# UMC: A Unified Bandwidth-efficient and Multi-resolution based Collaborative Perception Framework Supplementary Material 

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Figure 1. In the test set, we traverse all objects in each frame to obtain their corresponding types. Note that $s p, c p$ are short for detected points from single and collaborative view, respectively.


Figure 2. The detailed process of manually labelling.

## 1. Detailed information of Proposed Metrics

The detailed process of proposed metrics are shown in Figure 1. We traverse all objects in each frame to obtain their corresponding types. Note that the type of ARSV/ARCV can be automatically generated with code, as shown in Listing 1. And the type of ARCI/ARTC needs to be manually labeled, because whether it is visible at the last moment cannot be directly determined due to the movement of the vehicles from $t-1$ to $t$, as shown in Figure 2.

For detailed process of manually labelling, e.g., at

[^0]Table 1. The ARSV and ARCV performance with different threshold points $\tau$.

| Points | ARSV $_{50 / 70}$ | ARCV $_{50 / 70}$ |
| :---: | :---: | :---: |
| 10 | $81.48 / 77.48$ | $23.72 / 19.34$ |
| 7 | $79.44 / 75.05$ | $15.34 / 11.88$ |
| 5 | $77.73 / 73.21$ | $6.08 / 4.07$ |
| 4 | $76.90 / 72.35$ | $4.62 / 3.45$ |

timestamp $t$, we firstly label vehicles with yellow background as ARCI type. Then, by comparing with time $t-1$, we find that agent 1,2 are visible at time $t-1$ (with no yellow background). Based on that, we change the type of agent 1,2 from ARCI to ARTC. The pseudo code are as follows:

```
single_view = np.load (...)
collab_view = np.load(...)
for object in len(single_view.objects):
    if singel_view[object]. points > threhold:
        object.type = ARSV
    else:
        if collab_view[object]. points >
        threhold:
            object.type = ARCV
            else:
            object.type = ARCI
% Finally, we will manually label partial ARCI
    to ARTC, as shown in Figure 2.
        Listing 1. Pseudo code for proposed metrics
```

As for the threshold points $\tau$, the proposed metrics distinguish between ARSV and ARCV based on whether they are visible. Nevertheless, whether they are visible depends on the number of points included in each object and the performance of the detector. To verify at how many points the detector can not detect the object, we conducted the following experiments on the No Fusion model.

Table 1 shows the ARSV and ARCV in terms of different points. We can see that i) as the number of points decreases, so does the ARCV. This is because, as
the points become more accurate, the no fusion model should theoretically be 0 in terms of ARCV; ii) when the points are greater than 5, the decline in ARCV is very large. When points are less than 5 , the decline of the ARCV slows down, indicating it is close to the accurate points; iii) when points equal 4 , the ARCV is $4.62 \%$ in IoU@0.5 and $3.45 \%$ in IoU@0.7, which are within the acceptable error range of $5 \%$. So, to decide if an object is visible, we look at how many points it has and whether that number is greater than 4.

Note that the 'last frame' of ARTC's time interval varies based on the sampling frequency ( 5 Hz in V2XSim, 10 Hz in OPV2V). And, the ARSV and ARCV only take recall into account, while the AP is weighted by both recall and precision. Hence, a high AP does not necessarily mean high ARSV or ARCV values. Based on that, you may wonder why not utilize APSV/APCV as the new metric. It is because the each proposed model can only predict the classifications (background or foreground) and regressions ( $\mathrm{x}, \mathrm{y}, \mathrm{w}, \mathrm{h}$ ) of each pixel. Therefore, there is no prediction of the corresponding types for each detected objects.

## 2. Experiments details

### 2.1. Basic parameters

Our experiments are all performed on the workstation with AMD Core Ryzen Threadripper 3960X CPU and Nvidia 3090 GPU with Pytorch v1.7.1, CUDA 11.0. The SRAR-based's transmitted collaborative feature map (TCF) has a dimension of $32 \times 32 \times 256$. Our proposed UMC's TCFs have the dimension of $32 \times 32$ $\times 256,64 \times 64 \times 128$. As for hyper-parameter tuning, we choose Adam as the optimizer and set the batch size to 4 for both V2X-Sim and OPV2V datasets. Also, we utilize the same number of scenes (total 80 scenes) for training. For testing stage, the V2X-sim utilizes 10 scenes, and OPV2V utilizes 15 scenes. Meanwhile, we use initial learning rate of 0.001 and set the random seed to 622 .

### 2.2. Baseline setting

To ensure fairness, we fix the structure of the shared feature extractor MotionNet[9] and detector, and transplant the collaborative part of the different methods without modification. Meanwhile, all the models are trained 100 epoch with initial learning rate of 0.001 and set the learning rate update strategy as 'torch.optim.lr_scheduler.MultiStepLR(self. optimizer_head, milestones $=[50,100]$, gamma $=0.5)^{\prime}$.


Figure 3. Difference between where2comm and UMC communication strategy. (a) The ego agent's observation. (b) The ego agent's observation at feature level. (c) The collaborator's observation, red box denoted for the detected agents. (d) The collaborator's observation at feature level. (e) Communication map of where2comm. (f) Communication map of UMC.

### 2.3. Communication Volume

The communication volume for each method is calculated by: $\operatorname{mean}\left(\log \left(\sum_{i=1}^{\text {agents }} \sum_{t=1}^{T}(F\right.\right.$.size $+Q$.size $\left.\left.)\right)\right)$ during the test stage. $F$ represents the transmitted feature map, and $Q$ represents the query matrix, which is calculated in UMC, who2com, and when2com, and equals 0 in other methods.

