Faster and Better 3D Splatting via Group Training

Supplementary Material

A. Proof of Property 1: Opacity-based Effective Gaussians Densification

Under the assumptions of mutual independence between Gaussian attributes and intra-primitive parameter independence, the partial derivatives $\left[\frac{\partial \Delta x}{\partial x_{\rm m}}, \frac{\partial \Delta y}{\partial y_{\rm m}}\right]$ for any arbitrary Gaussian admit the following derivation:

$$\frac{\partial \alpha}{\partial G} = O + \frac{\partial O}{\partial G}G = O + 0 \cdot G = O, \tag{1}$$

$$\frac{\partial L}{\partial x_{\rm m}} = \sum_{\rm pixel} \frac{\partial L}{\partial G_m^{\rm 2D}} \frac{\partial G_m^{\rm 2D}}{\partial \Delta x} \frac{\partial \Delta x}{\partial x_{\rm m}}$$

$$= \sum_{\rm pixel} o_m \frac{\partial L}{\partial \alpha_m} \frac{\partial G_m^{\rm 2D}}{\partial \Delta x} \frac{\partial \Delta x}{\partial x_{\rm m}}$$
(2)

$$=o_m \sum_{\mathrm{pixel}} \frac{\partial L}{\partial \hat{C}} \frac{\partial \hat{C}}{\partial \alpha_m} \frac{\partial G_m^{\mathrm{2D}}}{\partial \Delta x} \frac{\partial \Delta x}{\partial x_m},$$

$$\frac{\partial L}{\partial y_{\rm m}} = o_m \sum_{\rm pixel} \frac{\partial L}{\partial \hat{C}} \frac{\partial \hat{C}}{\partial \alpha_m} \frac{\partial G_m^{\rm 2D}}{\partial \Delta y} \frac{\partial \Delta y}{\partial y_{\rm m}},\tag{3}$$

where $[\frac{\partial \Delta x}{\partial x_m}, \frac{\partial \Delta y}{\partial y_m}]$ remain constant parameters determined by the resolution [W,H]; $[\frac{\partial G_m^{\rm 2D}}{\partial \Delta x}, \frac{\partial G_m^{\rm 2D}}{\partial \Delta y}]$ derive from the scale, the rotation and the world coordinates of Gaussian primitives (independent of their opacity); and $\frac{\partial L}{\partial \hat{C}}$ represents the loss gradient with respect to the current pixel value.

Given that \hat{C} is formulated as the composite rendering of N Gaussians in Eq. (4), the derivative $\frac{\partial \hat{C}}{\partial \alpha_m}$ admits computation via Eq. (5).

$$\hat{C} = \underbrace{\sum_{i=1}^{m-1} \alpha_i c_i \prod_{j=1}^{i-1} (1 - \alpha_j)}_{\text{Before Gaussian } m} + \underbrace{\sum_{i=m+1}^{m-1} \prod_{j=1}^{m-1} (1 - \alpha_j)}_{\text{After Gaussian } m} + \underbrace{\sum_{i=m+1}^{N} \prod_{j=1}^{m-1} (1 - \alpha_j) \alpha_i c_i (1 - \alpha_m)}_{\text{After Gaussian } m} \underbrace{\prod_{j=m+1}^{m-1} (1 - \alpha_j)}_{\text{After Gaussian } m}$$
(4)

$$+ \underbrace{\prod_{i=1}^{N} (1 - \alpha_i) c_{\rm bg}}_{\text{background}},$$

$$\frac{\partial \hat{C}}{\partial \alpha_m} = \prod_{j=1}^{\text{Before G } m} \left[c_m - \sum_{i=m+1}^{N} \alpha_i c_i \prod_{j=m+1}^{i-1} (1 - \alpha_j) \right] - \frac{c_{\text{bg}} T_N}{1 - \alpha_m}$$
(5)

	Sampling		Т	anks&Tem	ples [6]		
	Strategy	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
3DGS*	-	23.730	0.8491	0.176	4.6	430	15.3
Group Training	Imp. score Vol. Opac. Vol.+Opac.	23.672 23.718 23.850 23.684	0.8486 0.8462 0.8500 0.8475	0.174 0.182 0.176 0.179	5.8 5.1 4.5 4.8	593 493 383 438	15.7 12.4 11.0 11.9

Table 1. Quantitative evaluation of training efficiency on the Tanks&Temples [6] reconstructed by 3DGS [5]. * indicates that we retrain the model. PM stands for GPU peak memory allocation, with Size in MB and Time in minutes. Imp. score = Importance score based, Vol. = Volume-based, Opac. = Opacity-based, Vol.+Opac. = Volume & Opacity-based.

