

Learning of low-level feature keypoints for accurate and robust detection: Supplementary materials

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This document is the supplementary material for *Learning of low-level feature keypoints for accurate and robust detection*. In this supplementary material, we provide additional results and analysis to support the results in the main paper. This document covers the following contents:

1. The impact of feature extraction parameters

- 1.1. Runtime performance.
- 1.2. The impact of scale detection size
- 1.3. The impact of the number of keypoints

2. Visual results for 3D reconstruction

- 2.1. Impact of *LLF* keypoints on 3D reconstruction
- 2.2. 3D reconstruction by state-of-the-art methods

3. More keypoint detection and matching

- 3.1. The comparison with ASLFeat v.2
- 3.2. Visual results of keypoint detection & matching

4. Additional details for training data

1. The impact of feature extraction parameters

The performance of our method as well as R2D2 is affected by the following settings: (1) the scale factor; (2) the range of scale detection sizes; and (3) the number of keypoints. To observe the impact of the parameter settings, we fix the scale factor to $2^{0.25}$ and the minimum scale detection size to 256. Therefore, we evaluate the performance at different maximum sizes and number of keypoints. The following sections discuss the impact of maximum sizes and number of keypoints on runtime performance, mean matching accuracy (*MMA*), and mean matched error (*MME*). All the evaluations are performed on the HPatch datasets [1].

1.1. Runtime performance.

The runtime performance is mainly determined by the scale detection size, which is associated with the spatial dimension $H \times W$ of each layer in R2D2 as well as our *LLF* detector. We evaluate our $100\%LLF+R2D2$ and our

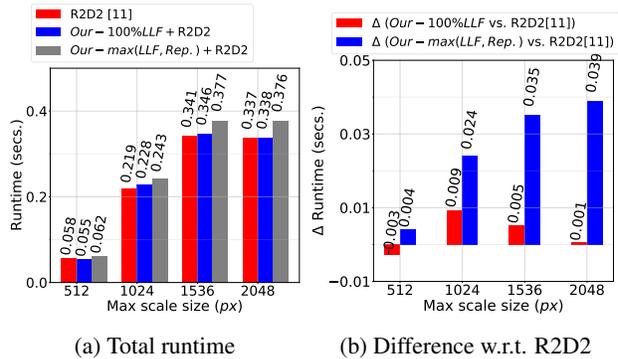


Figure 1: Runtime performance of our method across different scale detection sizes: (a) total runtime; and (b) time difference with respect to R2D2.

$\max(LLF, Rep.)+R2D2$, against R2D2 [11], at the maximum scale detection size (*max. scale size*) of 512px, 1024px, 1536px, and 2048px. The measurements are performed on NVIDIA GeForce RTX 2080 Ti GPU. We provide the average runtime in Figure 1a and calculate the difference between our runtime and R2D2’s in Figure 1b. The number of keypoints is set to 5K. As *max. scale size* increases, the runtime of every method increases. Our $100\%LLF+R2D2$ has the runtime similar to R2D2 because we have replaced R2D2’s repeatable detector with our *LLF* detector. Meanwhile, our $\max(LLF, Rep.)+R2D2$ requires additional runtime (4 ms - 39 ms) because the *LLF* detector is used in addition to the existing detectors.

1.2. The impact of scale detection size

To study the impact of scale detection size, we evaluate the *MMA* of our $100\%LLF+R2D2$ and R2D2 at different maximum scale detection size (*max. scale sizes*): 512px, 1024px, 1536px, and 2048px. The results are demonstrated in Figure 2. Both the *MMA* of our $100\%LLF+R2D2$ and R2D2 increase with the *max. scale sizes*. In Figure 2a, our method provides higher *MMA* in most range of *max. scales size*, when the error threshold $< 4px$.

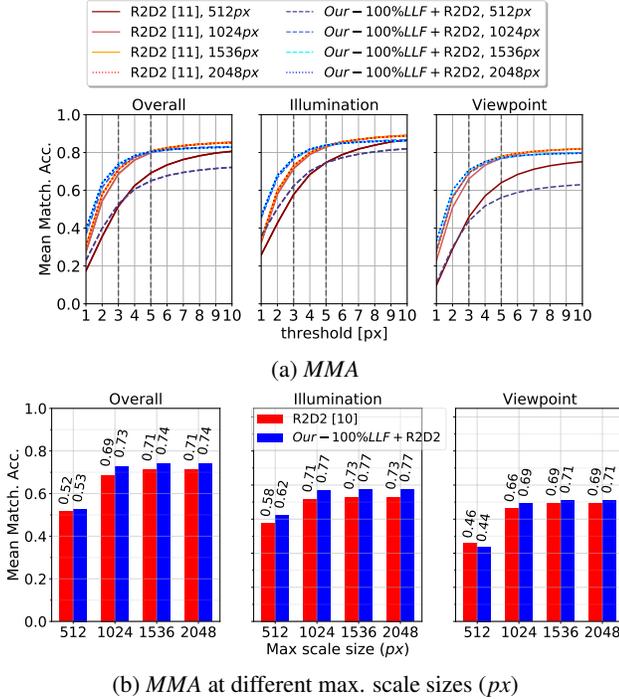


Figure 2: The impact of maximum scale detection size (*max. scales size*) on MMA [4]: (a) MMA across multiple error thresholds (1 – 10px), and (b) MMA across different *max. scales sizes* at the error threshold of 3px. Our method provides higher MMA when the error threshold < 4px, and in every *max. scales size* at the error threshold of 3px.