### 2.4. Setting of $\delta_{s}, \delta_{c}$

Table 2. The performance-bandwidth trade off with different $\delta_{s}, \delta_{c}$ values on V2X-Sim dataset.

| $\delta_{s}$ | $\delta_{c}$ | $\mathrm{ARSV}_{50 / 70} \uparrow$ | $\mathrm{ARCV}_{50 / 70} \uparrow$ | $\mathrm{ARCI}_{50 / 70} \downarrow$ | $\mathrm{ARTC}_{50 / 70} \uparrow$ | $\mathrm{AP}_{50 / 70} \uparrow$ | $\mathrm{C} . \mathrm{V} . \downarrow$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 100 | $85.66 / 81.87$ | $70.76 / 63.15$ | $2.41 / 1.7$ | $11.88 / 8.12$ | $68.97 / 61.35$ | 20.58 |
| 50 | 50 | $84.78 / 80.73$ | $67.46 / 60.72$ | $2.50 / 1.78$ | $11.88 / 8.12$ | $67.83 / 60.02$ | 19.92 |
| 50 | 10 | $80.62 / 75.39$ | $31.48 / 23.53$ | $2.17 / 1.37$ | $12.03 / 7.20$ | $59.57 / 50.50$ | 18.4 |
| 20 | 100 | $87.30 / 84.08$ | $74.08 / 66.77$ | $16.68 / 12.24$ | $22.15 / 17.41$ | $66.98 / 59.24$ | 19.68 |
| 20 | 50 | $83.23 / 78.98$ | $56.49 / 48.87$ | $2.12 / 1.51$ | $11.23 / 8.08$ | $64.77 / 56.79$ | 19 |
| 20 | 10 | $80.53 / 75.38$ | $19.02 / 12.33$ | $2.14 / 1.38$ | $9.16 / 6.74$ | $58.00 / 49.46$ | 17.63 |
| 10 | 100 | $86.57 / 82.97$ | $59.37 / 51.68$ | $14.57 / 10.51$ | $19.09 / 15.15$ | $63.59 / 55.84$ | 19.06 |
| 10 | 50 | $82.12 / 77.44$ | $38.52 / 31.28$ | $2.16 / 1.47$ | $10.77 / 8.35$ | $61.57 / 53.43$ | 18.376 |
| 10 | 10 | $80.78 / 75.51$ | $13.29 / 8.97$ | $2.21 / 1.39$ | $10.77 / 8.35$ | $57.62 / 49.27$ | 17.171 |
| 5 | 100 | $86.04 / 82.59$ | $47.19 / 40.44$ | $14.17 / 9.9$ | $19.25 / 15.14$ | $61.04 / 53.99$ | 18.375 |
| 5 | 20 | $80.87 / 75.72$ | $15.09 / 10.76$ | $2.12 / 1.36$ | $10.77 / 8.35$ | $57.67 / 49.45$ | 17.17 |
| 1 | 100 | $85.44 / 81.49$ | $34.59 / 28.72$ | $13.47 / 9.88$ | $20.49 / 17.35$ | $58.07 / 50.72$ | 17.15 |

We record the proposed UMC under different $\left(\delta_{s}, \delta_{c}\right)$ in terms of the trade-off between performance and communication bandwidth, as shown in Table 2.

Meanwhile, we comprehensively analyze the communication strategy between where2comm[1] and our proposed UMC. As shown in Figure 3, where2comm takes the advantages of sparsity of foreground information and only transmits the regions that the agents
have. However, as for different downstream tasks, such as segmentation[10] or scene completion[4], there are other no-measurement or sparse-measurement regions that need collaborator's communication, as shown in Figure 3.(b). Hence, our proposed UMC aim to optimize not only detection but also general downstream tasks based on the traditional information theory. From the Figure 3.(f), we can observe that UMC can transmit the necessary regions to ego agent for general downstream tasks.

Note that in addition to discussing the top- $\delta \%$ based filtering strategy of Eq. 1 in manuscript, we also explored the mean based filtering strategy, the corresponding performance is shown as follows:

Table 3. The performance of mean based filtering strategy on V2X-Sim dataset.

$$
\begin{array}{cccccccc}
\hline \delta_{s} & \delta_{c} & \operatorname{ARSV}_{50 / 70} \uparrow & \mathrm{ARCV}_{50 / 70} \uparrow & \mathrm{ARCI}_{50 / 70} \downarrow & \mathrm{ARTC}_{50 / 70} \uparrow & \mathrm{AP}_{50 / 70} \uparrow & \text { C.V. } \downarrow \\
\hline
\end{array}
$$

| mean | $84.67 / 80.68$ | $67.01 / 60.04$ | $2.38 / 1.70$ | $12.35 / 9.46$ | $67.80 / 60.01$ | 19.23 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |

## 3. Performance analysis

### 3.1. Computation complexity

The configuration of the experiment platform has been described in Section 2.1. Based on that, in terms of computations, the proposed entropy-cs only requires about 0.136 G FLOPS with 0.66 ms latency to process a $256 \times 32 \times 32(\mathrm{C}, \mathrm{H}, \mathrm{W})$ feature map (more architecture details are shown in Section 4.1).

Compared to DiscoNet[3], the proposed C-GRU costs about 4.10G FLOPS more with 12.7 ms latency.

