Supplementary for Self-Supervised Denoising Transformer with Gaussian Process

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1. Ablation study

1.1. λ_{GP}

We conduct different experiments for various values of k and N on BSD dataset [7]. Table 1 shows the performance of SST-GP when we vary the value of λ_{GP} used in training SST-GP.

Table 1. Ablation experiments for λ_{GP} using BSD dataset.

Noise type	Noise level	$\lambda_{GP} = 0.3$	$\lambda_{GP} = 0.03$	$\lambda_{GP} = 0.003$
Consister	$\sigma = 25$	31.12/0.878	31.18/0.880	31.01/0.877
Gaussian	$\sigma = [5, 50]$	31.08/0.868	31.12/0.869	30.94/0.862

1.2. Kernel Function

We conduct different experiments for different kernel function (Linear kernel LIN[.], Square Exponential SE[.], and Rational Quadratic RQ[.]) on BSD dataset [7]. Table 2 shows the performance of SST-GP is best when we rational quadratic kernel function for Gaussian process in SST-GP.

Table 2. Ablation experiments for kernel function used in SST-GP using BSD dataset.

Noise type	Noise level	LIN[.]	SE[.]	RQ[.]
Constant	$\sigma = 25$	30.88/0.872	31.02/0.877	31.18/0.880
Gaussian	$\sigma = [5, 50]$	30.91/0.863	30.99/0.865	31.12/0.869

1.3. Down-sampled images

In our SST-GP given a noisy image y we use downsampling technique proposed in [3] with cell size k = 2, and obtain down-sampled images. Additionally, we randomly cyclic-shift each down-sampled image four times to obtain $\{y_1^d y_2^d, y_3^d, \ldots, y_N^d\}$ (implies N = 8). An example down-sampled images are shown in Fig. 1. In Table 3, we conduct ablation study for different values of N.



Figure 1. Examle downsampled and cyclically shifted images.

Table 3. Ablation experiments for different values of N using BSD dataset.

Noise type	Noise level	N = 2	N = 4	N = 8	N = 12
Causaian	$\sigma = 25$	30.80/0.871	30.99/0.875	31.18/0.880	31.2/0.880
Gaussian	$\sigma = [5, 50]$	30.77/0.857	30.90/0.861	31.12/0.869	31.15/0.869

1.4. Random sampling

In our SST-GP given a noisy image y we use downsampling technique proposed in [3] with cell size k = 2, and obtain down-sampled images. Additionally, we randomly cyclic-shift each down-sampled image four times to obtain $\{y_1^d y_2^d, y_3^d, \ldots, y_N^d\}$ (implies N = 8). In Table 4, we conduct ablation study to know hoe random shifthing in obtaing down-sampled images effects SST-GP's performance.

Table 4. Ablation experiments for random shifting using BSD dataset.

	Noise type	Noise level	w/o random shifting	w/ random shifting	
Gaussian	Consister	$\sigma = 25$	30.83/0.872	31.18/0.880	
	$\sigma = [5, 50]$	30.75/0.857	31.12/0.869		

2. Algorithm

Algorithm 1 shows the pseudo algorithm for the proposed SST-GP.

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Algorithm 1 Pseudo code for training 3SD

Input: Set of noisy images $\mathcal{D} = \{y^i\}_{i=1}^M$ **Output**: $\hat{\theta}$, optimized network parameters of SST-GP. optimized GP parameters $\alpha, \beta, \sigma_{\epsilon}$.

1: **for** every epoch **do**

2: for $\{y^i\} \in \mathcal{D}$ do

- 3: Generate down-sampled images [3] and clyical shit the images to obtain $\{y_1^{d,i}, y_2^{d,i}, y_3^{d,i}, \dots, y_N^{d,i}\}$ from y^i
- 4: forward them through SST-GP to obtain $\{\hat{x}_{1,pred}^{d,i}, \hat{x}_{2,pred}^{d,i}, \hat{x}_{3,pred}^{d,i}, \dots, \hat{x}_{N,pred}^{d,i}\}$

5: using GP obtain corresponding pseudo-GT

$$\{\hat{x}_{1}^{d,i}, \hat{x}_{2}^{d,i}, \hat{x}_{2}^{d,i}, \hat{x}_{3}^{d,i}, \dots, \hat{x}_{N}^{d,i}, \dots, \hat{x}_{N}^{d,i}\}$$

- 6: Compute loss \mathcal{L}_{total}
- 7: update SST-GP parameters
- 8: compute gradients for GP parameters(α , β , and σ_{ϵ}) using loss \mathcal{L}_{total}
- 9: update GP parameters (α , β , and σ_{ϵ})
- 10: **end for**
- 11: end for

3. Comparisons

3.1. Quantitative Comparisons

Table 6 comparisons of SST-GP additional SOTA methods [8, 12] on BSD dataset for Guassian, and Poisson noise images test sets.

3.2. Training and Inference time

We both networks U-Net and Den-T for 60 epochs with training set images (please refer sections 4.3 and 5.1 in the main paper). Table 5 shows the training time for U-Net and Den-T. Additionally we compare inference time of U-Net and Den-T when the input images is 256 pixels.

Table 5. Training and tesing time comparisons for U0Net and Den-T.

Method	U-Net	U-Net w/ GP	Den-T	SST-GP (Den-T w/ GP)
Training time (hrs)	65	90	50	76
Inference time(ms)	98	98	84	84

4. Real Test Comparisons

The SIDD [1] dataset is used to compare the performance of SST-GP against the other methods. We train all the networks using the SIDD Medium training dataset images, and follow the steps mentioned in the respective SOTA methods. As BM3D [2] requires prior information to denoise, we use Anscombe for Poisson to estimate the priors. Results corresponding to this experiment are shown in Table 7 and Figure 2. In contrast to other methods [3,5,6,9], we used down-sampled images and modelled joint distribution using GP, that helped the proposed SST-GP outperform the other methods by a significant margin and it is able to produce sharper images than the other methods.

