Supplementary Materials for Neural Deformable Models

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1. Detailed Quantitative Results of Biventricular Shape Reconstruction

In Table 1, we show the detailed Chamfer distance (CD), earth mover's distance (EMD) and point-to-surface distance (P2F) for geometric similarity evaluation of LV-endo, LVepi and RV shape reconstructions. Our method outperforms all the baseline methods for LV-endo, LV-epi and RV shape reconstruction, respectively.

In Table 2, we show the detailed normal consistency (NC), easy non-manifold face (ENF) ratio and selfintersection (SI) ratio for reconstructed mesh quality evaluation of LV-endo, LV-epi and RV shapes. On average, our method can generate better cardiac meshes than all the baseline methods.

2. Detailed Quantitative Results of Biventricular Shape Registration

In Table 3, we show the detailed CD, EMD, P2F for LV-endo, LV-epi and RV shape registration accuracy evaluations. Note that we register shapes from ED phase to ES phase. Our method outperforms all the baseline methods for LV-endo, LV-epi and RV shape registration, respectively.

Phase	Method		CD (r	$nm)\downarrow$			EMD ($mm)\downarrow$		$P2F(mm)\downarrow$			
		Endo	Epi	RV	avg	Endo	Epi	RV	avg	Endo	Epi	RV	avg
ED	MR-Net	2.56 ± 1.14	3.32 ± 1.10	3.39 ± 1.07	3.09 ± 1.06	6.04 ± 1.19	6.67 ± 1.71	5.44 ± 1.67	6.05 ± 1.17	1.26 ± 0.984	1.32 ± 0.817	1.82 ± 0.945	1.47 ± 0.877
	NMF	5.85 ± 4.43	5.67 ± 4.33	7.40 ± 8.96	6.31 ± 5.54	6.16 ± 1.37	6.61 ± 1.68	6.73 ± 2.27	6.50 ± 1.43	4.07 ± 3.70	3.45 ± 3.88	5.69 ± 8.03	4.40 ± 4.90
	Ours-un	2.72 ± 0.915	4.38 ± 0.978	8.38 ± 4.46	5.16 ± 1.70	5.93 ± 1.31	6.42 ± 1.60	6.24 ± 1.99	6.20 ± 1.26	1.37 ± 0.704	2.15 ± 0.682	5.81 ± 3.56	3.11 ± 1.30
	Ours	2.25 ± 1.03	2.91 ± 0.762	3.02 ± 0.892	2.73 ± 0.795	5.70 ± 1.14	6.38 ± 1.72	5.33 ± 1.69	5.80 ± 1.17	1.01 ± 0.850	1.06 ± 0.515	1.43 ± 0.712	1.17 ± 0.606
ES	MR-Net	2.11 ± 0.898	2.73 ± 0.755	2.28 ± 0.805	2.37 ± 0.729	2.59 ± 0.524	5.27 ± 1.53	5.64 ± 1.63	4.50 ± 0.666	1.18 ± 0.801	1.16 ± 0.539	1.35 ± 0.767	1.23 ± 0.641
	NMF	3.41 ± 3.10	3.74 ± 1.47	4.05 ± 2.83	3.74 ± 2.26	2.76 ± 0.870	5.29 ± 1.38	6.17 ± 1.72	4.74 ± 0.796	2.25 ± 2.35	2.04 ± 1.13	3.11 ± 2.59	2.46 ± 1.86
	Ours-un	1.97 ± 0.631	3.44 ± 0.663	3.27 ± 1.55	2.90 ± 0.732	2.93 ± 0.633	5.14 ± 1.27	5.37 ± 1.56	4.48 ± 0.656	1.15 ± 0.483	1.77 ± 0.433	1.95 ± 1.13	1.63 ± 0.516
	Ours	1.50 ± 0.542	2.32 ± 0.582	1.92 ± 0.823	1.91 ± 0.556	2.23 ± 0.481	$\textbf{4.92} \pm 1.42$	5.06 ± 1.49	4.07 ± 0.607	0.759 ± 0.397	0.914 ± 0.356	0.947 ± 0.605	0.873 ± 0.392

Table 1. Detailed Chamfer distance (CD), earth mover's distance (EMD) and point-to-surface distance (P2F) for geometric similarity evaluation of LV-endo, LV-epi and RV shape reconstruction, respectively.