### 3.2. Is Early Fusion always be better?

We discuss the performance of early fusion model. As we all know, Early fusion aggregates the raw measurements from all collaborators, promoting a holistic perspective. From the Table 1 in manuscript, the early fusion performs extremely good, even better than all the other baselines in some metrics. However, V2VNet[8] actually shows early fusion is far from optimal due to noises in real sensors. To address the above issue, since the dataset of V2VNet is not open source, we conduct experiments on OPV2V[12] with Gaussian noises. As shown in Table 4, we agree that the performance of Early Fusion may be degraded by noises to some extent.

Table 4. Comparisons on OPV2V dataset.[Best, Worst]

| Method | $\mathrm{ARSV}_{50 / 70}$ | $\mathrm{ARCV}_{50 / 70}$ | $\mathrm{AP}_{50 / 70}$ |
| :---: | :---: | :---: | :---: |
| No Fusion | $69.33 / 46.35$ | $\mathbf{1 2 . 3 2 / 4 . 3 6}$ | $\mathbf{5 4 . 6 9 / 2 3 . 9 4}$ |
| Early Fusion | $\mathbf{6 4 . 6 2 / 4 6 . 9 5}$ | $45.00 / 24.39$ | $55.88 / \mathbf{2 5 . 8 9}$ |
| UMC | $\mathbf{7 6 . 5 6 / 4 7 . 6 8}$ | $47.82 / \mathbf{2 5 . 0 6}$ | $61.90 / 24.50$ |

Table 5. Comparisons of single-grain selection.

| Multi-Grains Selection |  |  | $\mathrm{AP}_{50 / 70} \uparrow$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{F}_{i, 1}^{e, t}$ | $\boldsymbol{F}_{i, 2}^{e, t}$ | $\boldsymbol{F}_{i, 3}^{e, t}$ | $\mathrm{~V} . \downarrow$ |  |
| $\checkmark$ |  |  | $56.73 / 49.22$ | 7.88 |
|  | $\checkmark$ |  | $58.96 / 52.86$ | 8.12 |
|  |  | $\checkmark$ | $57.43 / 51.66$ | 8.36 |

### 3.3. Grains selection

Table 3 in manuscript compares the performance of different selections of grain level. We also include comparisons of single-grain, as shown in Table 5. Note that the heavy memory burden of all resolution baseline is not applicable on our RTX 3090.

### 3.4. More details about ablations analysis

Table 4 in manuscript shows that a tremendous drop when adding Entropy-CS in variant 3 and 4. From our perspectives, variant 3 and 4 are based on singleresolution, then variant 3 (w/ entropy-cs)costs about $\frac{1}{4}$ communication of variant 4 . Based on [1], when the communication is too small, the collaborative detection performance will suffer, resulting in a tremendous drop in variant 3 . However, variant 3 still achieves detection gain compared with No Fusion (improved by $9.40 \% / 9.25 \% \uparrow$ in $\mathrm{AP}_{50 / 70}$, respectively).

Meanwhile, AP of variant 2 is worse than variant 4 with comparable ARSV and better ARCV, this is because The ARSV and ARCV only take recall into account, while the AP is weighted by both recall and precision. Therefore, in variants 2 and 4, a high AP does not necessarily mean high ARSV or ARCV values, more details about proposed metrics can be found in Section 1.

### 3.5. Unified framework design

We summarize the main contributions of recent collaborative algorithms in Table 6, , where $\checkmark$ indicates that a unique module is designed and - indicates that general operations are utilized. Our proposed UMC optimizes the communication, collaboration, and reconstruction process with multi-resolution technique.

Table 6. Contribution summary.

| Method |  |  |  |
| :---: | :---: | :---: | :---: |
| Who2com (ICRA 2020 [6]) | $\checkmark$ | - | - |
| When2com (CVPR 2020 [5]) | $\checkmark$ | - | - |
| V2VNet (ECCV 2020 [8]) | - | $\checkmark$ | - |
| DiscoNet (NIPS 2021 [3]) | - | $\checkmark$ | - |
| V2X-ViT (ECCV 2022 [11]) | - | $\checkmark$ | - |
| Where2comm (NIPS 2022 [1]) | $\checkmark$ | $\checkmark$ | - |
| UMC (ours) | $\checkmark$ | $\checkmark$ | $\checkmark$ |

## 4. Detailed architecture of the model

Note that we will release the source code.

### 4.1. Architecture of entropy-CS

```
def acc_entropy_selection(self, tg_agent,
    nb_agent, delta1, delta2, M=3, N=3):
    self.stack = stack_channel(1, 9,
    kernel_size= 3, padding=1)
    w = nb_agent.shape [-2]
    h = nb_agent.shape [ - 1]
    batch_nb = nb_agent.reshape( - 1, 1, 1,
    1)
    stack = self.stack(nb_agent).permute
    (2,3,1,0).contiguous().reshape(-1, 9, 1,
    1)
```