	Sampling]	Deep Blend	ing [4]		
	Strategy	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
3DGS*	-	29.503	0.9038	0.244	7.8	677	25.2
Group	Imp. score Vol.	29.589 29.448	0.9051 0.9036	0.246 0.251	8.5 7.5	765 623	23.2 19.8
Training	Opac. Vol.+Opac.	29.768 29.619	0.9067 0.9048	0.245 0.247	6.8 7.0	489 533	17.2 19.0

Table 2. Quantitative evaluation of training efficiency on the Deep Blending [4] reconstructed by 3DGS [5]. Group Training with Opacity-based Prioritised Sampling demonstrates the fastest reconstruction speed and superior performance compared to other sampling strategies.

Subsequently, the mathematical expectation of this derivative is formally established through Eq. (6)

$$\mathbb{E}\left[\frac{\partial \hat{C}}{\partial \alpha_{m}}\right] = \underbrace{(1-\alpha_{0})^{m-1}}_{\text{Before G }m} \left\{c_{0} - c_{0}\alpha_{0} \sum_{i=m+1}^{N} \mathbb{E}\left[\prod_{j=m+1}^{\text{After G }m} (1-\alpha_{j})\right]\right\} - \frac{c_{\text{bg}}T_{\text{sta.}}}{1-\alpha_{0}}$$

$$= (1-\alpha_{0})^{m-1} \left[c_{0} - c_{0}\alpha_{0} \sum_{i=m+1}^{N} (1-\alpha_{0})^{i-m-1}\right] - \frac{c_{\text{bg}}T_{\text{saturation}}}{1-\alpha_{0}}$$

$$= \frac{(c_{0} - c_{\text{bg}})T_{\text{saturation}}}{1-\alpha_{0}}$$

$$= \frac{(c_{0} - c_{\text{bg}})T_{\text{saturation}}}{1-\mathbb{E}\left[o_{i}\right]\mathbb{E}\left[G_{i}\right]},$$
(6)

B. Efficiency And Effectiveness For Various Sampling Strategies

We propose various sampling strategies for Group Training, incorporating Prioritized Sampling based on distinct sampling metrics. The sampling probability for each Gaussian primitive G_i is defined as follows:

$$p_i = \frac{\theta_i}{\sum_{i=1}^N \theta_i},\tag{7}$$

	Mip	-NeRF360) [1]	Tank	s&Temple	es [6]	Dee	p Blendin	g [4]	Blender [8]			
	PSNR ↑	Time ↓	Accel. ↑	PSNR ↑	Time ↓	Accel. ↑	PSNR ↑	Time ↓	Accel. ↑	PSNR ↑	Time ↓	Accel. ↑	
3D-GS [5] +Group Training	27.45 27.56	26.7 19.6	- 27%	23.70 23.85	15.0 11.0	- 27%	29.59 29.75	23.9 16.9	- 29%	33.77 33.81	6.1 4.8	- 21%	
Mini-Splatting [3]	27.27	20.7		23.26	12.6	-	29.95	17.8		31.60	10.0		
+Group Training	27.25	17.9	13%	23.10	9.9	21%	29.85	14.7	17%	31.98	8.4	16%	
LightGaussian [2] +Group Training	27.06 27.34	27.5 20.5	_ 25%	23.09 23.55	16.1 11.9	- 26%	27.28 28.50	25.9 19.0	_ 27%	32.95 33.18	6.1 4.6	- 24%	

Table 3. Quantitative comparisons on different baselines and datasets. Group Training with 3DGS achieves faster reconstruction speed than Mini-Splatting across all datasets. Furthermore, Group Training demonstrates consistent acceleration effects on both 3DGS acceleration model $(13\%\sim21\%$ speedup on Mini-Splatting [3]) and compression model $(24\%\sim27\%$ speedup on LightGaussian [2]). Accel. = Acceleration Ratio in training time compared to the baseline.



