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# Distracting Downpour: Adversarial Weather Attacks for Motion Estimation

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## Abstract

Current adversarial attacks on motion estimation, or optical flow, optimize small per-pixel perturbations, which are unlikely to appear in the real world. In contrast, adverse weather conditions constitute a much more realistic threat scenario. Hence, in this work, we present a novel attack on motion estimation that exploits adversarially optimized particles to mimic weather effects like snowflakes, rain streaks or fog clouds. At the core of our attack framework is a differentiable particle rendering system that integrates particles (i) consistently over multiple time steps (ii) into the 3D space (iii) with a photo-realistic appearance. Through optimization, we obtain adversarial weather that significantly impacts the motion estimation. Surprisingly, methods that previously showed good robustness towards small per-pixel perturbations are particularly vulnerable to adversarial weather. At the same time, augmenting the training with non-optimized weather increases a method's robustness towards weather effects and improves generalizability at almost no additional cost. Our code is available at https://github.com/cv-stuttgart/DistractingDownpour.

## 1. Introduction

Adversarial attacks that pose a severe threat to neural networks have recently been introduced in the context of optical flow. There, the goal is to compute the pixel-wise 2D motion f between two consecutive frames  $I_1$  and  $I_2$  of an image sequence over time. Current attacks on optical flow [1, 17, 31, 36, 37] modify these two frames in the 2D space and consequently ignore the actual 3D geometry of the scene as well as the objects moving within. Moreover, when modifying pixels, they impose bounds on the perturbation's  $L_p$  norm rather than imposing visual constraints, which yields attacked images that lack naturalism. Therefore, robustness analyses with these attacks might not necessarily reflect the robustness of optical flow methods in the



Figure 1. Weather attacks with *adversarial fog, snow, rain* and *sparks* to perturb optical flow estimation with GMA [15]. Our weather attacks obey the 3D geometry and camera motion, which is visible in the dynamic motion blur.

real world – where perturbations are more likely to appear in the form of weather phenomena.

This work investigates whether naturally occurring weather effects like snow, rain or fog can be manipulated to serve as adversarial samples for motion estimation. However, simulating weather in this context requires special care: First, the motion of weather elements should be consistent with the 3D geometry of the scene. Snowflakes should disappear behind objects and their falling distance should appear larger when closer to the camera. Second, their motion should be coherent in time. A raindrop should fall from top to bottom over the first and second frame, and a fog cloud between two objects should remain there – even if the camera moved or rotated.

Taking all this into account, we propose an adversarial attack framework that augments images with particlebased weather effects that feature a high degree of realism: We create weather particles with a view-consistent 3D motion over time, insert them into the 3D scene in a depthaware manner, and ensure photo-realism through visual effects. This enables us to generate adversarially manipulated weather that significantly deteriorates optical flow predictions, while still satisfying the spatiotemporal and visual constraints of naturalistic weather. Our proposed augmentation and attack procedure can generate a wide range of particle effects, where single particles or super-particles move independently of the remaining scene content. Fig. 1 shows examples of adversarial snowflakes, rain streaks, fire sparks and fog clouds, that differ in size, speed or motion blur, color and transparency.

Contributions. Our contributions are three-fold:

- (i) We present a differentiable particle-to-scene rendering framework that generates realistically moving particles in the 3D scene over multiple time steps. It supports a multitude of particle effects ranging from rain and snow over sparks to mist and fog.
- (ii) Based on this differentiable rendering framework, we devise the first adversarial weather attacks for optical flow. They optimize 3D spatial positions and color properties of particles in the scene rather than 2D perpixel perturbations, resulting in highly realistic images with regard to particle motion and appearance.
- (iii) While being visually indistinguishable from benign weather augmentations, our adversarial weather achieves significant degradations of optical flow predictions. Interestingly, this particularly holds for methods with high robustness towards small  $L_p$  perturbations.

## 2. Related work

Tab. 1 provides an overview of weather attacks or spatiotemporal weather augmentations, without direct links to motion estimation and optical flow. Before we discuss these methods in more detail, we review attacks and robustness towards weather for motion estimation with optical flow.

**Optical flow attacks and robustness to weather.** Current optical flow methods based on neural networks are susceptible to adversarially modified input images, which dramatically alter the attacked flow prediction. Existing adversarial attacks on optical flow methods generate either perturbations with small  $L_p$  norms [1, 17, 36, 37] or adversarial patches [31]. Koren *et al.* [17] add a constraint to modify semantically coherent pixels only, but none of the attacks introduces geometrical constraints for plausible motion in the 3D space or over time. Regarding the robustness of optical flow towards weather conditions, few methods explicitly consider rain [18, 19], snow [34] or fog [49, 50]. However, adversarial attacks have not yet been used to assess the robustness of optical flow methods towards weather effects.

