

Permutation-Aware Activity Segmentation via Unsupervised Frame-to-Segment Alignment

Quoc-Huy Tran* Ahmed Mehmood* Muhammad Ahmed Muhammad Naufil Anas Zafar Andrey Konin M. Zeeshan Zia

Retrocausal, Inc., Redmond, WA

www.retrocausal.ai

Abstract

This paper presents an unsupervised transformer-based framework for temporal activity segmentation which leverages not only frame-level cues but also segment-level cues. This is in contrast with previous methods which often rely on frame-level information only. Our approach begins with a frame-level prediction module which estimates framewise action classes via a transformer encoder. The frame-level prediction module is trained in an unsupervised manner via temporal optimal transport. To exploit segment-level information, we utilize a segment-level prediction module and a frame-to-segment alignment module. The former includes a transformer decoder for estimating video transcripts, while the latter matches frame-level features with segmentlevel features, yielding permutation-aware segmentation results. Moreover, inspired by temporal optimal transport, we introduce simple-yet-effective pseudo labels for unsupervised training of the above modules. Our experiments on four public datasets, i.e., 50 Salads, YouTube Instructions, Breakfast, and Desktop Assembly show that our approach achieves comparable or better performance than previous methods in unsupervised activity segmentation.

1. Introduction

Temporal activity segmentation [5, 8, 11, 17, 31, 34, 37, 43, 54] aims to associate each frame in a video capturing a human activity with one of the action/sub-activity classes. Temporally segmenting human activities in videos plays an important role in several computer vision, robotics, health-care, manufacturing, and surveillance applications. Examples include visual analytics [2, 22, 23] (i.e., compute time and motion statistics such as average cycle time from video recordings), ergonomics risk assessment [40, 41] (i.e., seg-

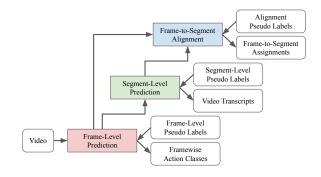


Figure 1. Prior works often use only frame-level cues via frame-level prediction modules (i.e., red) to predict framewise action classes. We adopt a segment-level prediction module and a frame-to-segment alignment module (i.e., green/blue), which exploit segment-level cues for permutation-aware results. Also, we introduce simple-yet-effective pseudo labels for unsupervised training.

ment actions of interest in videos for analyzing ergonomics risks), and task guidance [7, 19, 39] (i.e., offer instructions to workers based on expert demonstration videos).

Considerable efforts have been made in designing fullysupervised methods [12,17,32,33,37] or weakly-supervised methods [5, 8, 13, 25, 29, 34, 38, 43, 44, 46, 51] for temporal activity segmentation due to their great performance. However, acquiring dense framewise labels or weak annotations such as transcripts [29] and timestamps [38] is generally hard and expensive especially for a large number of videos. Therefore, we are interested in unsupervised approaches for temporal activity segmentation, which simultaneously extract actions and segment all video frames into clusters with each cluster representing one action. Early unsupervised methods [30, 36, 49, 57, 59] separate representation learning from clustering, preventing effective feedback between them, while using offline clustering, resulting in memory inefficiency. To address that, UDE [54] and TOT [31] develop joint representation learning and online clustering ap-

^{*} indicates joint first author. {huy,ahmedraza,ahmed,naufil,anas,andrey,zeeshan}@retrocausal.ai.

proaches. The above methods often leverage frame-level information only (i.e., red block in Fig. 1), while not explicitly utilizing high-level information such as transcript, which is crucial for handling permutations of actions, missing actions, and repetitive actions.

In this work, we present an unsupervised activity segmentation framework which is based on transformers [56] and exploits both frame-level cues and segment-level cues. Motivated by the strong performance of supervised transformer-based architectures [5, 14] in supervised activity segmentation, our unsupervised model includes a transformer encoder and a transformer decoder. The former performs self-attention to learn dependencies within the video sequence, while the latter relies on cross-attention to learn dependencies between the video sequence and the transcript sequence, resulting in effective contextual features. In addition to the frame-level prediction module for exploiting frame-level cues, we include a segment-level prediction module and a frame-to-segment alignment module (i.e., green and blue blocks in Fig. 1) to leverage segment-level cues, yielding permutation-aware segmentation results. For unsupervised training of the above modules, we propose simple-yet-effective pseudo labels based on temporal optimal transport [31]. We demonstrate comparable or superior performance of our approach over previous unsupervised activity segmentation methods on four public datasets.

In summary, our contributions include:

- We introduce a novel combination of modules and unsupervised losses to exploit both frame-level cues and segment-level cues for permutation-aware activity segmentation.
- We propose simple-yet-effective pseudo labels based on temporal optimal transport, enabling unsupervised training of the segment-level prediction module and the frame-to-segment alignment module.
- Extensive evaluations on 50 Salads, YouTube Instructions, Breakfast, and Desktop Assembly datasets show that our approach performs on par with or better than prior methods in unsupervised activity segmentation.

