FeFlow [13] and AdaCoF [25], whose training codes are *publicly available*. DAIN can generate the interpolated frame at arbitrary time t at once and the latter two can only synthesize the intermediate frame at the power of 2 in an iterative manner during the inference.

For a fair comparison, we retrain the three previous methods on X-TRAIN under their original hyperparameter settings except the patch size of  $384 \times 384$  and the total iterations of 110,200. For further comparison, we also use the original pretrained models of the three methods, which are denoted as the subscript *o* to distinguish from their retrained models with the subscript f on X-TRAIN. The lowest scale depths for our XVFI-Net are set to 3 for training  $(S_{trn})$  and 3 or 5 for testing  $(S_{tst})$ . We evaluate their performances for 7 interpolated frames per scene (multi-frame interpolation  $\times$ 8) on X-TEST in terms of three evaluation metrics: PSNR, SSIM [44] and tOF [8] that measures the temporal consistency for the pixel-wise difference of motions (the lower, the better). We also evaluate each method for 7 interpolated frames per clip on the Adobe240fps dataset [39], where 200 nonuplets clips are randomly extracted with  $1280 \times 720$ (HD) at 240fps.

**Quantitative Comparison.** Table 2 shows the quantitative comparisons of the VFI methods on both X-TEST and Adobe240fps. Please note that all runtimes ( $R_t$ ) in Table 2 are measured for 1024×1024-sized frames because DAIN and FeFlow are too heavy to run for each of 4K input frames (4096×2160) *at once*. As shown in Table 2, our proposed XVFI-Net with  $S_{tst}$  set to both 3 and 5 clearly outperforms all the previous methods with large margins on both X-TEST and Adobe240fps, even though the number of model parameters (#P) of our model is significantly smaller



Figure 5. PSNR profiles for multi-frame interpolation results  $(\times 8)$  on X-TEST.

Mathada (VN)	X-TEST	Adobe240fps	#D	D
Methous (XIV)	(PSNR/SSIM/tOF)	(PSNR/SSIM)	+ <sup>π</sup> Γ ↓	$\mathbf{K}_t \downarrow$
AdaCoF <sub>o</sub> ( $\times$ 5.8)	23.90/0.727/6.89	25.26/0.785	<u>21.8</u>	0.005
$AdaCoF_{f}$ [25]	25.81/0.772/6.42	25.21/0.791	<u>21.8</u>	0.005
$FeFlow_o (\times 5.3)$	24.00/0.756/6.59	25.18/0.785	102.5	1.681
$FeFlow_f$ [13]	25.16/0.783/6.54	24.17/0.780	102.5	1.681
$DAIN_o$ (×9.3)	26.78/0.807/3.83	29.89/ <u>0.911</u>	24	1.375
$\text{DAIN}_f$ [4]	27.52/0.821/3.47	29.99/0.910	24	1.375
Ours ( $S_{tst}=3$ )	<u>28.86/0.858/2.67</u>	30.29/0.912	5.5	<u>0.074</u>
Ours ( $S_{tst}=5$ )	30.12/0.870/2.15	<u>30.18/0.911</u>	5.5	0.075

×N: The ratio of number of iterations of the original version to that of retrained version in the fair condition. #P: The number of parameters (M).  $R_t$ : The runtime on 1024-sized frames in sec.

**RED**: Best performance, <u>BLUE</u>: Second best performance.

Table 2. Quantitative comparisons on both X-TEST (4K) and Adobe240fps (HD) [39] for multi-frame interpolation ( $\times$ 8).

than those of the others. It is also worthwhile to note that our model can infer the intermediate frames of 4K *at once*, without any patch-wise iteration. In particular, XVFI-Net ( $S_{tst}$ =5) outperforms DAIN<sub>f</sub> by 2.6dB, 0.049 and 1.32 in terms of PSNR, SSIM and tOF, respectively, for X-TEST, by utilizing only 22.9% of DAIN's parameters.