Figure 1. Comparsion of Under-Training Gaussian Primitives. Our Group-Training methodology selectively trains a subset of Gaussian primitives, demonstrating enhanced computational efficiency while mitigating loss of potentially critical points during opacity reset operations.

where θ_i represents the sampling metrics (opacity [2], volume [7] or importance score 1 [3, 9, 11]) of Gaussian primitive G_i , and N is the total number of Gaussian primitives. We also evaluated the metric which both Opacity and Volume are considered simultaneously, referred to as the Volume & Opacity-based method, as applied in [2]. The sampling metric θ_i for Volume & Opacity-based Prioritized Sampling is computed as follows:

$$\theta_i = \alpha_i \cdot V_i, \tag{8}$$

where α_i represents the opacity and V_i represents the volume of Gaussian primitive G_i .

We conducted experiments using 3D Gaussian Splatting (3DGS) on two datasets: Tanks&Temples [6] and Deep Blending [4], both captured with camera-based systems. The comprehensive comparative results are presented in Tab. 1 and Tab. 2. Our results demonstrate that Group

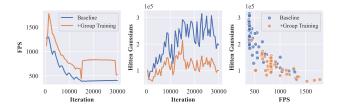


Figure 2. **Comparsion of Forward Rendering Efficiency.** We measured the number of hit Gaussians and forward rendering FPS throughout the training process. 3DGS with Group Training consistently demonstrated higher FPS and fewer hit Gaussians compared to the baseline method during training.

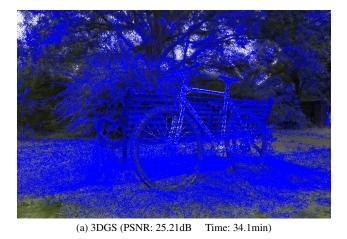
Training with Opacity-based Prioritized Sampling (OPS) consistently achieves significant improvements in both reconstruction speed and the quality of 3DGS models. Additionally, the reconstructed models exhibit greater compactness, as evidenced by a marked reduction in redundant Gaussian primitives.

However, volume and importance scores are not the most effective sampling metrics, as they fail to differentiate Gaussians that contribute to densification. This deficiency leads to abrupt vacancies in the Gaussian space under high sampling rates, causing the over-reconstruction and under-reconstruction [5]. Consequently, this exacerbates Gaussian densification, introducing redundancy between newly densified Gaussians and those already cached. The detailed analysis is provided in Sec. 3.2.

C. Temporal Evolution of Under-Training Gaussian Primitives

We visually compare the quantitative differences in undertraining Gaussian primitives between Group-Training and 3DGS during scene reconstruction in Fig. 1. 3DGS with Group-Training reduces the training overhead by avoiding full optimization of all Gaussian primitives. Furthermore, during each opacity reset operation, the proposed

 $^{^{1}}Based$ on code: https://github.com/fatPeter/mini-splatting.git





(b) 3DGS + Group Training (PSNR: 25.22dB Time: 21.8min)

Figure 3. The visual comparison of Gaussian primitive distributions in the imaging plane. We visualize the Gaussian projection information on the imaging plane during images rendering. **Left:** Gaussian distribution on the imaging plane for the "Bicycle" scene [1]. **Right:** 3DGS with Group Training achieves comparable rendering quality using fewer Gaussian primitives.

method retains a higher proportion of geometrically significant primitives compared to baseline. These retained elements, despite their low-opacity values, preserve critical structural information that contributes to scene geometry fidelity.

D. Comparison of Scene Representation Efficiency

Comparative analysis of per-iteration FPS and hit Gaussian counts was conducted during 3DGS reconstruction of the 'train' scene under baseline conditions and Group Training. Experimental results show the baseline method required 12.5 minutes to reach a PSNR of 21.985 dB, whereas Group Training with OPS acceleration attained a PSNR of 22.156 dB in just 9.3 minutes. These measurements confirm that Group Training consistently delivers accelerated rendering frame rates alongside a substantial reduction in hitten Gaussians count during training. Consequently, Group Training demonstrates higher scene representation efficiency, utilizing significantly fewer Gaussian primitives without compromising reconstruction quality.

