What Can Simple Arithmetic Operations Do for Temporal Modeling? Supplementary Material

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In this appendix, we provide additional details as follows: §A contains more implementation details, §B contains more ablation studies, §C contains additional results.

A. Implementation Details

A.1. Integration of ATM into Existing Backbones

Integration of ATM into ResNet [6]. As shown in Table A.1, we conduct experiments on two types of ResNet architectures: ResNet with basic blocks, and ResNet with bottleneck blocks. The ResNet basic block, which comprises two 3×3 convolutional layers, is utilized in ResNet-18/34. In contrast, ResNet-50/101/152 includes the ResNet bottleneck block, consisting of two 1×1 and one 3×3 convolutional layers. The ATM is integrated once after the last residual block of res₃, where the spatial resolution is 28×28 , in both two ResNet architectures. To optimize computational efficiency, we temporarily reduce the resolution to 14×14 during the Context Spanning operation, followed by upsampling to 28×28 during Domain Transformation.

Integration of ATM into ViT [2]. We seamlessly integrate the ATM into two representative ViT architectures: ViT-Base and ViT-Large, as provided by CLIP [8]. These architectures are outlined in Table A.2. In order to capture temporal cues for each anchor frame, we incorporate the ATM after the multi-head attention module of the 7-th layer in ViT-B (which consists of 12 layers) and after the 14-th layer in ViT-L (which consists of 24 layers). To prepare the input for the ATM, we reshape the visual tokens within the ViT blocks, transforming them from one-dimensional spatial dimensions ($N = H \times W$) to two-dimensional spatial dimensions. As a result, we obtain $X^{\text{IN}} \in \mathbb{R}^{T \times C \times H \times W}$. We then apply the ATM directly to X^{IN} , similar to the way we apply it in ResNet.

A.2. Training Hyperparameters

All experiments are implemented in PyTorch. We use the configuration listed in Table A.3 unless otherwise specified.

stage	ResNet18		ResNet50		output sizes
raw clip	-		-		64×224^2
data layer	stride 8, 1 ²		stride 8, 1 ²		8×224^2
conv_1	1×7^2 , 64 stride 1, 2 ²	1×7^2 , 64 stride 1, 2 ²		8×112^{2}	
$pool_1$	$1 \times 3^2 \max$ stride 1, 2^2		$1 \times 3^2 \max$ stride 1, 2^2		8×56^2
res ₂	$\left[\begin{array}{c}1\times3^2, 64\\1\times3^2, 64\end{array}\right]\times2$		$1 \times 1^{2}, 64 \\ 1 \times 3^{2}, 64 \\ 1 \times 1^{2}, 256$	×3	8×56^2
res ₃	$\left[\begin{array}{c} 1\times3^2, 128\\ 1\times3^2, 128\end{array}\right]\times2$		$1 \times 1^{2}, 128 \\ 1 \times 3^{2}, 128 \\ 1 \times 1^{2}, 512$	×4	8×28^2
res ₄	$\left[\begin{array}{c}1\times3^2, 256\\1\times3^2, 256\end{array}\right]\times2$		$1 \times 1^2, 256$ $1 \times 3^2, 256$ $1 \times 1^2, 1024$	×6	8×14^{2}
res ₅	$\left[\begin{array}{c}1\times3^2,512\\1\times3^2,512\end{array}\right]\times2$		$1 \times 1^{2}, 512 \\ 1 \times 3^{2}, 512 \\ 1 \times 1^{2}, 2048$	×3	8×7^2
	global average	poq	ol, fc		# classes

Table A.1. **Two backbones of the ResNet**. The dimensions of kernels are denoted by $\{T \times S^2, C\}$ for temporal, spatial, and channel sizes. Strides are denoted as {temporal stride, spatial stride²}.

	Embedding	Visio	n Transfo	ormer
Model	dimension	layers	width	heads
ViT-B/16	512	12	768	12
ViT-L/14	768	24	1024	16

Table A.2. Two backbones of the ViT.

B. Ablation Studies

Here, we present additional ablation studies conducted on the Something-Something V1 dataset, specifically using ResNet-18 as the backbone and utilizing 8 frames.

The Effect of Arithmetic Operations. In our ATM, we employ context spanning to generate L context frames for each frame, and then perform arithmetic operations between the features of the anchor frame and the L context frames to

Catting	ResNet			ViT		
Setting	SSV1/V2	K400	SSV1/V2	K400	ANet	Charades
Optimization						
Batch size	6	4	256	256	256	256
Epochs	60	150	20 (<i>B</i>), 15 (<i>L</i>)	20 (<i>B</i>), 15 (<i>L</i>)	15	15
Optimizer	SC	iD	AdamW	$(\beta_1 = 0.9, \beta_2 = 0.99)$	9)	
Initial LR	0.0	01	7e-4	3e-4 (<i>B</i>), 2e-4 (<i>L</i>)	2e-4	2e-4
Layer Decay	-		0.7 (<i>B</i>), 0.75 (<i>L</i>)	0.65 (<i>B</i>), 0.7 (<i>L</i>)	0.7	0.7
LR Schedule	Multi-step	$\gamma = 0.1$		Cosine		
LR Steps	[30,45,55]	[80,120,140]		-		
Weight Decay	5e	-4		0.05		
Linear Warm-Up	-			5 Epochs		
Pre-training	Imagel	Net-1K		WIT-400M		
Augmentation						
Training Resize	MultiSc	aleCrop	Ra	andomSizedCrop		
Rand Augment	-		rand-m7-n4-mstd0.5-inc1	-	-	-
Random Flip	0.	5		0.5		
Repeated Sampling	1			2		
Label Smoothing	-			0.1		
GrayScale	-		-	0.2	0.2	0.2
Mixup	-			0.8		
Cutmix	-			1.0		

