Distribution-Consistent Modal Recovering for Incomplete Multimodal Learning

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Abstract

Recovering missing modality is popular in incomplete multimodal learning because it usually benefits downstream tasks. However, the existing methods often directly estimate missing modalities from the observed ones by deep neural networks, lacking consideration of the distribution gap between modalities, resulting in the inconsistency of distributions between the recovered and the true data. To mitigate this issue, in this work, we propose a novel recovery paradigm, Distribution-Consistent Modal Recovering (DiCMoR), to transfer the distributions from available modalities to missing modalities, which thus maintains the distribution consistency of recovered data. In particular, we design a class-specific flow based modality recovery method to transform cross-modal distributions on the condition of sample class, which could well predict a distribution-consistent space for missing modality by virtue of the invertibility and exact density estimation of normalizing flow. The generated data from the predicted distribution is integrated with available modalities for the task of classification. Experiments show that DiCMoR gains superior performances and is more robust than existing state-of-the-art methods under various missing patterns. Visualization results show that the distribution gaps between recovered modalities and missing modalities are mitigated. Codes are released at https://github.com/mdswyz/DiCMoR.

1. Introduction

Multimodal machine learning dedicates to designing a strong model for understanding, reasoning, and learning by fusing multimodal data, such as language, acoustic, image, et al [15, 24]. Researchers have extensively exploited how to effectively encode the discriminative representations from different modalities [22, 33, 3, 28]. However, in real world scenarios, the well-trained model may be deployed when certain modalities are not available, e.g., language may be unavailable due to speech recognition errors; acoustic modality may be lost due to background noise or sensor sensing limitations; visual data may be unavailable due to lighting, occlusion, or social privacy security. In practice, the problem of missing modality inevitably degrades the multimodal understanding performance.

Figure 1. Two paradigms for missing modality recovery. (a) Typical paradigm usually exploits a well-crafted encoder and decoder modality recovery. (b) Our method transfers the distribution from the available to the missing modality, aiming to guarantee the distribution consistency. (c) Recovered and ground truth modality distribution visualization comparison between MCTN [20] (top) and our DiCMoR (bottom). DiCMoR exhibits a higher degree of proximity to the ground truth. More results can be found in Fig. 3.

To address this problem, a straightforward way is to conduct data recovery and then perform downstream tasks on the recovered data. As shown in Fig. 1 (a), this is a typical recovery paradigm that has been extensively studied by researchers [23, 20, 34, 16]. The core of this paradigm aims to design a well-crafted encoder and decoder, and then take as input the available modality so as to recover the missing modality. Tran et al. [23] proposed a cascaded residual autoencoder architecture to reconstruct the missing modalities; Lian et al. [16] leveraged graph neural networks to estimate the missing modalities from partially observed in-
put. However, this paradigm fails to fully consider the distribution gap caused the inherent modality heterogeneity, resulting in the inconsistent distribution between the vanilla available and the corresponding recovered modality.

In this work, we propose a novel framework to mitigate the above issues. As shown in Fig. 1 (b), different from the previous paradigm, we transfer the distribution from the available modalities to the missing modalities before decoding the missing data. The missing modality is then recovered under the estimated distribution. Thus, the key is to construct and learn a model that has the ability to perform transformations between cross-modal distributions.

To this end, we propose a distribution-consistent modal recovering (DiCMoR) method to complete those missing modalities for robust multimodal understanding. To transform cross-modal distributions, we introduce the modality-related flows and bridge different modalities within the embedded distribution space. To facilitate the distribution transfer, the invertible modality-specific normalizing flow is used for each modality to map the features of different modalities into the latent spaces with gaussian distributions, which reduces the distribution gap between the modalities. In the latent distribution space, the latent states of the missing modality could be sampled to feed into the inverse flow to faithfully estimate the original missing data. To increase the discriminability, the modality-related flows are built on condition of class labels to avoid the common collapse of different-class samples. In other words, we constrain the latent spaces from the same class but different modalities share the same class-specific Gaussian distribution, aiming to enhance the discriminative ability of the recovered modality. Owing to the favorable attributes inherent to flow-based models, such as their invertibility and capacity for precise density estimation, an assurance of distributional congruence emerges between the inferred data and the actual ground truth. Finally, the recovered modalities together with the available modalities could be jointly fed into multimodal fusion network for the downstream tasks. The contributions of this work are summarized as:

- We propose a novel missing modality recovery framework by transferring the distributions from the available modalities to the missing modalities, which reduces the distribution gap between the recovered data and the vanilla available data.
- We propose a cross-modal distribution transformation method by designing class-specific multimodal flows, which not only ensures the congruence of the distributions but also enhances the discriminative capacity.
- We experimentally verify the superiority of the method in various modality-missing patterns. Visualization results demonstrate that distribution gaps between recovered and missing modalities are obviously reduced.

2. Related Works

2.1. Incomplete multimodal learning

Learning from incomplete multimodal data is an essential research topic in machine learning, which allows trained models to be robust to inevitable modality-missing environments in real-world scenarios. Depending on whether to recover incomplete multimodal data, current methods can be divided into two categories: non-recovery methods [29, 11, 5] and recovery methods [19, 32, 20].

The non-recovery methods can be roughly classified into grouping strategy-based, correlation maximization-based, and knowledge distillation-based. The grouping strategy-based methods aim to split incomplete multimodal data into multiple complete subgroups and perform feature learning for each subgroup individually [29]. The correlation maximization-based methods aim to maximize the correlation between modalities and constrain different modalities to have correlated low-dimensional representations [11, 17]. The knowledge distillation-based methods learn a separate prediction model for each modality, and then distill knowledge between modalities, using the model of the partial modality for prediction in the inference phase [5, 18].

The basic principle of the recovery methods is to estimate and reconstruct the data of the missing modalities explicitly from the data of available modalities. The representative methods include zero-based recovery [19], average-based recovery [32], and deep learning-based recovery [20]. Among them, the zero and average-based recovery methods still cause a considerable gap between the recovered data and the true data because they do not utilize any supervision information. In contrast, deep learning-based methods can better estimate missing modalities by leveraging their powerful feature representation capabilities. For example, Tran et al. [23] proposed a cascaded residual autoencoder for the imputation of missing modalities. Pham et al. [20] and Zhao et al. [34] combined autoencoder with cycle consistency loss for modality reconstruction. Lian et al. [16] utilized graph neural networks to recover missing modalities to further improve the performance of downstream tasks. Our method has an essential difference from previous methods because we recover the missing modality from the perspective of data distribution, maintaining the distribution consistency and discriminability of recovered data.

2.2. Flow-based generative model

Normalizing flow is a classical generative probabilistic model, also known as a flow-based generative model, introduced by Dinh et al. [4] for efficient and exact density estimation. This model can be seen as a transformation of a known and tractable distribution \( p_Z(z) \) (e.g., a Gaussian distribution) into an unknown and arbitrary distribution \( p_U(u) \) by a sequence of invertible (i.e., bijective) and differ-
The generative process is defined as \( u = G(z) \), where \( z \sim p_Z(z) \) is a sample usually from standard MVG (multivariate Gaussian) distribution, \( u \sim p_U(u) \) is a true sample. As the \( u \) is observed during the training phase, the \( z \) can be obtained by \( z = F(u) = G^{-1}(u) \), \( F \) is the inverse function of \( G \), and \( z \) is called a latent variable. \( F \) is composed of \( N \) invertible transformations: \( F = f_1 \circ f_2 \circ \cdots \circ f_N \), the transformation between \( u \) and \( z \) is \( u \xrightarrow{f_1} h_1 \xrightarrow{f_2} h_2 \cdots \xrightarrow{f_N} z \), such a sequence of invertible transformations is called a normalizing flow. Then, the log-likelihood of any \( u \in U \) can be estimated by