E. Distribution of Gaussian Primitives in Imaging Plane Space

Fig. 3 illustrates the projection of rendering Gaussian primitives onto the imaging plane. Our Group Training approach significantly reduces the number of primitives required per image compared to the baseline, without compromising rendering quality, and further improves reconstruction speed.

F. Methodological Applicability

We perform comparative validation across two distinct 3DGS architectures: an acceleration-optimized model [3] and a compression-focused LightGaussian [2].

Empirical results demonstrate Group-Training's consistent efficacy across dataset scales, particularly evidenced by reduced temporal overhead in the Blender [8], as shown in Tab. 3. Crucially, our method synergistically integrates with existing acceleration techniques like Mini-Splatting [3], achieving compounded acceleration gains while providing sustained acceleration for compressed models with concurrent fidelity enhancement.

G. Detailed Experimental Results for All Scenes

We present the reconstruction results for all scenes using Group Training with Random Sampling (RS) and Opacity-based Prioritized Sampling (OPS), evaluated on 3D Gaussian Splatting (3DGS) [5] and Mip-Splatting [10]. The detailed results are provided in Tabs. 4 to 11.

The experimental results demonstrate that Group Training consistently delivers significant improvements in both reconstruction speed and quality across all tests, with the acceleration effect being particularly pronounced on complex datasets. Notably, Group Training with OPS achieves the fastest reconstruction times while maintaining optimal or near-optimal reconstruction quality.

We compare the effects of enabling RS and OPS during the Gaussian densification phase. The results indicate that Group Training with RS generates a significantly larger number of Gaussian primitives across all scenarios. For example, when reconstructing the "Bicycle" scene using Mip-Splatting, the high density of Gaussian primitives required

the use of an NVIDIA A100 GPU for Group Training with RS. In contrast, Group Training with OPS produces sparser Gaussian primitives while delivering comparable or even superior reconstruction quality. Additionally, the reduced number of Gaussian primitives significantly alleviates the burden on peak memory usage.

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	Grouping			Dr. John	Dr. Johnson					Playroc	m		
	Iterations	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
3D Gaussian Splatting [5]	-	28.766	0.899	0.244	_	_	_	30.044	0.906	0.241	_	_	_
3D Gaussian Splatting*	_	29.190	0.901	0.2442	9.0	782	26.8	29.981	0.907	0.2431	6.4	549	21.0
Carrie Tarinia a m/ DC	0~15K	28.383	0.894	0.2517	8.8	733	24.2	29.987	0.908	0.2429	6.5	554	19.5
Group Training w/ RS	$0\sim30K$	28.701	0.902	0.2513	8.8	734	20.3	30.133	0.912	0.2448	6.5	552	16.6
Group Training w/ OPS	0~15K 0~30K	29.287 29.309	0.903 0.904	0.2430 0.2451	8.1 8.1	592 594	21.7 18.6	30.138 30.183	0.909 0.910	0.2439 0.2448	5.6 5.6	382 380	16.8 15.1

Table 4. Comprehensive quantitative evaluation results on the DeepBlending [4] reconstructed by 3DGS [5]. RS denotes Random Sampling, and OPS denotes Opacity-based Prioritized Sampling.

