



# Seal Your Backdoor with Variational Defense

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#### **Abstract**

We propose VIBE, a model-agnostic framework that trains classifiers resilient to backdoor attacks. The key concept behind our approach is to treat malicious inputs and corrupted labels from the training dataset as observed random variables, while the actual clean labels are latent. VIBE then recovers the corresponding latent clean label posterior through variational inference. The resulting training procedure follows the expectation-maximization (EM) algorithm. The E-step infers the clean pseudolabels by solving an entropy-regularized optimal transport problem, while the M-step updates the classifier parameters via gradient descent. Being modular, VIBE can seamlessly integrate with recent advancements in self-supervised representation learning, which enhance its ability to resist backdoor attacks. We experimentally validate the method effectiveness against contemporary backdoor attacks on standard datasets, a large-scale setup with 1k classes, and a dataset poisoned with multiple attacks. VIBE consistently outperforms previous defenses across all tested scenarios.

### 1. Introduction

Deep models possess enough capacity to learn any pattern present within the data [8, 42, 101]. This remarkable flexibility comes at the cost of control since it limits our ability to influence the specific motifs the model learns [2, 37]. For instance, a model may base its decisions on image backgrounds rather than focusing on the actual objects [21]. Such bias towards simpler [75] and possibly spurious patterns [34] may lead to undesirable generalizations that reveal themselves only in specific test cases. This deep learning loophole can be maliciously exploited by attackers who manipulate training examples using triggers that steer the model towards harmful generalization. Such practice is commonly referred to as *backdoor learning* [49] and presents a serious threat in contemporary machine learning.

The majority of existing backdoor attacks [12, 23] modify a portion of the training dataset by installing triggers

onto selected inputs and altering the corresponding labels<sup>1</sup>. On such data, standard supervised learning delivers a *poisoned* model [49]. During inference, attackers can exploit the installed backdoor by applying triggers to the desired inputs, which causes the model to behave maliciously [23, 60]. Our goal is to defend against such attacks by training a *clean* model invariant to triggers present in the data.

Recent empirical defenses [11, 53, 107] partition the training dataset into clean and poisoned subsets according to some heuristics. The two subsets then take different roles during the model training (*e.g.* semi-supervised learning with labeled clean data and unlabeled poisoned data [33]). However, heuristics are prone to failure modes and can be exploited by adaptive attacks [67]. Also, pruning labels often leads to information loss, ultimately degrading recognition performance. Our approach avoids data partitioning and label pruning. Instead, we leverage optimal transport to refine potentially corrupted samples and labels into clean pseudolabels that guide the training of a robust classifier.

In this work, we present VIBE (Variational Inference for **B**ackdoor Elimination), a framework for training backdoorrobust classifiers on poisoned data. Our key concept is to treat dataset examples and the corresponding corrupted labels as observed random variables, while the desired clean labels are latent. Then, we achieve resilience against backdoor attacks by recovering the latent clean posterior parametrized as a deep classifier. VIBE training takes the form of an expectation-maximization algorithm that alternates between classifier updates via gradient descent (Mstep), and inference of approximate clean class posterior (E-step). In practice, the approximate clean labels are recovered by solving an entropy-regularized optimal transport problem [15]. We validate the resilience against contemporary backdoor attacks on standard benchmarks, on a largescale setup with 1k classes, and on a dataset poisoned with multiple attacks. Experiments indicate consistent improvements over previous defenses in all tested scenarios. Remarkably, VIBE attains over 12pp absolute improvement in

<sup>&</sup>lt;sup>1</sup>Some attacks do not alter the labels [80]. However, our experiments show that they are much easier to defend from.

ASR over the best baseline on the CIFAR-10 dataset.

### 2. Related work

**Backdoor attacks.** Backdoor attacks achieve malicious model behaviour through direct modifications of trainable parameters [70], changes in model structure [31], or data poisoning [23]. Contemporary machine learning models are trained in-house and deployed via APIs which makes parameter- and structure-based attacks largely impractical. Therefore, we focus on a more realistic scenario where the attacker only controls the data collection process.

Early data poisoning attacks [23] steer the model towards malicious generalization by introducing localized triggers and altering the corresponding labels. Subsequent attacks rely on invisible [13, 36, 67, 83] or sample-specific [46, 102] triggers, which are significantly harder to detect. Clean-label attacks [6, 80, 99] avoid modifying labels altogether but typically deliver lower attack success rates. All these approaches devise broad method-agnostic attacks. Contrary, recent adaptive attacks improve effectiveness by targeting the latest defenses [20, 33].

Another line of work considers data poisoning attacks that target contrastive self-supervised learning [45, 51, 73]. However, these attacks may require access to the optimization procedure [35] and typically have a lower success rate than direct attacks on supervised learning [45]. A detailed survey of backdoor attacks can be found in [49].

**Backdoor defenses.** Existing defenses can be categorized as either certified or empirical. Certified defenses provide theoretical guarantees of success [92]. However, their underlying assumptions typically do not hold in practice [49]. Empirical defenses devise preprocessing strategies to avoid training on corrupted examples [79], correct the malicious generalization of poisoned models via postprocessing [54], or propose heuristic additions to standard training algorithms [48]. Preprocessing-based defenses [9, 25, 32, 39] aim to filter out poisoned examples from the dataset, allowing the remaining clean data to be safely used for supervised training. Such methods cannot distinguish poisoned examples from their hard counterparts with the correct label [39].

Post-training defenses [47, 64, 93, 100] focus on removing backdoors from already trained models. A common approach involves re-synthesizing the injected triggers and using them to purify the model [24, 55, 68, 76, 77, 81, 86, 91, 94, 106]. Other approaches correct malicious generalization through model pruning [50, 52, 90], knowledge distillation [98], loss landscape analysis [104], or by enhancing robustness against adversarial examples [59]. All these methods assume access to a small subset of definitively clean data, which may not be available in practice.