2. Related Work

Fully-Supervised Activity Segmentation. Early works in fully-supervised activity segmentation often rely on sliding temporal window with non-maximum suppression [24, 47] or structured temporal modeling via hidden Markov models [28,55], while recent methods are mostly based on temporal convolutional networks (TCNs) [12, 17, 32, 33, 37]. Lea et al. [32] develop the first TCN-based solution, which includes an encoder-decoder architecture with temporal convolutions and deconvolutions to capture long-range temporal dependencies. TricorNet [12] replaces the above de-

coder by a bi-directional LSTM, while TDRN [33] employs deformable temporal convolutions instead. Since these methods downsample videos to a temporal resolution, they fail to capture fine-grained details. Thus, multi-stage TCNs [17, 37] are introduced to maintain a high temporal resolution. However, due to performing framewise prediction, the above methods suffer from over-segmentation. To address that, refinement techniques, e.g., graph-based reasoning [20] and boundary detection [21], are proposed.

Weakly-Supervised Activity Segmentation. supervised activity segmentation methods utilize different forms of weak labels, including the ordered list of actions appearing in the video, i.e., transcript supervision [8, 13, 29, 34, 44, 46], or the set of actions occurring in the video, i.e., set supervision [18, 35, 45]. Recently, timestamp supervision [25, 38, 43, 51], which requires labeling a single frame per action segment, has attracted research interests, since it has similar annotation costs as transcript supervision but it yields better results thanks to the additional approximate segment location information in timestamp labels. More recently, Behrmann et al. [5] introduce a unified fully-supervised and timestamp-supervised method, achieving competitive results. The above methods need either framewise labels for full supervision or weak labels for weak supervision, whereas our approach does not.

Unsupervised Activity Segmentation. Early attempts [3, 50] in unsupervised activity segmentation often utilize the narrations accompanied with the videos, however, these narrations are not always provided. That motivates the development of methods with only visual inputs [30, 31, 36, 49, 54, 57, 59]. Mallow [49] learns an appearance model and a temporal model of the activity in an alternating manner. CTE [30] first learns a temporal embedding and then clusters the embedded features with K-Means. To improve CTE, VTE [57] adds a visual embedding, while ASAL [36] adds an action-level embedding. SSCAP [59] first uses a video-based self-supervised model for feature extraction and then performs co-occurrence action parsing to capture the temporal structure of the activity. The aforementioned methods separate representation learning from offline clustering, preventing effective feedback between them, whereas we follow recent approaches, i.e., UDE [54] and TOT [31], to perform joint representation learning and online clustering. Furthermore, unlike UDE [54] and TOT [31], which exploit frame-level cues only, we propose modules for exploiting segment-level cues and pseudo labels for unsupervised training, yielding improved results.

Transformers in Activity Segmentation. After successes of transformers [56] in natural language processing, there has been a wide adoption of transformers in computer vision [4, 6, 9, 14]. Transformers focus on attention mechanism to extract contextual information over the entire sequence. Recently, a few methods [5,60] have applied trans-

formers for temporal activity segmentation. ASFormer [60] consists of encoder blocks, each of which includes a dilated temporal convolution and a self-attention layer, and decoder blocks, where cross-attention is used to gather information from encoder blocks. Due to making framewise prediction, ASFormer suffers from over-segmentation. To address that, UVAST [5] uses a transformer decoder to predict the transcript and exploit segment-level cues. In this work, we adopt the transformer encoder of ASFormer [60] and the transformer decoder of UVAST [5]. However, our overall architecture is different from them. Also, they require labels for supervised training, whereas we propose pseudo labels for unsupervised training.