\[
\log p_U(u) = \log p_Z(z) + \log |\text{det}(\frac{\partial z}{\partial u})| \\
= \log p_Z(z) + \sum_{i=1}^{N} \log |\text{det}(\frac{\partial h_i}{\partial h_{i-1}})|,
\]

where \( \log |\text{det}(\frac{\partial h_i}{\partial h_{i-1}})| \) denotes the log-determinant of the Jacobian matrix \( (\frac{\partial h_i}{\partial h_{i-1}}) \) and this value is the change in log-density when going from \( h_{i-1} \) to \( h_i \) under transformation \( f_i \). By maximizing \( \log p_U(u) \), the function \( F \) can be optimized to transfer \( p_U(u) \) into \( p_Z(z) \), and the \( p_U(u) \) can be transferred from \( p_Z(z) \) by \( F^{-1} \) (i.e., \( G \)).

Based on the above principles, various methods had been proposed. For example, Dinh et al. [4] proposed a real-valued non-volume preserving flow that combined multi-scale architecture with coupling layers. Kingma and Dhariwal [10] designed an invertible \( 1 \times 1 \) convolution layer to construct normalizing flow. Further, many applications are use normalizing flow including image generation [7], video generation [12], audio generation [21], word embedding enhancement [13], anomaly detection [5], etc.

### 3. The Proposed Method

In this section, we first give the basic formulation to illustrate our main idea, then introduce the designed network, followed by three crucial modules.

#### 3.1. Problem Formulation

Let a tuple \( (X^{(1)}, X^{(2)}, \ldots, X^{(M)}) \) denotes \( M \) heterogeneous modalities of an example, where \( X^{(m)} \) is the input of the \( m \)-th modality. In the complete case, all modalities are observed and easily fused to feed the downstream tasks. But in many limited scenes, some modalities could not be observed and need to be recovered for better fusion. For simplification, we introduce an indicator \( \lambda \in \{0, 1\} \) to denote with \( \lambda_m = 0 \) if the \( m \)-th modality is missing, otherwise \( \lambda_m = 1 \). In the incomplete case, thus, the target is to recover those unobserved modalities \( I_{\text{miss}} = \{m|\lambda_m = 0\} \) based on those observed ones \( I_{\text{obs}} = \{m|\lambda_m = 1\} \). It is worth noting that the missing modalities need not to be consistent for the testing examples.

Our main idea is to transfer the distributions from observed modalities to missing ones through cross flows, and generate more confident prediction with high distribution consistency as shown in Fig. 1 (b). Concretely, we assume all modalities of one-class examples could be embedded into a latent space with Gaussian distributions. Due to the
powerful transfer ability, the normalizing flow is used as the embedding function, formally,

\[ Z^{(m)} = \varphi^{(m)}(X^{(m)}) \sim \mathcal{N}(\mu_c, \Sigma_c), \quad m \in \mathcal{I}_{\text{obs}}, \tag{2} \]

where \( Z^{(m)} \) is the latent state of the \( m \)-th modality, \( \varphi^{(m)} \) is the corresponding forward flow function, and \( c \) is the class label of the input sample \( \mathcal{X} \). According to the known latent states, we infer each missing modality \( X^{(k)}(k \in \mathcal{I}_{\text{miss}}) \) as follows:

\[
\begin{align*}
\hat{Z}^{(k)} &\leftarrow \psi(\{Z^{(m)}|m \in \mathcal{I}_{\text{obs}}\}) \sim \mathcal{N}(\mu_c, \Sigma_c), \\
\hat{X}^{(k)} &= (\varphi^{(k)})^{-1}(\hat{Z}^{(k)}) \sim p_X(X^{(k)}),
\end{align*}
\tag{3}
\]

where the estimated latent state \( \hat{Z}^{(k)} \) is sampled from the Gaussian distribution of class \( c \) according to the observation on those existing modalities. In virtue of the invertibility of flow, we can infer the missing modality \( \hat{X}^{(k)} \), abided by its original distribution \( p_X(X^{(k)}) \).

