

Supplementary: “PC-GZSL: Prior Correction for Generalized Zero Shot Learning”

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1. Proposed Algorithm

We present the summary of our approach in the form of a pseudo-code in **Algorithm 1**. Proposed approach is quite simple, the overall steps involve computing seen unseen prior $P(\mathcal{Y})$ using total number of samples n_s and n_u for respective case. Similarly, using ground truth data, the number of samples for each class are computed to estimate $P^t(y)$. Finally, model bias or effective prior is computed as an empirical average of $P^m(y|x_i)$ for x_i in validation dataset using original trained model. The last step involves, tuning the parameters α and β which give best harmonic mean accuracy. It is noted that, validation data and test data must have the same prior distribution $P^t(y)$.

2. Additional analysis on CUB and AWA2

We show in Figure 1 the confusion between seen and unseen classes. The top row show results for CUB and bottom

		Baseline		PC		
+Ve	Seen	0.87	0.36	0.8	0.76	CUB
		0.11	0.6	0.078	0.11	
		0.015	0.04	0.13	0.13	
-Ve	Unseen					
+Ve	Seen	0.96	0.4	0.88	0.78	AWA2
		0.039	0.53	0.031	0.053	
		0.0056	0.064	0.085	0.16	
-Ve	Unseen					
		Seen	Unseen	Seen	Unseen	

Figure 1. We show the confusion between seen and unseen classes for incorrectly classified examples for the CUB and AWA2 datasets.

Algorithm 1 Algorithm for model prior correction

Input:

Trained model M

Validation data $(x_i, y_i)_{i=1}^{n_s}$ and $(x_i, y_i)_{i=1}^{n_u}$

Output:

Adjusted model M^a

Start:

Compute the adjustment terms

$$P(\mathcal{Y}) = \begin{cases} \frac{n_s}{n_s+n_u} & \text{if } y \in \mathcal{Y}_s \\ \frac{n_u}{n_s+n_u} & \text{otherwise} \end{cases}$$

$$P^t(y) = \frac{1}{n_s+n_u} \sum_i^{n_s+n_u} 1_{hot}(y_i)$$

$$P^m(y) = \frac{1}{n_s+n_u} \sum_i^{n_s+n_u} M(x_i)$$

Tune the adjustment strength

for $(\alpha = 0, \alpha < 2, \alpha+ = 0.1)$ **do**

for $(\beta = 0, \beta < 2, \beta+ = 0.1)$ **do**

$$y_i^{pred} = ArgMax \left(M(x_i) \cdot \left(\frac{P^t(y)}{P^m(y)} \right)^\alpha \cdot P(\mathcal{Y})^\beta \right)$$

h = Get_Harmonic_Mean_Acc (y, y^{pred})

if **h** is the best

$$(\alpha^*, \beta^*) = (\alpha, \beta)$$

end for

end for

$$M^a = \left(\frac{P^t(y)}{P^m(y)} \right)^{\alpha^*} P(\mathcal{Y})^{\beta^*} \cdot M$$

Return M^a

End

row is for AWA2 dataset. One may note that, accuracy numbers in the 1st row (+Ve detections) for each case improves when using PC. Similarly, the bias of unseen classes toward

the seen classes (-Ve detections classified into Seen classes) is lower for PC.

3. Ablation on AwA2

Table 1 and Table 2 show results on AwA2 dataset where each component for the adjustment is tested for its effectiveness.

$\log \frac{P^t(y)}{P^m(y)}$	$\log P(\mathcal{Y})$	\mathcal{U}	\mathcal{S}	\mathcal{H}	A
AwA2					
X	X	34.9	95.3	51.1	63.9
✓	X	71.0	88.1	78.6	82.3
X	✓	46.9	94.0	62.6	69.6
✓	✓	72.7	87.6	79.5	82.7

Table 1. We show contribution of individual adjustment terms in removing seen unseen class bias for AwA2.

Adjustment	\mathcal{U}	\mathcal{S}	\mathcal{H}	A
AwA2				
-	34.9	95.3	51.1	63.9
$\log P^t(y)$	59.8	89.5	71.7	80.6
$\log P^m(y)$	44.6	92.8	60.2	64.2
$\log \frac{P^t(y)}{P^m(y)}$	71.0	88.1	78.6	82.3

Table 2. The effectiveness of bias removal using $\log P^t(y)$ and $\log P^m(y)$ terms for AwA2.