3. Our Approach

We present below our main contribution, an unsupervised transformer-based framework for temporal activity segmentation. Fig. 2 shows an overview of our approach. **Notations.** Let us first represent the encoder function and the decoder function as f_{θ} and g_{ϕ} respectively (with learnable parameters θ and ϕ). Our approach takes as input a sequence of B frames, represented as X = $[\boldsymbol{x}_1, \boldsymbol{x}_2, \dots, \boldsymbol{x}_B]^{\top}$. The encoder features of \boldsymbol{X} are expressed as $m{E} = [m{e}_1, m{e}_2, \dots, m{e}_B]^{ op} \in \mathbb{R}^{B \times d}$ with $m{e}_i =$ $f_{\boldsymbol{\theta}}(\boldsymbol{x}_i) \in \mathbb{R}^d$ (d is the feature dimension). Next, let us denote $\mathbf{A} = [1, 2, \dots, K]^{\top} \in \mathbb{R}^{K}$ as the sequence of Kaction classes in the activity. Our approach learns a group of K prototypes, represented as $C = [c_1, c_2, \dots, c_K]^{\top} \in$ $\mathbb{R}^{K \times d}$ with $c_j \in \mathbb{R}^d$ corresponding to the j-th action class in A. We denote $T = [a_1, a_2, \dots, a_N]^{\top} \in \mathbb{R}^N$ (with $a_i \in A$) as the transcript which contains the sequence of actions appearing in $oldsymbol{X}$, and $oldsymbol{S} \in \mathbb{R}^{N imes d}$ as the transcript features. The decoder features are written as D = $[\boldsymbol{d}_1, \boldsymbol{d}_2, \dots, \boldsymbol{d}_N]^{\top} \in \mathbb{R}^{N \times d}$ with $\boldsymbol{d}_j \in \mathbb{R}^d$ corresponding to a_j in \boldsymbol{T} . Finally, we represent $\boldsymbol{P}_f \in \mathbb{R}^{B \times K}$, $\boldsymbol{P}_s \in \mathbb{R}^{N \times K}$, and $\boldsymbol{P}_a \in \mathbb{R}^{B \times K}$ as the *predicted* assignment probabilities (i.e., predicted "codes") at the frame-level prediction module (i.e., between frames and actions), the segmentlevel prediction module (i.e., between transcript positions and actions), and the frame-to-segment alignment module (i.e., between frames and actions) respectively. Similarly, $\boldsymbol{Q}_f \in \mathbb{R}^{B \times K}, \, \boldsymbol{Q}_s \in \mathbb{R}^{N \times K}, \, \text{and} \, \boldsymbol{Q}_a \in \mathbb{R}^{B \times K}$ denote the corresponding pseudo-label assignment probabilities (i.e., pseudo-label "codes") for P_f , P_s , and P_a respectively.

3.1. Unsupervised Frame-Level Prediction

Here we describe our frame-level prediction module. In particular, we adopt the joint representation learning and online clustering method of [31]. Unlike [31], we include modules and unsupervised losses in Secs. 3.2 and 3.3 for exploiting segment-level cues. Also, instead of the MLP encoder of [31], we utilize the transformer encoder of [5] to capture long-range dependencies via self-attention.

The input frames X are first fed to the transformer encoder f_{θ} to yield the encoder features E. The frame-level predicted codes P_f (with P_f^{ij} denoting the probability that the i-th frame in X is assigned to the j-th action in A) are then computed as $P_f = \operatorname{softmax}\left(\frac{1}{\tau}EC^{\top}\right)$ with a temperature τ . We follow [31] to obtain the frame-level pseudolabel codes Q_f by solving the below fixed-order temporal optimal transport problem:

$$\max_{\boldsymbol{Q} \in \mathcal{Q}} Tr(\boldsymbol{Q}^{\top} \boldsymbol{E} \boldsymbol{C}^{\top}) - \rho KL(\boldsymbol{Q} || \boldsymbol{M}_{\boldsymbol{A}}), \qquad (1)$$

$$Q = \left\{ Q : \quad Q \mathbf{1}_K = \frac{1}{B} \mathbf{1}_B, Q^{\mathsf{T}} \mathbf{1}_B = \frac{1}{K} \mathbf{1}_K \right\}, \quad (2)$$

where ρ is a balancing parameter, and $\mathbf{1}_B$ and $\mathbf{1}_K$ are vectors of ones with B and K dimensions respectively. The first term in Eq. 1 measures the similarity between the features E and the prototypes C, while the second term denotes the Kullback-Leibler divergence between Q_f and the prior distribution M_A [53]. In particular, M_A assumes the fixed order of actions A, and enforces initial frames in Xto be assigned to initial actions in A and subsequent frames in X to be assigned to subsequent actions in A. In Sec. 3.2, we will discuss relaxing the above fixed-order prior by introducing the transcript T and enabling permutations of actions. Eq. 2 represents the *equal partition* constraint, which imposes that each action in A is assigned the same number of frames in X to avoid a trivial solution. As mentioned in [31], the method works relatively well for activities with various action lengths since the above equal partition constraint is applied on soft assignments. The solution for the above fixed-order temporal optimal transport problem is:

$$Q_f = \operatorname{diag}(u) \exp\left(\frac{EC^{\top} + \rho \log M_A}{\rho}\right) \operatorname{diag}(v),$$
 (3)

where $u \in \mathbb{R}^B$ and $v \in \mathbb{R}^K$ are renormalization vectors [10]. Fig. 3 shows an example of M_A and Q_f , where the red boxes highlight the fixed order of actions $\{3,4,5\}$. We minimize the below cross-entropy loss with respect to θ and C (note that we do not backpropagate through Q_f):

$$L_f = -\frac{1}{B} \sum_{i=1}^{B} \sum_{j=1}^{K} Q_f^{ij} \log P_f^{ij}.$$
 (4)