Although the estimated \( \hat{X}^{(k)} \) follows the original distribution, it would deviate from the ground truth when the scatter degree of intra-class samples is large. Thus, we can further refine it with a light-weight decoder \( \varphi^{(k)} \), i.e., \( \hat{X}^{(k)} = \varphi^{(k)}(\hat{Z}^{(k)}) \). At the training stage, we minimize the reconstruction error between \( \hat{X}^{(k)} \) and \( X^{(k)} \). And, we find such a refinement step could improve the performance as shown in the experiment part.

3.2. Network Overview

The framework of our DiCMoR is illustrated in Fig. 2. It mainly consists of three parts: shallow feature extractor, cross-modal distribution transfer (CMDT), and multimodal fusion and prediction. Considering the difference in the original dimensional space between modalities, we first extract multimodal shallow features and align the dimension of each modality to facilitate subsequent distribution transformation and modality recovery. To mitigate the distribution gap between recovered data and true data, we next build a CMDT network to learn the latent distribution space of each modality, and conduct cross-modal distribution transformation to estimate the distribution of missing modality, and finally recover the missing data by a decoder. To perform the classification task, in the end, the multimodal fusion and prediction part receives recovered complete multimodal data and uses multimodal transformers to fuse multimodal representation for label regression. The detail is introduced in the next subsections.

3.3. Shallow Feature Extractor

We consider three modalities: language \( L \), visual \( V \) and acoustic \( A \). Since the original dimensional spaces of the three modalities are often distinct, they are not suitable to be used directly for cross-modal transformations. To solve this problem, we design a shallow feature extractor that contains three independent temporal convolutional layers to extract the shallow features of three modalities and project them into the same dimensional space. Hence, the subsequent recovery task aims to estimate the shallow features of missing modalities from that of available modalities.

Given an input example of the class \( c \), we can obtain the shallow features, \( \mathcal{X} = \{X^{(m)}\}, X^{(m)} \in \mathbb{R}^{T \times d} \), where \( m \in \{L, V, A\} \) and \( d \) indicate the sequence length and the feature dimensionality. In the incomplete multimodal case, some modalities are missing either fixedly or randomly by guaranteeing at least one modality is available in \( \mathcal{X} \). For the three modalities mentioned above, a total of seven missing combinational cases are included, which are reported in Tab. 1. For a convenient statement but without loss of generality, below we estimate the missing acoustic modality \( X^{(A)} \) from the other two modalities \( X^{(L)}, X^{(V)} \), as shown in the exhibition of Fig. 2.

3.4. Cross-Modal Distribution Transfer

Let \( \varphi^{(m)} \) denotes a normalizing flow model of modality \( m \) and \( (\varphi^{(m)})^{-1} \) for its inverse transformation. Each normalizing flow model receives the shallow features \( X^{(m)} \) of that modality respectively and outputs multimodal latent states with the same Gaussian distribution, represented as \( Z^{(m)} = \varphi^{(m)}(X^{(m)}) \). At the same time, \( Z^{(m)} \) can be input to \( (\varphi^{(m)})^{-1} \) to generate a sample \( \hat{X}^{(m)} \) with the true distribution, \( \hat{X}^{(m)} \sim p_X(X^{(m)}) \). Taking the example that the language and visual modalities are available, the acoustic modality is missing, as shown in Fig. 2. \( X^{(L)} \) and \( X^{(V)} \) can be input to \( \varphi^{(L)} \) and \( \varphi^{(V)} \) to obtain \( Z^{(L)} \) and \( Z^{(V)} \), respectively. As \( Z^{(L)} \sim \mathcal{N}(\mu_c, \Sigma_c) \) and \( Z^{(V)} \sim \mathcal{N}(\mu_c, \Sigma_c) \), we simply perform an average operation on them to sample a latent acoustic state \( \hat{Z}^{(A)} \sim \mathcal{N}(\mu_c, \Sigma_c) \). Then it is injected to \( (\varphi^{(A)})^{-1} \) to generate sample \( \hat{X}^{(A)} \) with the acoustic modality distribution. Formally,

\[
\hat{X}^{(A)} = (\varphi^{(A)})^{-1}(\varphi^{(L)}(X^{(L)}) + \varphi^{(V)}(X^{(V)}))/2 \sim \mathcal{N}(\mu_c, \Sigma_c). \tag{5}
\]