		Grouping				Mip	-NeRF36	0 [1]			
		Iterations	bicycle	flowers	garden	stump	treehill	bonsai	counter	kitchen	room
	3DGS [5] 3DGS*	- -	25.246 25.205	21.520 21.484	27.410 27.397	26.550 26.620	22.490 22.514	31.980 32.202	28.700 28.980	31.317 31.222	30.632 31.377
PSNR	Group Training w/ RS	0~15K 0~30K	25.228 25.217	21.748 21.806	27.552 27.463	26.854 27.095	22.441 22.671	32.430 31.975	29.121 28.850	31.579 31.319	31.634 31.438
	Group Training w/ OPS	0~15K 0~30K	25.260 25.219	21.751 21.741	27.434 27.418	26.809 26.830	22.402 22.522	32.312 32.205	29.031 28.973	31.539 31.425	31.699 31.744
	3DGS [5] 3DGS*	_ _	0.771 0.765	0.605 0.605	0.868 0.866	0.775 0.773	0.638 0.634	0.938 0.942	0.905 0.908	0.922 0.927	0.914 0.919
SSIM	Group Training w/ RS	0~15K 0~30K	0.769 0.769	0.619 0.616	0.872 0.871	0.787 0.795	0.638 0.642	0.946 0.942	0.913 0.909	0.930 0.927	0.923 0.920
	Group Training w/ OPS	0~15K 0~30K	0.770 0.768	0.617 0.616	0.869 0.868	0.785 0.786	0.635 0.637	0.945 0.944	0.911 0.909	0.929 0.927	0.922 0.921
	3DGS [5] 3DGS*	_ _	0.205 0.2103	0.336 0.3355	0.103 0.1069	0.210 0.2149	0.317 0.3240	0.205 0.2036	0.204 0.2001	0.129 0.1261	0.220 0.2184
LPIPS	Group Training w/ RS	0~15K 0~30K	0.2094 0.2225	0.3246 0.3324	0.0985 0.1061	0.1989 0.2032	0.3182 0.3281	0.1936 0.2008	0.1909 0.2008	0.1216 0.1280	0.2110 0.2198
	Group Training w/ OPS	0~15K 0~30K	0.2074 0.2125	0.3262 0.3307	0.1033 0.1051	0.2044 0.2075	0.3203 0.3226	0.1968 0.1992	0.1954 0.1987	0.1245 0.1272	0.2148 0.2161
	3DGS*	_	11.6	7.7	11.3	9.0	7.5	7.7	6.7	8.4	8.5
PM	Group Training w/ RS	0~15K 0~30K	12.1 12.0	8.8 8.8	12.0 12.0	10.9 10.9	9.0 9.0	8.4 8.4	7.1 7.2	8.5 8.5	8.8 8.7
	Group Training w/ OPS	0~15K 0~30K	11.1 11.1	8.1 8.0	10.6 10.6	9.4 9.3	8.2 8.4	7.6 7.6	6.4 6.4	7.6 7.6	8.1 8.1
	3DGS*	-	1450	858	1391	1163	896	296	284	428	366
Size	Group Training w/ RS	0~15K 0~30K	1516 1491	1019 1016	1474 1472	1457 1452	1106 1105	408 407	348 349	439 439	397 390
	Group Training w/ OPS	0~15K 0~30K	1192 1195	795 790	1083 1084	1078 1060	899 921	267 267	225 225	277 275	287 291
	3DGS*	_	34.1	24.0	35.9	27.2	24.0	20.5	22.8	28.3	23.7
Time	Group Training w/ RS	0~15K 0~30K	31.2 24.8	24.2 20.1	33.2 27.3	28.7 23.6	25.0 20.3	22.1 20.6	24.3 21.7	27.6 24.2	23.3 20.6
	Group Training w/ OPS	0~15K 0~30K	26.9 21.8	21.1 17.9	27.4 23.2	23.5 19.4	22.0 18.4	18.5 17.4	20.4 18.7	22.4 20.4	20.6 18.8

Table 5. Comprehensive quantitative evaluation results on the Mip-NeRF360 [1] reconstructed by 3DGS [5].

	Grouping			Train						Truck			
	Iterations	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
3D Gaussian Splatting [5]	_	21.097	0.802	0.218	=	=	=	25.187	0.879	0.148	_	=	=
3D Gaussian Splatting*	-	21.985	0.815	0.2063	3.6	257	12.5	25.409	0.882	0.1464	5.5	610	17.5
Consum Training and DC	0~15K	22.064	0.818	0.2031	3.9	278	11.7	25.482	0.885	0.1375	6.3	714	17.5
Group Training w/ RS	$0\sim30K$	21.910	0.812	0.2185	3.8	273	10.1	25.495	0.884	0.1460	6.3	716	14.4
Group Training w/ ODS	0~15K	22.159	0.818	0.2040	3.6	228	10.7	25.524	0.884	0.1411	5.5	539	14.9
Group Training w/ OPS	$0\sim30K$	22.156	0.816	0.2104	3.6	227	9.3	25.549	0.884	0.1424	5.5	540	12.6

Table 6. Comprehensive quantitative evaluation results on the Tanks&Temples [6] reconstructed by 3DGS [5].

