Multi-Task Hypergraphs for Semi-supervised Learning using Earth Observations

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\section*{Abstract}

There are many ways of interpreting the world and they are highly interdependent. We exploit such complex dependencies and introduce a powerful multi-task hypergraph, in which every node is a task and different paths through the hypergraph reaching a given task become unsupervised teachers, by forming ensembles that learn to generate reliable pseudolabels for that task. Each hyperedge is part of an ensemble teacher for a given task and it is also a student of the self-supervised hypergraph system. We apply our model to one of the most important problems of our times, that of Earth Observation, which is highly multi-task and it often suffers from missing ground-truth data. By performing extensive experiments on the NASA NEO Dataset, spanning a period of 22 years, we demonstrate the value of our multi-task semi-supervised approach, by consistent improvements over strong baselines and recent work. We also show that the hypergraph can adapt unsupervised to gradual data distribution shifts and reliably recover, through its multi-task self-supervision process, the missing data for several observational layers for up to seven years.

\section{1. Introduction}

The accuracy of deep learning is directly correlated with the quality and quantity of labeled data, especially in the context of supervised learning. Consequently, researchers focused their efforts on unsupervised pretraining methods or learning with limited supervision, by exploiting consistency among multiple tasks. However, a holistic semi-supervised solution that combines information from all available sensors and interpretation layers is still missing. The problem of learning for Earth Observation from satellite data, which we address in this paper, is increasingly important and it would greatly benefit from such a solution, as it includes data from a large number of observation layers, which are often missing due to faulty sensors.

Despite such real-world needs in applications that are by nature multi-task, there are still a very limited number of works that approach the problem from a holistic semi-supervised perspective. Most unsupervised learning papers focus on exploiting relations between only a limited number of tasks, such as relative pose, depth and even semantic segmentation \cite{5, 57, 37, 2, 15, 49, 43, 18, 3, 41} or modalities \cite{22, 28, 53, 34, 21, 55}. On the other hand, other methods that explore the relationships between many tasks do not fully address the semi-supervised learning scenario \cite{52, 51, 12}.

\textbf{Main contributions:} We introduce several contributions, which come to address the limitations of the current semi-supervised multi-task learning literature by offering an integrated and robust solution to the problem: 1) We consider higher-order relationships between several tasks, which represent hyperedges in the hypergraph and can also act as standalone models that predict any output layer (task) from potentially many input ones. 2) Second, we propose to learn robust hyperedge ensembles, which combine multiple pathways reaching a given task node and become unsupervised teachers for the edges and hyperedges trained at the next semi-supervised iteration. 3) Third, we choose a problem that is by nature multi-task and also relevant for our society, that of Earth Observation, which is also novel in the multi-task semi-supervised learning literature.

Our hypergraph approach to the aforementioned problem is related to well-known recent papers on semi-supervised learning using graphs \cite{29, 42, 17, 11, 44, 26, 19, 52, 51}, pretraining and task-specific fine-tuning \cite{14, 23, 6, 7}, teacher-student distillation \cite{30, 46, 16, 47, 54, 13} and semi-supervised learning over multiple iterations \cite{31, 56, 50}. However, previous works are more limited with respect to the number of tasks considered, the lack of higher-order relationships between them or the inability to learn unsupervised. For more specific details of our approach, please go to Sec. 2 onward. For a general overview see Fig. 1.

\textbf{Climate impact.} One of the main contributions of our
Figure 1: Overview of our Multi-Task Hypergraph for Semi-supervised Learning for Earth Observation, using available multi-sensor satellite data from the NEO platform (Planetary 2D maps logged since 2000). We sample data monthly, process it, and use multiple climate indicators to define the structure of our hypergraph: determine the input nodes (Earth observation layers that are always available), output nodes (layers to be predicted), and edge/hyperedge functions (modeling different input to output predictions). Multiple hyperedges will form ensembles to generate pseudolabels for data points with missing layers. We demonstrate that considering pseudolabels during training significantly improves learning over several iterations.