    \(\mathrm{p}=\mathrm{F} . \operatorname{sigmoid}((\) stack - batch_nb) ). mean
    \((\operatorname{dim}=1)\). reshape (w, \(h\) )
    entropy_tmp \(=p *\) torch. \(\log (p)\)
    with torch. no_grad ():
        top_delta \(=\) torch. sort (entropy_tmp
    . reshape \((-1)\), descending=True)
            self_holder \(=\) top_delta \([0][\operatorname{int}(w * h\)
    * delta1)]
    masker \(=\) torch.where(entropy_tmp>=
    self_holder)
    stack_tg \(=\) self.stack (tg_agent).
    permute ( \(2,3,1,0\) ). contiguous (). reshape ( -1 ,
    9, 1, 1)
    \(p_{-} t=F . s i g m o i d((\) stack_tg - batch_nb \())\)
    . mean \((\operatorname{dim}=1)\). reshape ( \(w, h\) )
        entropy_t \(=\) p_t \(*\) torch. \(\log \left(p_{-} t\right)\)
    tmp_masker \(=-\) torch.ones_like (
    entropy-t)
    tmp_masker[masker] = entropy_t[masker]
    with torch. no_grad ():
        top_delta2 \(=\) torch.sort (tmp_masker
    [tmp_masker! \(=-1\) ]. reshape \((-1)\), descending \(=\)
    True)
        thresholds \(=\) top_delta \(2[0][\) int \((w * h\)
        * delta 2\()\) ]
    return torch.where(tmp_masker \(>=\)
    thresholds)
    class stack_channel(nn. Conv2d):
def __init_-(self, in_channels,
out_channels, kernel_size, stride=1,
padding $=0$, bias $=$ False, interplate $=$ 'none'):
super (stack_channel, self).__init_(
in_channels, out_channels, kernel_size=
kernel_size, stride=stride, padding=
padding, bias=bias)
square_dis $=n p . z e r o s(($ out_channels,
kernel_size, $k e r n e l$ _size) )
for i in range(out_channels):
square_dis [i, i//3, i $\% 3$ ] $=1$
self.square_dis $=n n$. Parameter (torch.
Tensor (square_dis), requires_grad=False)


Figure 4. The architecture of G-CGRU.

```
def forward(self, x):
    kernel = self.square_dis.detach().
unsqueeze(1)
    stack = F.conv2d(x, kernel, stride=1,
padding=1, groups=1)
    return stack
        Listing 2. Entropy-CS code
```

Our contribution of entropy-based selection is both theoretical and practical. The intuition of entropycs is low computational complexity and high interpretability. The entropy-cs is no parameter and singleround communication to reduce heavy bandwidth burden brought by multi-resolution technique.

### 4.2. Architecture of G-CGRU

To facilitate understanding, we have simplified many formulas and steps in manuscript. Hence, we add more technique details about the section of Graph-based Collaborative GRU.

For the ego agent $i$ of the $j$-th resolution intermediate feature maps, the inputs of G-CGRU are hidden states $\boldsymbol{h}_{i, j}^{e, t-1}$, the ego agent observation $\boldsymbol{F}_{i, j}^{e, t}$, and the supporters' selected feature maps $\left\{\boldsymbol{F}_{k \rightarrow i, j}^{\prime e, t}\right\}_{k \neq i}$, then the updates for G-CGRU at $t$-th step can be formulated as:

$$
\begin{align*}
& \hat{\boldsymbol{h}}_{i, j}^{e, t-1}=\Lambda\left(\boldsymbol{h}_{i, j}^{e, t-1}, \boldsymbol{\xi}_{i}^{t-1 \rightarrow t}\right) \\
& \boldsymbol{R}_{i, j}^{t}=\operatorname{Reset}\left(\boldsymbol{F}_{i, j}^{e, t}, \hat{\boldsymbol{h}}_{i, j}^{e, t-1}\right) \\
& \boldsymbol{Z}_{i, j}^{t}=\operatorname{Update}\left(\hat{\boldsymbol{h}}_{i, j}^{e, t-1}, \boldsymbol{F}_{i, j}^{e, t}\right) \\
& \boldsymbol{h}_{i, j}^{\prime e, t-1}=\hat{\boldsymbol{h}}_{i, j}^{e, t-1} \odot \boldsymbol{R}_{i, j}^{t}  \tag{1}\\
& \boldsymbol{C}_{i, j}^{e, t}=\operatorname{Collab}\left(\boldsymbol{h}_{i, j}^{e, t-1},\left\{\boldsymbol{F}_{k \rightarrow i, j}^{\prime e, t}\right\}_{k \neq i}, \boldsymbol{F}_{i, j}^{e, t}\right) \\
& \boldsymbol{E}_{i, j}^{e, t}=\boldsymbol{Z}_{i, j}^{t} \odot \boldsymbol{C}_{i, j}^{e, t}+\left(1-\boldsymbol{Z}_{i, j}^{t}\right) \odot \hat{\boldsymbol{h}}_{i, j}^{e, t-1} \\
& \boldsymbol{h}_{i, j}^{e, t}=\boldsymbol{W}_{3 \times 3} * \boldsymbol{E}_{i, j}^{e, t}
\end{align*}
$$

where $\odot, *$ represent dot product and $3 \times 3$ convolution operation, respectively. $\boldsymbol{W}_{3 \times 3}$ indicates trainable parameters. The last time hidden feature $\boldsymbol{h}_{i, j}^{e, t-1}$ needs conduct feature alignment operation from $t-1$ to $t$ to get $\hat{\boldsymbol{h}}_{i, j}^{e, t-1}$, which ensure the $\hat{\boldsymbol{h}}_{i, j}^{e, t-1}$ and $\boldsymbol{F}_{i, j}^{e, t}$ are supported in the same coordinate system.