3.2. Unsupervised Segment-Level Prediction

The above module leverages frame-level cues and the fixed-order prior. In this section, we describe the segment-level prediction module to exploit segment-level cues and allow permutations of actions. In particular, we introduce the transcript T, which indicates the sequence of actions

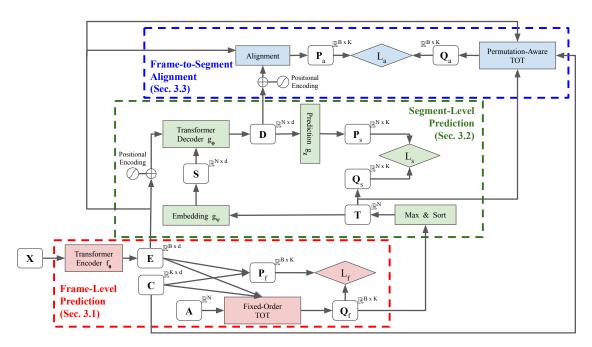


Figure 2. Our approach includes a frame-level prediction module (i.e., red) which extracts frame-level features E via a transformer encoder and uses temporal optimal transport to compute frame-level pseudo labels Q_f for unsupervised training. To exploit segment-level information, we utilize a segment-level prediction module (i.e., green), which extract segment-level features D via a transformer decoder, and a frame-to-segment alignment module (i.e., blue), which matches frame-level features E and segment-level features D. In addition, we introduce segment-level pseudo labels Q_s and alignment-level pseudo labels Q_g for unsupervised training of the above modules.

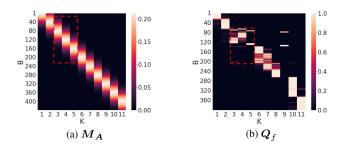


Figure 3. (a) Fixed-order prior distribution M_A . (b) Frame-level pseudo-label codes Q_f .

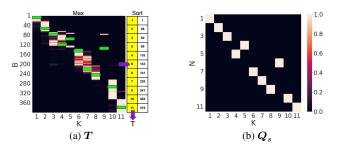


Figure 4. (a) Permutation-aware transcript T. (b) Segment-level pseudo-label codes Q_s .

of A occurring in the input sequence X. For example, let us assume A = [1, 2, 3, 4, 5], it is possible that T =

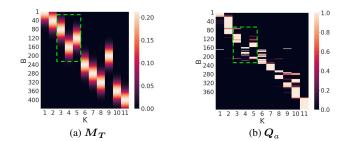


Figure 5. (a) Permutation-aware prior distribution M_T . (b) Alignment-level pseudo-label codes Q_a .

[1, 3, 2, 5, 4], which is a permutation of \boldsymbol{A} . We will discuss later how \boldsymbol{T} is estimated for unsupervised training.

Assuming the transcript T is given, we first pass it to the embedding layer g_{ψ} to obtain the transcript features S, which are then fed to the transformer decoder g_{ϕ} . In addition, we also feed the encoder features E (after positional encoding) to the transformer decoder g_{ϕ} , which performs cross-attention between E and S to yield the decoder features D. The segment-level predicted codes P_s (with P_s^{ij} corresponding to the probability that the i-th position in T contains the j-th action in A) are computed by passing the decoder features D to the prediction layer g_{χ} . In practice, we employ the transformer decoder of [5], which computes P_s in an auto-regressive manner, i.e., a part of T up to the

i-th position is used to predict the (i+1)-th row of P_s . In parallel, we convert the transcript T into the segment-level pseudo-label codes Q_s . Specifically, we set $Q_s^{ij}=1$ if the i-th position in T contains the j-th action in A, and $Q_s^{ij}=0$ otherwise. We minimize the following cross-entropy loss between P_s and Q_s with respect to θ , ψ , ϕ , and χ (note that we do not backpropagate through Q_s):

$$L_{s} = -\frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{K} Q_{s}^{ij} \log P_{s}^{ij}.$$
 (5)

In contrast with the supervised method of [5], where framewise labels or timestamp labels are required for supervised training, we estimate the transcript T from the frame-level pseudo-label codes Q_f for unsupervised training. For each j-th action, we find the i-th frame where Q_f^{ij} has the maximum assignment probability along the j-th column, yielding an action-frame pair (i, i). Next, we sort all action-frame pairs by their frame indexes. The resulting temporally sorted list of actions is considered as our estimated transcript T. Our motivation is that to predict each action correctly, the method only needs to select a single frame correctly, which is easier than obtaining the correct framewise segmentation result. Note that the above imply that N (the length of the transcript T) is equal to K (the length of the action list A), and our predicted transcript Tshares the same set of unique actions with A despite having different orderings. Fig. 4 illustrates an example of computing T from Q_f , and computing Q_s from T. Similar to [31], our method tends to assign a small number of frames to the missing actions, leading to minor impacts on the overall segmentation accuracy. Handling repetitive actions is an interesting topic and remains our future work. As we will show later in Sec. 4.2, despite using the above simple heuristic for transcript estimation, our method achieves state-of-the-art results on four public datasets.