At the error threshold of 3px, both methods saturate when *max. scale sizes* > 1536px, from Figure 2b. Our 100%LLF+R2D2 achieves higher MMA (0.74 vs 0.71).

The performance on MME is shown in Figure 3. Both the MME of our 100%LLF+R2D2 and R2D2 reduces as the *max. scale sizes* increase. For each *max. scale size*, our 100%LLF+R2D2 provides lower MME across different error threshold as shown in 3a, which indicates the improved sub-pixel accuracy. Figure 3b shows the MME at different *max. scale sizes* (px) at the error threshold of 3px. Both methods saturate when *max. scale size* is above 1536px. R2D2 yields the MME of 1.29. Meanwhile, our 100%LLF+R2D2 can achieve the lowest MME of 1.10, across different *max. scale sizes*.

1.3. The impact of the number of keypoints

This section we study the impact of number of keypoints (#*kpts*). We use the MMA and MME to observe the impact on the performance of our 100%LLF+R2D2 and R2D2 [11]. We evaluate the performance at different #*kpts*: 1K, 5K, 7.5K, and 10K. Figure 4a shows the MMA for each #*kpts* setting across different error thresholds (1 – 10px). Our 100%LLF+R2D2 offers higher MMA

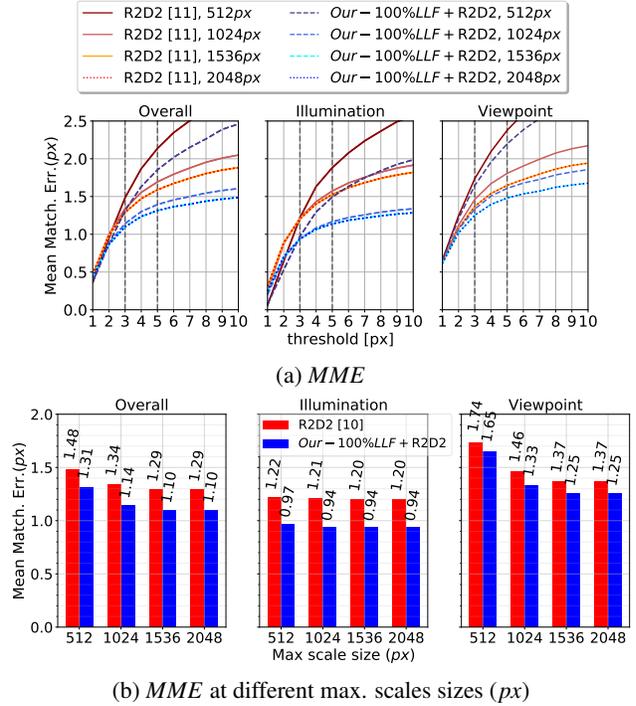


Figure 3: The impact of maximum scale detection size (*max. scales size*) on MME: (a) MME across multiple error thresholds 1 – 10px; and (b) MME across different *max. scales sizes* at error threshold of 3px. Our method provides lower MME than R2D2 across the *max. scales sizes*.

than R2D2 when the error threshold is < 5px. Figure 4b provides the MMA across different #*kpts*: 1K, 5K, 7.5K, and 10K, where the error threshold is set to 3px. The MMA of both our 100%LLF+R2D2 and R2D2 decreases as #*kpts* increases. Nevertheless, our method provides the higher MMA across different cases.

The impact on MME is provided in Figure 5. Our 100%LLF+R2D2 at each setting of #*kpts* offers lower MME than R2D2 across different error thresholds. The worst MME of our 100%LLF+R2D2 (at #*kpts* = 10K) is still better than the best MME of R2D2 (at #*kpts* = 1K) as shown in Figure 5a. This confirms the improved performance on the matched keypoint accuracy by our method. The performance on MME across different #*kpts* is in Figure 5b, where the error threshold is set to 3px. Both our 100%LLF+R2D2 and R2D2 provide worse MME as #*kpts* increases; nevertheless, 100%LLF+R2D2 provides lower MME than R2D2 in all cases, across different #*kpts*.

2. Visual results for 3D reconstruction

This section provides visual results of 3D reconstruction: more results for the impact of LLF keypoints in Section 2.1 and 3D reconstruction by the state-of-the-art in Section 2.2.

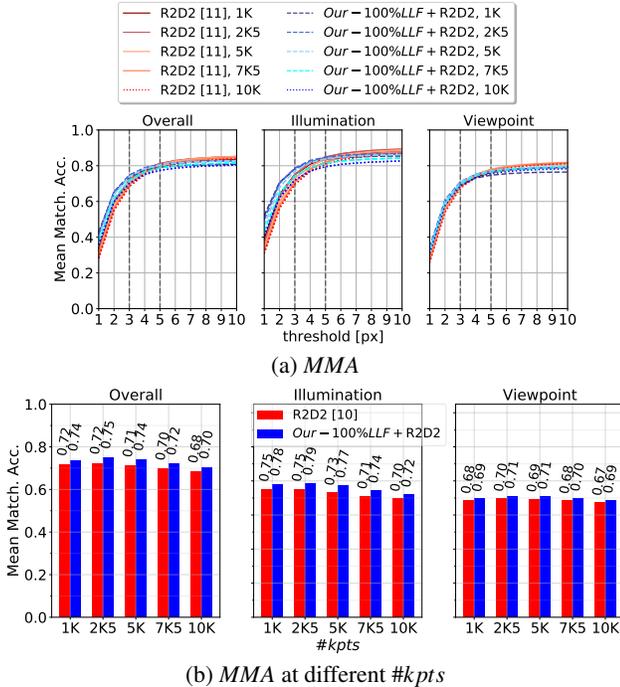


Figure 4: The impact of number of keypoints ($\#kpts$) on *MMA*: (a) *MMA* across multiple error thresholds 1 – 10px; and (b) *MMA* across different $\#kpts$ at the error threshold of 3px. The *MMA* of our method and R2D2 decreases as $\#kpts$ increases. Our method has higher *MMA* when the error threshold $< 5px$, and in every $\#kpts$ at the error threshold of 3px.