Adversarial weather attacks. In contrast, adversarial attacks that imitate weather effects have been investigated for

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Adversarial weather attacks								
Sava et al. [35]	) Inti	$\bullet \bullet \circ$	1	-	-			
Zhai et al. [52]	Sim	•••	1	-	-			
Marchisio et al. [23]	Sin 🗰	000	1	-	-			
Gao et al. [8]	)m 🗰	$\bullet \circ \circ$	1	-	-			
Wang et al. [44]	¥	$\bullet \bullet \bigcirc$	1	-	-			
Kang et al. [16]	₩ *	$\bullet \bullet \circ$	1	-	-			
Machiraju et al. [21]		$\bullet \bullet \bigcirc$	1	-	-			
Gao et al. [7]		•••	1	1	-			
Realistic	weather	augmenta	tions					
Rousseau et al. [33]		•00	-	1	-			
Starik & Werman [38]	)mi	$\bullet \bullet \circ$	-	1	-			
Volk et al. [41]	Sim	•••	-	1	1			
Garg & Nayar [9]	Sim	•••	-	1	1			
Halder et al. [10]	Ser III	$\bullet \bullet \circ$	-	1	1			
Tremblay et al. [40]	Ser III	•••	-	1	1			
von Bernuth et al. [42]	₩ *	•••	-	1	1			
Wiesemann & Jiang [46		•••	-	1	-			
Ours	₩111 ₩	•••	1	1	1			

Table 1. Generating rain  $\Im$ , fog  $\blacksquare$  and snow \* in images. The *methods* may support adversarial *attacks*, respect the scene's *3D* geometry or ensure temporal consistency over frames.

classification [7,8,16,23,53], object detection [8,35,52], instance segmentation [8], human pose estimation [44] or autonomous steering [21]. They range from rain [8,23,35,52] over snow [8, 16, 23] to fog [7, 16, 21] and shadows [53]. As these weather attacks have only been applied to single images rather than sequences, they do not consider temporal consistency. With exception of [7], they also neglect the 3D scene geometry. Both shortcomings prevent their application to realistic motion estimation scenarios. Moreover, the visual results of weather attacks are often only moderately convincing [16, 23] compared to conventional, nondifferentiable rendering of weather effects [9,40,42]. Weather effects and attack capabilities are summarized in Tab. 1.

**Realistic weather augmentations.** Before applying any vision-based method in the real world, testing its performance under non-perfect weather conditions is crucial. As a result, there are numerous augmentations to transform clean images into their bad-weather counterparts, *e.g.* via modeled distributions [11, 28], generative networks [20, 29, 32, 43, 45, 51], or classical rendering techniques [40, 42].

However, only a few augmentations respect the 3D geometry of the scene and, ideally, create time-consistent effects for realistic motion of weather across multiple frames and camera perspectives, see Tab. 1. All such augmentations use classical rendering because generative mod-



Figure 2. Model for particle motion in the 3D space.

els [20,32,45] cannot ensure the spatiotemporal consistency of their generated effects. Augmentations that respect both, 3D geometry and temporal consistency were proposed for rain [9,41], rain & fog [10,40], or fog & snow [42]. Augmentations that respect only the 3D geometry but not the temporal consistency exist for rain [33,38] and fog [46]. To ensure a realistic 3D motion in time, our attack explicitly models the trajectory of weather particles, which is close in spirit to the augmentation of Halder *et al.* [10], and its extension by Tremblay *et al.* [40]. However, unlike all discussed rendering approaches, our augmentation is differentiable and thus can readily be used for adversarial attacks.

#### **3.** Adversarial weather for motion estimation

To study the robustness of optical flow methods towards weather effects, we design an adversarial attack framework that augments image sequences with particle-based weather. There, we augment an image sequence with parametrized particles to simulate snowflakes, rain streaks or fog clouds of realistic appearance and motion. Then, we optimize the particle parameters to cause wrong flow predictions with these snowy, rainy or foggy images.

## 3.1. Particle-based weather augmentation

The generation of spatiotemporally consistent and visually appealing weather imposes several constraints on the particles: Because motion estimation detects moving objects in a 3D scene, a simple 2D animation of the weather particles in the image plane is not realistic enough. Instead, we model their 3D motion, which also respects object depth and camera motion. Moreover, expanding our pursuit of realism to the appearance of the weather effects, the particles are integrated with appropriate visual effects. These include an occlusion-aware depth placement as well as out-of-focus and motion blur. Finally, the parametrized particles need to be rendered in a differentiable manner to allow their adversarial optimization.