Training-time defenses [11, 20, 33, 53, 72, 87, 103, 105, 107] attempt to train robust classifiers from poisoned data. An early approach [47] isolates poisoned examples in early

training stages and later uses them to unlearn the backdoors. Subsequent methods [11, 20, 33] focus on removing only the labels of potentially poisoned samples and proceed with semi-supervised training. These approaches identify the poisoned data by heuristics, which increases the defense vulnerability. VIBE avoids such heuristics by recovering clean pseudolabels through variational inference.

Representation learning. The main goal of representation learning [65, 71, 85] is to recover features that generalize across a spectrum of downstream tasks. A widely used representation learning strategy involves optimizing self-supervised pretext objectives [22, 62]. Recent such methods reconstruct masked inputs [30], optimize contrastive objectives [10] or learn latent centroids [63]. Representation quality can be further enhanced by training on large multimodal datasets [69], which delivers effective features even without fine-tuning on target datasets [14, 63].

Representation learning received limited attention in the context of backdoor defenses. Initial works design heuristics that leverage self-supervised representations to remove poisoned labels [33] or filter the dataset [82]. These heuristics fail for some attacks, as indicated by our experimental evaluation. In contrast, VIBE uses self-supervised pretraining to jumpstart the optimization process.

Recent works [7, 26, 95, 96] suggest that (multimodal) contrastive learning can be conveniently adapted to resist data poisoning attacks that target self-supervised pretraining. Pre-training VIBE feature extractor according to such objectives further boosts the performance.

**Latent variable models.** Latent variable models [19] explain relations between observed random variables with latent variables. This concept is successfully applied in different fields [40, 56, 88]. VIBE introduces latent variables into backdoor defenses by viewing clean labels as latents.

### 3. Backdoor resilience via variational inference

**Problem setup.** Let  $\mathcal{D}_{\text{raw}} = \left\{ (\tilde{\boldsymbol{x}}^i, l^i) \right\}_{i=1}^N$  be a benign dataset consisting of input examples  $\tilde{\boldsymbol{x}}^i \in \mathcal{X}$  and clean labels  $l^i \in \mathcal{Y}$ , where  $\mathcal{X}$  and  $\mathcal{Y}$  are input and label space respectively. A malicious attacker  $\tau : \mathcal{X} \times \mathcal{Y} \to \mathcal{X} \times \mathcal{Y}$  with a budget  $\gamma \in [0,100]$  modifies  $\gamma\%$  examples by triggering inputs and corrupting their labels. The remaining  $(100-\gamma)\%$  of the data remain unchanged and correctly labeled in order to conceal the attack. Given a corrupted dataset  $\mathcal{D} = \tau(\mathcal{D}_{\text{raw}}) = \{(\boldsymbol{x}^i, y^i)\}_{i=1}^N$ , our goal is to train a robust classifier  $f: \mathcal{X} \to \mathcal{Y}$  that assigns clean labels  $l^i \in \mathcal{Y}$  to every input  $\boldsymbol{x}^i$  while ignoring the malicious triggers.

The core concept behind VIBE is to treat clean labels as unobserved latent variables  $\underline{l}$ . We then frame the training of a clean classifier as a latent posterior recovery from observed inputs x and corrupted labels y.

Backdoor attacks typically poison a small portion of the data in order to stay undetected [49]. In our framework, this

means that corrupted and clean labels are often identical. Thus, a natural optimization objective is to maximize the conditional log-likelihood of the i.i.d dataset  $\mathcal{D}$  given a set of model parameters  $\theta$ :

$$\ell(\theta|\mathcal{D}) = \ln \prod_{i=1}^{N} p_{\theta}(y^{i}|\boldsymbol{x}^{i}) = \sum_{i=1}^{N} \ln \sum_{l=1}^{K} p_{\theta}(y^{i}|l,\boldsymbol{x}^{i}) p_{\theta}(l|\boldsymbol{x}^{i}). \tag{1}$$

For simplicity, we abbreviate  $p(\underline{l} = l | \underline{x} = x^i)$  as  $p(l | x^i)$ . Given the likelihood factorization (1), we proceed by deriving a tractable optimization objective. Note that we defer concrete parametrization of the clean class posterior  $p_{\theta}(\underline{l} | \underline{x})$  and the corrupted class posterior  $p_{\theta}(y | \underline{l}, \underline{x})$  to Section 3.2.

# 3.1. Optimizing the variational objective via EM

Direct maximization of  $\ell(\theta|\mathcal{D})$  does not ensure the correct recovery of the clean class posterior since the clean class is latent [57]. Fortunately, we can turn to variational inference and maximize likelihood lower bound  $\ell_{\text{ELBO}}$  that introduces an approximate latent posterior q:

$$\ell(\theta|\mathcal{D}) = \sum_{i=1}^{N} \ln \sum_{l=1}^{K} p_{\theta}(y^{i}|l, \boldsymbol{x}^{i}) p_{\theta}(l|\boldsymbol{x}^{i}) \frac{q(l|\boldsymbol{x}^{i}, y^{i})}{q(l|\boldsymbol{x}^{i}, y^{i})}$$

$$\geq \sum_{i=1}^{N} \mathbb{E}_{l^{i} \sim q(\cdot|\boldsymbol{x}^{i}, y^{i})} \left[ \ln \frac{p_{\theta}(y^{i}|l^{i}, \boldsymbol{x}^{i}) p_{\theta}(l^{i}|\boldsymbol{x}^{i})}{q(l^{i}|\boldsymbol{x}^{i}, y^{i})} \right]$$