2.1. Impact of *LLF* keypoints on 3D reconstruction

Here, we provide the additional visual results to demonstrate the impact of *LLF* keypoints on 3D reconstruction of Herzjesu. The proportion of *LLF* keypoints as the percent to the total keypoints from *LLF* and R2D2’s repeatable detectors is varied from 0%, 25%, 50%, 100%. Here, we provide the visual results in Figure 6 corresponding the numerical results in the main paper (Table 2). To reflect the number of correct 3D points, we vary the point maximum error thresholds from 3px (top), 1px, and 0.60px (bottom), where the lower threshold filters out more erroneous points. From Figure 6, the higher proportion of *LLF* keypoints results in the more complete and correct 3D shape at the low point maximum error thresholds. Our 100%*LLF*+R2D2 offers the most complete and correct 3D shape at the lowest threshold (0.60px).

2.2. 3D reconstruction by state-of-the-art methods

The example 3D reconstruction by state-of-the-art local features, namely, (a) SIFT [7], (b) ASLFeat [8], (c) R2D2 [11], and (d) our 100%*LLF*+R2D2, on Herzjesu and

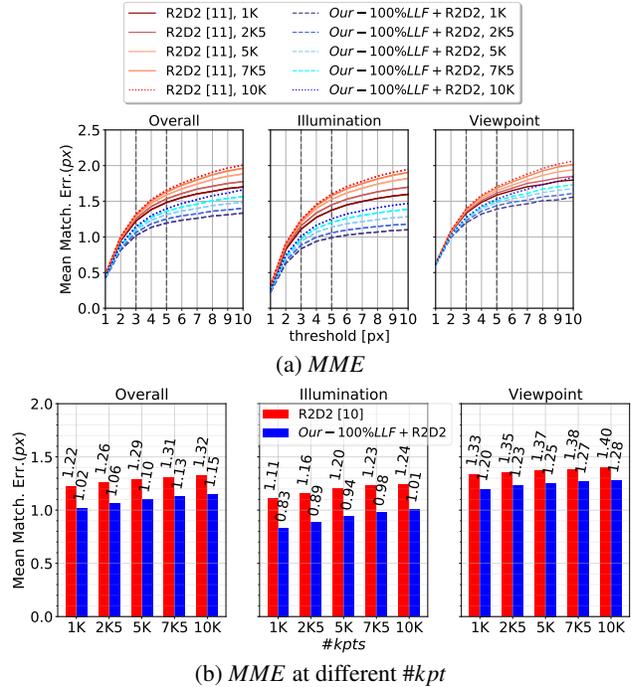


Figure 5: The impact of number of keypoints ($\#kpts$) on *MME*: (a) *MME* across multiple error thresholds 1 – 10px; and (b) *MME* across $\#kpt$ at error threshold of 3px. The *MME* of both R2D2 and our method increases with $\#kpts$. Our method gives lower *MME* than R2D2 in all cases.

Fountain are provided in Figure 8 and 9, respectively. For every method, we set the number of keypoints to 20K and the maximum scale detection size to 2048px. At first, the noticeable differences between these methods is the distribution of 3D points. Our 100%*LLF*+R2D2 and R2D2 provide the sparse 3D points spreading over the building, yet our 100%*LLF*+R2D2 has slightly more points clustering on the edges and corner of Herzjesu building. Meanwhile, ASLFeat provides dense 3D points. The 3D points of SIFT and ASLFeat densely cluster around the edges and corner.

Then, we varied the point maximum error thresholds to 0.7px and the point minimum tracking length to 5 to reflect the amount of correct 3D points. Our 100%*LLF*+R2D2 offers the complete and correct 3D shape in most cases, where our *Reproj. Err.* is the second best after SIFT, and our *Track. Len.* slightly lower than R2D2. ASLFeat offers a good reconstruction in Herzjesu, but a noisy results on Fountain. The numerical results are provided in Table 1.

3. More keypoint detection and matching

Here, we provide additional results and discussion on keypoint detection and matching. In Section 3.1, we provided the comparison on the keypoint detection and matching where ASLFeat v.2 is included. The visual results on