To create weather-augmented 2D images  $I_1, I_2$ , we initialize 3D particles and then render them into the images. During the initialization, we generate a fixed set of particles



Figure 3. Breakdown of our realistic snow rendering.

 $\mathcal{P}$  in the 3D scene and equip them with properties: initial 3D positions  $p_1$ , 3D motion m, 3D offsets  $\delta_{p_1}$  before and  $\delta_{p_2}$  after the motion, shapes, scaling, color  $\gamma$  and transparencies  $\theta$  (see Fig. 2 for the motion model). Here,  $p_1$ , m,  $\delta_{p_1}$ ,  $\delta_{p_2} \in \mathbb{R}^3$  are vectors and  $\gamma, \theta \in \mathbb{R}$  scalars. For the differentiable rendering of particles in both frames, we make use of the 3D scene information and assume that a depth map of the scene  $D \in \mathbb{R}^{H \times W}$ , camera poses  $T_1, T_2 \in SE(3)$  and a camera projection matrix P are given. Below, we describe initialization and rendering in more detail.

Weather particle initialization. To initialize the particle positions, we uniformly sample a fixed number of points  $p_1$ from the 3D scene that is visible in the first frame  $I_1$  or – after adding the 3D motion m – in the second frame  $I_2$ . Every particle is assigned a 2D gray-scale particle template  $B \in \mathbb{R}^{h \times w}$  (billboard), randomly sampled from a template library and rotated by a random angle (Fig. 3, row 1). Then, each particle template is scaled by its particle's inverse depth (row 2), and the particle transparency  $\theta$ is set to a depth-dependent value (rows 3). Finally, we generate realistic out-of-focus blur by convolving the particle template with a disk-shaped point spread function (row 4).

Weather particle rendering. We render the particles with their associated motion blur, 3D positions, colors and transparencies in the given input frames in four steps, detailed below: We initially add motion blur particles, then project all particle templates onto the image plane, subsequently handle occlusions and finally update the pixels with the colored particle template.

First, if motion blur is added, each initial particle is replaced by K particles. These are evenly spaced along the 3D motion vector and their transparency is reduced to  $\frac{1}{K}$ ; Otherwise, the rendering proceeds as described below. In contrast to simple 2D approximations, this true motion blur respects 3D motion and camera motion (Fig. 3, row 5).

Second, for each particle, we compute the 2D points in both frames from its position in 3D. This yields the center positions  $p_1^I$ ,  $p_2^I \in \mathbb{R}^2$  of the 2D particle templates in the 2D images  $I_1$ ,  $I_2 \in \mathbb{R}^{H \times W \times 3}$ . Using the camera projection matrix P and the relative transformation matrix  $T_{\text{rel}} = T_2 T_1^{-1}$ , we project the 3D points and their motion-displaced positions into the first and second frame, respectively:

$$p_1^I = P(p_1 + \delta_{p_1}),\tag{1}$$

$$p_2^I = P(T_{\rm rel}(p_1 + \delta_{p_1}) + (m + \delta_{p_2})).$$
(2)

Because this maps the template to subpixel locations, interpolating the 2D particle templates at the true pixel locations becomes necessary. Using bilinear interpolation enables differentiation w.r.t. the 3D particle positions.

Third, we handle occlusions by multiplying the particle template with a visibility map. The visibility map  $V \in \mathbb{R}^{h \times w}$  uses a scene depth map  $D \in \mathbb{R}^{h \times w}$ , cropped to the location of B, and the particle depth  $d \in \mathbb{R}$  per camera:

$$V_t = (1 + e^{\beta(d_t - D_t)})^{-1}$$
 for  $t = 1, 2.$  (3)

This sigmoid function is  $\approx 1$  (full visibility) for particles whose depth is smaller than the scene depth, and  $\approx 0$  (full occlusion) otherwise. When the depths are similar, it creates a smooth transition to allow differentiation. We use sharper transitions  $\beta = 250$  for pure rendering and smoother ones  $\beta = 30$  for differentiation. Overall, this yields a realistic, occlusion-aware scene integration (Fig. 3, row 5).