3.3. Unsupervised Frame-to-Segment Alignment

To further exploit segment-level cues and improve segmentation results, we employ the frame-to-segment alignment module of [5], which matches frame-level features with segment-level features and models permutations of actions. We pass both the encoder features \boldsymbol{E} and the decoder features \boldsymbol{D} (after positional encoding) to the frame-to-segment alignment module, which performs cross-attention between \boldsymbol{E} and \boldsymbol{D} to predicts the alignment-level predicted codes \boldsymbol{P}_a . Here, \boldsymbol{P}_a^{ij} corresponds to the probability that the i-th frame in \boldsymbol{X} is mapped to the j-th action in \boldsymbol{A} . We compute $\boldsymbol{P}_a = \operatorname{softmax} \left(\frac{1}{\tau^{\prime}} \boldsymbol{E} \boldsymbol{D}^{\top} \right)$ with a temperature τ' .

Unlike with the supervised method of [5], where framewise labels or timestamp labels are required for supervised training, we propose a modified temporal optimal transport module which is capable of handling permutations of

actions to compute the alignment-level pseudo-label codes Q_a for unsupervised training. Specifically, instead of using the prior distribution M_A which enforces the fixed order of actions A, we utilize the prior distribution M_T which imposes the permutation-aware transcript T, yielding the permutation-aware temporal optimal transport problem:

$$\max_{\boldsymbol{Q} \in \mathcal{Q}} Tr(\boldsymbol{Q}^{\top} \boldsymbol{E} \boldsymbol{C}^{\top}) - \rho KL(\boldsymbol{Q} || \boldsymbol{M}_{\boldsymbol{T}}).$$
 (6)

The solution for the permutation-aware temporal optimal transport problem is:

$$Q_a = \operatorname{diag}(u) \exp\left(\frac{EC^{\top} + \rho \log M_T}{\rho}\right) \operatorname{diag}(v).$$
 (7)

Fig. 5 shows an example of M_T and Q_a , where the green boxes highlight the permutations of actions $\{3,5,4\}$. This is in contrast with M_A and Q_f in Fig. 3, where the red boxes highlight the fixed order of actions $\{3,4,5\}$. As we will show later in Sec. 4.1.2, using the permutation-aware Q_a derived from T yields better performance than using the fixed-order Q_a derived from A. We minimize the crossentropy loss between P_a and Q_a with respect to θ , ψ , and ϕ (note that we do not backpropagate through Q_a):

$$L_{a} = -\frac{1}{B} \sum_{i=1}^{B} \sum_{j=1}^{K} Q_{a}^{ij} \log P_{a}^{ij}.$$
 (8)

Our final loss for unsupervised training is a combination of the fixed-order loss L_f (Eq. 4) and the permutation-aware losses L_s (Eq. 5) and L_a (Eq. 8):

$$L = L_f + \alpha L_s + \beta L_a,\tag{9}$$

where α and β are the balancing parameters for L_s and L_a respectively. Following [5], we set $\alpha = \beta = 1$.

4. Experiments

Implementation Details. We train our model in two stages. In the first stage, we train only the frame-level prediction module with the loss in Eq. 4 for 30 epochs, which is then used for initialization in the second stage, where we train the entire model with the loss in Eq. 9 for 70 epochs. Note that we reduce the transformer encoder and transformer decoder of [5] to two layers to avoid overfitting. We implement our approach in pyTorch [42]. We use ADAM optimization [26] with a learning rate of 10^{-3} and a weight decay of 10^{-5} . For inference, we follow [31] to compute cluster assignment probabilities for all frames and then pass them to a Viterbi decoder which smooths out the probabilities given the action order T (instead of A in [31]). More details are provided in the supplementary material.

Competing Methods. We compare our approach, namely *UFSA* (short for *U*nsupervised *F*rame-to-*S*egment

Alignment), against a narration-based method [3], sequential learning and clustering methods [30,36,49,57,59], and joint learning and clustering methods [31,54].

Datasets. We evaluate our approach on four public datasets, i.e., 50 Salads [52], YouTube Instructions (YTI) [3], Breakfast [27], and Desktop Assembly [31]:

- 50 Salads includes 50 videos capturing 25 actors making 2 types of salads. The total duration of all videos is over 4.5 hours with an average of 10k frames per video. We test on 2 granularity levels, i.e., Eval with 12 action classes and Mid with 19 action classes. Following [30], we use pre-computed features by [58].
- YouTube Instructions (YTI) contains 150 videos capturing 5 activities with 47 action classes in total and an average video length of about 2 minutes. These videos contain many background frames. We use precomputed features provided by [3].
- *Breakfast* includes 70 hours of videos (30 seconds to a few minutes long per video) capturing 10 cooking activities with 48 action classes in total. We follow [49] to use pre-computed features proposed by [28].
- Desktop Assembly contains 2 sets of videos. Orig contains 76 videos of 4 actors performing desktop assembly in a fixed order. Extra includes all Orig videos and additionally 52 videos with permuted and missing steps, yielding 128 videos in total. We evaluate on both sets using pre-computed features provided by [31].