work from a real-world perspective is the chosen problem of Earth Observation, which is essential for better understanding Earth Climate. Climate forecasting for Earth Observation [32] requires solutions from scientific, technical and social domains. Starting from the data, we are limited by the existing infrastructure: actual sensors and satellites, orbiting the Earth and making aggregated observations. One factor that influences the atmosphere and has an insufficiently understood impact is the aerosols, which often occur from natural elements of the Earth’s ecosystem, like sea salt or wildfires. These minute particles can be found at all altitudes and are a complex element of the climate model with both positive (aerosols encourage cloud formation which heats and cools the Earth) and negative (aerosols can reflect solar energy into space) effects [10]. Ocean salinity is another factor that links to the causal chain of climate change, reshaping the density structure of oceans, which leads to a most alarming effect: sea-level changes [8]. Compared to the traditional technique of weather forecasting from [1] or forest cover and road length, which are general prediction tasks exposed in [38], we aim at integrating multiple climate factors, into our Multi-Task Hypergraph and exploit the relationships and consensus formed among different pathways to better understand and form cross-task correlations between multiple Earth layers. We experimentally show that for having a robust prediction of a given climate variable, we need multiple sensors that interact with each other and coordinate on different prediction paths.

Remote sensing and AI for climate change. With the help of aerial images, we can monitor the transitional stages of vegetation over a large period of time and determine the potential impacts of land and forest biomass. The work from [25] fuses different ocean satellite images together using classical Computer Vision techniques to provide a high-quality ocean dataset for scientific purposes. The work from [48] uses various modalities, such as CO₂ and vegetation to predict the gross primary production (GPP) of a particular area, which is a determiner of the quality of life. The authors from [40] use GNNs and satellite imagery to predict air quality in relation to COVID-19 spreading during the 2020 pandemic. The work from [39] used a CNN-based approach to detect clouds from satellite images, which are then further used to process other types of modalities where cloud removal is necessary. The model proposed in [45] is a classification framework for the identification of believer/denier attitudes expressed on social media platforms regarding the climate change problem. This work formulates environmental deviations as a multi-task learning problem within the natural language domain by combining stance detection and sentiment analysis. Other works [27] used a multi-modal neural network to detect benthic tropical marine systems, such as coral reefs. In a recent article [9], the authors formulate the Land Cover Classification task as a Multiple Instance Learning regression problem to reduce the computational cost.

While there is a rapidly increasing body of literature on AI for understanding the Earth Climate, our model is the first, to our best knowledge, that offers a holistic multi-view semi-supervised approach. We argue that such an integrated research direction is needed for capturing the Earth System in its full interconnected complexity.

2. Our Approach

Our multi-task hypergraph (Fig. 1) has two sets of nodes, each node representing a different layer (view) of the world: known input nodes (N_i) and predicted output nodes (N_o). These nodes are connected by edges and hyperedges, such that, within each hyperedge (or edge) one or several nodes
learning to minimize the L2 loss: $\|Y_{\text{ens}}^i - Y_{gt}^i\|_2$.

**Step 3 - Generate pseudolabels:** At iteration $k$, on the Unlabeled Set $S_U$, we pass information (inference) from input nodes $X_i$ all the way to the output ones, using the set of learned edges, hyperedges and their ensembles, to produce final pseudolabels $Y_{\text{ens}}^{i,k}$ for each output node $i$.

**Step 4 - Semi-supervised learning:** We add the Unlabeled Set $S_U$ with the newly generated pseudolabels to the fully Labeled Set $S_L$, and retrain from scratch all the neural links used to form edges and hyperedges, by minimizing the total sum of squared error loss over all links, which map inputs to outputs directly and can be efficiently trained independently:

$$L = \sum_{i=1}^{N_o} \left( \sum_{X \in S_L} \|f_i(X) - Y_{gt}^i\|^2_2 + \sum_{X \in S_U} \|f_i(X) - Y_{\text{ens}}^{i,k}\|^2_2 \right)$$

(1)

After retraining the links (which implicitly updates all edges and hyperedges), we return to Step 2 for a new semi-supervised learning iteration $k \rightarrow k + 1$, until convergence.