Fourth and last, the particle color templates can be applied to the previously computed pixel positions. Our rendering framework supports two color modes for this: additive color blending and alpha blending. Additive blending creates a brightening effect (Fig. 3, last row left), similar to colored light sources, by updating the pixel color as

$$I_c = I_c + \sum_{j \in \mathcal{P}} \gamma_c^j \theta^j B^j \quad \text{for } c = \text{R,G,B.}$$
(4)

For each particle,  $\gamma_c$  is the color per channel,  $\theta$  the transparency scaling and *B* the template, which itself is a transparency map. In contrast, alpha blending creates more "solid" particles (Fig. 3, last row right) by weighting background and particle color according to particle transparency.

We use Meshkin's method [27] for an order-independent alpha blending that can process all particles in parallel:

$$I_c = I_c \left( 1 - \sum_{j \in \mathcal{P}} \theta^j B^j \right) + \sum_{j \in \mathcal{P}} \gamma_c^j \theta^j B^j \text{ for } c = \mathbf{R}, \mathbf{G}, \mathbf{B}.$$
(5)

## 3.2. Adversarial weather optimization

After the particles  $\mathcal{P}$  are initialized and rendered, we adversarially optimize certain weather parameters to change the output  $\check{f}$  of optical flow networks towards a desired target flow  $f^T$ . In this context, we consider the particle motion offsets  $\delta_{p_1}$  before and  $\delta_{p_2}$  after the motion as well as transparency  $\delta_{\theta}$  and color  $\delta_{\gamma}$  offsets. Other parameters like initial 3D positions, 3D motion and 2D template are fixed. To ensure a valid range of color  $\gamma$  and transparency  $\theta$  values after the optimization, we transform these bounded variables to unbounded ones  $\eta_{\gamma}$ ,  $\eta_{\theta}$  via an atanh-transformation [5]

$$\eta_{\xi} = \operatorname{atanh}(2\xi - 1), \quad \xi = \theta, \gamma \tag{6}$$

and optimize  $\eta_{\gamma} + \delta_{\gamma}$  and  $\eta_{\theta} + \delta_{\theta}$  in this domain. Then, our loss function measures the difference between initial and attacked flow via the average endpoint error (AEE) [36]:

$$\mathcal{L}(\check{f}, f^T, \mathcal{P}) = \operatorname{AEE}(\check{f}, f^T) + \sum_{t \in 1, 2} \frac{\alpha_t}{|\mathcal{P}|} \sum_{j \in \mathcal{P}} \frac{\|\delta_{p_t}^j\|_2^2}{d_t^j}.$$
 (7)

Additionally, this loss restricts the magnitude of the motion offset via an  $\alpha$ -balanced MSE-like term, where  $|\mathcal{P}|$  is the number of particles. It allows larger offsets  $\delta_{p_1}$ ,  $\delta_{p_2}$  for distant snowflakes, as the same 3D motion in the background yields smaller 2D offsets than in the foreground. Hence, we encourage similar motion offsets in the rendered 2D images by scaling the offsets with the inverse particle depth d.

## 4. Experiments

In several experiments, (i) we demonstrate our augmentation framework and identify weather that strongly impacts the optical flow estimation, (ii) we attack current optical flow methods with adversarially optimized particles to evaluate their sensitivity and (iii) we augment training data with snow to improve quality and robustness towards weather. A full list of parameters for the experiments is given in the supplement. Our PyTorch framework is available at https://github.com/cv-stuttgart/DistractingDownpour.

In the experiments, we augment frames from Sintel [4], a standard optical flow dataset providing depth and camera information. We calculate the adversarial robustness  $AEE(f, \check{f})$  [36], which measures how the benign optical flow f on unchanged images differs from the optical flow on weather-augmented images  $\check{f}$ . For robust methods, the output should only change proportional to the input. This is

		0	æ	Her.	¢,	4.	
W	eather	47°	ET L	593	Phi	CIM	÷ <sup>¢</sup>
	1000	3.94	5.28	3.55	1.39	1.16	0.83
les	2000	7.58	7.94	5.33	2.97	2.51	1.86
rtic	3000	11.95	10.29	6.75	5.03	4.14	3.27
$\mathbf{Pa}$	4000	17.01	12.35	7.75	7.40	5.91	4.42
	5000	23.42	14.62	8.67	9.81	7.91	5.53
н	0.0	11.95	10.29	6.75	5.03	4.14	3.27
рĮ	0.0375	15.60	12.95	6.44	4.04	3.22	3.17
ion	0.075	15.01	13.35	5.78	3.90	3.04	3.22
Iot	0.1125	13.27	12.97	5.30	3.78	2.76	2.73
	0.15	10.86	11.52	4.64	3.50	2.49	2.05
d.	white	10.03	10.70	4.95	3.88	3.74	2.93
-pl	red	9.41	9.03	3.14	2.72	2.56	2.74
rα	green	6.81	8.46	2.84	2.44	2.35	2.11
olc	blue	6.32	8.18	2.67	2.69	2.76	1.85
0	color	8.20	8.14	3.22	2.91	3.17	2.39
ive	white	14.05	14.68	6.47	5.49	4.63	4.68
diti	red	12.57	12.07	4.21	3.74	2.95	3.03
ad	green	9.02	9.64	3.68	3.16	2.76	2.56
oloi	blue	7.84	10.47	3.37	3.52	3.31	2.30
ŭ	color	11.17	11.50	4.36	4.11	3.75	3.18
	small	5.48	5.52	4.41	4.58	4.41	4.47
ze	medium	4.45	4.47	5.63	3.04	3.03	2.50
Si	large	2.23	2.91	3.51	1.17	1.16	0.92
	fog	4.72	5.25	5.87	3.59	3.66	3.24