Phase	Method	$NC\uparrow$					EN	lF↓		SI↓			
		Endo	Epi	RV	avg	Endo	Epi	RV	avg	Endo	Epi	RV	avg
	MR-Net	0.713 ± 0.034	0.707 ± 0.033	0.866 ± 0.012	0.762 ± 0.024	1.48 ± 0.004	1.48 ± 0.002	1.47 ± 0.004	1.48 ± 0.003	0.035 ± 0.024	0.016 ± 0.012	0.055 ± 0.018	0.035 ± 0.013
	NMF	0.715 ± 0.031	0.707 ± 0.033	0.854 ± 0.024	0.759 ± 0.024	1.47 ± 0	1.47 ± 0	1.44 ± 0	1.46 ± 0	0.011 ± 0.027	0.016 ± 0.026	0.030 ± 0.046	0.019 ± 0.020
ED	Ours-un	0.717 ± 0.033	0.701 ± 0.032	0.835 ± 0.016	0.751 ± 0.022	1.47 ± 0	1.47 ± 0.002	1.42 ± 0.004	1.45 ± 0.002	0 ± 0	0 ± 0.001	0.007 ± 0.011	0.002 ± 0.004
	Ours	0.716 ± 0.032	0.709 ± 0.034	$\textbf{0.871} \pm 0.011$	0.765 ± 0.023	1.47 ± 0	1.47 ± 0	$1.44{\pm}0$	1.46 ± 0	0 ± 0	0 ± 0.001	0 ± 0	0 ± 0
	MR-Net	0.708 ± 0.028	0.698 ± 0.033	0.843 ± 0.017	0.750 ± 0.022	1.46 ± 0.010	1.49 ± 0.003	1.46 ± 0.006	1.47 ± 0.005	0.113 ± 0.042	0.012 ± 0.014	0.078 ± 0.024	0.068 ± 0.018
	NMF	0.716 ± 0.030	0.699 ± 0.034	0.840 ± 0.021	0.752 ± 0.023	1.47 ± 0	1.47 ± 0	1.44 ± 0	1.46 ± 0	0.012 ± 0.025	0.018 ± 0.025	0.051 ± 0.082	0.027 ± 0.030
ES	Ours-un	0.719 ± 0.031	0.693 ± 0.033	0.830 ± 0.015	0.747 ± 0.022	1.47 ± 0	1.47 ± 0.001	1.43 ± 0.004	1.45 ± 0.001	0 ± 0	0 ± 0	0.004 ± 0.006	0.002 ± 0.002
	Ours	0.715 ± 0.032	0.701 ± 0.033	0.857 ± 0.013	0.758 ± 0.022	1.47 ± 0	1.47 ± 0	1.44 ± 0	1.46 ± 0	0 ± 0	0 ± 0.004	0 ± 0.002	0 ± 0.001

Table 2. Detailed normal consistency (NC), easy non-manifold face (ENF) ratio and self-intersection (SI) ratio for reconstructed mesh quality evaluation of LV-endo, LV-epi and RV shape, respectively.

Method		CD (r	$nm)\downarrow$			EMD ($mm)\downarrow$		$P2F(mm)\downarrow$			
	Endo	Epi	RV	avg	Endo	Epi	RV	avg	Endo	Epi	RV	avg
MR-Net	2.19 ± 0.754	2.82 ± 0.789	2.33 ± 0.737	2.44 ± 0.678	4.23 ± 1.09	5.37 ± 1.01	4.63 ± 1.11	4.74 ± 0.635	1.21 ± 0.560	1.44 ± 0.595	1.35 ± 0.627	1.33 ± 0.532
NMF	3.39 ± 2.48	3.85 ± 1.36	4.02 ± 2.34	3.76 ± 1.84	4.18 ± 1.08	5.94 ± 1.25	4.63 ± 1.28	4.92 ± 0.909	2.19 ± 1.91	2.26 ± 1.07	2.90 ± 2.19	2.45 ± 1.54
Ours-un	1.99 ± 0.635	3.58 ± 0.682	3.51 ± 1.58	3.03 ± 0.739	3.75 ± 0.715	5.37 ± 0.803	4.12 ± 1.05	4.41 ± 0.545	1.21 ± 0.484	2.15 ± 0.486	2.37 ± 1.42	1.91 ± 0.603
Ours	1.54 ± 0.535	2.36 ± 0.584	1.91 ± 0.714	1.94 ± 0.525	3.43 ± 0.653	5.18 ± 0.820	3.23 ± 0.872	3.95 ± 0.514	0.827 ± 0.389	1.15 ± 0.390	1.03 ± 0.621	1.00 ± 0.402

Table 3. Detailed Chamfer distance (CD), earth mover's distance (EMD) and point-to-surface distance (P2F) for shape registration accuracy evaluation of LV-endo, LV-epi and RV, respectively. We register shapes from ED phase to ES phase.