$$=: \ell_{\text{ELBO}}(\theta, q|\mathcal{D}). \tag{2}$$

The inequality follows directly from Jensen's inequality. We optimize the proposed  $\ell_{\rm ELBO}$  objective with the expectation-maximization (EM) algorithm [57]. In practice, this involves alternating between updates of the approximate latent posterior q (E-step) and parameters  $\theta$  (M-step). **E-step: updating the approximate latent posterior.** We begin by observing that the  $\ell_{\rm ELBO}$  objective requires only the recovery of q for dataset examples, rather than an exact closed-form distribution. With this observation in mind, we rewrite the objective (2) averaged over N examples as:

$$\frac{1}{N} \ell_{\text{ELBO}} = \sum_{i=1}^{N} \sum_{l=1}^{K} \frac{1}{N} q(l|\boldsymbol{x}^{i}, y^{i}) \ln[p_{\theta}(y^{i}|l, \boldsymbol{x}^{i}) p_{\theta}(l|\boldsymbol{x}^{i})] 
- \sum_{i=1}^{N} \sum_{l=1}^{K} \frac{1}{N} q(l|\boldsymbol{x}^{i}, y^{i}) \ln q(l|\boldsymbol{x}^{i}, y^{i}).$$
(3)

We next substitute  $\mathbf{P}_{i,l} := p_{\theta}(y^i|l, \boldsymbol{x}^i)p_{\theta}(l|\boldsymbol{x}^i)$  and  $\mathbf{Q}_{i,l} := \frac{1}{N}q(l|\boldsymbol{x}^i, y^i)$ , where 1/N ensures that  $\mathbf{Q}$  is a proper joint distribution [3, 61]. Replacing the summations with matrix multiplication reveals the same objective in the matrix form:

$$\frac{1}{N} \ell_{\text{ELBO}} = \operatorname{tr}(\mathbf{Q}^{\top} \ln \mathbf{P}) + \mathbb{H}(\mathbf{Q}) + 1 - \ln N$$
$$\geq \operatorname{tr}(\mathbf{Q}^{\top} \ln \mathbf{P}) + \frac{1}{\lambda} \mathbb{H}(\mathbf{Q}) + 1 - \ln N \qquad (4)$$

Here,  $\operatorname{tr}(\cdot)$  is the matrix trace operator,  $\lambda>1$  is a hyperparameter, and  $\mathbb{H}(\mathbf{Q})$  is the entropy of coupling matrix  $\mathbf{Q}$  [66]. The complete derivation is deferred to Appendix  $\ref{eq:quantum}$ . The term  $1-\ln N$  is constant and thus can be ignored.

Each matrix row  $\mathbf{Q}_{i,:}$  sums to 1/N by the definition of  $\mathbf{Q}$ , while columns sum to the prior over clean classes  $\pi$ . Consequently, the set of all possible solutions for the objective (4) forms a polytope:

$$Q[\boldsymbol{\pi}] = \{ \mathbf{Q} \in \mathbb{R}_+^{N \times K} | \mathbf{Q}^\top \mathbf{1}_N = \boldsymbol{\pi}, \, \mathbf{Q} \mathbf{1}_K = \frac{1}{N} \mathbf{1}_N \}.$$
 (5)

Here,  $\mathbf{1}_N$  is an *N*-dimensional column vector. Maximizing the objective (4) over  $\mathcal{Q}[\pi]$  is equivalent to solving the entropy-regularized optimal transport problem [3, 15, 66]:

$$\mathbf{Q}^* = \underset{\mathbf{Q} \in \mathcal{Q}[\boldsymbol{\pi}]}{\min} \left( \operatorname{tr}(\mathbf{Q}^{\top} \mathbf{M}) - \frac{1}{\lambda} \mathbb{H}(\mathbf{Q}) \right). \tag{6}$$

Here, the cost matrix contains the model outputs in dataset examples ( $\mathbf{M} = -\ln \mathbf{P}$ ). The optimal solution  $\mathbf{Q}^*$  can be efficiently obtained with the Sinkhorn-Knopp's matrix scaling algorithm [41, 66], which we revisit in Appendix ??. This approach is computationally efficient even for large N, as discussed in the experiments. The recovered solution  $\mathbf{Q}^*$  contains outputs of the approximate posterior q for the dataset examples and allows us to proceed with the M-step. **M-step: updating model parameters.** Given the outputs of approximate posterior q, we can turn to the optimization of parameters  $\theta$ . Maximizing the  $\ell_{\text{ELBO}}$  objective (2) is equivalent to the following minimization problem:

$$\min_{\theta} \sum_{i=1}^{N} \text{CE}[q || p_{\theta}(l^{i} | \boldsymbol{x}^{i})] + \mathbb{E}_{l^{i} \sim q} \left[ -\ln p_{\theta}(y^{i} | l^{i}, \boldsymbol{x}^{i}) \right]$$
(7)

Here, CE denotes the cross-entropy loss. The full derivation can be found in Appendix  $\ref{Appendix}$ . The objective (7) is continuous w.r.t parameters  $\theta$  and can be optimized by (stochastic) gradient descent. The rewritten objective highlights the role of the approximate posterior q: it acts as a pseudolabel generator. These pseudolabels are also conditioned on the corrupted labels and thus provide a learning signal for the actual clean posterior. The second objective term models the relation between the corrupted labels and the pseudolabels. This term presents an opportunity to uncover the attacker's poisoning patterns that can guide human inspection.

Altogether, VIBE training alternates between the described E and M steps as visualized in Figure 1. The full algorithm is in Appendix ??. Next, we discuss the implementations of distributions parameterized with  $\theta$ .