### 3. Multi-Task Hypergraph Structure

Below we present the different types of hyperedges and ensemble models that define our hypergraph:

#### 3.1. Hyperedges

Within the structure of our hypergraph, we form four types of hyperedges: 1. **Edges (E):** They learn a transformation between each input node to an output node through a single neural network link, for a total of $N_i \times N_o$ edges. 2. **Ensemble Hyperedges (EH):** All the edge (E) predictions for an output node are combined using the pixelwise median ensemble function, to obtain an output map for each of the $N_o$ output nodes (T=1). Then from each such output map at T=1, we learn a separate link for each of the remaining $N_o - 1$ output nodes (T=2). Thus, each output receives (at T=2) $N_o - 1$ candidates from such EH edges, which are $N_o(N_o - 1)$ in total number. 3. **Aggregation Hyperedges (AH):** They concatenate all input nodes and use a single direct neural link (with a modified input volume to include all input layers) to directly produce an output node. There are in total $N_o$ AH hyperedges in the hypergraph. 4. **Cycle Hyperedges (CH):** They concatenate all the $N_i$ input nodes together with the $N_o$ outputs of all AH hyperedges (T=1) to produce the output node at T=2 by another direct link (with correctly modified input volume). There is one such CH hyperedge for each of the $N_o$ nodes.

#### 3.2. Multi-path Ensemble Models

Different from previous work, which used simpler non-parametric ensemble models for generating pseudolabels at
output nodes, we introduce ensembles that learn how to combine the different candidates at each output node layer and get retrained with each semi-supervised iteration. We propose several such models, starting from simpler ones that linearly combined the candidates using fixed weights, to more powerful ones, using neural nets, that learn to produce directly a final output map from several candidates.

We also introduce an automatic input candidate selection procedure for all ensemble models, which learns a non-linear weight function \( \frac{1}{1+\exp(-\alpha c)} \) per input candidate channel, by which we multiply each candidate before entering the ensemble model. Being between 0 and 1, this weight effectively turns on or off a given candidate, and thus learns to keep only the relevant ones, for improved robustness. In Fig. 3 we show the different learned selection and ensemble models, which are of the following types: S-LFW is a linear model with selection, which learns to linearly combine the channel candidates by a fixed set of weights \( w_c \), such that the final weight per candidate is effectively \( w_c \frac{1}{1+\exp(-\alpha c)} \). S-NNFW: a neural net model with selection, which learns to produce a dynamic weight \( w_c \) per channel (that changes dynamically depending on the input), such that the final output is obtained by linearly combining the channels multiplied by the dynamic weights. S-NNDPFW: a neural net model with selection, which learns to produce a dynamic pixelwise weight \( w_{ci} \) per channel \( c \) and pixel \( i \), such that the final output is obtained by linearly combining the pixels of each input channels multiplied with the corresponding output pixelwise weights. S-NNFW: a neural net with selection, which learns a direct transformation between all input candidate layers to the final output. Note that, in principle, S-NNFW is the most flexible, non-linear model. However, since the ensembles are trained on the limited Labeled Set \( S_L \), where true target values are available, a simpler weighted combination of the input channels (fixed, dynamic or pixelwise dynamic) could be more robust. What changes in the training of these ensembles during semi-supervised iterations are their input candidates \( Y_c \) - produced every iteration by updated edges and hyperedges. Also note that all these models, including the initial selection module, are trained end-to-end.