Table 2. Robustness AEE $(f, \tilde{f}) \downarrow [36]$  of particle-based weather augmentations for *optical flow methods* on Sintel train [4], worst robustness is bold. " $\alpha$ -bld." is "alpha blending". The main augmentations, highlighted in grey, are from top to bottom: snow, rain, sparks and fog. They are visualized in Fig. 4.

formalized by the Lipschitz constant (the concept underlying adversarial robustness), which allows robustness comparisons for input changes of similar magnitude. Note that this robustness definition is independent of the ground truth optical flow, which would be ambiguous for blurred, semitransparent particles using the classical definition of optical flow. Following [36], we select RAFT [39] & GMA [15], FlowNet2 (FN2) [14] and SpyNet [30] as optical flow methods with either high quality & low robustness, medium quality and robustness or low quality & high robustness, respectively. Additionally, we consider FlowFormer (FF) [13] for its transformer architecture and its top results, and Flow-NetCRobust (FNCR) [37] for its robustified design.

#### 4.1. Weather augmentations

To observe how *random augmentations* change the predictions of optical flow methods, we first investigate the impact of various particle effects on Sintel [4] data and select default configurations for snow, rain, sparks and fog.



Figure 4. Visual examples for *snow, rain, sparks* and *fog* augmentations on a single frame for highlighted effects from Tab. 2. Note the realistic motion blur (birds-eye view) in column 1 row 4.

Then, we illustrate our flexible rendering on further datasets and finally discuss how augmenting realistic datasets with weather differs from augmenting the synthetic Sintel data.

**Particle parameters for weather creation.** We create diverse weather effects through complex hyper-parameter combinations in our rendering framework to test their effect on flow predictions. The hyperparameters listed in Tab. 2 are the most prominent ones that were altered, *i.e.* the number of particles, the motion blur length, the color (with different blending modes) and the size. A full list of altered parameters is provided in the supplement.

Tab. 2 summarizes the robustness of optical flow methods on particle-augmented Sintel training data without adversarial optimization. Visualizations for all parameter setups are in the supplement. Being most sensitive to the number of particles, all methods change their prediction strongest when many particles are present. The sensitivity also increases for non-transparent effects, e.g. for motion blur: 0.0 or particle size: small. Also, large color offsets on multiple channels are strongly perturbing, *i.e.* most for white or random colors. Additive blending perturbs more than alpha blending, but the ranking across colors is the same for both color-blending methods. To summarize, optical flow methods change their predictions significantly in the presence of many small, bright particles, which do not exist in the standard training datasets [4,6,24,26]. However, we find that accurate methods like FlowFormer, RAFT or GMA are more robust, already hinting at an improved particle recognition that is discussed in the next subsection.

Because the most effective configurations, *i.e. motion blur: 0.0, color additive: white* and *size: small*, all basically represent snow, we also select setups that represent



Figure 5. Example augmentations for *KITTI* [26] and *Spring* [25] datasets, with snow (top) and rain (bottom).

Augment.	ET22	FICE	SPILLE	PAFT	GMA	÷ <sup>¢</sup>
snow	8.32	7.71	5.49	3.08	3.27	4.21
rain	3.70	4.99	3.59	1.51	1.91	2.67
sparks	4.16	4.28	3.15	1.43	1.91	2.73
fog	7.30	7.20	11.48	2.98	3.25	4.83

Table 3. Robustness  $AEE(f, \tilde{f})$  [36] of random particle-based weather augmentations for *optical flow methods* on KITTI train [26], worst robustness is bold. The results correspond to the highlighted weather augmentations in Tab. 2 on the Sintel dataset.

other weather effects for further experiments. Hence, we choose **snow** (*particles: 3000*), **rain** (*motion blur: 0.15*), **sparks** (*color additive: red*) and **fog** (*size: fog*) as representative effects, which are highlighted gray in Tab. 2 and illustrated in Fig. 4. Note that for snow, *particles: 3000* is computationally more efficient than the most perturbing configuration *particles: 5000*.