Especially for the X-TEST that contains significantly extreme motions in 4K frames, our XVFI-Net can effectively capture large motion in earlier stages and then precisely interpolate the 4K input frames better than the previous methods. It is noted that FeFlow is inappropriate for large motion alignment in the feature domain, which results in blurry output and is computationally heavy for 4K input frames. In addition, the center-frame interpolation methods such as AdaCoF, FeFlow and others [50, 13, 25, 34, 32] tend to synthesize intermediate frames generally worse than those of arbitrary time VFI methods such as DAIN and XVFI-Net as shown in Fig. 5. The errors of the center-frame interpolation methods tend to be accumulated iteratively due to inaccurate predictions. On the other hand, our model can accurately generate intermediate frames at arbitrary time t. Qualitative Comparison. Fig. 6 shows the visual comparison for VFI performances. The first column images in Fig. 6 show overlapped images of two 4K input frames. As shown, huge pixel displacements are observed between two input frames, which is very challenging for VFI. The interpolated



Figure 6. Visual comparisons for VFI results (t = 0.5) on X-TEST for our and retrained SOTA methods with X-TRAIN. (\*,\*): occlusions and optical flow magnitudes between the two input frames measured by [16], respectively. *Best viewed in zoom*.



Figure 7. Approximated optical flows  $F_{t0}$  by three different flow approximation methods. (a) Linear combination, (b) flow reversal, (c) CFR (proposed). *Best viewed in zoom*.

results in Fig. 6 correspond to the center time (t = 0.5) of the two input frames which is the most challenging frame interpolation. As shown in Fig. 6, our XVFI-Net ( $S_{tst} = 5$ ) surprisingly captures very complex structures of objects with extremely fast motions, which are failed by all the previous methods.

### **5.2.** Ablation Studies

Flow Approximation. We compare the three flow approximations that enable to produce intermediate frames at arbitrary t: (a) the linear approximation [18] with  $F_{01}$ ,  $F_{10}$ , (b) flow reversal [47] of  $F_{0t}$  and  $F_{1t}$ , and (c) our proposed complementary flow reversal (CFR). In this comparison, we approximated  $F_{t0}$  with the three methods using the estimated optical flows  $F_{01}$ ,  $F_{10}$  which are obtained by IRR-PWC [16] between the input  $I_0$  and  $I_1$ . The importance mask z's in Eq. 1 and 2 are excluded in this comparison. Fig. 7 visualizes an example of the approximated optical flows by the three methods and the pseudo ground truth which is estimated between  $I_t$  and  $I_0$  by IRR-PWC [16]. To evaluate

the flow approximations quantitatively, the averaged endpoint errors (EPEs) for the three methods are calculated between the approximated flows and the pseudo ground truth on the testset of Vimeo90K [48], which are shown in Table 3. The linear approximation reveals misalignment due to the different anchor frames, which is indicated by yellow arrows in Fig. 7. The flow reversal resolves the misalignment problem, but is inferior to the linear approximation because it causes holes that are not projected from any flow vector, as shown in the second optical flow map (red arrows). Also, the EPE value of the flow reversal is the worst among the three methods. On the other hand, our proposed CFR can appropriately fill in the holes since the bidirectional flows complement each other, as shown in Fig. 7, which is consistent with the lowest EPE value of CFR in Table 3.

In order to investigate the efficacy of the proposed CFR for VFI, we trained three VFI models from scratch by adopting each of the three flow approximations in their BiOF-T modules, *without* any help of pretrained networks. The lowest scale depths for both training  $S_{trn}$  and test  $S_{tst}$  are set to 3. The VFI performances on our X-TEST (PSNR/SSIM/tOF) for the three models are listed in Table 3, showing a superiority of our proposed CFR.

Adjustable Scalability. The lowest scale depth  $S_{tst}$  for the inference can be adaptive to the degree of motion magnitudes and spatial resolution of the input frames, even after once trained, as shown in Fig. 3. We show the adjustable scalability of our framework with  $S_{trn} = 1, 3, 5$  for  $S_{tst} = 1, 3, 5$ . For this, we train XVFI-Net variants by fully utilizing  $512 \times 512$ -sized patches because the spatial resolution of the training inputs should be multiple of 512 for  $S_{trn} = 5$ 

Metrics Methods	EPE↓	PSNR↑	SSIM↑	tOF↓
(a) Linear comb.	0.0752	28.73	0.8518	2.89
(b) Flow reversal	0.0892	28.30	0.8425	2.98
(c) CFR (ours)	0.0721	28.86	0.8582	2.67

Table 3. The endpoint error (EPE) between the approximated  $F_{t0}$  and the pseudo ground truth is obtained by IRR-PWC [16] on Vimeo90K [48] testset. Note that the VFI performances are measured on X-TEST in terms of PSNR, SSIM and tOF for three models that adopt each approximation method.