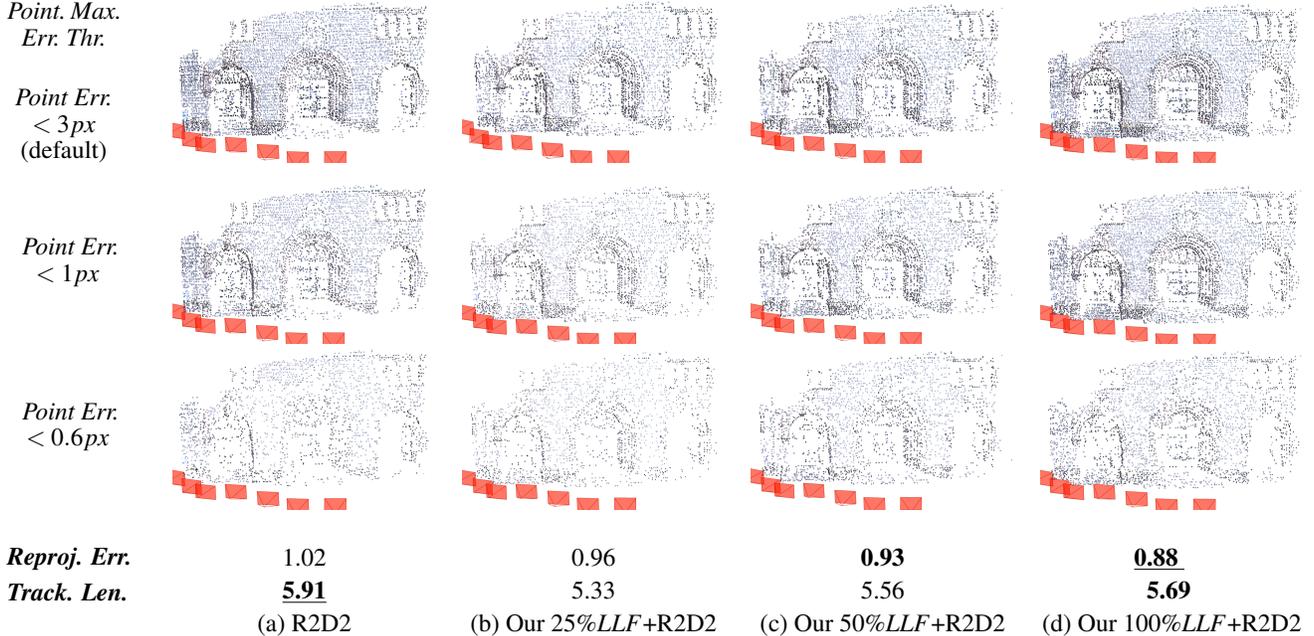


Figure 6: Full comparison: (a) R2D2, (b) our 25%LLF+R2D2, (c) our 50%LLF+R2D2, and (d) our 100%LLF+R2D2. The point maximum error thresholds are varied from 3px (top), 1px, and 0.60px (bottom). The lower threshold filters out more erroneous points. Our LLF keypoints improve the accuracy of 3D points.

the keypoint detection and matching are in Section 3.2.

3.1. The comparison with ASLFeat v.2

The comparison with ASLFeat v.2 is provided in Table 2. We provide this comparison in the Supplementary because ASLFeat v.2 is improved from ASLFeat [8] by using more advanced training data: a large database with additional depth information for training, i.e., blended images and rendered depths, which is out of the scope of our work.

Nevertheless, similar to our report in the main paper (Table 3), our 100%LLF+R2D2, have the highest MMA, and both of our works, our 100%LLF+R2D2 and max(LLF, Rep.)+R2D2, achieve the top three in MME and $\epsilon_{IoU}(SL)$. ASLFeat yields moderate results in many area. However, ASLFeat v.2 can achieve the top three performance in MMA and repeatability (L) and achieve the best $\epsilon_{IoU}(L)$. Nevertheless, similar to KeyNet and SuperPoint, ASLFeat v.2 still has higher error MME and $\epsilon_{IoU}(SL)$. This indicates that ASLFeat v.2 still has high error in matched keypoints and the lacks of robustness against the changed scales in viewpoint.

3.2. Visual results of keypoint detection & matching

We provide the visual results on keypoint matching in Figure 10. The green lines denote the correct matching, and the red lines denote the wrong matches under the error threshold of 3px. The results are sorted by the range of ge-

Datasets	Methods	#Reg.	#Sparse	Track.	Reproj.	#Obs.
		Imges	Points	Len.	Error	Points
Herzjesu 8 images	SIFT [7]	8	3.2K	4.01	0.531	13K
	ASLfeat [8]	8	15.3K	5.14	0.881	78K
	R2D2 [11]	8	13.6K	5.91	1.020	80K
	Our 100%LLF+R2D2	8	13.0K	5.69	0.880	74K
Fountain 11 images	SIFT [7]	11	5.7K	4.47	0.431	25K
	ASLfeat [8]	11	25.2K	6.11	1.010	154K
	R2D2 [11]	11	16.6K	7.53	1.036	125K
	Our 100%LLF+R2D2	11	16.3K	7.31	0.883	119K

Table 1: 3D reconstruction by state-of-the-art methods

ometric noise distributions in HPatches sequences [1], from the easy sequence (top row) to the very tough sequence (at bottom row). MMA and MME under 3px are also provided.

From Figure 10, although our method provides similar or lower number of matches, our method offers the least amount of wrong matches, which is associated with the highest MMA and the best MME among the learning-based methods. Our MME is the second best after SIFT. However, SIFT has a much higher number of wrong matches, which results in the worse MMA in most cases. Meanwhile, ASLFeat and R2D2 has high number of keypoint matches. ASLFeat tends to have more wrong matches than R2D2 and ours. Nevertheless, our LLF detector is more selective than R2D2’s detector, leading to the superior MMA and MME.