The Reset and Update gate modules share the same structure. Here we take Reset as an example:

$$
\begin{align*}
& \boldsymbol{W}_{i r}=\sigma\left(\boldsymbol{W}_{3 \times 3} *\left(\left[\hat{\boldsymbol{h}}_{i, j}^{e, t-1} ; \boldsymbol{F}_{i, j}^{e, t}\right]\right)\right) \\
& \boldsymbol{R}_{i, j}^{t}=\sigma\left(\boldsymbol{W}_{i r} \odot \hat{\boldsymbol{h}}_{i, j}^{e, t-1}+\left(1-\boldsymbol{W}_{i r}\right) \odot \boldsymbol{F}_{i, j}^{e, t}\right) \tag{2}
\end{align*}
$$

where $\sigma(\cdot),[\cdot ; \cdot]$ represent Sigmoid function and concatenation operation along channel dimensions. The gate $\boldsymbol{R}_{i, j}^{t} \in \mathbb{R}^{K, K, C}$ learns where the hidden features $\boldsymbol{h}_{i, j}^{e, t-1}$ are conducive to the present.

Based on the above Reset and Update modules, we thus derive the Collab module. To make better collaborative feature integration, we construct a collaboration graph $\mathcal{G}_{c}^{t}(\mathcal{V}, \mathcal{E})$ in Collab module, where node $\mathcal{V}=\left\{\mathcal{V}_{i}\right\}_{i=1, \ldots, N}$ is the set of collaborative agents in environment and $\mathcal{E}=\left\{\boldsymbol{W}_{k \rightarrow i}\right\}_{i, k=1, \ldots, N}$ is the set of trainable edge matrix weights between agents and models the collaboration strength between two agents. Let $\mathcal{C}_{\mathcal{G}_{c}^{t}}(\cdot)$ be the collaboration process defined in the Collab module's graph $\mathcal{G}_{c}^{t}$. The $j$-th resolution enhanced maps of ego $i$ agent after collaboration are $\boldsymbol{E}_{i, j}^{e, t} \leftarrow \mathcal{C}_{\mathcal{G}_{c}^{t}}\left(\boldsymbol{h}_{i, j}^{e, t-1}, \boldsymbol{F}_{k \rightarrow i, j}^{\prime e, t}, \boldsymbol{F}_{i, j}^{e, t}\right)$. This process has two stages: message attention ( $\mathbf{S 1}$ ) and message aggregation (S2).

$$
\begin{align*}
& \boldsymbol{W}_{k \rightarrow i}=\Pi\left(\left[\boldsymbol{h}_{i, j}^{\prime e, t-1} ; \boldsymbol{F}_{k \rightarrow i, j}^{\prime} ;, \boldsymbol{F}_{i, j}^{e, t}\right] \in \mathbb{R}^{K, K}\right. \\
& \overline{\boldsymbol{W}}_{k \rightarrow i}=\frac{e^{\boldsymbol{\boldsymbol { W } _ { k \rightarrow i }}}}{\sum_{m=1}^{N} e^{\boldsymbol{W}_{m \rightarrow i}^{t}}}  \tag{3}\\
& \boldsymbol{C}_{i, j}^{e, t}=\sum_{m=1}^{N} \overline{\boldsymbol{W}}_{m \rightarrow i} \circ \boldsymbol{F}_{m \rightarrow i, j}^{\prime e, t}
\end{align*}
$$

In the message attention stage (S1), each agent determines the matrix-valued edge weights, which reflect the strength from one agent to another at each individual cell. To determine the edge weights, we firstly get the conductive history information from hidden features by Reset gates through $\boldsymbol{h}_{i, j}^{\prime e, t-1} \leftarrow \hat{\boldsymbol{h}}_{i, j}^{e, t-1} \odot \boldsymbol{R}_{i, j}^{t}$. Then, we utilize the edge encode $\Pi$ to correlate the history information, the feature map from another agent and ego feature map; that is, the matrix-value edge weight from $k$-th agent to the $i$-th agent is $\boldsymbol{W}_{k \rightarrow i}=$ $\Pi\left(\boldsymbol{h}_{i, j}^{\prime e, t-1}, \boldsymbol{F}_{k \rightarrow i, j}^{\prime e, t}, \boldsymbol{F}_{i, j}^{e, t}\right) \in \mathbb{R}^{K, K}$, where $\Pi$ concatenates three feature maps along the channel dimension and
then utilizes four $1 \times 1$ convolutional layers to gradually reduce the number of channels from $3 C$ to 1 , more details are shown in Section 4.6. Also, to normalize the edge weights across different agents, we implement a softmax operation on each cell of the feature map.

In the message aggregation stage (S2), each agent aggregates the feature maps from collaborators based on the normalized matrix-valued edge weights, the updated feature map $\boldsymbol{C}_{i, j}^{e, t}$ is utilized by $\sum_{k=1}^{N} \boldsymbol{W}_{k \rightarrow i} \circ$ $\boldsymbol{F}_{k \rightarrow i, j}^{\prime e, t}$, where $\circ$ represents the dot production broadcasting along the channel dimension.

Finally, the collaborative map is $\boldsymbol{E}_{i, j}^{e, t}=\boldsymbol{Z}_{i, j}^{t} \odot \boldsymbol{C}_{i, j}^{e, t}+$ $\left(1-\boldsymbol{Z}_{i, j}^{t}\right) \odot \boldsymbol{h}_{i, j}^{e, t-1}$. Note that the $\boldsymbol{Z}_{i, j}^{t}$ is generated by Update gate and $\odot$ is the dot product. And, the hidden state is updated as $\boldsymbol{h}_{i, j}^{e, t} \leftarrow \boldsymbol{W}_{3 \times 3} * \boldsymbol{E}_{i, j}^{e, t}$.