Evaluation Metrics. Following [30, 31, 49], we perform Hungarian matching between ground truth and predicted segments, which is conducted at the activity level. This is unlike the Hungarian matching performed at the video level in [1, 15, 48]. Note that video-level segmentation, e.g., ABD [15], (i.e., segmenting just a single video) is a subproblem and in general easier than activity-level segmentation, e.g., our work, (i.e., jointly segmenting and clustering frames across all videos). Due to space limits, we convert video-level segmentation results of ABD [15] to activitylevel segmentation results via K-Means and evaluate them in the supplementary material. We compute Mean Over Frames (MOF), i.e., the percentage of frames with correct predictions averaged over all activities, and F1-Score, i.e., the harmonic mean of precision and recall, where only positive detections with more than 50% overlap with ground truth segments are considered. We compute F1-Score for each video and take the average over all videos.

4.1. Ablation Studies

4.1.1 Impacts of Different Model Components

We first study the effects of various network components on the 50 Salads (*Eval* granularity) and YTI datasets. The re-

		Method	MOF	F1
П	Eval	Frame	43.1	34.4
İİ		Frame+Segment	<u>43.2</u>	<u>38.1</u>
		Frame+Segment+Alignment	55.8	50.3
П	YTI	Frame	42.8	30.2
II		Frame+Segment	<u>45.0</u>	<u>30.8</u>
		Frame+Segment+Alignment	49.6	32.4

Table 1. Impacts of different model components on 50 Salads with the Eval granularity (*Eval*) and YouTube Instructions (*YTI*). Best results are in **bold**, while second best ones are *underlined*.

sults are reported in Tab. 1. Firstly, using only the framelevel prediction module presented in Sec. 3.1 yields the lowest overall results. The frame-level prediction module exploits frame-level cues only and utilizes the fixed-order prior which does not account for permutations of actions. Next, we expand the network by adding the segment-level prediction module described in Sec. 3.2 to exploit segmentlevel cues. For 50 Salads, MOF is not changed much, while F1-score is improved by 3.7%. For YTI, MOF is increased by 2.2%, while F1-Score is slightly improved by 0.6%. Although the segment-level prediction module estimates the permutation-aware transcript, the framewise predictions are still suffered from over-segmentation. To address that, the frame-to-segment alignment module proposed in Sec. 3.3 is appended to the network to simultaneously leverage framelevel cues and segment-level cues and refine the framewise predictions, leading to significant performance gains. On 50 Salads, the results are boosted to 55.8% and 50.3% for MOF and F1-Score respectively, while on YTI, MOF is increased to 49.6% and F1-Score to 32.4%.

4.1.2 Impacts of Different Pseudo Labels

Here, we conduct an ablation study on the 50 Salads (Eval granularity) and YTI datasets by using various versions of pseudo labels Q_s and Q_a computed from either the fixed order of actions A or the permutation-aware transcript T. Tab. 2 presents the results. Firstly, using the fixed order of actions A for computing both Q_s and Q_a (i.e., we use T = A in both Secs. 3.2 and 3.3) yields the lowest overall numbers on both datasets, i.e., on 50 Salads, 46.1% and 45.2% for MOF and F1-Score respectively, and on YTI, 44.3% and 29.4% for MOF and F1-Score respectively. Next, we experiment with using the permutationaware transcript T for computing either Q_s or Q_a , resulting in performance gains, e.g., for the former (T for Q_s , A for Q_a), we achieve 50.8% for MOF and 46.9% for F1-Score on 50 Salads, while for the latter (\boldsymbol{A} for \boldsymbol{Q}_s , \boldsymbol{T} for \boldsymbol{Q}_a), we obtain 54.0% for MOF and 48.7% for F1-Score on 50 Salads. Finally, we employ the permutation-aware transcript ${m T}$ for computing both ${m Q}_s$ and ${m Q}_a$, leading to the best performance on both datasets, i.e., 55.8% for MOF and 50.3%

	$oldsymbol{Q}_s$	$oldsymbol{Q}_a$	MOF	F1
	\boldsymbol{A}	\boldsymbol{A}	46.1	45.2
E	T	\boldsymbol{A}	50.8	46.9
Eval	\boldsymbol{A}	T	<u>54.0</u>	<u>48.7</u>
	T	T	55.8	50.3
	\boldsymbol{A}	\boldsymbol{A}	44.3	29.4
	T	\boldsymbol{A}	45.7	29.7
YTI	\boldsymbol{A}	T	<u>46.5</u>	<u>29.8</u>
	T	T	49.6	32.4

Table 2. Impacts of different pseudo labels on 50 Salads with the Eval granularity (*Eval*) and YouTube Instructions (*YTI*). Best results are in **bold**, while second best ones are *underlined*.

for F1-Score on 50 Salads, and 49.6% for MOF and 32.4% for F1-Score on YTI. The above results confirm the benefits of using the permutation-aware transcript T for computing both pseudo labels Q_s and Q_a .