The visual results of keypoint detection corresponding to the previous matching results are in Figure 11-12. Among

Methods	Overall									Illumination				Viewpoints			
	Feat. Matching			ϵ_{IoU}		Repeatability				Feat. Matching		ϵ_{IoU}		Feat. Matching		ϵ_{IoU}	
	<i>MMA</i>	<i>MME</i>	# <i>Inlie.</i>	<i>SL</i>	<i>L</i>	<i>SL</i>	<i>L</i>	# <i>Corr.</i>	<i>MMA</i>	<i>MME</i>	<i>SL</i>	<i>L</i>	<i>MMA</i>	<i>MME</i>	<i>SL</i>	<i>L</i>	
SIFT [7]	0.51	1.014	232	0.178	0.120	37.8	59.0	402	0.48	0.897	0.118	0.120	0.55	1.127	0.237	0.119	
SURF [2]	0.47	1.211	213	0.173	0.120	44.2	62.1	451	0.47	1.040	0.109	0.113	0.48	1.378	0.235	0.127	
Key.Net [5]	0.72	1.186	408	0.138	0.093	60.3	68.2	591	0.72	1.010	0.090	0.092	0.71	1.360	0.185	0.094	
D2-Net [4]	0.30	1.725	141	0.219	0.183	37.2	54.7	210	0.39	1.607	0.179	0.168	0.22	1.843	0.257	0.197	
ASLFeat [8]	0.69	1.178	358	0.142	0.089	49.8	61.3	573	0.72	1.024	0.088	0.088	0.66	1.330	0.195	0.091	
ASLFeat v.2 [8]	0.73	1.175	387	0.140	0.087	50.9	63.0	589	0.77	1.036	0.083	0.084	0.69	1.315	0.195	0.090	
DELf [9]	0.47	1.016	280	0.151	0.128	47.7	60.3	369	0.89	0.043	0.005	0.011	0.07	1.986	0.293	0.242	
SuperPoint [3]	0.59	1.381	273	0.153	0.110	57.7	79.1	320	0.65	1.135	0.101	0.101	0.53	1.623	0.202	0.119	
R2D2 [11]	0.71	1.265	311	0.118	0.096	51.9	59.2	559	0.73	1.100	0.099	0.097	0.69	1.428	0.136	0.096	
Our max(<i>LLF, Rep.</i>)+R2D2	0.72	1.083	262	0.124	0.088	46.6	55.8	570	0.75	0.835	0.099	0.087	0.70	1.327	0.148	0.089	
Our 100% <i>LLF</i> +R2D2	0.74	1.070	269	0.126	0.092	47.3	57.1	562	0.77	0.819	0.102	0.092	0.71	1.318	0.148	0.092	

Table 2: Comparison to state-of-the-art methods on the full HPatches dataset [1] with mean matching accuracy (*MMA*), mean matched keypoint error (*MME*), average intersection over union error (ϵ_{IoU}), and repeatability (%). The error threshold is set to $3px$. Our 100%*LLF*+R2D2 is the best in *MMA* and achieves the top three in *MME* and ϵ_{IoU} (*SL*) in overall.

all the detected keypoints, the pink color denotes the *inliers*, and the blue color denotes the *outliers* of the matched keypoints. The green color denotes the other detected keypoints. Figure 11 provides the keypoint detection of the easy and the hard sequences. Figure 12 provides the keypoint detection of the tough and the very tough sequences.

Similar to R2D2, our 100%*LLF*+R2D2 provides the sparse keypoints. Nevertheless, our 100%*LLF*+R2D2 has less *outliers* than R2D2, which explains the higher *MMA*. Our keypoints are not as structured as ASLFeat nor SIFT. The keypoints of ASLFeat and SIFT are very dense around the edge and corner in images, and both have more *outliers*.

4. Additional details for training data

From the main paper (Section 4.1, **Baseline and training data.**), we employed the same training data and settings of R2D2-*WAF-N16* and R2D2-*WASF-N16* released from the official site of [11]. In this section, we clarify the details of training data of *WAF* and *WASF* for training our *LLF* detector and R2D2’s backbone from scratches. According to [11], *WASF* or *W-A-S-F* is the tag names refer to combination of the following image pairs sets, *i.e.*:

W – denote *random web images*, *i.e.*, the distractors from a retrieval dataset [10], and the synthetic image pairs are generated by applying random transformations (homography and color jittering) ;

A – denotes *Aachen database images* where the images are obtained from the Aachen dataset [13, 12], and the previous strategy is used to build the synthetic pairs;

S – denotes *Aachen style transfer pairs* where the style transfer [6] is used for building pairs from Aachen;

F – denotes *Aachen optical flow pairs* which are the pairs

of nearby views from the Aachen dataset, and the pseudo ground-truth of the correspondence pixels between image pairs is obtained using optical flow [11].

Therefore, *WASF*- refers to the settings where all the image pairs sets are used. Meanwhile, *WAF*- refers to using *random web images*, *Aachen database images* and *Aachen optical flow pairs* to form training dataset. To confirm consistent performance, we compare our work with R2D2 for both settings, *WAF* and *WASF*, in Figure 7. Our method yield better *MMA* when error threshold $< 4px$ and better *MME* in all cases for both settings.

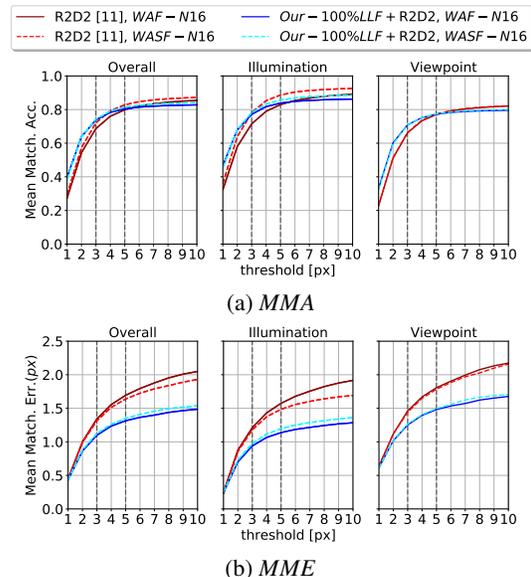


Figure 7: Comparison on *WAF*- and *WASF-N16* settings.