Augmenting different datasets. Even though we focus on Sintel, our rendering approach also permits the augmentation of other datasets. Augmented samples from KITTI [26] and Spring [25] are shown in Fig. 5. For KITTI, we use interpolated depth maps and estimate camera poses from the 3D motion in rigid parts of the scene [2].

Weather augmentations on real-world data. To test how well our experiments on synthetic Sintel data transfer to real-world data, we evaluate the robustness values [36] AEE $(f, \check{f})$  on weather-augmented realistic data from the KITTI train dataset [26]. Tab. 3 summarizes the robustness values for all optical flow methods on KITTI data with random augmentations using snow, rain, sparks and fog. Compared to the Sintel augmentations in Tab. 2, snow, rain and sparks (which are based on additive color-rendering) behave similarly, *i.e.* snow is the most effective, sparks and rain have comparable strength.

In contrast, fog has a larger effectiveness on KITTI as it obfuscates more objects because the dataset has fewer foreground objects and more scene depth than Sintel. An-

Parameters	ET22	FICE	SPYLet	PAFT	GMA	ŕ
Initial	10.23	10.68	4.42	3.80	3.77	2.56
$ \begin{array}{c} \delta_{p_1} \\ \delta_{p_2} \\ \delta_{\gamma} \\ \delta_{\theta} \end{array} $	13.54 11.99 12.86 11.70	15.65 14.21 15.95 14.45	7.08 5.64 7.52 6.75	7.39 5.83 6.00 5.29	8.64 6.69 7.58 6.24	5.33 4.04 4.74 3.56
$ \begin{array}{c} \delta_{p_1,p_2} \\ \delta_{\gamma,\theta} \end{array} $	$\frac{14.08}{14.06}$	15.87 <b>16.71</b>	7.71 <b>8.94</b>	<u>8.27</u> 7.39	<u>9.42</u> 8.99	5.49 <b>5.84</b>
$\delta_{p_1,p_2,\gamma,\theta}$	14.23	16.01	7.78	8.32	9.50	5.71

Table 4. Adversarial robustness AEE $(f, \tilde{f}) \downarrow [36]$  of adversarial particles, optimized for combinations of *particle parameters*  $\delta_{p_1}$ ,  $\delta_{p_2}$ ,  $\delta_{\gamma}$  and  $\delta_{\theta}$  on Sintel-tr115. *Initial* measures the robustness of randomly initialized particles. The most vulnerable setup is bold.

other potential cause for its larger effectiveness is its additive color blending in combination with the lighter colors in KITTI scenes. The scenes are often captured in bright or sunny conditions, where further brightening through alphablending would cause less color change. However, real situations with snow or rain in bright sunshine are not very common. Therefore, we focus our subsequent evaluation on Sintel data due to its dense depth fields but have seen that results on Sintel data can generally be transferred to real-world scenarios.

## 4.2. Adversarial weather attacks

With our framework to generate natural weather effects, we now evaluate the *attack capabilities* of this differentiable weather. First, we investigate the sensitivity of optical flow methods toward optimizing different particle parameters. Second, we attack them with snow, rain, sparks and fog from the previous section. Third and last, we compare the effectiveness of a non-L<sub>p</sub> snow attack to previous L<sub>p</sub> attacks on optical flow. All attacks use  $\alpha_1 = \alpha_2 = 1000$  in the loss, Adam with learning rate 1e-5 and, following [36], a zero-flow target  $f^T = 0$  which yields a white flow visualization.

**Investigation of weather attack parameters.** To understand the impact of adversarial particles on optical flow, we consider artificial weather, initialized with 3000 gray particles that fall down without motion blur. Each particle starts with own initial values  $(p_1, p_2, \gamma, \theta)$  without offsets  $\delta_{p_1} = \delta_{p_2} = \delta_{\gamma} = \delta_{\theta} = 0$ . Then, we adversarially optimize the offsets per particle, *i.e.* the positions before the motion  $\delta_{p_1}$ , the positions after the motion  $\delta_{p_2}$ , the colors  $\delta_{\gamma}$  and the transparencies  $\delta_{\theta}$ . For optimizing  $\delta_{\gamma}$ ,  $\delta_{\theta}$  and  $\delta_{\gamma,\theta}$ , we set the learning rate to 1e-3 and use a subset "Sintel-tr115" with 115 frame pairs (the first five per scene) of Sintel-train.