4.2. Comparisons with the State-of-the-Art

4.2.1 Results on 50 Salads

We now compare the performance of our approach with state-of-the-art unsupervised activity segmentation methods on the 50 Salads dataset for both granularities, i.e., Eval and Mid. Tab. 3 illustrates the results. It is evident from Tab. 3 that our approach obtains the best MOF and F1-Score numbers on both granularities, outperforming all competing methods. In particular, UFSA outperforms TOT [31] by 8.4% and 4.9% on MOF on the Eval and Mid granularities respectively, and UDE [54] by 15.9% on F1-Score on the *Eval* granularity. Although TOT [31] and UDE [54] conduct joint representation learning and online clustering as our approach, they only exploit frame-level cues, whereas UFSA leverages segment-level cues as well. Moreover, our approach achieves better results than SSCAP [59], which uses recent self-supervised learning features [16], and ASAL [36], which exploits segment-level cues via action shuffling, e.g., on the Eval granularity, UFSA achieves 55.8% MOF, whereas SSCAP [59] and ASAL [36] obtain 41.4% MOF and 39.2% MOF respectively. The substantial improvements of UFSA over previous methods demonstrate the effectiveness of our approach.

4.2.2 Results on YouTube Instructions

Tab. 4 presents the quantitative results of our approach along with previous unsupervised activity segmentation methods on the YTI dataset. We follow the protocol of prior works and report the accuracy excluding the background frames. It is clear from Tab. 4 that our approach achieves the best MOF, outperforming all previous methods, and the second best F1-Score, slightly worse than TOT+TCL [31] (note that our approach currently relies on TOT only, and can further include TCL for potential

Method	Eval		Mid	
	MOF	F1	MOF	F1
CTE [30]	35.5	36.3	30.2	25.6
VTE [57]	30.6	-	24.2	-
ASAL [36]	39.2	-	<u>34.4</u>	-
UDE [54]	42.2	34.4	-	-
SSCAP [59]	41.4	30.3	-	-
TOT [31]	<u>47.4</u>	42.8	31.8	22.5
TOT+TCL [31]	44.5	<u>48.2</u>	34.3	<u>28.9</u>
Ours (UFSA)	55.8	50.3	36.7	30.4

Table 3. Results on 50 Salads. *Eval* denotes the Eval granularity, while *Mid* denotes the Mid granularity. Best results are in **bold**, while second best ones are *underlined*.

Method	MOF	F1
Frank-Wolfe [3]	-	24.4
Mallow [49]	27.8	27.0
CTE [30]	39.0	28.3
VTE [57]	-	29.9
ASAL [36]	44.9	32.1
UDE [54]	43.8	29.6
TOT [31]	40.6	30.0
TOT+TCL [31]	<u>45.3</u>	32.9
Ours (UFSA)	49.6	<u>32.4</u>

Table 4. Results on YouTube Instructions. Best results are in **bold**, while second best ones are *underlined*.

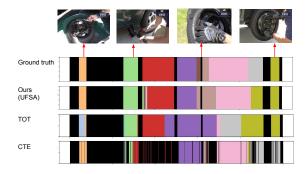


Figure 6. Segmentation results on a YouTube Instructions video (*changing_tire_0005*). Black color indicates background frames.

improvements). Specifically, UFSA has an improvement of 9.0% MOF and 2.4% F1-Score over TOT [31], and an improvement of 5.8% MOF and 2.8% F1-Score over UDE [54]. In addition, our approach obtains a noticeable gain of 4.7% MOF and a slight gain of 0.3% F1-Score over ASAL [36]. Fig. 6 plots the qualitative results of UFSA, TOT [31], and CTE [30] on a YTI video. Our approach demonstrates significant advantages over CTE [30] and TOT [31] in terms of capturing the temporal order of actions and aligning them closely with the ground truth. Due to space constraints, please refer to the supplementary material for more qualitative examples, especially with permuted, missing, and repetitive actions.

Method	MOF	F1
Mallow [49]	34.6	-
CTE [30]	41.8	26.4
VTE [57]	48.1	-
ASAL [36]	52.5	37.9
UDE [54]	47.4	31.9
SSCAP [59]	51.1	39.2
TOT [31]	47.5	31.0
TOT+TCL [31]	39.0	30.3
Ours (UFSA)	<u>52.1</u>	<u>38.0</u>

Table 5. Results on Breakfast. Best results are in **bold**, while second best ones are *underlined*.