### 4.3. Architecture of shared encoder

We use the main architecture of MotionNet[9] as our shared encoder. The input BEV map's dimension is $(c, w, h)=(13,256,256)$. We describe the architecture of the encoder below:

```
nn.Sequential(
    nn.Conv2d(13, 32, 3, stride=1, padding=1)
    nn.BatchNorm2d(32)
    nn.ReLU()
    nn.Conv2d(32, 32, 3, stride=1, padding=1)
    nn.BatchNorm2d(32)
    nn.ReLU()
    nn.Conv3D(64, 64, (1,1,1), stride=1)
    nn.Conv3D(128, 128, (1,1,1), stride=1)
    nn.Conv2d(32, 64, 3, stride=2, padding=1)
    nn.BatchNorm(64)
    nn.ReLU()
    nn.Conv2d(64, 128, 3, stride=2, padding=1)
    nn.BatchNorm(128)
    nn.ReLU()
    nn.Conv2d(128, 128, 3, stride=1, padding
    =1)
    nn.BatchNorm(128)
    nn.ReLU()
    nn.Conv2d(128, 256, 3, stride=2, padding
    =1)
    nn.BatchNorm(256)
    nn.ReLU()
    nn.Conv2d(256, 256, 3, stride=1, padding
    =1)
    nn.BatchNorm(256)
    nn.ReLU()
    nn.Conv2d(256, 512, 3, stride=2, padding
    =1)
    nn.BatchNorm(512)
    nn.ReLU()
    nn.Conv2d(512, 512, 3, stride=1, padding
    =1)
    nn.BatchNorm(512)
    nn.ReLU())
        Listing 3. Shared encoder code
```


### 4.4. Architecture of SRAR-based shared decoder

The input of the SRAR-based shared decoder is the intermediate feature output by each layer of the encoder. Its architecture is shown below:

```
nn.Sequential(
    nn.Conv2d(512 + 256, 256, 3, 1, 1)
    nn.BatchNorm2d (256)
    nn.ReLU()
    nn.Conv2d(256, 256, 3, 1, 1)
    nn.BatchNorm2d(256)
    nn.ReLU()
    nn.Conv2d(256 + 128, 128, 3, 1, 1)
    nn.BatchNorm2d(128)
    nn.ReLU()
    nn.Conv2d(128, 128, 3, 1, 1)
    nn.BatchNorm2d (128)
    nn.ReLU()
    nn.Conv2d(128 + 64, 64, 3, 1, 1)
    nn.BatchNorm2d(64)
    nn.ReLU()
    nn.Conv2d(64, 64, 3, 1, 1)
    nn.BatchNorm2d(64)
    nn.ReLU()
    nn.Conv2d(64 + 32, 32, 3, 1, 1)
    nn.BatchNorm2d(32)
    nn.ReLU()
    nn.Conv2d(32, 32, 3, 1, 1)
    nn.BatchNorm2d(32)
    nn.ReLU())
```


### 4.5. Architecture of query generator

The entropy-CS compresses the intermediate feature to generate query matrix by query generator, which is for light communication. Its architecture is shown below:

```
nn.Sequential(
    nn.Conv2d(256, 64, 1, 1, 0)
    nn.BatchNorm2d(64)
    nn.ReLU()
    nn.Conv2d(64, 1, 1, 1, 0)
    nn.ReLU())
```

        Listing 4. Query generator code
    
### 4.6. Architecture of edge encoder $\Pi$

```
class EdgeEncoder(nn.Module)
    def __init__(self, channel):
        super(EdgeEncoder, self).__init__()
        self.conv1_1 = nn.Conv2d(channel, 128,
        kernel_size=1, stride=1, padding=0)
        self.bn1_1 = nn.BatchNorm2d(128)
        self.conv1_2 = nn.Conv2d(128, 32,
    kernel_size=1, stride=1, padding=0)
        self.bn1_2 = nn.BatchNorm2d(32)
        self.conv1_3=nn.Conv2d(32, 8,
    kernel_size=1, stride=1, padding=0)
        self.bn1_3 = nn.BatchNorm2d(8)
```

self.conv1_4 $=\mathrm{nn} . \operatorname{Conv} 2 \mathrm{~d}(8,1$, kernel_size $=1$, stride $=1$, padding=0)

```
def forward(self, x):
```

    \(\mathrm{x}=\mathrm{x} \cdot\) view \((-1, \mathrm{x} \cdot \operatorname{size}(-3)\), \(\mathrm{x} \cdot \operatorname{size}(-2)\),
    x.size( -1 ) )
        x_1 = F.relu (self.bn1_1 (self.conv1_1 (x
    ) ))
x_1 = F.relu(self.bn1_2(self.conv1_2(
x_1)) )
$\mathrm{x}_{-} 1=$ F.relu(self.bn1_3(self.conv1_3(
x_1) ) )
$x_{\_} 1=$ F.relu (self.conv1_4(x_1))
return x_1