Tab. 4 summarizes the adversarial robustness for the dif-



Figure 6. Qualitative results for weather attacks on optical flow predictions for FlowNet2 [14], FlowNetCRobust [37], SpyNet [30], RAFT [39], GMA [15] and FlowFormer [13] (*top left to bottom right*). Images from the Sintel final dataset, with *random* initialization and after *adversarial* weather optimization towards zero-target (white flow). See the supplement for more visualizations.

ferent optimization parameters on all tested optical flow methods. Considering single parameters, the particle offset  $\delta_{p_1}$  before the motion has the strongest influence. That motion offsets have the strongest influence on motion estimation is intuitively plausible. However, our motion model favors the first motion offset over the second, as  $\delta_{p_1}$  affects both frames while  $\delta_{p_2}$  affects only the second one. Jointly optimizing all parameters generally leads to the worst degradation of optical flow estimates. Yet, focusing on motion parameters  $\delta_{p_1,p_2}$  or hue parameters  $\delta_{\gamma,\theta}$  alone also strongly degrades performance. Interestingly, the tested flow methods show either a high sensitivity towards motion, for RAFT and GMA, or a high sensitivity towards hues, for FlowNetCRobust, SpyNet and FlowFormer. For the latter, optimizing hues even yields the strongest degradation overall. This insight is valuable for color-reduced environments, *e.g.* night scenes, where greater independence of the color representation may be wanted.

**Robustness against snow, rain, sparks and fog.** Next, we transition to more natural attacks with snow, rain, sparks

Attack	ET?	FILCR	SPYLet	RAFT	GMA	ŕ
snow	21.37	18.23	9.99	11.20	10.90	7.22
rain	21.95	19.85	8.37	9.53	8.22	5.82
sparks	22.76	19.54	8.25	8.72	9.39	6.41
fog	2.32	3.37	2.28	0.92	0.97	0.73

Table 5. Adversarial robustness AEE $(f, \check{f}) \downarrow$  [36] for *adversarial* snow, rain, sparks and fog on Sintel-tr115. Worst robustness bold.

Attack	FT	FINCR	SPYNet	RAFT	GMA	É.
PCFA [36]	11.77	13.82	7.83	12.96	12.83	14.68
I-FGSM [37]	7.58	13.69	5.07	11.07	11.40	12.35
Snow (ours)	16.83	16.28	9.94	10.32	9.85	7.10

Table 6. Adversarial robustness  $AEE(f, \check{f}) \downarrow [36]$  for *different attacks* on Sintel train, the worst robustness per method is bold.

and fog. We optimize all parameters for snow, rain and sparks, but do not optimize  $\delta_{p_2}$  for fog, keeping it static in the scene. Tab. 5 summarizes the optical flow robustness against adversarial weather, again on Sintel-tr115. For adversarial weather, the methods rank similar to pure augmentation, cf. Tab. 2, but the optimization amplifies optical flow changes. For every weather, lower-quality methods, e.g. FlowNet2, are very vulnerable while high-quality methods, e.g. FlowFormer, are comparatively robust against any weather. For GMA, Fig. 1 visualizes the attacked weather and resulting flows. Remarkably, moving particles eradicate the estimated motion despite their constant movement due to falling and camera motion. When we compare randomly initialized particles to their adversarial counterparts in Fig. 6 their positions hardly differ, making the adversarial sample indistinguishable from random weather to human observers. As adversarial snow greatly affects all optical flow methods, we select it for further analysis.

**Comparison to**  $L_p$  **attacks.** To conclude our attack evaluation, we compare our adversarial snow attack to previous attacks on optical flow and analyze the performance of optical flow methods in detail. Tab. 6 compares the robustness of optical flow methods under two  $L_p$  attacks to our non- $L_p$  attack with adversarial snow on the full Sintel training set. The  $L_2$  attack PCFA [36] is the strongest adversarial attack in the literature, while I-FGSM [37] is a weaker  $L_{\infty}$  attack. Despite being much more constrained by its physically plausible motion, our adversarial snow can compete with PCFA in terms of induced flow perturbation.