### 3.2. Parameterizing the posteriors

Let  $g_{\theta_{\rm E}}: \mathcal{X} \to S^{d-1}$  be a feature extractor that encodes inputs onto a (d-1)-dimensional unit hypersphere, e.g. a

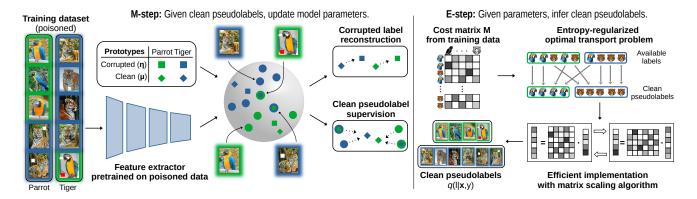


Figure 1. VIBE training alternates between iterative parameter updates (M-step) and inference of clean pseudolabels by solving entropy-regularized optimal transport problem efficiently implemented with matrix scaling algorithm (E-step).

ResNet with  $L_2$ -normalized outputs. We model the conditional likelihood of the encoded input  $v^i = g_{\theta_E}(x^i)$  given the clean class  $l^i$  with a von Mises-Fisher distribution [5]:

$$p_{\theta}(\mathbf{v}^{i}|l^{i}) = C_{d}(\kappa) \exp(\kappa \boldsymbol{\mu}_{l^{i}}^{\top} \mathbf{v}^{i}). \tag{8}$$

The vector  $\mu_{l^i} \in S^{d-1}$  sets the mean direction, the hyperparameter  $\kappa$  controls the distribution spread, while  $C_d(\kappa)$  is a normalization constant [5]. We can derive the clean label posterior as a vMF mixture via the Bayes rule:

$$p_{\theta}(l^{i}|\boldsymbol{x}^{i}) = \frac{\exp(\kappa \boldsymbol{v}^{i}^{\top} \boldsymbol{\mu}_{l^{i}} + \ln \pi_{l^{i}})}{\sum_{l'} \exp(\kappa \boldsymbol{v}^{i}^{\top} \boldsymbol{\mu}_{l'} + \ln \pi_{l'})}.$$
 (9)

Here, the mixing coefficient  $\pi$  induces a prior over clean classes. In practice, we compute  $\pi = \sigma(c \cdot \theta_\pi)$ , where  $\sigma$  is softmax activation that ensures  $\pi$  is a distribution, c is a hyperparmeter, and  $\theta_\pi \in \mathbb{R}^d$  are learnable parameters. The full derivation is in Appendix  $\ref{eq:theory:eq:theo$ 

We model the corrupted class posterior  $p_{\theta}(y^{i}|l^{i}, x^{i})$  as cosine similarity between the corrupted class prototypes  $\theta_{y} = \{\eta_{1}, \dots, \eta_{K}\}$  and output of function h that process the encoded input  $v^{i}$  and the clean label prototype  $\mu_{l^{i}}$ :

$$p_{\theta}(y^{i}|l^{i}, \boldsymbol{x}^{i}) := \frac{\exp(\nu \cdot \boldsymbol{\eta}_{y^{i}}^{\top} h(\boldsymbol{\mu}_{l^{i}}, \boldsymbol{v}^{i}))}{\sum_{y'} \exp(\nu \cdot \boldsymbol{\eta}_{y'}^{\top} h(\boldsymbol{\mu}_{l^{i}}, \boldsymbol{v}^{i}))}.$$
 (10)

Here,  $\nu$  is a scalar hyper-parameter, while details on h are deferred to implementation details. Note that the full corrupted posterior can be approximated as  $p_{\theta}(y^{i}|l^{i}, x^{i}) \approx p_{\theta}(y^{i}|l^{i})$  by replacing output of h with  $\mu_{l^{i}}$ . The detailed description of the approximated corrupted posterior is in Appendix ??. While this approximation makes optimization

more challenging, it enables seamless reconstruction of the systematic poisoning rules of the attacker  $\tau$ . We experimentally evaluate both the full and approximate posterior.

Alltogether, the set of free parameters is a union  $\theta = \theta_{\rm E} \cup \theta_l \cup \theta_\pi \cup \theta_y$ . Next we analyze convergence of the EM algorithm with the introduced parametrization.

## 3.3. Steering the EM algorithm convergence

Our E-step solves a convex optimization problem [15], while the M-step conducts non-convex training of a deep model. As a result, the EM algorithm may end up in a suboptimal stationary point [4, 57, 89]. In fact, the convergence point of the EM algorithm strongly depends on the initialization [58]. Fortunately, recent works observe that self-supervised pre-training of feature extractors [10, 18, 29] lowers the sample complexity of the downstream task [1, 44] and improves generalization [84].

Therefore, we conduct self-supervised pre-training on the poisoned dataset instance (similar to [33]) before end-to-end optimization of our  $\ell_{ELBO}$  objective. Figure 2 shows that self-supervised pre-training on poisoned data jump-starts the EM optimization, leads to faster convergence, and increases the likelihood lower bound  $\ell_{ELBO}$ . Moreover, the corresponding solution generalizes better and turns out to be near optimal compared to supervised learning on clean labels. Still, the self-supervised pre-training does not compromise the generality of VIBE, as pre-training objectives are already available for various modalities [27, 38, 97].

Scaling the concept of feature extractor pre-training in terms of dataset size leads to foundation models [14, 63, 69] like CLIP and DINOv2. Modular design of VIBE posteriors enables integration of these off-the-shelf extractors, allowing performance analysis in the *transfer learning* setup. Nevertheless, foundation models should be carefully downloaded from trusted third-party providers or pre-trained with robust procedures [95, 96] that avoid backdoor injection during self-supervised pre-training stage.

