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1. Introduction

We present a novel formulation for 3D model tracking in color and depth data via a joint error over both the contour and an ICP energy

 $E_{Joint} = E_C + \lambda E_{ICP}$



We can deal with typical problems such as multiple instance tracking, occlusion and scale changes

$$E_C := -\sum_{m \in \Omega} \log$$



[1] V. A. Prisacariu and I. D. Reid. PWP3D: Real-Time Segmentation and Tracking of 3D Objects. IJCV, 2012.

2. Viewpoint approximation

To speed up computation, we introduce approximations that enable us to track many objects in real-time on a single core.



By pre-rendering the object from densely sampled viewpoints, we extract scale-invariant *information such as 3D* contour points and interior surface points. This allows us to avoid any GPU involvement during tracking.

We define a 'plane-to-point' ICP energy, where the normals are coming from the source and must be rotated as well. Since we pre-computed our viewpoints, we can use the 3D normals of the sparse interior surface points without additional costs.

 E_{ICP} :

We transform the local 3D information into the scene $\overline{s}_i =$

and find the projective correspondence $d_i := \prod_D^{-1}(\pi(\bar{s}_i))$

Real-Time 3D Model Tracking in Color and Depth on a Single CPU Core

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3a. Contour energy

Following PWP3D [1], we define the pixel-wise posterior via foreground/ background probabilities and the Heaviside function of an implicit contour. We then sum over the negative logs to finally retrieve:

 $g \left(H_{\phi}(x) P_{f}(I(x)) + (1 - H_{\phi}(x) P_{b}(I(x))) \right)$

Tracking two Stanford bunnies side by side. While the left bunny is tracked densely [1], our approach evaluates the energy using the sparse 3D contour points extracted in the offline stage. We can thus both circumvent a rendering step and a distance transform.

3b. ICP energy

$$= \underset{\Xi}{\operatorname{argmin}} \sum_{i} \left(\left(\Xi(\bar{s}_i) - d_i \right) \cdot \Xi_{SO}(\bar{n}_i) \right)$$

$$= R \cdot s_i + t \qquad \bar{n}_i = R \cdot n$$

By deriving in respect to the object pose, we retrieve both the separate terms for the contour over pixels and the ICP energy over 3D correspondences:

$$\frac{\partial E_C}{\partial \xi} =$$

$$J_i := - \begin{bmatrix} \bar{n}_i^\mathsf{T} \end{bmatrix}$$

$$\nabla \xi = \left(\sum_{x} J_x^{\mathsf{T}} J_x + \sum_{i} \lambda J_i^{\mathsf{T}} J_i \right)^{-1} \left(\sum_{x} J_x + \sum_{i} \sqrt{\lambda} J_i \cdot r_i \right)$$



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4. Optimization

$$\frac{(P_f - P_b)}{H_{\phi}(P_f - P_b) + P_b} \frac{\partial H_{\phi}}{\partial \phi} \frac{\partial \phi}{\partial x} \frac{\partial \pi(X)}{\partial X} \frac{\partial \Xi(X)}{\partial \xi}$$
$$\left(\left(\bar{s}_i \times \bar{n}_i \right) + \bar{n}_i \times \left(\bar{s}_i - d_i \right) \right)^{\mathsf{T}} \right] \quad r_i := \left(\bar{s}_i - d_i \right) \cdot \bar{n}_i$$

The final twist is then computed as a weighted update between those two energies of pixel-wise and correspondence-wise errors



We constantly demonstrate better performance.

[2] C. Choi and H. Christensen. RGB-D Object Tracking: A Particle Filter Approach on GPU. In IROS, 2013

[3] D. J. Tan, F. Tombari, S. Ilic, and N. Navab. A Versatile Learning-based 3D Temporal Tracker: Scalable, Robust, Online. In ICCV, 2015.



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5. Results

| Krull | Tan | А | В |
|-------|------|------|------|
| 0.8 | 1.54 | 1.2 | 0.76 |
| 1.67 | 1.90 | 1.16 | 1.09 |
| 0.79 | 0.34 | 0.30 | 0.38 |
| 1.11 | 0.42 | 0.14 | 0.17 |
| 0.55 | 0.22 | 0.23 | 0.18 |
| 1.04 | 0.68 | 0.22 | 0.20 |
| 143 | 1.5 | 2.70 | 8.10 |
| 0.51 | 1.23 | 0.91 | 0.64 |
| 1.27 | 0.74 | 0.71 | 0.59 |
| 0.62 | 0.24 | 0.26 | 0.24 |
| 2.19 | 0.50 | 0.44 | 0.41 |
| 1.44 | 0.28 | 0.31 | 0.29 |
| 1.90 | 0.46 | 0.43 | 0.42 |
| 135 | 1.5 | 2.72 | 8.54 |
| 0.52 | 1.10 | 0.59 | 0.50 |
| 0.74 | 0.94 | 0.64 | 0.69 |
| 0.63 | 0.18 | 0.18 | 0.17 |
| 1.28 | 0.35 | 0.12 | 0.12 |
| 1.08 | 0.24 | 0.22 | 0.20 |
| 1.20 | 0.37 | 0.18 | 0.19 |
| 129 | 1.5 | 2.79 | 8.79 |
| 0.69 | 0.73 | 0.36 | 0.34 |
| 0.81 | 0.56 | 0.51 | 0.49 |
| 0.81 | 0.24 | 0.18 | 0.18 |
| 2.10 | 0.31 | 0.20 | 0.15 |
| 1.38 | 0.25 | 0.43 | 0.39 |
| 1.27 | 0.34 | 0.39 | 0.37 |
| 116 | 1.5 | 2.71 | 9.42 |
| 0.82 | 0.81 | 0.58 | 0.51 |
| 1.38 | 0.37 | 0.28 | 0.26 |
| 131 | 1.5 | 2.73 | 8.71 |



Comparison to related work on [2].

Convergence experiments to highlight the recovery abilities of our method for imperfect initializations



Tracking error for changing number of sample points, i.e. the degree of approximation. Even with a only a few points, tracking is possible!

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