Table A.3. Default training recipes. LR denotes the learning rate. B represents ViT-Base and L represents ViT-Large.

extract temporal clues. To evaluate the impact of arithmetic operations, we remove parameter-free arithmetic operations and directly use the features of context frames as temporal clues for the anchor frame. We find that this approach provides a basic level of temporal modeling. Next, we incorporate the outputs of arithmetic operations between the anchor frame and context frames as our temporal clues. We observe that different arithmetic operations yield varying degrees of improvement in temporal modeling, as shown in Table A.4.

Method	Top-1
w/o ATM	16.5%
ATM (Context features)	40.6%
$\overline{ATM}(\mathbf{+})$	41.1%
ATM (—)	43.6%
ATM (X)	46.5%
ATM (+)	43.1%

Table A.4. The effect of arithmetic operations. Backbone: R18.

Different Combinations of ATMs. In this part, we present several approaches for amalgamating ATMs (*e.g.*, ATM (\checkmark) and ATM (\frown)). These approaches include (a) the cascade connection, (b) the parallel connection, and (c) the proposed ATM-style connection, as depicted in Figure A.1. We present the experimental results in Table A.5. The findings indicate that combining ATMs with either the cascade or

parallel style leads to only marginal improvements over a single ATM (\bigstar). This result emphasizes the importance of domain transformation operations that transform signals to a temporal-irrespective stem.

Combinations	Top-1
Single ATM (\bigstar)	46.5%
Single AI M (-)	43.0%
(a) Cascade (b) Parallel	46.0% 46.9%
(c) ATM-style	48.2%

Table A.5. Several combinations of ATMs. Backbone: R18.

C. Additional Results

More Results on Kinetics-400, Something-Something V1 & V2. For readers' reference, we present our results with various views in Table A.7 and Table A.6.

Results on ActivityNet. To demonstrate the generalization ability of our method, we evaluate its performance on the widely-used untrimmed video benchmark, ActivityNetv1.3 [1]. This dataset consists of 19,994 videos ranging from 5 to 10 minutes in length, covering 200 activity categories. We fine-tune the CLIP pre-trained ViT-L backbone with 16 frames on this dataset and report the top-1 accuracy

Mada	Destaria		CELOD	SS	V1	SS	V2
Method	Pretrain	Frame×Crops×Clip	GFLOPS	Top-1	Top-5	Top-1	Top-5
ATM ResNet50	ImageNet-1K	$8 \times 1 \times 1$	37×1	53.9%	81.8%	65.5%	89.9%
ATM ResNet50	ImageNet-1K	$8 \times 1 \times 2$	37×2	54.7%	82.6%	66.1%	90.2%
ATM ResNet50	ImageNet-1K	16×1×1	74×1	56.3%	83.4%	67.4%	91.1%
ATM ResNet50	ImageNet-1K	$16 \times 1 \times 2$	74×2	56.7%	83.6%	67.6%	91.2%
ATM ResNet50	ImageNet-1K	$32 \times 1 \times 1$	148×1	57.1%	84.0%	68.4%	91.5%
ATM ResNet50	ImageNet-1K	$32 \times 1 \times 2$	148×2	57.2%	84.3%	68.5%	91.6%
ATM ResNet50	ImageNet-1K	(8+16)×1×1	111×1	57.6%	84.4%	68.3%	91.6%
ATM ResNet50	ImageNet-1K	(8+16)×1×2	111×2	57.8%	84.8%	68.7%	91.7%
ATM ResNet50	ImageNet-1K	(8+16+32)×1×1	259×1	59.1%	85.7%	69.7%	92.4%
ATM ResNet101	ImageNet-1K	8×1×1	67×1	54.9%	82.3%	66.4%	90.3%
ATM ResNet101	ImageNet-1K	$8 \times 1 \times 2$	67×2	55.8%	82.9%	66.9%	90.7%
ATM ResNet101	ImageNet-1K	16×1×1	134×1	57.2%	84.1%	68.2%	91.5%
ATM ResNet101	ImageNet-1K	$16 \times 1 \times 2$	134×2	57.4%	84.4%	68.6%	91.6%
ATM ResNet101	ImageNet-1K	$32 \times 1 \times 1$	268×1	57.9%	84.3%	69.3%	92.0%
ATM ResNet101	ImageNet-1K	(8+16)×1×1	201×1	58.6%	84.9%	69.4%	92.1%
ATM ResNet101	ImageNet-1K	(8+16)×1×2	201×2	58.9%	85.1%	69.6%	92.3%
ATM ResNet101	ImageNet-1K	(8+16+32)×1×1	469×1	60.0%	86.1%	70.8%	92.9%
ATM ViT-B/16	WIT-400M	$8 \times 1 \times 1$	99×1	58.1%	84.7%	69.4%	92.2%
ATM ViT-B/16	WIT-400M	$8 \times 3 \times 2$	99×6	58.8%	85.4%	70.5%	92.7%
ATM ViT-B/16	WIT-400M	16×1×1	198×1	59.5%	86.1%	70.9%	92.8%
ATM ViT-B/16	WIT-400M	$16 \times 3 \times 2$	198×6	60.6%	86.5%	71.5%	93.0%
ATM ViT-B/16	WIT-400M	$32 \times 1 \times 1$	378×1	60.9%	85.9%	71.6%	93.2%
ATM ViT-B/16	WIT-400M	$32 \times 3 \times 2$	378×6	61.5%	86.2%	71.9%	93.3%
ATM ViT-L/14		8×1×1	421×1	61.9%	87.0%	71.3%	93.1%
ATM ViT-L/14	WIT-400M	$8 \times 3 \times 2$	421×6	62.8%	87.6%	72.1%	93.6%
ATM ViT-L/14	WIT-400M	16×1×1	842×1	63.3%	87.5%	73.1%	93.5%
ATM ViT-L/14	WIT-400M	$16 \times 3 \times 1$	842×3	63.7%	88.0%	73.2%	93.7%
ATM ViT-L/14	WIT-400M	$16 \times 3 \times 2$	842×6	64.0%	88.0%	73.5%	93.7%
ATM ViT-L/14	Merged-2B	$8 \times 3 \times 2$	421×6	64.9%	88.9%	73.7%	94.1%
ATM ViT-L/14	Merged-2B	$16 \times 3 \times 2$	842×6	65.6%	88.6%	74.6%	94.4%