4. Implementation Details

We used PyTorch [35] as our main Python Machine Learning framework, alongside [33] for the semi-supervised iterative graph-ensemble library. Below we detail the architecture of the direct neural links (DNL):

Direct neural link architecture (DNL): This link is the building block used to create all edges and hyperedges. It is a small U-Net of 1M parameters, the same as the one used in NGC [26]. It has an encoder branch with 3 down-sampling blocks, a central part with summed dilated convolutions and increasing dilation rates of 1, 2, 4, 8, 16 and 32, and a decoder with three up-scaling blocks. All kernels are of size \( 3 \times 3 \), and each dilated convolution produces a set of 128 activation maps. Each downsampling block has 2 convolution layers with stride 1, followed by a convolution layer with (2, 2) strides to halve the feature maps. Similarly, each up-scaling block consists of a transposed convolution layer, a feature map concatenation with the corresponding map from the downsampling layers and 2 convolutional layers with stride 1. The number of feature maps is 16, 32 and 64 for the downsampling blocks and the opposite order for the upsampling blocks. Across the entire network, we only use ReLU as the activation function.

Training details. We used the same training setup for all neural links that form the edges and hyperedges. All learning tasks are treated as regression problems, with standard L2-norm loss function. The networks are optimized for 100 epochs, with the Adam optimizer, an initial learning rate of 0.01 and a learning rate scheduler, that after an initial 10 epochs, divides by 2 the current learning rate if there is no improvement for 5 consecutive epochs.

Training infrastructure. We used a medium-sized server with 8x NVIDIA 2080ti, a Xenon Gold 5218 CPU and 512GB of RAM. On average, training one edge (1 input and 1 output) took between 1-2h, depending on the iteration.

5. Experimental Analysis

NASA Earth Observations. We use the multi-layer representations from the Earth Observations NEO Dataset provided by NASA [32]. Satellites continually orbit the globe,
collecting information about Earth in five main domains: Atmosphere, Energy, Land, Life and Ocean. In order to maximize the amount of overlap between multiple layers in time we sample monthly data points for each representation spanning the period from 2000-2022. The NEO dataset consists of multiple satellite observations, each of them being a monthly aggregate of that particular representation. Although we tried to maximize the amount of overlap between the representational layers, we faced challenges due to missing data, as some sensors began or ended at different points in time.

**Graph configuration for NEO data.** We use the following 12 representations as input nodes: Normalized Difference Vegetation Index (NDVI), Snow Cover (SnowC), Land Surface Temperature Day and Night (LSTD, LSTN), Cloud Optical Thickness (CLODT), Cloud Particle Radius (CLPRD), Cloud Fraction (CLFR), Cloud Water Content (CLCW), Nitrogen Dioxide (NO2), Ozone layer (OZONE), Chlorophyll (CHLORA), Sea Surface Temperature (SST). Our multi-task learning graph predicts the following 7 types of output representations: Aerosol Optical Depth (AOD), Active Fires (FIRE), Water Vapor (WV), Anomaly Layers for LSTN and LSTD (LSTNAN, LSTDAN), Leaf Area Index (LAI) and Carbon Monoxide (CM). Visual samples are provided in Figure 1. All maps corresponding to raw sensor values, from the NEO platform [32], were rescaled to a resolution of 1080 × 540 and normalized in a range of [0 : 1]. As explained in Sec. 3), we have \( N_i \times N_o = 84 \) single edges (E), \( N_o \times (N_o - 1) = 42 \) ensemble hyperedges (EH), \( N_o = 7 \) aggregation hyperedges (AH) and \( N_o = 7 \) cycle hyperedges (CH). Please see again Figure 2 for a visual presentation of these types of hyperedges.

**Dataset Split.** The Labeled Set, used for supervised learning (Iteration 1) of all neural links, consists of the first 119 months. The following 30 months, the Test Set, are used for evaluation. The next remaining 62 months (until 2022) represent the Unlabeled Set, used for semi-supervised learning (Iteration 2). The main steps of the learning algorithm are presented in Sec. 2.

