



## Motivation

### Existing image restoration methods

- **Model-based optimization methods**
  - Flexible but time-consuming and less effective
- **Discriminative learning methods**
  - Fast and effective but application-specific

### Basic idea

- With the aid of variable splitting techniques such as **alternating direction method of multipliers (ADMM)** and **half quadratic splitting (HQS)** algorithms, denoiser prior can be plugged in as a modular part of model-based optimization methods to solve other inverse problems.
- Learning fast and expressive discriminative CNN (convolutional neural network) denoisers.

## Half Quadratic Splitting (HQS) Algorithm

The general model for image restoration

$$\min_x \|y - Hx\|_2^2 + \lambda \cdot R(x)$$

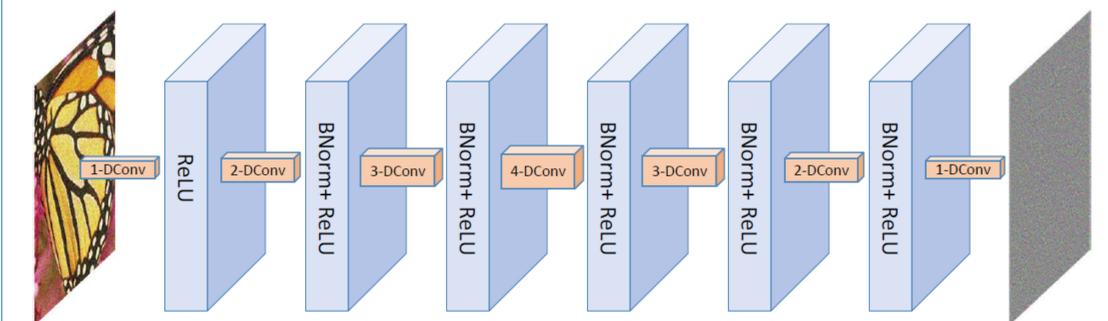
Introducing an auxiliary variable  $z$  ( $z \approx x$ )

$$\min_{x,z} \|y - Hx\|_2^2 + \lambda \cdot R(z) + \eta \|z - x\|_2^2$$

Solving  $x$  and  $z$  alternatively and iteratively

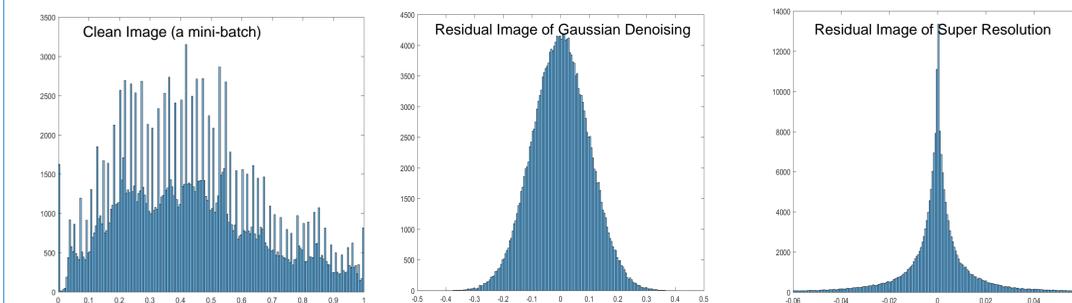
- (a)  $\min_x \|y - Hx\|_2^2 + \eta \|z - x\|_2^2$  % Quadratic regularized least-squares problem
- (b)  $\min_z \eta \|x - z\|_2^2 + \lambda \cdot R(z)$  % Denoising sub-problem

## Network Architecture



Note that “s-DConv” denotes s-dilated convolution,  $s = 1, 2, 3$  and  $4$ ; “BNorm” represents batch normalization; “ReLU” is the rectified linear units ( $\max(\cdot, 0)$ ).

## Design Rationale and Training Details



- **The residual image of Gaussian denoising has a simple Gaussian distribution.**
- **Batch normalization and residual learning are beneficial to each other [1].**
- Using dilated filter to enlarge receptive field.
- Using training samples with small size to help avoid boundary artifacts.
- Learning specific denoiser model with small interval noise levels.

## Experiments

### Image Denoising

Table: The averaged PSNR(dB) results of different methods on BSD68 dataset.

Methods	BM3D	WNNM [2]	TNRD	Proposed
15	31.07	31.37	31.42	<b>31.73</b>
25	28.57	28.83	28.92	<b>29.23</b>
50	25.62	25.87	25.97	<b>26.23</b>



### Image Deblurring

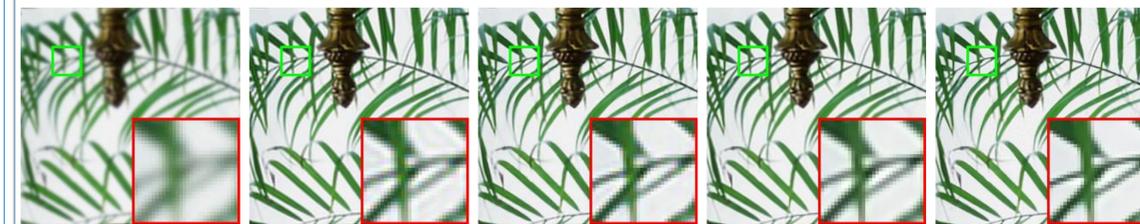


Figure: Image deblurring performance comparison (the blur kernel is Gaussian kernel with standard deviation 1.6, the noise level is 2).

### Image Super-Resolution

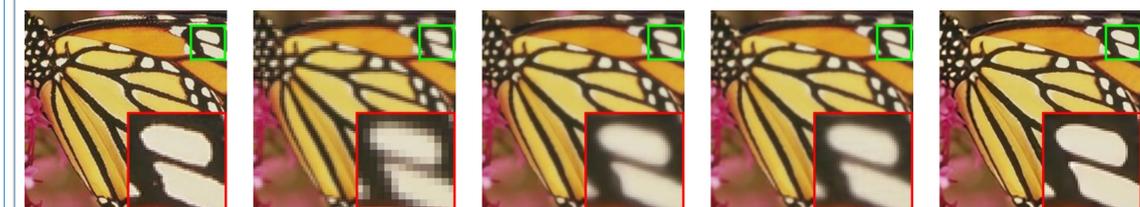


Figure: Single image super-resolution performance comparison for Butterfly image from Set5 (the blur kernel is  $7 \times 7$  Gaussian kernel with standard deviation 1.6, the scale factor is 3). The proposed deep CNN denoiser prior based optimization method can super-resolve LR image by tuning the blur kernel and scale factor without training.

## Reference

- [1] K. Zhang, W. Zuo, Y. Chen, D. Meng and L. Zhang, "Beyond a Gaussian Denoiser: Residual Learning of Deep CNN for Image Denoising", in IEEE Transactions on Image Processing, vol. 26, no. 7, pp. 3142-3155, July 2017.
- [2] S. Gu, L. Zhang, W. Zuo and X. Feng, "Weighted nuclear norm minimization with application to image denoising", Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition, 2014: 2862-2869.

Code: <https://github.com/csxn/ircnn>