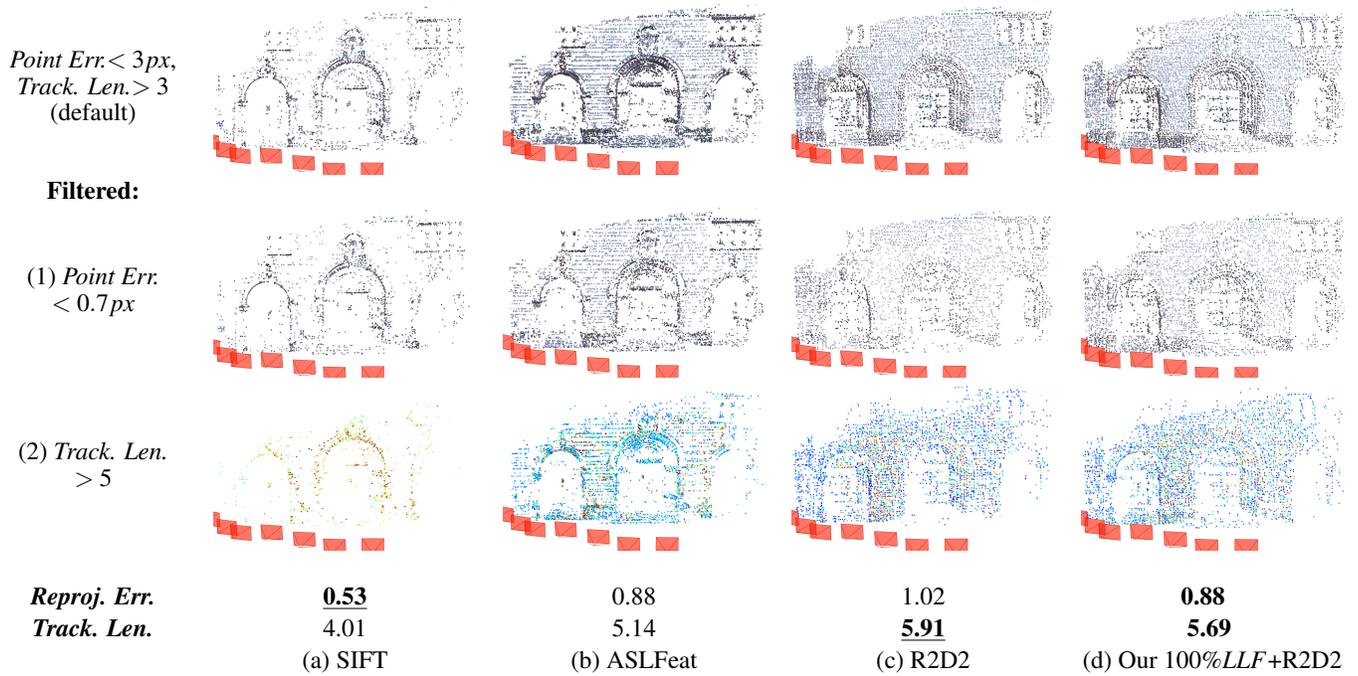


Figure 8: Example 3D reconstruction of Herzjesu: (a) SIFT (b) ASLFeat, (c) R2D2, and (d) our 100%LLF+R2D2.