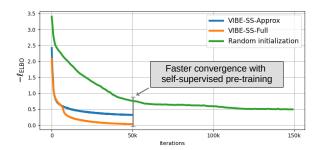


Figure 2. VIBE achieves faster convergence and improved generalization with self-supervised pre-training.

# 3.4. Clean-label attacks diverge from data manifold

Poisoned-label attacks strive for stealthiness by injecting minimal triggers. Thus, the poisoned examples remain near the clean data manifold. However, clean-label attacks [6, 80] operate by significantly perturbing the inputs to construct a successful attack. These perturbations shift the poisoned examples away from the data manifold in the self-supervised feature space, as illustrated in Figure 3. We propose a pre-processing technique that exploits this property of clean-label attacks to identify the poisoned examples.

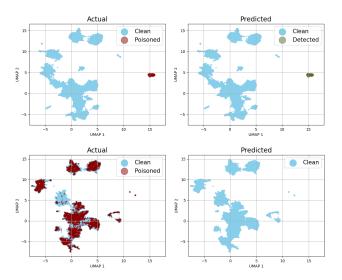


Figure 3. Clean-label attacks shift the poisoned examples away from the clean data manifold (top-left). Thus, we can detect them as outlier communities (top-right). Poisoned-label attacks remain on the manifold and can be useful for model training (down-left). Thus, our preprocessing strategy keeps them (down-right).

Our preprocessing strategy captures the data manifold within a self-supervised feature space and identifies perturbed examples as outlier communities. Specifically, we construct k nearest neighbors graph, represented by the adjacency matrix  $A_k$ . Then, we apply a community detection algorithm [78] that partitions graph  $A_k$  into K+1 distinct

communities. We proceed by computing pairwise distances between the communities to identify the most distant one. Finally, we remove the most distant community if its average distance to other communities exceeds some predefined threshold  $\delta$ . In the case of clean-label attacks, the most distant community corresponds to off-manifold data which is then removed. If poisoned examples are absent from the data, the most distant community is retained due to being much closer to the data manifold. While some clean examples may be lost if  $\delta$  is poorly selected, they typically do not affect the model generalization. More details on preprocessing strategy are in Appendix  $\ref{eq:total_continuous_continu$ 

# 4. Experimental setup

Datasets & metrics. We evaluate VIBE on the standard backdoor benchmarks: CIFAR-10, CIFAR-100 [43], and a subset of 30 classes from the ImageNet-1k dataset [16]. Furthermore, we scale the problem by considering the full ImageNet dataset with 1k classes and 1.2M training examples. We evaluate the performance with the standard metrics: accuracy on the clean test set labels (ACC), and the attack success rate (ASR). Lower ASR indicates more accurate recognition of poisoned samples and better defense. Attacks. We consider eight attacks that represent the major backdoor attack families. For visible patch-like attacks, we include BadNets [23] and Adap-Patch [67]). For invisible attacks, we consider Blend [12], WaNet [60], Adap-Blend [67] and Frequency [83]. Clean-label attacks are represented by LC [80]. We also validate the all-to-all attack [49] using a variant of BadNets. By default, the poisoning rate is set to 10% except for Adap-Patch and Adap-Blend attacks in which 1% of the data is poisoned as suggested in [67]. Also, in the case of clean-label attacks, we poison 2.5% of the data as suggested in [20, 33]. We set the target label as the zeroth class except for the all-to-all attack. As observed in previous works [11, 48], some attacks cannot be reproduced for all datasets. Thus, experiments conducted on ImageNet-30 and CIFAR-100 show a subset of attacks. Detailed configurations are in Appendix ??.

Baseline defenses. We consider five state-of-the-art defenses. Anti-backdoor learning (ABL) [48] first isolates poisoned examples and then uses them to break the correlation between the trigger and the target class. Decoupling based defense (DBD) [33] preserves the labels for samples with low training loss of a linear classifier atop self-supervised features and proceeds with semi-supervised end-to-end fine-tuning. Causality-inspired backdoor defense (CBD) [103] trains a poisoned model to capture the confounding effects of triggers and corrects them in subsequent classifier training. Backdoor defense via adaptive splitting (ASD) [20] dynamically partitions the dataset into clean and poisoned subsets. The two subsets are then used for semi-supervised training. Victim and Beneficiary (VaB)

[107] trains a victim model on a poisoned data subset. The victim model is then utilized for semi-supervised training of the clean model. More details are in Appendix ??. In the transfer learning setup, we also consider the **K-Means** clustering atop frozen features as an unsupervised baseline, **logistic regression** as a supervised counterpart, and a **zero-shot** CLIP-style baseline that relies on encoded textual class descriptions [69].

Implementation details. We pre-train ResNet-18 [28] feature extractor with self-supervised objective All4One [18] on the poisoned dataset of interest. We then train with VIBE objective for 30k iterations with the proposed EM algorithm. In every iteration, we perform the M-step using SGD. We perform E-step every T=1k iterations on a sufficiently large training subset by running a CUDA-accelerated implementation of entropy-regularized optimal transport. Transfer learning experiments involve ViT-G/14 [17] pretrained with DINOv2 [63]. Other details are in Appendix  $\ref{Modes}$ ? Our code is publicly available<sup>2</sup>.

**VIBE models.** We experimentally validate two model variants. VIBE-SelfSupervised (**VIBE-SS**) uses a randomly initialized feature extractor that we first pre-train with self-supervision [18] on the poisoned dataset. Then, we append the classification heads (3.2) and optimize  $\ell_{\rm ELBO}$ . This is our main model. Additionally, we consider VIBE-FoundationModel (**VIBE-FM**) that appends classification heads atop an off-the-shelf frozen feature extractor. In this transfer learning setup, we keep the extractor frozen and op-

timize the remaining parameters. We validate both models with the full factorization  $p(y|\boldsymbol{x},l)$  and the approximation p(y|l) as denoted with (F) and (A) respectively.