		Grouping				Blen	der [8]			
		Iterations	chair	drumps	ficus	hotdog	lego	materials	mic	ship
	3DGS [5] 3DGS*	_ _	33.83 35.581	26.15 26.258	34.87 35.481	37.72 38.004	35.78 36.062	30.00 30.461	35.36 36.649	30.80 31.677
PSNR	Group Training w/ RS	0~15K 0~30K	35.736 35.637	26.273 26.224	35.494 35.436	38.242 38.142	36.580 36.441	30.675 30.588	36.842 36.786	31.829 31.765
	Group Training w/ OPS	0~15K 0~30K	35.688 35.623	26.270 26.227	35.487 35.467	38.145 38.017	36.435 36.335	30.569 30.452	36.719 36.654	31.800 31.692
	3DGS*	_	0.988	0.955	0.987	0.985	0.983	0.960	0.993	0.906
SSIM	Group Training w/ RS	0~15K 0~30K	0.988 0.988	0.955 0.956	0.987 0.987	0.986 0.987	0.985 0.985	0.962 0.963	0.993 0.993	0.909 0.910
	Group Training w/ OPS	0~15K 0~30K	0.988 0.988	0.955 0.955	0.987 0.987	0.986 0.986	0.984 0.984	0.962 0.961	0.993 0.992	0.909 0.909
	3DGS*	_	0.0104	0.0367	0.0118	0.0201	0.0161	0.0370	0.0064	0.1060
LPIPS	Group Training w/ RS	0~15K 0~30K	0.0097 0.0107	0.0355 0.0357	0.0117 0.0118	0.0170 0.0184	0.0131 0.0140	0.0340 0.0351	0.0061 0.0063	0.0998 0.1037
	Group Training w/ OPS	0~15K 0~30K	0.0099 0.0102	0.0359 0.0364	0.0118 0.0119	0.0181 0.0189	0.0139 0.0143	0.0356 0.0367	0.0064 0.0065	0.1016 0.1042
	3DGS*	_	3.1	2.9	2.7	2.6	2.9	2.6	2.6	2.8
PM	Group Training w/ RS	0~15K 0~30K	2.9 2.9	2.8 2.8	2.6 2.6	2.7 2.7	3.0 3.0	2.6 2.6	2.6 2.6	2.8 2.8
	Group Training w/ OPS	0~15K 0~30K	2.8 2.8	2.7 2.7	2.5 2.5	2.6 2.6	2.8 2.8	2.6 2.5	2.6 2.6	2.7 2.7
	3DGS*	_	116	92	63	44	82	39	46	66
Size	Group Training w/ RS	0~15K 0~30K	88 87	78 78	39 39	46 47	97 97	47 47	42 43	69 69
	Group Training w/ OPS	0~15K 0~30K	59 61	57 58	27 27	31 31	58 58	32 30	30 30	49 49
	3DGS*	_	7.4	6.6	5.3	5.9	6.5	4.9	5.3	6.6
Time	Group Training w/ RS	0~15K 0~30K	6.0 5.5	5.7 5.3	4.5 4.3	6.0 5.5	6.4 5.8	5.2 4.9	4.8 4.6	6.7 6.2
	Group Training w/ OPS	0~15K 0~30K	5.3 5.1	5.3 5.0	4.1 4.0	5.2 5.0	5.3 5.0	4.6 4.5	4.5 4.2	5.8 5.5

Table 7. Comprehensive quantitative evaluation results on the Blender [8] reconstructed by 3DGS [5].

	Grouping			Dr. John	son					Playroc	om		
	Iterations	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
Mip-Splatting*	-	28.711	0.898	0.2431	10.5	981	39.3	30.005	0.907	0.2348	7.4	673	30.8
Group Training w/ RS	0~15K 0~30K	27.957 28.500	0.892 0.902	0.2526 0.2486	10.1 10.1	898 902	34.3 28.2	29.901 30.283	0.908 0.914	0.2335 0.2354	8.0 8.0	749 748	29.1 24.7
Group Training w/ OPS	0~15K 0~30K	29.145 29.271	0.903 0.904	0.2393 0.2407	9.4 9.4	732 734	31.0 26.0	30.185 30.305	0.910 0.911	0.2334 0.2360	6.6	520 518	25.2 22.0

Table 8. Comprehensive quantitative evaluation results on the DeepBlending [4] reconstructed by Mip-Splatting [10].