	Method	MOF	F1
20	CTE [30]	47.6	44.9
Orig	TOT [31]	56.3	51.7
0	TOT+TCL [31]	<u>58.1</u>	<u>53.4</u>
	Ours (UFSA)	65.4	63.0
я	CTE [30]	40.8	35.6
Extra	TOT [31]	51.0	40.4
图	TOT+TCL [31]	<u>57.9</u>	<u>54.0</u>
	Ours (UFSA)	58.6	55.9

Table 6. Results on Desktop Assembly. *Orig* includes original fixed-order videos only, while *Extra* further includes additional permuted-step and missing-step videos. Best results are in **bold**, while second best ones are *underlined*.

4.2.3 Results on Breakfast

Tab. 5 includes the performance of different methods on the Breakfast dataset. From Tab. 5, our results are on par with ASAL [36], which leverages segment-level information via action shuffling, and SSCAP [59], which employs more sophisticated self-supervised features [16]. Particularly, ASAL [36] and SSCAP [59] yield the best MOF number (i.e., 52.5%) and the best F1-Score number (i.e., 39.2%) respectively, while UFSA achieves the second best results for both metrics (i.e., 52.1% and 38.0%). In addition, our approach outperforms a number of competing methods, namely Mallow [49], CTE [30], VTE [57], UDE [54], and TOT [31], which exploit frame-level cues only.

4.2.4 Results on Desktop Assembly

We test the performance of our approach on the Desktop Assembly dataset for both *Orig* and *Extra* sets. The results are reported in Tab. 6, which shows superior performance of our approach over CTE [30], TOT [31], and TOT+TCL [31]. For example, UFSA achieves an improvement of 14.9% MOF and 20.5% F1-Score over TOT [31] on the *Orig* set, and a gain of 7.6% MOF and 15.5% F1-Score over TOT [31] on the *Extra* set. Results on the *Orig* set indicate the effectiveness of our approach in preserving the fixed order of actions, while results on the *Extra* set show the ability of our method in handling permuted actions.

	Method	MOF	F1
	CTE [30]	28.6	26.4
Eval	TOT [31]	39.8	37.0
=	TOT+TCL [31]	<u>42.8</u>	44.9
	Ours (UFSA)	47.6	<u>41.8</u>
	CTE [30]	38.4	25.5
X	TOT [31]	40.4	<u>28.0</u>
~	TOT+TCL [31]	<u>40.6</u>	26.7
	Ours (UFSA)	46.8	28.2
ast	CTE [30]	39.8	25.5
K	TOT [31]	<u>40.6</u>	<u>27.6</u>
Breakfast	TOT+TCL [31]	37.4	23.2
m	Ours (UFSA)	44.0	36.7
20	CTE [30]	35.6	31.8
Orig	TOT [31]	<u>55.3</u>	<u>50.2</u>
	TOT+TCL [31]	49.2	44.6
	Ours (UFSA)	63.9	63.7
g	CTE [30]	35.7	30.4
Extra	TOT [31]	43.6	35.0
	TOT+TCL [31]	<u>45.9</u>	<u>40.0</u>
	Ours (UFSA)	57.9	54.0

Table 7. Generalization results. Best results are in **bold**, while second best ones are underlined

4.2.5 Generalization Results

We follow [31] to evaluate the generalization ability of our approach. We divide the datasets, i.e., 50 Salads (*Eval*), YTI, Breakfast, Desktop Assembly (*Orig*, *Extra*) into 80% for training and 20% for testing. For instance, for 50 Salads with 50 videos, 40 videos are used for training and 10 for testing. Tab. 7 shows the results. UFSA continues to outperform CTE [30], TOT [31], and TOT+TCL [31] in this experiment setting. Note the results of CTE [30], TOT [31], and TOT+TCL [31] in Tab. 7 differ from those reported in [31] since different training/testing splits are used (we could not acquire the splits from the authors of [31]). Our splits are available at https://tinyurl.com/57ya6653.

5. Conclusion

We propose a novel combination of modules and unsupervised losses to exploit both frame-level cues and segment-level cues for permutation-aware activity segmentation. Our approach includes a frame-level prediction module which uses a transformer encoder for obtaining framewise action classes and is trained in unsupervised manner via temporal optimal transport. To leverage segment-level cues, we utilize a segment-level prediction model based on a transformer decoder for predicting video transcripts and a frame-to-segment alignment module for corresponding frame-level features with segment-level features, resulting in permutation-aware segmentation results. For unsupervised training of the above modules, we introduce simple-yet-effective pseudo labels. We show comparable or superior results over prior methods on four public datasets.

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