Subsequently, \( \hat{X}^{(A)} \) is fed into the reconstruction module of acoustic modality to obtain the final recovered features: \( \hat{X}^{(A)} = D^{(A)}(\hat{X}^{(A)}) \), where \( D^{(A)} \) denotes the feature reconstruction module of the acoustic modality. We stack several residual channel attention blocks [27] to build a reconstruction module for each modality, where the 2D convolutional layers are replaced with 1D convolution to fit the temporal features. For any missing patterns, the set of recovered features can be denoted as \( Y^{\text{rec}} = \{\hat{X}^{(m)}|m \in \mathcal{I}_{\text{miss}}\} \), thus the reconstruction loss \( \mathcal{L}_{\text{rec}} \) is denoted as:

\[
\mathcal{L}_{\text{rec}} = \sum_{m \in \mathcal{I}_{\text{miss}}} \|\hat{X}^{(m)} - X^{(m)}\|_F^2. \tag{6}
\]
Class-specific flows. To optimize normalizing flows, the objective is typically to make all $\mathbf{Z}^{(m)}$ with the same standard MVG distribution (i.e., $\mathbf{Z}^{(m)} \sim \mathcal{N}(0, \mathbf{I})$), but this may lead to loss of discriminability for different classes samples. To address this issue, we introduce labels to adaptively learn class-specific Gaussian distributions, so that the latent states of different classes of different Gaussian distributions, thereby enhancing the discriminability. Given a sample $\mathbf{X}$ of class $c$, formally, according to Eq. (1), the loss function $L_{\text{cdd}}$ of cross-modal distribution transfer can be defined as:

$$L_{\text{cdd}} = - \sum_{m \in \mathcal{I}_{\text{obs}}}[\log p_{\mathbf{Z}^{(m)}}(\mathbf{Z}^{(m)}|y=c) + \log |\det(\partial \mathbf{Z}^{(m)}/\partial \mathbf{X}^{(m)})|]$$

where the first term denotes the log-density of $\mathbf{Z}_m$ on the condition of its own category, and the second term denotes the log-determinant of normalizing flow model for modality $m$. In detail, $p_{\mathbf{Z}^{(m)}}(\mathbf{Z}^{(m)}|y=c) \sim \mathcal{N}(\mu_c, \Sigma_c)$, thus the terms can be further formulated as:

$$\log p_{\mathbf{Z}^{(m)}}(\mathbf{Z}^{(m)}) = \log (2\pi)^{-\frac{d}{2}}\det(\Sigma_c)^{-\frac{1}{2}} - \frac{1}{2}(\mathbf{Z}^{(m)} - \mu_c)^T \Sigma_c^{-1}(\mathbf{Z}^{(m)} - \mu_c),$$

$$\log |\det(\partial \mathbf{Z}^{(m)}/\partial \mathbf{X}^{(m)})| = \sum_{i=1}^{N} \log |\det(s_i^{(m)})|,$$

where $\log |\det(s_i^{(m)})|$ denotes the log-determinant of $i^{th}$ affine coupling layer for normalizing flow of modality $m$, as used in [10].