5. Synthetic Test Qualitative Analysis

Figure 3 and Figure 4 illustrates sample denoising results compared with recent approaches. As it can be observed, the results of the proposed method are more clearer and sharper in contrast to the outputs of the other methods [3, 5, 6, 9].

6. Comparison with Liu etal.

we compared our SST-GP with Liu *etal.*[2] using Confocal Mice dataset [3], where our SST-GP method outperformed Liu *etal.*[2] (refer to Table 8) by 0.35dB.

7. Sigma values Σ_i^d

Figure 5 shows Σ_j^d values at different epochs of training SST-GP. Here we can clearly observe that initial Σ_j^d values are high as the corresponding output prediction images are noisy and eventually the variance values reduce over the training process as the output predictions get clearer and sharper. This shows that minimizing the variance helps GP model to learn the joint distribution more accurately, and obtain accurate pseudo-GT labels.

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⁰https://github.com/AbdoKamel/simple-camera-pipeline

Table 6. PSNR/SSIM comparisons on synthetic test sets created using Gaussian noise and Poison noise. Higher number represents better performance.

Type of	Detecat	N2C [0]	N2N [6]	CPM2D [2]	DID [10]	N2V [4]	Lainal0 mu [5]	Lainal0 nma [5]	DRSN[11]	Salf2calf [9]	Noisa2Sama [12]	Huong et al. [2]	SST-GP	Den-T w/ GP								
Noise	Dataset	N2C [9]	11211 [0]	CBWI5D [2]	DIF	142 V [4]	Lame 19-mu [J]	Lamer 9-pine [3]	DBSN[11]	Sen2sen [6]	Noise25anie [12]	ritiang et al. [5]	(ours)	oracle (ours)								
Gaussian	DED	21.05/0.870	21 04/0 979	20 48/0 861	26 28/0 708	20 24/0 824	28 62/0 802	20.00/0.877	20 80/0 820	28 70/0 807	27.05/0.782	20 70/0 872	21 19/0 990	31 44/0 000								
$\sigma = 25$	630	51.05/0.879	51.04/0.878	50.46/0.801	20.38/0.708	29.34/0.824	28.02/0.803	50.99/0.877	29.80/0.839	28.70/0.807	21.95/0.182	30.79/0.875	31.10/0.000	31.44/0.900								
Poisson	DCD	20 2610 868	20 25/0 969	20 10/0 042	26 07/0 608	28 4610 708	28 25/0 704	20.25/0.966	28 10/0 700	28 16/0 701	27 41/0 764	20 10/0 862	20 84/0 807	21.04/0.010								
$\sigma = 30$	BSD 30.36/0.868	50.50/0.808	58 30.35/0.868	30.35/0.868 2	30.35/0.868	30.35/0.868	30.35/0.868	30.35/0.868	30.33/0.868	30.35/0.868	30.35/0.868	5 29.18/0.842	20.07/0.698	28.40/0.798	28.25/0.794	30.25/0.866	28.19/0.790	28.10/0./91	27.41/0.764	30.10/0.863	30.84/0.89/	51.04/0.910

Table 7. PSNR/SSIM comparisons onreal-world noise dataset SIDD [1]. PSNR/SSIM higher the better performance.

Methods	N2C [9]	N2N [6]	BM3D [2]	N2V [4]	Laine19-mu [5]	Laine19-mu [5]	DBSN [11]	Huang et al. [3]	Huang et al. [3]	SST-GP
		- · · [•]			(Gaussian)	(Poisson)				(ours
Network	II N. (II N.		LI N. 4	LI N. (LI N. 4	DDCN	LI N. 4	DDC.	Due Terl CD
used	U-Net	U-Net	_	U-Net	U-INet	U-INet	DBSN	U-INet	KKGS	Den-1 W/ GP
SIDD [1]	50 60/0 991	50 62/0 991	48 60/0 986	48 01/0 983	49 82/0 989	50 28/0 989	49 56/0 987	50 47/0 990	50 76/0 991	50 87/0 992
Benchmark	50.00/0.771	50.02/0.771	40.00/0.900	40.01/0.202	47.02/0.707	50.20/0.707	47.50/0.707	50.4770.550	50.70/0.771	50.07/0.772
SIDD [1]	51 10/0 001	51 21/0 001	49.00/0.000	40 5510 004	50 11/0 000	50 80/0 000	50 12/0 000	51.0(/0.001	51 20/0 001	51 57/0 002
Vaidation	51.19/0.991	51.21/0.991	48.92/0.986	48.55/0.984	50.44/0.990	50.89/0.990	50.15/0.988	51.06/0.991	51.59/0.991	51.57/0.992



Figure 2. Comparisons on real-world noisy images from the SIDD Benchmark in RAW formats. For display purpose we use the code provided by the authors of SIDD¹ to convert images from raw format to srgb

Table 8. Ablati	on experiments	for random shifting.	

Dataset	Confocal Mice[3]	Confocal ZebraFish[3]	Two-Photon Mice[3]
SST-GP (ours)	38.28	32.70	34.11
Liu etal. [1]	37.97	32.26	33.83

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Figure 3. Comparisons on noisy images with Gaussian noise $\sigma=25$

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 $|\Sigma| = 1.71$ Figure 5. Denoised images on a sample down-sampled image at different epochs with corresponding variances computed using GP.

 $|\Sigma| = 0.83$