# 5. Experimental results

Resilience to backdoor attacks. Table 1 compares VIBE-SS against five baseline defenses on three standard benchmarks. The averaged performance over all attacks indicates that VIBE-SS outperforms all baselines by a large margin. In particular, the absolute ASR improvement of VIBE-SS-F over the best baseline on CIFAR-10 (ABL) is more than 12pp. Similarly, VIBE-SS-F achieves over 14pp ASR improvement over the best baseline ASD on CIFAR-100. Finally, both versions of VIBE-SS attain 0.1% ASR on ImageNet-30, resulting in almost complete resilience to the considered attacks. These improvements in robustness do not impact clean label accuracy (ACC), which does not hold for previous methods.

Interestingly, our experiments reveal failure modes in all existing baselines. For example, ABL and DBD are ineffective against the Adap-Blend attack, while VAB does not defend against the all-to-all attack. Likewise, ASD fails against Frequency and Adap-Style attacks. In contrast, VIBE-SS-F demonstrates near-complete resilience to all attacks except Adap-Patch and Adap-Blend, while still outperforming the best defense with over a 20pp ASR improvement for the latter.

**Transfer learning.** Modular formulation of VIBE allows integration of large-scale pretrained feature extractors.

	Defense →	No De	efense	AI	3L	DE	3D	CE	BD	AS	SD	VA	ΛB	VIBE	-SS-A	VIBE	-SS-F
Data	Attack ↓	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
	No Attack	95.0	-	85.2	-	91.6	-	91.3	-	93.3	-	94.5	-	94.4	-	94.7	-
	BadNets	94.9	100	93.8	1.1	92.4	1.0	91.8	1.2	92.1	3.0	93.5	0.7	94.4	0.6	94.4	0.1
	Blend	94.2	98.3	91.9	1.6	92.2	1.7	90.0	96.6	93.4	1.0	93.9	0.4	93.6	8.7	94.6	0.0
10	WaNet	94.3	98.0	84.1	2.2	91.2	0.4	91.6	97.3	93.3	1.2	94.2	0.5	94.1	0.9	94.3	0.7
4	Frequency	94.9	100	81.3	8.8	92.3	2.6	91.6	100	88.8	100	93.8	0.4	94.1	0.8	94.4	0.0
CIFAR-10	Adap-Patch	95.2	80.9	81.9	0.0	92.9	1.8	91.6	97.8	93.6	100	94.3	1.1	94.3	1.1	94.5	8.6
$\Box$	Adap-Blend	95.0	64.9	91.5	81.9	90.1	99.9	92.3	87.5	94.0	93.9	94.5	29.1	94.5	36.7	94.5	9.0
	LC	94.9	99.9	86.6	1.3	89.7	0.0	91.3	24.7	93.1	0.9	94.0	16.6	93.2	5.3	93.0	6.0
	BN-all2all	92.2	91.5	91.2	0.4	92.9	0.6	92.6	91.9	93.6	2.2	94.5	92.2	94.3	0.6	94.6	1.2
	Average	94.5	90.5	87.3	16.0	91.4	17.7	91.4	84.0	92.8	42.7	94.1	18.0	94.1	6.8	94.3	3.2
	No Attack	74.9	-	70.5	-	66.2	-	71.1	-	71.3	-	65.4	-	75.1	-	73.9	-
CIFAR-100	BadNets	71.7	99.9	66.2	99.9	66.9	0.2	67.1	96.8	69.9	1.0	75.9	0.3	74.5	0.1	73.5	0.4
<u>-</u>	Blend	72.1	100	69.4	0.0	66.7	0.3	67.8	97.4	69.3	26.8	73.0	0.1	73.7	13.2	74.1	1.2
ΕĀ	WaNet	70.8	94.7	69.9	0.9	66.3	0.4	68.0	85.0	68.1	32.9	17.2	81.8	73.9	0.2	73.3	0.6
C	Frequency	76.2	100	70.6	0.0	64.1	100	70.1	99.3	70.1	1.4	75.7	0.1	75.2	0.5	74.8	0.0
	Average	72.7	98.7	69.0	25.2	66.0	25.2	67.6	93.0	69.4	15.5	60.5	20.6	74.3	3.5	73.9	0.5
	No Attack	95.9	-	94.4	-	89.9	-	93.2	-	90.0	-	94.5	-	96.9	-	96.7	-
t-3(	BadNets	95.3	100	94.3	0.2	91.2	0.5	92.9	0.4	90.7	9.7	94.2	0.2	97.4	0.1	96.7	0.1
Š	Blend	83.7	99.9	93.1	0.1	90.3	0.6	91.3	100	89.9	2.1	95.2	0.0	97.2	0.1	96.8	0.1
ige	WaNet	93.5	100	92.0	1.3	90.5	0.5	93.8	99.9	88.8	2.9	94.5	0.1	97.3	0.2	97.1	0.1
ImageNet-30	Frequency	92.0	93.3	92.0	0.3	88.8	0.4	91.3	96.5	87.7	3.9	94.3	0.4	96.8	0.1	96.6	0.1
	Average	91.1	98.3	92.9	0.5	90.2	0.5	92.3	74.2	89.3	5.5	94.6	0.2	97.2	0.1	96.8	0.1

Table 1. Accuracy (ACC) and attack success rate (ASR) on three standard datasets. VIBE consistently outperforms all previous defenses across all attacks. The results are averaged over three runs and the variance does not exceed 0.2%.