Another question is how to learn $\{\mu_c, \Sigma_c\}$ for different classes. Let’s take class c as an example, we first construct two tensors filled with the scalar value zero and two convolutional layers initialized with zero, and the two convolutional layers are denoted as ZeroConv$^c_p(\cdot)$ and ZeroConv$^c_\Sigma(\cdot)$. Then, two zero tensors are injected into two convolution layers to obtain the initialized mean $\mu_c$ and log covariance matrix $\log \Sigma_c$ of the Gaussian distribution for class c respectively, represented as $\mu_c = \text{ZeroConv}_p^c(0)$ and $\log \Sigma_c = \text{ZeroConv}_\Sigma(0)$. Therefore, in the initialization phase, the Gaussian distribution of class c is initialized to have a mean $\mu_c = 0$ and a covariance $\Sigma_c = \mathbf{I}$. During the training process, $\mu_c$ and $\log \Sigma_c$ of Gaussian distribution are changed additively as the bias of the convolution layers is updated, thereby adaptively fitting the class-specific Gaussian distributions based on different classes of training samples.

### 3.5. Multimodal Fusion and Prediction

The recovered data $\mathbf{X}_{\text{miss}} = \{\mathbf{X}^{(m)}|m \in \mathcal{I}_{\text{miss}}\}$ and the input available data $\mathbf{X}_{\text{obs}} = \{\mathbf{X}^{(m)}|m \in \mathcal{I}_{\text{obs}}\}$ are combined as the complete multimodal data for downstream multimodal fusion and prediction tasks. We employ multimodal transformers [24] to fuse multimodal features $\mathbf{X}_{\text{miss}} \cup \mathbf{X}_{\text{obs}}$, and the fused feature is used to predict results by fully connected layers. We integrate the above losses to reach the full optimization objective:

$$L_{\text{total}} = L_{\text{task}} + \beta (L_{\text{cdd}} + L_{\text{rec}}),$$

where $L_{\text{task}}$ is the task-specific loss that is defined as mean absolute error in our experiments, $\beta$ controls the importance of different loss functions. The entire optimization is implemented in an end-to-end manner, and the concrete training about the configuration of incomplete modalities could be found in the experiment part.

### 4. Experiments

#### 4.1. Datasets and Implementation Details

Datasets. To verify the effectiveness of DiCMoR, we conduct experiments on two standard multimodal video understanding datasets, including CMU-MOSI [30] and
CMU-MOSEI [31]. The above two datasets mainly focus on human multimodal sentiment analysis. **CMU-MOSEI** contains 2,199 short monologue video clips. Among the samples, 1,284, 229, and 686 samples are used as training, validation, and testing set. **CMU-MOSEI** contains 22,856 samples of movie review video clips from YouTube. According to the predetermined protocol, 16,326 samples are used for training, the remaining 1,871 and 4,659 samples are used for validation and testing. On the two datasets, we extract the language features via pre-trained BERT model [9] and obtain a 768-dimensional hidden state as the word features. For visual modality, each video frame was encoded via Facet [8] to represent the presence of the total 35 facial action units [14]. The acoustic modality was processed by COVAREP [2] to obtain the 74-dimensional features. Each sample in CMU-MOSEI and CMU-MOSEI was labeled with a human sentiment score that ranges from -3 to 3, including highly negative, negative, weakly negative, neutral, weakly positive, positive, and highly positive. To make a comprehensive comparison, we evaluate the performance using the following metrics: 7-class accuracy (ACC), binary accuracy (ACC$_2$), and F1 score.

**Implementation details.** We investigate the performance of different methods on multimodal datasets with two missing protocols, including a fixed missing protocol and a random missing protocol. For the **fixed missing protocol**, we let the missing patterns be consistent for all samples (i.e., the available modalities are the same for all samples). Since the three modalities can produce seven different missing patterns, this protocol contains seven sets of experiments for seven different missing patterns. For the **random missing protocol**, the missing patterns are randomized for each sample (i.e., one or two modalities may be missing for each sample). We use the missing rate (MR) to measure the overall missingness of the dataset. The MR is defined as $MR = 1 - \frac{\sum_{i=1}^{L} a_i}{L \times M}$, where $a_i$ denotes the number of available modalities for the $i$th sample, $L$ denotes the total number of samples, and $M$ indicates the number of modalities. We also ensure that at least one modality is available for each sample, so $a_i \geq 1$ and $MR \leq \frac{M-1}{M}$. For three modalities, we choose the MR from [0.0, 0.1, · · · , 0.7], where 0.7 is an approximation of $\frac{M-1}{M}$ with the same meaning. We keep the same MR during training, validation, and testing phases, consistent with previous work [16]. The detailed neural network configurations are listed in the supplementary file, including the 1D temporal convolutions, the normalizing flow models, the reconstruction modules, and the multimodal transformers. The optimal setting for $\beta$ is set to 0.1 via the performance on the validation set. We implemented all the experiments using PyTorch on an RTX 3090 GPU with 24GB memory. We set the training batch size as 16 and train DiCMoR for 50 epochs until convergence. We run each experiment five times and report the average values on the testing set.