	$(PSNR(dB)\uparrow / SSIM[44]\uparrow / tOF[8]\downarrow)$			
Strn	1	3	5	
1	26.85/0.806/4.90	28.40/0.852/3.46	27.14/0.842/3.69	
3	23.61/0.729/6.56	29.22/0.863/2.68	30.35/0.879/1.98	
5	22.37/0.699/6.71	23.70/0.724/6.39	29.48/0.864/2.08	
<b>RED</b> : Best performance of each row				

Table 4. Ablation study on adjustable scalability depending on the lowest scale depth  $S_{trn}$  and  $S_{tst}$  measured on X-TEST.

where the number 512 is determined as  $2^{S_{trn}=5} \times M(=4)$  $\times$  4 (via the bottlenecks of the autoencoders). Table 4 compares the performances of the XVFI-Net variants. As shown in Table 4, the performances are generally boosted by increasing the value of  $S_{tst}$  with the help of effectively enlarging receptive field sizes and elaborately refining the resulting flows, especially in capturing extremely large motions and detailed structures. This trend is also observed in Table 2 for the XVFI-Net trained with  $384 \times 384$ -sized patches of  $S_{trn} = 3$ . Furthermore, as shown in the rightmost four columns of Fig. 6, the details of the objects, letters and textures are more precisely synthesized for  $S_{tst} = 5$ than 3 qualitatively. Both quantitative and qualitative results clearly show the effectiveness of the XVFI-Net's adjustable scalability. On the other hand, the occlusions and flow magnitudes of the Adobe240fps dataset [39] are much smaller than those of X-TEST as shown in Table 1. It is noted in Table 2 that our XVFI-Net with  $S_{tst} = 3$  shows better performance than that with  $S_{tst} = 5$  on the Adobe240fps dataset with smaller resolutions than X-TEST, which also clearly supports the efficacy of our adjustable scalability.

**Robustness of our XVFI-Net Framework**. To show the robustness of our XVFI-Net framework for LR-LFR benchmark dataset, we construct a variant of XVFI-Net, called XVFI-Net<sub>v</sub>, with M = 2 for the dataset with lower resolution frames. The XVFI-Net<sub>v</sub> is then trained on a standard VFI dataset that is the Vimeo90K [48] training set with 51,313 triplets (t = 0.5) of  $448 \times 256$  size. The training went through 200 epochs with randomly cropped  $256 \times 256$ -sized patches and a mini-batch size of 16, where both  $S_{trn}$  and  $S_{tst}$  are set to 1. We compare our XVFI-Net<sub>v</sub> with four SOTA methods: DAIN [4], FeFlow [13], AdaCoF [25] and BMBC [33], where their pretrained models and testing



Figure 8. PSNR/SSIM vs runtime (s) on Vimeo90K [48] with model size (M) indicated in each circle.

code are publicly available. Fig. 8 shows the PSNR/SSIM and runtime (s) performances of our and SOTA methods with their model sizes (M) evaluated on Vimeo90K testset. As shown, our XVFI-Net<sub>v</sub> outperforms BMBC, DAIN and AdaCoF with a significantly smaller model size (5.5 million parameters), by taking advantage of the recursive multi-scale and shared structure. However, the XVFI-Net<sub>v</sub> shows lower performance than that of FeFlow but has a much smaller model size only with 5.4% of the number of the FeFlow's parameters, thus leading to about ×7 faster runtime. As a result, our XVFI-Net framework designed for high-resolution VFI with extremely large motion shows its robustness to the LR-LFR benchmark dataset by simply adjusting module scale factor M,  $S_{trn}$  and  $S_{tst}$ .

# 6. Conclusion

We first proposed a high-quality HFR dataset in HR, called X4K1000FPS with a wide range of motions. The proposed XVFI-Net can handle large pixel displacements with an adjustable scalability for inference to cope with the input resolutions or the motion magnitudes, even if training is once over. The XVFI-Net showed state-of-the-art performance on HR datasets compared to the previous methods and its robustness to the LR-LFR benchmark dataset.

Although our proposed X4K1000FPS dataset was obtained by using one single camera, such an extreme HFR 4K dataset is very valuable for the research community of VFI because such kinds of cameras are few. Besides, we delicately select clips as X-TRAIN/X-TEST to be publicly available by considering both occlusions and flow magnitudes for a new challenging VFI task, called the eXtreme Video Frame Interpolation (XVFI). We hope that this research would be a valuable milestone to extend the current VFI for more recent real-world applications with HR video.

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