 $<sup>^2</sup> https://github.com/ivansabolic/VIBE\\$ 

Thus, we can analyze the performance of backdoor attacks in the transfer learning setup. We consider four relevant baselines: K-Means, logistic regression, zero-shot CLIP, and the state-of-the-art defense DBD. DBD relies on selfsupervised features, so it fits well within this setup. Table 2 indicates that VIBE-FM consistently outperforms the considered baselines across all attacks. In particular, VIBE-FM-A delivers a complete ASR resilience on CIFAR-100 and only 0.1% ASR on CIFAR-10, while VIBE-FM-F attains only slightly worse results. Again, improved resilience comes without impact on the clean label accuracy. Thus, VIBE framework is effective even with foundation models. Interestingly, K-Means and the zero-shot baseline exhibit considerable resilience due to not training with corrupted labels. Still, both of them underperform in terms of accuracy, which emphasizes the importance of labels even for powerful feature extractors. Logistic regression is more vulnerable than K-means due to naive training on corrupted labels. Evaluating backdoor defenses in combination with frozen backbones is becoming increasingly important with the advent of robustly trained foundation models [95, 96].

D-4-	$\mathrm{Def} \rightarrow$	Log	Reg	Zero	-shot	DE	BD	V-FI	M-A	V-F	M-F
Data	Att↓	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
	BNets	97.4	5.2	94.2	0.4	99.3	0.1	99.3	0.0	99.3	0.0
0	Blend	97.3	17.8	94.2	0.5	99.3	0.1	99.3	0.1	99.3	0.1
-1-	WaNet	97.4	5.2	94.2	0.5	99.3	0.1	99.3	0.1	99.3	0.1
CIFAR-	Freq	97.6	2.9	94.2	0.3	99.3	0.0	99.2	0.0	99.3	0.0
Ħ	Patch	99.0	0.2	94.2	0.2	99.3	0.1	99.2	0.1	99.3	0.0
•	Blend	99.0	15.5	94.2	0.6	99.4	20.5	99.2	0.6	99.3	0.9
	LC	99.1	0.2	94.2	0.2	99.3	0.2	99.3	0.1	99.3	0.1
	Avg.	98.1	6.7	94.2	0.4	99.3	3.0	99.3	0.1	99.3	0.2
8	BNets	63.6	66.6	74.1	0.3	90.7	6.7	92.3	0.0	91.6	0.1
<b>2</b> -1	Blend	63.0	66.3	74.1	0.4	90.5	8.5	92.3	0.0	91.5	2.1
CIFAR-1	Wanet	57.9	52.4	74.1	0.5	90.8	0.1	92.2	0.0	91.6	0.1
CE	Freq	57.9	45.6	74.1	0.2	90.7	0.0	92.2	0.0	91.6	0.0
	Avg.	60.6	57.7	74.1	0.4	90.7	3.8	92.3	0.0	91.6	0.6

Table 2. VIBE performance atop large-scale pretrained models.

Large-scale evaluation. The standard evaluation benchmarks for backdoor attacks consider datasets with a relatively small class count. Thus, we further consider a largescale setup on the ImageNet-1k dataset. We consider the standard attacks BadNets, Blend and WaNet, as well as a universal backdoor attack (UBA) [74] that is specifically tailored for targeting many classes at once. Table 3 shows that VIBE-FM with DINOv2 consistently outperforms relevant baselines and attains near complete resilience to the considered attacks. For reference, baseline defense DBD fails in the case of the Blend attack and yields almost 1.4pp lower accuracy. Both logistic regression and K-Means attain lower accuracies and higher attack success rates. Interestingly, the zero-shot baseline achieves competitive resilience of 0.1% at the cost of poor accuracy. This analysis shows that VIBE-FM is beneficial in large-scale setups.

In the case of large-scale evaluation with VIBE-SS, we

Method	K-M	eans	Log	Reg	Zero	-shot	DE	BD	V-FI	M-A	V-F	M-F
Attack	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
BNets	65.0	1.6	78.1	4.0	69.2	0.0	80.9	0.1	82.9	0.0	81.1	0.0
Blend	65.0	1.9	78.6	9.1	69.0	0.1	81.5	4.3	83.1	0.0	81.5	0.1
WaNet	64.9	1.6	78.4	5.1	69.0	0.1	81.6	0.2	83.1	0.0	81.5	0.1
UBA-P	65.3	3.2	79.5	0.1	69.0	0.1	82.0	0.1	82.8	0.1	81.3	0.1
UBA-B	65.5	3.2	79.4	0.1	69.0	0.1	81.5	0.1	83.0	0.1	81.3	0.1
Avg.	65.3	2.3	78.8	3.7	69.0	0.1	81.6	1.0	83.0	0.0	81.3	0.1

Table 3. VIBE-FM performance on the ImageNet-1k dataset.

use ResNet-50 feature extractor pretrained on poisoned instances of the ImageNet-1k dataset. Again, VIBE-SS attains significantly higher accuracy than baseline DBD while keeping ASR at 0.1%, as detailed in Appendix ??.

Attacks on self-supervision. VIBE framework relies on feature extractor pre-training. Thus, we analyze robustness against backdoor attacks [45, 73] that target self-supervised objective. Figure 4 compares VIBE-SS with the DBD baseline on CIFAR-10 poisoned with the CTRL attack [45]. VIBE outperforms the DBD baseline when built atop the standard SimCLR [10] pre-training and its robust counterpart MIMIC [26], as detailed in Appendix ??.

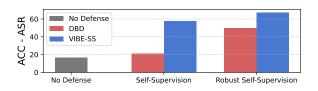


Figure 4. VIBE defends against the attacks on self-supervision.