Table A.6. More results on Something-Something V1 & V2.



Figure A.1. The different combinations of $ATM(\bigstar)$ and $ATM(\frown)$.

and mean average precision (mAP) using official evaluation

metrics. As shown in Table A.8, our method outperforms recent works, achieving an mAP accuracy of 94.7%.

Results on Charades. We also conduct experiments on the multi-label video recognition task using the Charades dataset [9]. This dataset consists of over 10,000 short video clips covering 157 action categories. We trained the CLIP pre-trained ViT-L backbone for this task and evaluated the results using the Mean Average Precision (mAP) metric. Table A.9 illustrates the effectiveness of our method in multi-label video classification.

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Method	Pretrain	Frame×Crops×Clip	GFLOPs	Top-1	Top-5
ATM ResNet50	ImageNet-1K	8×3×10	37×30	77.0%	92.9%
ATM ResNet50	ImageNet-1K	16×3×10	74×30	77.6%	93.2%
ATM ResNet101	ImageNet-1K	8×3×10	67×30	78.0%	93.5%
ATM ResNet101	ImageNet-1K	16×3×10	134×30	78.8%	93.7%
ATM ResNet152	ImageNet-1K	16×3×10	191×30	79.4%	93.7%
ATM R101+R152	ImageNet-1K	(16+16)×3×10	326×30	80.5%	94.4%
ATM ViT-B/16	WIT-400M	8×3×4	99×12	84.1%	96.3%
ATM ViT-L/14	WIT-400M	$8 \times 3 \times 4$	421×12	87.3%	97.4%
ATM ViT-L/14	WIT-400M	$32 \times 3 \times 4$	1684×12	88.0%	97.6%
ATM ViT-L/14 (336†)	WIT-400M	$32 \times 3 \times 4$	3784×12	88.2%	97.9%
ATM ViT-L/14	Merged-2B	$8 \times 3 \times 4$	421×12	88.0%	97.6%
ATM ViT-L/14 (336†)	Merged-2B	$8 \times 3 \times 4$	946×12	88.9%	97.8%
ATM ViT-L/14 (336†)	Merged-2B	32×3×4	3784×12	89.4%	98.3%

Table A.7. More results on Kinetics-400.

Method	Top-1	mAP
ListenToLook [5]	-	89.9
MARL [13]	85.7	90.1
DSANet [14]	-	90.5
TSQNet [15]	88.7	93.7
Ours ViT-L	90.2	94.7

Table A.8. Comparisons with previous works on ActivityNet.

Method	Frames	mAP
MultiScale TRN [16]	-	25.2%
STM [7]	16	35.3%
Nonlocal [11]	-	37.5%
SlowFast R50 [4]	8+32	38.0%
SlowFast R101 [4]	16+64	42.5%
LFB+NL [12]	32	42.5%
X3D-XL (312†) [3]	16	43.4%
ActionCLIP [10]	32	44.3%
Ours ViT-L	16	48.5%

Table A.9. Comparison with previous works on **Multi-Label** video dataset Charades.

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