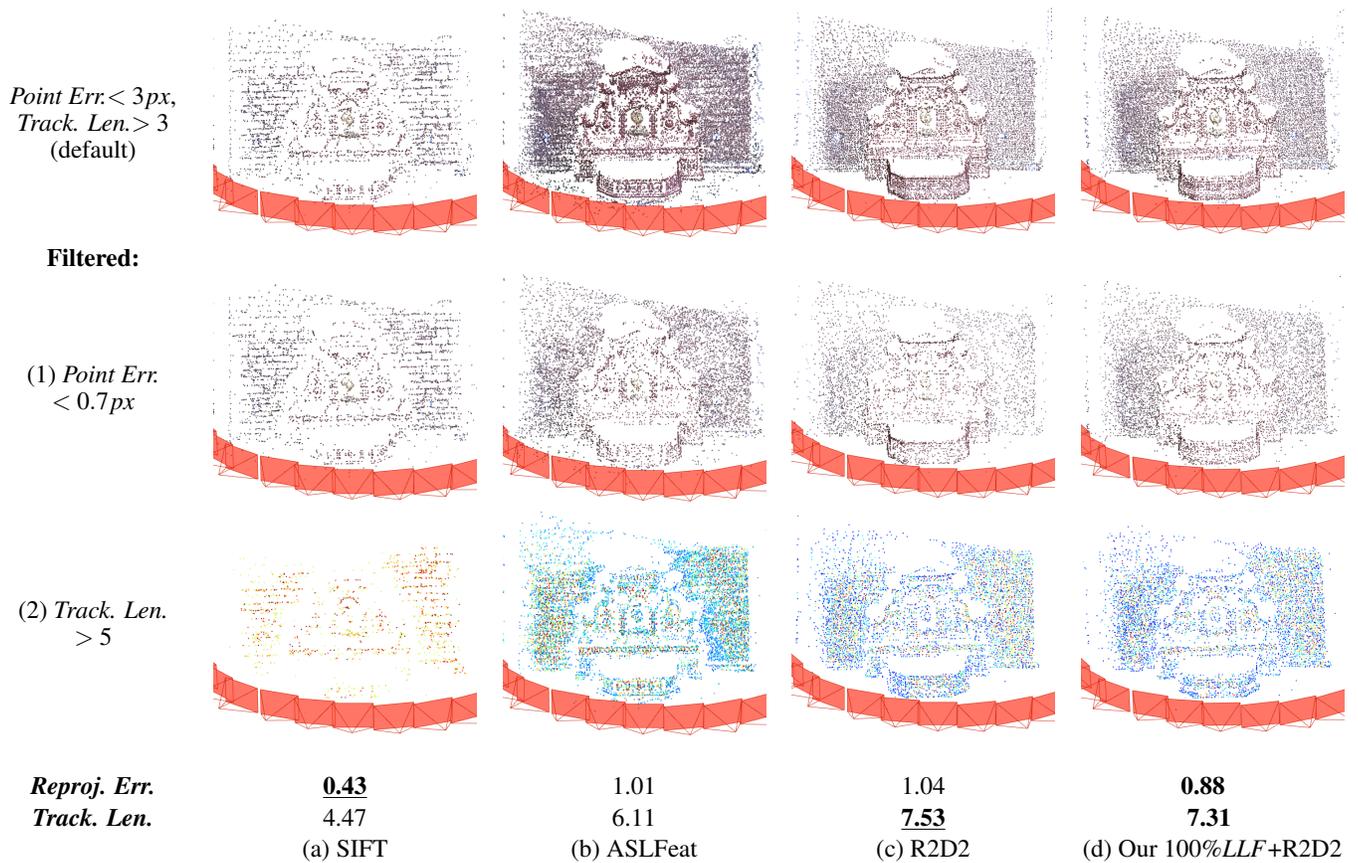


Figure 9: Example 3D reconstruction of Fountain: (a) SIFT (b) ASLFeat, (c) R2D2, and (d) our 100%LLF+R2D2.

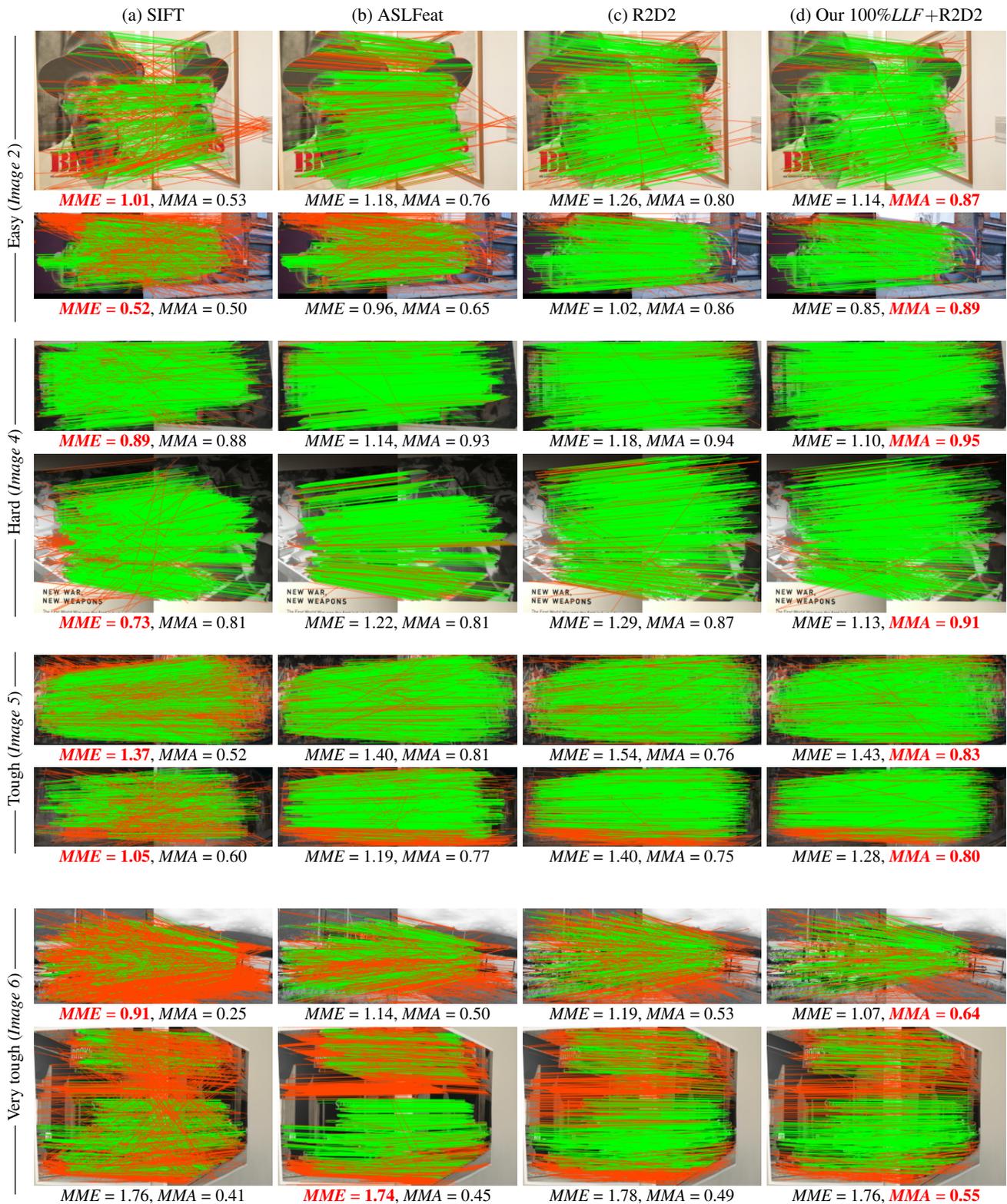


Figure 10: Qualitative results on HPatch by (a) SIFT, (b) ASLFeat, (3) R2D2, and (4) our 100%LLF keypoints+R2D2. The green lines show the correct matching, and the red lines show the wrong matches under the error threshold of $3px$. The results of keypoint matching are sorted by the range of geometric noise distributions in HPatches sequences [1], from the easy sequence (top row) to the very tough sequence (at bottom row). Our method offers high correct matches with small number of wrong matches which explain the highest MMA . Our MME is the second best after *SIFT*.