Listing 5. Edge encoder code

### 4.7. Architecture of MGFE

```
class MGFE(nn.Module):
    def __init__(self, input_channel):
        super(MGFE, self).__init_-()
        self.guide_v1 = nn.Conv2d(128, 128,
    kernel_size=1, stride=1, padding=0)
        self.guide_v1_bn = nn.BatchNorm2d(128)
        self.guide = nn.Conv2d(256, 256,
    kernel_size=1, stride=1, padding=0)
        self.guide_bn = nn.BatchNorm2d(256)
        self.conv5_1 = nn.Conv2d(512 + 256 +
    256, 256, kernel_size=3, stride=1, padding
    =1)
        self.bn5_1 = nn.BatchNorm2d(256)
        self.conv5_2 = nn.Conv2d(256, 256,
    kernel_size=3, stride=1, padding=1)
        self.bn5_2 = nn.BatchNorm2d(256)
        self.conv6_1 = nn. Conv2d(256 + 128+
    128, 128, kernel_size=3, stride=1, padding
    =1)
        self.bn6_1 = nn.BatchNorm2d(128)
        self.conv6_2=nn.Conv2d(128, 128,
    kernel_size= 3, stride=1, padding=1)
        self.bn6_2 = nn.BatchNorm2d(128)
        self.conv7_1 = nn. Conv2d(128 + 64, 64,
    kernel_size= 3, stride=1, padding=1)
        self.conv7_2 = nn.Conv2d(64, 64,
    kernel_size= 3, stride=1, padding=1)
        self.conv8_1 = nn.Conv2d(64 + 32, 32,
    kernel_size=3, stride=1, padding=1)
        self.conv8_2=nn.Conv2d(32, 32,
    kernel_size=3, stride=1, padding=1)
        self.bn7_1 = nn.BatchNorm2d(64)
        self.bn7_2 = nn.BatchNorm2d(64)
        self.bn8_1 = nn.BatchNorm2d(32)
        self.bn8_2 = nn.BatchNorm2d(32)
    self.norm1 = L2Norm(512)
    self.norm2 = L2Norm(256)
```

$$
\begin{aligned}
& \text { self.norm } 3=\operatorname{L} 2 \operatorname{Norm}(128) \\
& \text { self.norm } 4=\operatorname{L} 2 \operatorname{Norm}(64) \\
& \text { self.norm } 5=\operatorname{L} 2 \operatorname{Norm}(32)
\end{aligned}
$$

def forward(self, x, x_1, x_2, x_3, x_4, enhance_v1, enhance, batch, kd_flag $=0$ ):
enhance_v1 = enhance_v1. view (batch,
-1 , enhance_v1.size (1), enhance_v1.size (2) , enhance_v1.size (3))
enhance_v1 $=$ enhance_v1.permute $(0,2$,

```
1, 3, 4).contiguous()
```

enhance_v1 $=$ enhance_v1. permute $(0,2$,
$1,3,4)$. contiguous ()
enhance_v1 = enhance_v1. view $(-1$, enhance_v1.size (2), enhance_v1.size (3), enhance_v1.size (4)). contiguous ()
guide_v1 = torch. max (F. relu (self.
guide_v1_bn(self.guide_v1 (enhance_v1))), $\operatorname{dim}=1$, keepdim=True) $[0]$
guide $=$ torch. $\max (F$.relu (self.guide_bn (self.guide(enhance))), $\operatorname{dim}=1$, keepdim $=$ True) [0]
x_3_guide $=$ guide $* x_{\_} 3$
$\mathrm{x}_{-} 5=\mathrm{F} . \mathrm{relu}\left(\mathrm{self} . \mathrm{bn} 5 \_1\left(\mathrm{self} . \operatorname{conv} 5 \_1(\right.\right.$ torch.cat ( (self.norm1 (F.interpolate (x_4, scale_factor $=(2,2))$ ), self. norm2 $x_{-} 3 \_$guide $)$, self. norm2(enhance)), $\left.\left.\operatorname{dim}=1\right)\right)$ ) )
$\mathrm{x}_{-} 5=\mathrm{F} . \mathrm{rel} u\left(\mathrm{self} . \mathrm{bn} 5 \_2\left(\mathrm{self} . \operatorname{conv} 5 \_2(\right.\right.$ x_5) ) )
$x_{-} 2=x_{-} 2$. view (batch, $-1, x_{-} 2 . \operatorname{size}(1)$, $\left.x_{-} 2 . \operatorname{size}(2), \quad x_{-} 2 . \operatorname{size}(3)\right)$
$x_{\_} 2=x_{\_} 2$. permute $(0,2,1,3,4)$.
contiguous ()
$x_{-} 2=x_{-} 2$. permute $(0,2,1,3,4)$. contiguous ()
$x_{-} 2=x_{-} 2$. view $\left(-1, x_{-} 2 . \operatorname{size}(2), x_{-} 2\right.$. size (3), $\left.x_{-} 2 . \operatorname{size}(4)\right)$. contiguous ()
x_2_guide $=$ guide_v1 * x_2
$x_{-} 6=F . r e l u\left(s e l f . b n 6 \_1(\right.$ self.conv6_1 ( torch.cat ( (self.norm2 (F.interpolate ( $x_{-} 5$, scale_factor $=(2,2))$ ), self.norm3 $x_{-} 2$ _guide), self.norm3(enhance_v1)), dim =1)) ) )
$x_{-} 6=F . r e l u\left(s e l f . b n 6 \_2\left(s e l f . c o n v 6 \_2(\right.\right.$ x_6)) )
$x_{-} 1=x_{-} 1 \cdot$ view (batch, $-1, x_{\_} 1 . \operatorname{size}(1)$, x_1.size (2), $\left.x_{-} 1 . \operatorname{size}(3)\right)$
$x_{\_} 1=x_{\_} 1$.permute $(0,2,1,3,4)$. contiguous ()
$x_{\_} 1=x_{-} 1$ permute $(0,2,1,3,4)$. contiguous ()
$x_{-} 1=x_{-} 1 . \operatorname{view}\left(-1, x_{-} 1 . \operatorname{size}(2), x_{-} 1\right.$. size (3), $\left.x_{-} 1 . \operatorname{size}(4)\right)$. contiguous ()
$x_{-} 7=F . r e l u($ self.bn7_1 (self.conv7_1 ( torch.cat ((self.norm3 (F.interpolate (x_6, scale_factor $=(2,2))$ ), self. $\left.\operatorname{norm} 4\left(x_{-} 1\right)\right)$, $\operatorname{dim}=1))$ )
def _-init_-(self, $n_{-c h a n n e l s, ~ s c a l e=10.0) ~}^{\text {en }}$
super (L2Norm, self).__init__()
self.n_channels $=n_{-} c h a n n e l s$
self.scale $=$ scale
self.eps $=1 \mathrm{e}-10$
self. weight $=$ nn. Parameter (torch.
Tensor (self.n_channels))
self.weight.data $*=0.0$
self. weight. data $+=$ self.scale
def forward(self, x):
norm $=x \cdot \operatorname{pow}(2) \cdot \operatorname{sum}(\operatorname{dim}=1$, keepdim=
True).sqrt() + self.eps
$\mathrm{x}=\mathrm{x} / \operatorname{norm} *$ self.weight. view $(1,-1$,
1, 1)
return $x$