### 4.2. Comparison with the state-of-the-arts

We compare DiCMoR with the current state-of-the-art incomplete multimodal learning methods, including two deep learning-based non-recovery methods with canonical correlation maximization: DCCA [1] and DCCAE [26], three deep learning-based recovery methods: MCTN [20], MMIN [34], GCNet [16]. Below, we report the quantitative and qualitative experimental results. **Quantitative results.** Tab. 1 and Tab. 2 illustrate the comparison of fixed missing protocol and random missing protocol on two datasets, respectively. From these experimental results, we have the following observations:

1. On average, our method achieves the best perfor-

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**Table 2. Comparison on random missing protocol. The values reported in each cell denote ACC$_7$/F1/ACC$_2$. **Bold** is the best.**

<table>
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<th>MR</th>
<th>ACC$_7$</th>
<th>F1</th>
<th>ACC$_2$</th>
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<td></td>
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<td>75.6 / 75.7 / 38.5</td>
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<td>82.1 / 82.0 / 42.3</td>
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<td>0.3</td>
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<td>72.3 / 71.1 / 43.8</td>
<td>73.2 / 70.3 / 45.6</td>
<td>76.7 / 73.7 / 46.8</td>
</tr>
<tr>
<td>0.7</td>
<td>65.6 / 61.0 / 42.1</td>
<td>66.6 / 62.6 / 42.5</td>
<td>72.7 / 70.5 / 43.6</td>
<td>75.4 / 72.2 / 46.2</td>
</tr>
<tr>
<td>Average</td>
<td>71.5 / 70.3 / 44.1</td>
<td>72.6 / 71.2 / 45.0</td>
<td>77.0 / 76.1 / 46.9</td>
<td>77.9 / 76.8 / 48.3</td>
</tr>
</tbody>
</table>
performance on all datasets with two missing protocols. Compared with the non-recovery methods, the recovery methods including our DiCMoR obtain better performance. This is because the recovery methods can estimate and reconstruct missing modalities explicitly from the available modalities. Compared with the recovery methods [20, 34, 16], our proposed DiCMoR obtains consistent improvements, indicating the superiority of maintaining consistency of distribution between recovered data and true data. For further investigation, we will visualize the distribution of recovered data for different methods in the next part.

2) From the experimental results in Tab. 1, we can observe that the prediction performance of all methods tend to be better when the language modality is available, and this phenomenon also emerged in previous work [20, 34]. The potential reason is that language modality is a high-level semantic abstraction that contains more discriminative information. Therefore, it is crucial to enhance the performance of missing scenarios without language modality. Compared with these state-of-the-arts, our DiCMoR consistently obtains better results in missing scenarios without language modality. This suggests that the distribution transformed from the weak modality can improve the performance.

3) Experimental results in Tab. 2 show that the performance degradation of DiCMoR tends to be smaller than that of other recovery methods as the MR increases. Taking the results on the CMU-MOSI dataset as an example, as the MR increases from 0.0 to 0.7, the ACC2 performance of other recovery methods declines 19.5% ~ 21.8% while our DiCMoR declines 14.6%. Notably, the performance gap between DiCMoR and other recovery methods becomes more obvious as the MR increases. For example, compared with the strongest baseline GCNet on the CMU-MOSI dataset, the ACC2 performance gap increases from 0.5% to 5.4% as the MR increases from 0.0 to 0.7. These results demonstrate that the DiCMoR improves prediction performance in missing scenarios, especially in severely missing cases.