We further devise our adaptive attack that targets All4One [18] pre-training objective used in the main experiments. We construct a trigger that moves feature representations of poisoned examples towards the target classes. VIBE successfully defends against this adaptive attack on the CIFAR-10 dataset with accuracy of 94.5% and ASR of 0.6%. Details of the attack are in Appendix ??.

Combining multiple attacks. Existing evaluation benchmarks consider every backdoor attack in isolation. We further harden the task by applying multiple backdoor attacks to the same instance of the CIFAR-10 dataset. In particular, we inject visible patch attack BadNets and the clean-label attack LC. We then evaluate robustness against each attack independently and the combined attack. Table 4 shows that VIBE can successfully defend against combined attacks, while the filtering strategy of the DBD baseline fails.

Method	ASR (BadNets)	ASR (LC)	ASR (BN & LC)	ACC
DBD-SS	99.7	99.8	99.8	79.1
VIBE-SS-A	1.2	1.7	1.3	93.8
VIBE-SS-F	1.8	2.2	2.0	93.5

Table 4. VIBE performance on combined attacks.

**Inferring attacker behavior.** VIBE with approximate factorization can seamlessly recover class poisoning patterns by analyzing  $p(\underline{y}|\underline{l})$  for every combination of y and l. To showcase this, we consider BadNets all-to-all attack that poisons all the classes in the CIFAR-10 dataset. Figure 5 visualizes the inferred poisoning patterns (left) that resemble the actual patterns (right). In the case of full factorization (10), poisoning rules can be recovered by marginalization. This property emerges from the VIBE formulation and may not be easily recovered with previous defenses.

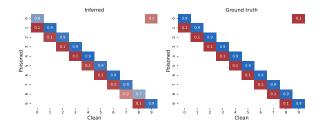


Figure 5. Inferred poisoning distributions p(y|l) for all-to-all attack on CIFAR-10 (left) and the corresponding groundtruth (right).

Computational requirements. Our main experiments are conducted on a single NVIDIA RTX A4500 with 20GB of RAM. Table 5 shows that VIBE training necessitates similar computational requirements as previous works, facilitating reproducibility. Furthermore, VIBE converges  $3\times$  faster than the DBD baseline on the full ImageNet-1k dataset. In this case, the entropy-regularized optimal transport from Estep requires 10.5GB of GPU RAM and takes 36.5 seconds. Still, E-step is ran only 30 times throughout the training, keeping the runtime feasible.

 Def → ASD [20]
 VaB [107]
 self-sup
 +DBD [33]
 +VIBE-SS

 Data ↓ Mem Time Mem Time Mem Time Mem Time Mem Time
 Mem Time Mem Time Mem Time

 C-100 4.0GB 3.8h 1.8GB 2.7h 2.1GB 8.5h 2.7GB 5.4h 1.6GB 0.9h

 IN-30 3.7GB 7.2h 7.6GB 51.5h 4.1GB 7.0h 4.8GB 7.7h 5.9GB 2.3h

Table 5. Computational requirements of VIBE-SS.

### 6. Discussion

On different poisoning rates. Backdoor attacks typically drop the poisoning rate  $\gamma$  in order to obstruct the defense. Decreasing the poisoning rate  $\gamma$  does not affect VIBE since it simplifies the posterior recovery due to better overall alignment of the observed  $\underline{y}$  and the latent  $\underline{l}$ . The left side of Figure 6 shows the attack success rate in log-scale for different poisoning rates on BadNets-poisoned CIFAR-10. While other baselines lose their performance with low poisoning rate, VIBE remains robust. The strong performance across different poisoning rates can be attributed to accurate pseudolabels. Our pseudolabels match 99% of clean labels on CIFAR-10 and 95% of clean labels on CIFAR-100.

On the choice of feature extractor. VIBE can be built atop different self-supervised pre-training objectives and frozen feature extractors. The right side of Figure 6 shows the average performance over six attacks on CIFAR-10. VIBE-SS and VIBE-FM deliver competitive results in all cases.

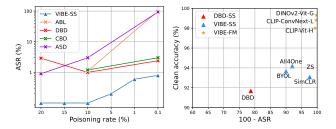


Figure 6. VIBE preserves strong performance for different poisoning rates (left) and can be pre-trained with different self-supervised objectives as well as built atop foundation models (right).

On the impact of preprocessing. The proposed preprocessing strategy (3.4) removes samples outside the training manifold. This design decision improves performance on clean label attacks without hampering generalization or the performance on other attack types. For example, data preprocessing reduces the LC attack ASR from 14% to 6.3% on the CIFAR-10 dataset. Similar performance gains can be observed for other clean-label attacks [6, 99], as shown in Appendix ??. Furthermore, improvement in resilience does not affect clean label accuracy significantly.

On hyper-parameter sensitivity. We validate VIBE performance for different temperatures  $\nu$ ,  $\kappa$  and c, E-step frequency T, values of the learning rate, distance thresholds  $\delta$  and entropy regularization  $\lambda$  in Appendix ??. VIBE performance is consistent across different hyper-parameter values.

## 7. Conclusion

We have presented VIBE, the first backdoor defense that views clean labels as unobserved latent variables. We frame the training of a clean classifier as a latent posterior recovery problem and show how to efficiently solve it through expectation maximization (EM). Specifically, our E-step infers clean pseudolabels by solving an entropy-regularized optimal transport problem via the computationally efficient matrix scaling algorithm [15]. Our M-step conducts gradient descent updates on the model parameters that are pre-trained with self-supervised objective on the poisoned dataset to improve convergence [33]. Our experiments indicate that VIBE-SS provides substantial defense against all considered backdoor attacks and remains effective against both adaptive and combined attacks. Being modular, VIBE can also incorporate off-the-shelf foundation models and attain strong performance in this increasingly relevant setup.

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