		Grouping				Mip	-NeRF36	0 [1]			
		Iterations	bicycle	flowers	garden	stump	treehill	bonsai	counter	kitchen	room
	Mip-Splatting*	_	25.535	21.753	27.603	26.874	22.304	32.301	29.214	31.803	31.740
PSNR	Group Training w/ RS	0~15K 0~30K	25.664 25.784	21.960 22.257	27.726 27.881	27.124 27.446	22.371 22.711	32.299 32.381	29.291 29.084	31.719 31.510	31.756 31.682
	Group Training w/ OPS	0~15K 0~30K	25.651 25.634	21.852 21.844	27.825 27.858	27.166 27.145	22.411 22.441	32.745 32.653	29.330 29.255	31.870 31.864	31.721 31.856
	Mip-Splatting*	_	0.792	0.641	0.877	0.790	0.639	0.945	0.914	0.931	0.925
SSIM	Group Training w/ RS	0~15K 0~30K	0.800 0.803	0.653 0.656	0.881 0.882	0.805 0.816	0.647 0.658	0.949 0.947	0.917 0.914	0.932 0.931	0.926 0.925
	Group Training w/ OPS	0~15K 0~30K	0.796 0.796	0.648 0.646	0.879 0.879	0.803 0.804	0.645 0.646	0.948 0.948	0.915 0.915	0.932 0.931	0.926 0.926
	Mip-Splatting*	_	0.1670	0.2727	0.0950	0.1889	0.2740	0.1881	0.1864	0.1194	0.2011
LPIPS	Group Training w/ RS	0~15K 0~30K	0.1607 0.1708	0.2628 0.2748	0.0895 0.0933	0.1736 0.1751	0.2619 0.2704	0.1823 0.1874	0.1807 0.1891	0.1163 0.1213	0.1995 0.2050
	Group Training w/ OPS	0~15K 0~30K	0.1655 0.1673	0.2657 0.2710	0.0922 0.0929	0.1782 0.1799	0.2683 0.2723	0.1843 0.1861	0.1847 0.1864	0.1185 0.1200	0.2026 0.2029
	Mip-Splatting*	_	15.6	9.5	12.3	10.9	10.1	8.4	7.4	9.2	9.7
PM	Group Training w/ RS	0~15K 0~30K	19.2 19.2	12.6 12.7	17.2 17.1	15.5 15.6	13.7 13.7	9.6 9.6	8.3 8.3	9.9 9.9	10.0 10.0
	Group Training w/ OPS	0~15K 0~30K	15.8 15.7	10.6 10.6	13.9 13.9	12.4 12.4	11.4 11.5	8.4 8.4	7.2 7.2	8.4 8.4	9.0 9.0
	Mip-Splatting*	_	1957	1089	1475	1398	1232	388	364	523	517
Size	Group Training w/ RS	0~15K 0~30K	2494 2489	1550 1570	2194 2187	2083 2094	1763 1764	560 560	491 490	615 610	558 560
	Group Training w/ OPS	0~15K 0~30K	1968 1961	1230 1230	1684 1684	1564 1562	1410 1429	379 378	329 329	388 394	403 412
	Mip-Splatting*	_	54.9	35.4	49.5	39.3	37.3	28.6	31.9	39.0	33.6
Time	Group Training w/ RS	0~15K 0~30K	43.7 35.1	39.9 32.5	57.7 45.3	46.3 37.0	42.1 34.2	32.2 28.8	34.1 30.0	40.3 34.2	32.8 28.9
	Group Training w/ OPS	0~15K 0~30K	47.9 37.7	34.3 28.3	47.7 38.8	37.4 30.0	36.2 29.5	27.2 24.9	28.7 26.1	32.0 28.5	28.5 25.9

Table 9. Comprehensive quantitative evaluation results on the Mip-NeRF360 [1] reconstructed by Mip-Splatting [10].