Qualitative results. Fig. 3 visualize the distribution of recovered data and ground truth for different recovery methods when merely one modality remains, we randomly select 100 samples in the testing set from the CMU-MOSEI dataset. The features of the selected samples are projected into a 2D space by t-SNE [25]. From these results, we can observe that the distribution between true data and recovered data estimated by our DiCMoR is closer than other methods. The main reason is that DiCMoR explicitly models and learns the distribution space of different modalities and has ability to transfer the distribution across modalities.

4.3. Ablation study

Quantitative analysis. We evaluate the effects of key components for DiCMoR, including distribution transfer ($F^{(m)}$) and feature reconstruction ($D^{(m)}$). The results are illustrated in Tab. 3, we can draw the following conclu-
Table 4. Ablation study of $\mathcal{F}^{(m)}$ on MCTN under average random missing protocol.

<table>
<thead>
<tr>
<th>Methods</th>
<th>CMU-MOSI</th>
<th>CMU-MOSEI</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ACC$_2$</td>
<td>F1</td>
</tr>
<tr>
<td>MCTN</td>
<td>70.6</td>
<td>70.1</td>
</tr>
<tr>
<td>MCTN w/ $\mathcal{F}^{(m)}$</td>
<td>72.4</td>
<td>72.4</td>
</tr>
</tbody>
</table>

Figure 4. Visualization of recovered data and ground truth for MCTN and MCTN w/ $\mathcal{F}^{(m)}$. Obviously, our method can improve the distribution consistency of recovered data for MCTN.

Figure 5. Visualization of class-specific Gaussian distributions.

**Visualization of the class-specific Gaussian distributions and multimodal latent states.** First, we visualize the class-specific Gaussian distributions learned by CMDT in Fig. 5, where we draw the one-dimensional Gaussian distribution curves by averaging the elements of $\mu_c$ and $\Sigma_c$ respectively for each class. From this result, we can observe that the learned Gaussian distributions of different classes are basically scattered, which indicates that our proposed CMDT has the ability to adaptively learn Gaussian distributions with discrimination w.r.t different classes. One question arises, can these learned Gaussian distributions help improve the discriminability of the latent states? We further visualize the multimodal latent states of different classes in Fig. 6. Specifically, we randomly select 35 samples (five samples for each class) in the testing set of the CMU-MOSEI dataset. The features of the selected samples are projected into a 2D space by t-SNE [25]. We can discover that when using a standard Gaussian distribution (DiCMoR w/ $\mathcal{N}(\mu_c, \Sigma_c)$ as the objective, different classes of multimodal latent states suffer from mode collapse due to their sharing a same Gaussian distribution space. In contrast, when using class-specific Gaussian distributions as the objective (DiCMoR w/ $\mathcal{N}(\mu_c, \Sigma_c)$), the latent states are distinguishable in seven classes, indicating that the learned Gaussian distributions can improve the discriminability of latent states.

5. Conclusion and discussion

In this paper, we have proposed a recovery paradigm (DiCMoR) for incomplete multimodal learning that transfers the distributions from available modalities to missing modalities to maintain the distribution consistency. Further, we have designed a class-specific flow based modality recovery paradigm to transform cross-modal distributions. It facilitates cross-modal distribution transformation and enables the anticipation of a distribution-consistent latent space for the missing modality. The robustness and efficacy of DiCMoR are substantiated through extensive evaluations. It should be noted, however, that our method necessitates the availability of labels as a conditioning factor during its training phase to generate class-associated data. Under scenarios where unlabeled tasks are encountered, our method may be susceptible to a decline in performance.
6. Acknowledgement

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References


[23] Luan Tran, Xiaoming Liu, Jiayu Zhou, and Rong Jin. Missing modalities imputation via cascaded residual autoencoder.