**Dataset timespan details.** Visual samples from the dataset show that some layers can have large areas of missing information (blank), depending on what a particular sensor is focusing on: e.g. land (sparse) or atmosphere (dense), which makes learning transformations between each of these layers cumbersome. The visual differences between each of the selected layers from the dataset are highlighted in Figure 4. Our selection of Earth layers from NEO was not arbitrary. The data spans the period between 2000-2022, but as Figure 5 shows, there are still many missing data points. Although we tried to maximize the amount of temporal overlap between multiple representational layers, we still had some missing data points for observations such as NO2 and OZONE where the data collection started in 2004, and for LAI and CM, where it stopped in 2017. This lack of data points motivates our choice of dataset split - since we can use our hypergraph to generate pseudolabels and then use them in the iterative semi-supervised learning procedure. In the lower part of Fig. 5, we present the dataset split. Train indicates \( S_L \), the period used for supervised training (Iteration 1). Where data is missing (Unlabeled Set \( S_U \)), we generate pseudolabels and use them alongside ground truth for semi-supervised training (Iterations 2 and 3).

**Evaluation metrics.** Our main metric is the Relative Performance Improvement (RPI) with reference to the L2 score, against a fixed baseline: \( RPI\% = \frac{(L2(y_{\text{baseline}}, gt) - L2(y_{\text{pred}}, gt))}{L2(y_{\text{baseline}}, gt)} \cdot 100 \). We use this due to scaling issues that arise when using absolute values for multiple tasks, each of them having its own scale. The fixed baseline is the top-performing supervised edge (E) for each task. Furthermore, the L2 metric is computed as \( L2(y, gt) = \sum_{\text{mask}}((y - gt) \cdot \text{mask})^2 \sum_{\text{mask}}(gt \cdot \text{mask}^2) \), where \( mask = (gt \neq \text{NaN}) \). Since satellite maps contain invalid values in the regions where the sensors could not pick any reliable information, we only train and evaluate on the valid ones. Here, mask refers to a binary map, with a constant of 1 only for valid data. For clarity and analysis of the overall trends, we also report the Average Relative Performance Improvement (ARPI), that is the average of the RPI across all tasks combined.

### 5.1. Comparison to multi-task baselines

One of the main objectives of multi-task learning is to leverage multiple tasks simultaneously in order to improve generalization performance across all tasks. Due to the problem of negative transfer [24], it is still unclear how to combine these tasks without hurting the overall performance. Our experiments here also prove this point (Tab. 1). We consider 3 multi-task baselines to compare against, referred to as MTE, with different numbers of parameters:

<table>
<thead>
<tr>
<th>Method</th>
<th>Iteration 1 (sup)</th>
<th>Iteration 2 (semi-sup)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MTE-1M</td>
<td>-37.91</td>
<td>-33.83</td>
</tr>
<tr>
<td>MTE-70M</td>
<td>-15.22</td>
<td>-10.15</td>
</tr>
<tr>
<td>MTE-140M</td>
<td>-37.33</td>
<td>-39.89</td>
</tr>
<tr>
<td>HG-140M</td>
<td><strong>7.77</strong></td>
<td><strong>8.85</strong></td>
</tr>
</tbody>
</table>

Table 1: Quantitative comparison in ARPI (↑) to multi-task baselines (MTE) with different numbers of parameters, varying from 1M (similar to one edge) to 140M (similar to the whole hypergraph), for both supervised and semi-supervised scenarios. MTE concatenates all input nodes and transforms them into all output ones. Our hypergraph (HG) is vastly superior, while the highly inter-connected MTE clearly overfits. This justifies our multi-path hyperedge ensemble approach.

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addressed in this paper. In the semi-supervised case, the hypergraph and the MTE models are all trained on the same available ground truth together with the pseudolabels they generate on the Unlabeled Set.