	Grouping			Train						Truck	:		
	Iterations	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓	PSNR ↑	SSIM ↑	LPIPS ↓	PM ↓	Size ↓	Time ↓
Mip-Splatting*	-	21.783	0.826	0.1892	4.4	351	19.5	25.714	0.893	0.1232	6.8	767	26.5
Group Training w/ RS	0~15K 0~30K	22.004 22.358	0.829 0.829	0.1861 0.1975	4.8 4.7	405 403	18.9 16.3	25.901 25.934	0.896 0.896	0.1146 0.1221	9.2 9.2	1123 1119	30.3 24.4
Group Training w/ OPS	0~15K 0~30K	21.994 22.167	0.830 0.829	0.1859 0.1915	4.4 4.4	346 348	17.4 14.7	25.921 25.991	0.896 0.895	0.1178 0.1205	7.5 7.6	874 876	25.9 21.1

Table 10. Comprehensive quantitative evaluation results on the Tanks&Temples [6] reconstructed by Mip-Splatting [10].

		Grouping				Blen	der [8]			
		Iterations	chair	drumps	ficus	hotdog	lego	materials	mic	ship
	Mip-Splatting*	_	35.773	26.357	35.890	38.267	36.354	30.645	36.934	31.738
PSNR	Group Training w/ RS	0~15K 0~30K	36.078 35.910	26.367 26.293	35.930 35.865	38.474 38.376	36.883 36.860	30.839 30.780	37.152 36.968	31.902 31.931
	Group Training w/ OPS	0~15K 0~30K	35.981 35.958	26.369 26.363	35.912 35.914	38.396 38.326	36.748 36.739	30.756 30.704	37.067 37.049	31.823 31.824
	Mip-Splatting*	_	0.988	0.956	0.988	0.986	0.984	0.961	0.993	0.907
SSIM	Group Training w/ RS	0~15K 0~30K	0.989 0.989	0.956 0.957	0.988 0.988	0.987 0.987	0.986 0.986	0.963 0.964	0.993 0.993	0.909 0.911
	Group Training w/ OPS	0~15K 0~30K	0.989 0.989	0.956 0.956	0.988 0.988	0.987 0.987	0.985 0.985	0.963 0.963	0.993 0.993	0.909 0.909
	Mip-Splatting*	-	0.0109	0.0366	0.0111	0.0186	0.0150	0.0359	0.0062	0.1022
LPIPS	Group Training w/ RS	0~15K 0~30K	0.0101 0.0110	0.0355 0.0358	0.0110 0.0111	0.0163 0.0173	0.0126 0.0132	0.0330 0.0341	0.0059 0.0060	0.0980 0.0998
	Group Training w/ OPS	0~15K 0~30K	0.0105 0.0105	0.0360 0.0359	0.0111 0.0111	0.0169 0.0171	0.0133 0.0134	0.0343 0.0349	0.0060 0.0061	0.0997 0.1001
	Mip-Splatting*	_	3.0	3.0	2.7	2.7	2.9	2.6	2.8	2.9
PM	Group Training w/ RS	0~15K 0~30K	3.3 3.3	3.3 3.4	2.9 2.9	2.9 2.9	3.3 3.3	2.8 2.8	3.0 3.0	3.4 3.4
	Group Training w/ OPS	0~15K 0~30K	3.1 3.1	3.1 3.1	2.7 2.7	2.7 2.7	3.1 3.1	2.7 2.7	2.9 2.9	3.1
	Mip-Splatting*	_	90	98	51	51	76	40	64	83
Size	Group Training w/ RS	0~15K 0~30K	141 141	146 147	79 80	70 71	136 136	71 71	94 94	146 146
	Group Training w/ OPS	0~15K 0~30K	109 109	115 115	57 57	55 55	98 99	51 51	72 72	109 109
	Mip-Splatting*	_	9.2	8.8	6.2	8.4	8.8	6.2	9.3	10.7
Time	Group Training w/ RS	0~15K 0~30K	9.6 8.5	9.7 8.7	6.9 6.4	8.8 8.1	9.8 8.8	7.3 6.9	9.8 8.5	12.1 10.8
	Group Training w/ OPS	0~15K 0~30K	8.6 7.8	8.8 8.0	6.2 6.0	7.8 7.3	8.6 7.7	6.6 6.3	8.4 7.6	10.4 9.6

Table 11. Comprehensive quantitative evaluation results on the Blender [8] reconstructed by Mip-Splatting [10].