Surprisingly, high-quality methods like RAFT, GMA or FlowFormer that suffer most from  $L_p$  attacks [36] offer the best robustness towards adversarial snow. Instead, lowerquality methods like FlowNet2 and SpyNet that are most robust towards  $L_p$  attacks alter their predictions disproportionately to the added snow particles – or any other particlebased weather (*cf*. Tab. 5). We ascribe the better weather robustness to the more detailed flow estimations of highquality methods, which detect the localized motion of single particles (*cf*. Fig. 6, snow and sparks on RAFT and FlowFormer, where circular particles are visible). The less accurate methods FlowNet2, FlowNetCRobust and SpyNet instead propagate the detected particle motion over larger areas, rather than attributing it to small moving objects (*cf*. Fig. 6, rows 2/3, where flow predictions have few details). Notably, the robustness of FlowNetCRobust against patch attacks as reported in [37] does not transfer, making it one of the most vulnerable methods irrespective of the attack.

#### 4.3. Training with weather

As all optical flow methods change their predictions significantly in the presence of weather, we end our experiments by presenting a robustifying training strategy. Here, we choose RAFT [39], which is the baseline architecture for GMA and FlowFormer. We retrain RAFT from the authorprovided C+T checkpoint according to their training protocol [39] but augment 0%, 50% or 100% of the Sintel final training data with *random* snow. We evaluate the quality, and the robustness towards random augmentations as well as optimized weather attacks, *cf*. Tab. 2 and Tab. 5.

Tab. 7 summarizes the results. Compared to standard training, augmenting any percentage of Sintel-final frames with snow clearly improves the robustness. Furthermore, augmenting half of Sintel clean improves the quality on all datasets and shows a better generalization. It is remarkable that training with random snow has such a positive effect on robustness and quality [39], because training with  $L_p$  perturbations does not generally improve the robustness towards adversarial perturbations. For example, FlowFormer [13] augments its training with random noise, but is highly vulnerable against  $L_p$  attacks, cf. Tab. 6. Therefore, adversarial training [22] is commonly used to improve the robustness against  $L_p$  attacks. However, adversarial training (i) significantly increases the training time because adversarial samples are continuously included, leading to a slowlyconverging training and (ii) often lowers the quality of nonattacked samples. Both drawbacks are not observed for training with snow augmentations. This makes it particularly noteworthy that a simple augmentation with 50% non- $L_p$  snow improves robustness, quality and generalization at the same time. It also clearly shows that simulated weather has merits for training methods that shall be exploited in the real world, as we find that augmenting 50% of the synthetic Sintel data with snow during training improves the accuracy on real-world sequences from the KITTI dataset.

	Sintel EPE $\downarrow$ (te.)		KITTI $\downarrow$ (tr.)	Augmentation robustness $\downarrow$			Attack robustness $\downarrow$				
Snow	clean	final	F1-all	snow	rain	sparks	fog	snow	rain	sparks	fog
0%	1.642	3.167	5.65	4.19	3.60	3.64	3.54	9.93	8.02	8.47	0.87
50%	1.589	3.155	5.54	0.91	1.66	1.29	3.52	3.76	5.96	5.68	0.93
100%	1.551	3.384	5.69	0.83	1.37	1.32	3.57	3.48	5.61	5.49	1.04

Table 7. Training RAFT [39] with 0, 50 or 100% snowy Sintel-final frames during the Sintel/KITTI (S/K) training phase [39] The quality is measured on Sintel test and KITTI train, robustness values for weather augmentations on Sintel test and weather attacks on Sintel-tr115.

# 5. Limitations

Although we focus on realism, our attack does not aim at threatening optical flow methods in the real world, where manipulating weather is clearly impossible. While most optical flow attacks [1, 17, 36, 37] are not designed be directly applicable in the real world, our adversarial weather assesses methods under worst-case weather conditions, which is a more realistic attack scenario that even allows significant alterations without being noticeably adversarial. Furthermore, optimizing snow on Sintel-test may take several days on an Nvidia A100 GPU. However these higher computational costs are tolerable in such an offline benchmarking setting.

## 6. Conclusion

In this paper, we developed a novel framework for adversarial attacks on motion estimation with realistic weather. We proposed a differentiable particle renderer that can be used to generate adversarial weather with a strong impact on optical flow methods. With its realistic appearance, our adversarial weather is hard to notice; yet it lets optical flow networks predict zero-flow although the particles undergo both individual and camera motion. Surprisingly, accurate methods that are very vulnerable to  $L_p$  attacks appear to be more robust towards adversarially optimized weather, as they detect the motion of single particles rather than propagating it into the wider image. Finally, we find that augmenting a network's training with unoptimized weather not only improves the robustness towards weather augmentations and attacks but also increases generalization across datasets at a much lower cost than adversarial training.

Also, our weather attacks could easily be extended to problems that also require 3D-awareness or temporal motion consistency. Such attacks would target domains like monocular depth estimation [12, 48], stereo reconstruction [3, 47] or scene flow computation.

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