5.2. Impact of the unsupervised ensemble teachers

Before proceeding with the iterative semi-supervised learning scenario, we first evaluate the performance of the ensemble models proposed, to better understand the importance of learning to combine the candidates for each given output node. We also compare our ensembles with relevant published methods, such as the powerful Extreme Gradient Boosting method [4], in two variants, linear XGB-L and tree-based XGB-T, and recent work on multi-task graphs, based on non-parametric ensembles, such as NGC [26] (simple mean ensemble without selection) and CShift [20] (pixelwise kernel-based ensemble). We also add to the pool a simple ensemble, S-Mean, which simply averages the candidate layers after our automatic candidate selection procedure. In these tests, We let all approaches (including ours) have access to the same candidate layers, but using only Edges and Ensembles Hyperedges (EH). For a study of how the addition of the more complex hyperedges (AH and CH) boosts performance, see Sec. 5.6. The results, reported in Tab. 2, show that the selection procedure improves performance (e.g. see S-Mean vs. NGC and CShift), while an increased degree of model flexibility also improves performance. However, the top performer is not the most flexible full neural net mapping (S-NN\textsubscript{D}) from input layers to output, but the next most flexible model that produces dynamic pixelwise linear weighting of the input layers (S-NN\textsubscript{DPW}). In general simpler linear models (S-L and XGB-L) prove robust in these experiments, due to the limited unlabeled training data on which richer models can easily overfit.

1.1M (the same as one edge), 70M and 140M (the same as the whole hypergraph). The MTE is a single U-Net model, having a similar basic structure as our neural links (but different number of filters), which takes all 12 input layers and transforms them into all 7 output ones. The results show that such a model, which maps input to output, and lacks the robust multi-path hypergraph structure is not able to generalize when having very limited labeled data. By varying the number of parameters from very small to large, we show that this is not a problem of model capacity, but rather of model structure, which is exactly one of the main issues addressed in this paper. In the semi-supervised case, the hypergraph and the MTE models are all trained on the same available ground truth together with the pseudolabels they generate on the Unlabeled Set.

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presents the distillation

CM and AN, (7) - AN, with reference to the best-performing LAI, AOD we show the quantitative results (using the ARPI AN FW FIRE. The first ensemble gives equal weights to the 6 WV LSTN LSTD, (3) - , (4) - .


S-Mean 3.31 14.71 12.42 8.97 -9.50 -2.48 5.93 4.77 S-SLR$, FW$ $XGB-L$ $CShift$ $NGC$ $Ens. Type (1) (2) (3) (4) (5) (6) (7) ARPI ($\uparrow$)


Table 2: Evaluation on the Test Set of different ensemble models, for each output node separately (using RPI metric) and overall (ARPI metric). Ours have names starting with “S-” (denoting our proposed automatic candidate selection procedure). The best numbers are bolded, while the second best are underlined. We report relative performance (in percentage) for each output node in order: (1) - AOD, (2) - CM, (3) - FIRE, (4) - LAI, (5) - LST$D_{AN}$, (6) - LST$N_{AN}$, (7) - WV, with reference to the best-performing edge for each task.

5.3. Impact of semi-supervised learning iterations

For the scenario of multiple iterations of semi-supervised learning, when unlabeled data is added, we experiment with three ensemble models for generating pseudolabels, ranging from simple to more complex: S-Mean, S-LR$, FW$ and S-NN$D_{W}$ . The first ensemble gives equal weights to the candidate layers, the second has different but fixed weights, while the third linearly combines the pixels of the input layers with weights that change dynamically, depending on the input. The same ensemble is used for each iteration of semi-supervised learning, resulting in three different hypergraph models (each with its own ensemble type) - so we can evaluate the impact of these types of ensembles completely independently, through several semi-supervised iterations. In Figure 6 we show the quantitative results (using the ARPI metric, over all tasks). The Distillation plot shows the average of the best-performing edges per task, after each semi-supervised retraining iteration (e.g., the distilled iteration 2 edges are the ones retrained on the ground truth labels + pseudolabels obtained at Iteration 1). Interestingly, the results show that very simple models, such as S-Mean are not able to sustain the effectiveness of semi-supervised learning over several iterations, while models of medium complexity (such as S-LR) could be almost as efficient as more powerful ones based on neural nets (S-NN). Note that the improvement in the distilled single best edge due to our semi-supervised hypergraph training means that there is in fact no added time or memory cost at test time. The hypergraph can be efficiently used only at training time.