Figure 11: Visual results of keypoints detection by (a) SIFT, (b) ASLFeat (c) R2D2 and (d) our 100%LLF+R2D2, corresponding to the previous keypoint matching. The pink color denotes the *inliers*. The blue color denotes the *outliers* of the matched keypoints. The green color denotes the other detected keypoints. From the easy to the hard sequences, our 100%LLF+R2D2 less *outliers* than the other methods, which explain the high *MMA* of our keypoints. Similar to R2D2, our keypoints are sparse and not as dense nor structured as ASLFeat and SIFT.

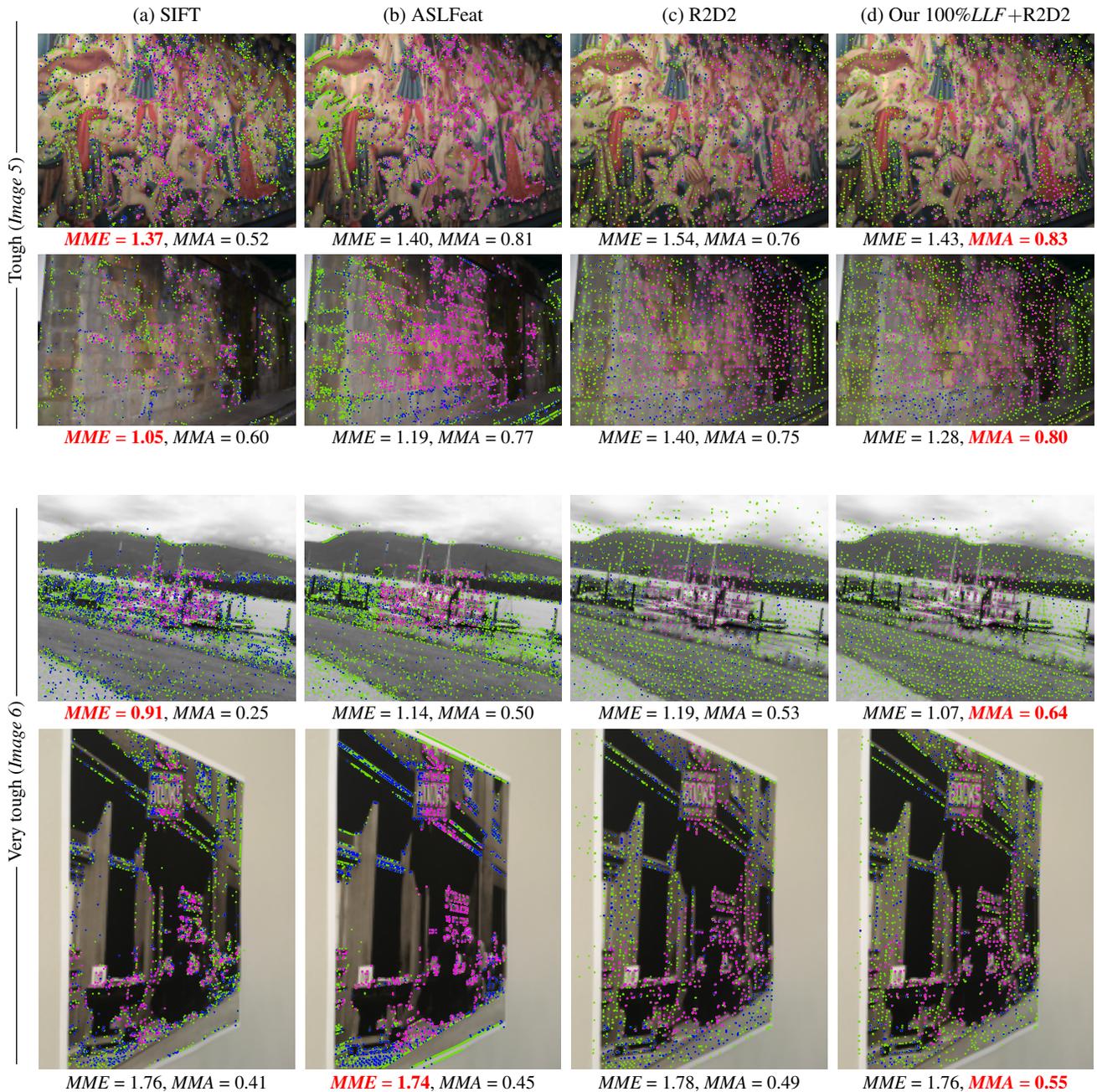


Figure 12: (cont') Visual results of keypoints detection by (a) SIFT, (b) ASLFeat (c) R2D2 and (d) our 100%*LLF*+R2D2. The results of the tough sequence to the very tough sequences are sorted from the top to the bottom rows. The pink and blue color denotes *inliers* and *outliers* among all the keypoints which are denoted by green color. In these tough samples, our 100%*LLF*+R2D2 has notably less *outliers* than the others. ASLFeat and SIFT keypoints are more dense at the edge and corners and much more number of *outliers*.

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