Listing 6. MGFE code

## 5. Detailed information of Interpolation

We utilize the main architecture of ADP-C[7] as our interpolate function in entropy-CS module. We assume the input feature as $\boldsymbol{f}_{i n} \in \mathbb{R}^{K, K, C}$ and suppose the pixels of the $\boldsymbol{f}_{i n}$ are indexed by $\boldsymbol{p}$. Then, we form a mask $M \in \mathbb{R}^{K, K}$ :

$$
M(\boldsymbol{p})= \begin{cases}0, & \text { if } \boldsymbol{f}_{\text {in }}(\boldsymbol{p})=\mathbf{0}  \tag{4}\\ 1, & \text { otherwise }\end{cases}
$$

Assuming $C$ is a convolution layer with input $\boldsymbol{f}_{i n}$, the by applying the mask, the output $f_{\text {out }}$ at position $p$ becomes:

$$
\boldsymbol{f}_{\text {out }}(\boldsymbol{p})= \begin{cases}C\left(\boldsymbol{f}_{\text {in }}\right)(\boldsymbol{p}), & \text { if } \boldsymbol{M}(\boldsymbol{p})=1,  \tag{5}\\ \mathbf{0}, & \text { if } \boldsymbol{M}(\boldsymbol{p})=0\end{cases}
$$

Denoting the interpolation operation as $\boldsymbol{I}$, the final output feature $\boldsymbol{f}_{\text {out }}^{*}$ is:


Figure 5. Detection results of UMC, Early Fusion, Where2comm, V2VNet and DiscoNet on OPV2V dataset.


Figure 6. Detection results of UMC, Early Fusion, When2com[5], V2VNet and DiscoNet on V2X-Sim dataset.

$$
\boldsymbol{f}_{\text {out }}^{*}(p)= \begin{cases}\boldsymbol{f}_{\text {out }}(\boldsymbol{p}), & \text { if } \boldsymbol{M}(\boldsymbol{p})=1  \tag{6}\\ \boldsymbol{I}\left(\boldsymbol{f}_{\text {out }}\right)(\boldsymbol{p}), & \text { if } \boldsymbol{M}(\boldsymbol{p})=0\end{cases}
$$

The value of $I\left(\boldsymbol{f}_{\text {out }}\right)(\boldsymbol{p})$ is weighted average of all the neighboring pixels centered at $\boldsymbol{p}$ within a radius $r$ :

$$
\begin{equation*}
I\left(\boldsymbol{f}_{\text {out }}\right)(\boldsymbol{p})=\frac{\sum_{s \in \Psi(p)} W_{(p, s)} f_{\text {out }}(s)}{\sum_{s \in \Psi(p)} W_{(p, s)}} \tag{7}
\end{equation*}
$$

where $s$ indicates $p$ 's neighboring pixels and $\Psi(\boldsymbol{p})=$ $\left\{\boldsymbol{s}\|\boldsymbol{s}-\boldsymbol{p}\|_{\infty} \leqslant r, s \neq \boldsymbol{p}\right\}$, the neighborhood of $\boldsymbol{p}$. In UMC, we set radius $r=7 . W_{(\boldsymbol{p}, \boldsymbol{s})}$ is the weight assigned to point $s$ for interpolating at $\boldsymbol{p}$, for which we utilize the RBF kernel, a distance-based exponential decaying weighting scheme:

$$
\begin{equation*}
\boldsymbol{W}_{(\boldsymbol{p}, \boldsymbol{s})}=\exp \left(-\lambda^{2}\|\boldsymbol{p}-\boldsymbol{s}\|_{2}^{2}\right) \tag{8}
\end{equation*}
$$

with $\lambda$ being a trainable parameter. This indicates that the closer $\boldsymbol{s}$ is to $\boldsymbol{p}$, the larger its assigned weight will be. Note that masked-out features $\boldsymbol{M}(\boldsymbol{p})=0$ still participate in the interpolation process as inputs with values of $\mathbf{0}$.

## 6. Detailed Qualitative results

We visualize the detection results between different collaborative approaches on V2X-sim[2] and OPV2V[12] datasets, as shown in Figure 5 and 6.

## 7. Loss curve

We visualize the loss curve of UMC, Early Fusion, When2com, Where2comm, V2VNet and DiscoNet on V2X-Sim and OPV2V on Figure 7 and 8, respectively.


Figure 7. Epoch vs. loss on V2X-Sim dataset.

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Figure 8. Epoch vs. loss on OPV2V dataset.
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