5.4. Improving over temporal distribution shifts

We analyze the evolution of prediction errors across 7 years. These tests are conducted on 5 out of the 7 tasks, for which we had continuous ground truth labels for evaluation. Results are reported in Figure 7. In the left plot, we start with the average L2 error of the edge baselines (trained fully supervised) across all tasks (blue line). We observe that the error follows a sinusoidal curve, which correlates precisely with the different times of the year (seasons). We also add a smoothed and linear fit variant and observe that the error increases as we stray away from the Labeled Set used for training the edges. The relative error increase between 2014 and 2021 is 7.79%. Also, there is an increase in the oscillation amplitude as well. These changes in error average and variance suggest that the data distribution is gradually shifting, probably due to changes in the Earth’s climate. It also motivates the need to be able to continuously track such changes in an unsupervised way, when real ground truth data is missing.

The right-side plot from Figure 7 presents the distillation
results, on the same single edges as the first plot, following the iterative training done on $S-NN_{DW}$, but also averaged across each year to cancel the seasonal changes. We present relative errors to the baseline, with 0 being the result of the first plot. The only difference between the first iteration and the next one are the pseudolabels added. We observe that, on average and across all tasks, adding pseudolabels not only improves the predictions but also stabilizes the distribution shift across time. We also observe that Iteration 3 improves over Iteration 2, but the added value is lower.

### 5.5. Improving temporal consistency

We introduce a time-consistency metric, as the inverse of the prediction variance at a given geographic location (pixel) across a short time window centered around a given moment in time. True values at a given location, do not fluctuate strongly, on average, over short periods of time - so the lower this variance, the more consistent and trustworthy the results should be, in general. For each particular output task, we compute all such variances for all locations and around all moments in time, in the test data set - and take the average as the overall consistency for a given task.

Our experiments reveal that the semi-supervised learning iterations (when pseudolabels are added) significantly improve, for the same edges, not only average performance (ARPI) but also the temporal consistency, for all tasks (Table 3). We compare the distilled version at Iteration 3 of the same network against its supervised counterpart (baseline).

It should be noted that better consistency does not necessarily mean better performance, but rather a complementary score to performance. A constant prediction of 0 would have perfect consistency, however, the performance of the prediction would be bad. This metric can help us choose between two classifiers with similar performance but with different consistency scores. For a video representation of consistency maps, see [36].

### 5.6. Impact of complex hyperedges vs edges

We evaluate the introduction of the more complex cycle and aggregation hyperedges (as presented in Fig. 2 and Sec. 3), to study the effect of these more robust candidates in the selection and aggregation ensemble process. For the previous tests, we used a pool of 18 candidates for each output node (12 edges(E) and 6 ensembles hyperedges EH) when creating our ensembles. In Tab. 4 we show the results where we add these two hyperedges to the selection and aggregation pool, resulting in an ensemble of 20 edges, for each output node. Also, when we evaluate the performance of each edge or hyperedge independently for each task, one or both of these two complex hyperedges are the top performers on 5 out of 7 tasks. This clearly demonstrates the power of capturing higher-order relationships between tasks, but the power of the ensembles remains of great importance, as shown by our comparisons between different ensemble models and to single large nets MTE baselines.

### 6. Conclusions

Our novel semi-supervised learning approach learns from robust ensemble teachers in a multi-task hypergraph of neural nets. Our experiments prove several points: 1) the addition of hyperedges that capture higher-order relationships between tasks can bring a strong boost to the performance of the ensemble teachers and the overall multi-task system. 2) Learning how to select and combine the relevant candidates also significantly boosts performance and improves the effectiveness of unsupervised learning. Also, when faced with very limited labeled data, simpler (e.g. selection + linear regression), but not simplistic (plain average) ensemble functions, can be almost as powerful as complex ones (neural nets). 3) Grouping the set of tasks into separate hyperedges and then combining them through ensembles can be much more robust than considering all tasks together in a single dense neural net. 4) Our multi-task hypergraph is also able to handle, self-supervised, multi-task distribution shifts that take place over longer periods, which makes it suitable for further development in the context of semi-supervised continual learning.

**Acknowledgements:** This work was funded in part by UE-FISCDI, under Projects EEA-RO-2018-0496 and PN-III-P4-ID-PCE-2020-2819 and by a Google Research Gift.
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